A review of R neural network packages (with NNbenchmark): accuracy and ease of use

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Abstract

In the last three decades, neural networks (NN) have evolved from an academic topic to a common scientific computing tool. CRAN currently hosts approximately 80 packages in May 2020 involving neural network modeling, some offering more than one algorithm. However, to our knowledge, there is no comprehensive study which checks the accuracy, the reliability and the ease-of-use of those NN packages.

In this paper, we attempted to test this rather large number of packages against the common set of datasets with different levels of complexity, and to benchmark and rank them with certain metrics.

Restricting our evaluation to regression algorithms applied on the one-hidden layer perceptron and ignoring those for classification or other specialized purposes, there were approximately 60 package::algorithm pairs left to test. The criteria used in our benchmark were: (i) the accuracy, i.e. the ability to find the global minima on 13 datasets, measured by the Root Mean Square Error (RMSE) in a limited number of iterations; (ii) the speed of the training algorithm; (iii) the availability of helpful utilities; (iv) and the quality of the documentation.

We have attempted to give a score for each evaluation criterion and to rank each package::algorithm pair in a global table. Overall, 15 pairs are considered accurate and reliable and can be recommended for daily usage. Most others should be avoided as they are either less accurate, too slow, too difficult to handle, or have poor or no documentation.

To carry out this work, we developed various codes and templates, as well as the NNbenchmark package used for testing. This material is available at https://akshajverma.com/NNbenchmarkWeb/index.html and https://github.com/pkR-pkR/NNbenchmark, and can be used to verify our work and, we hope, improve both packages and their evaluation. Finally, we provide some hints and features to guide the development of an idealized neural network package for R.

Introduction

The R Project for Statistical Computing (www.r-project.org), as any opensource platform, relies on its contributors to keep it up to date. Neural networks (NN), inspired on the brain's own connections system, are a class of models in the growing field of machine learning forwhich R has a number of tools. During the last 30 years, neural networks have evolved from an academic topic to a common tool in scientific computing. Previously, neural networks were considered more theory than practice, partly because the algorithms used were computationally demanding.

As a convenience in the general conversation, the same term is used in a generic manner for different model structures and applications: multilayer perceptron for regression, multilayer perceptron for classification, multilayer perceptron for specialized applications, recurrent neural network for autoregressive time series, convolutional neural networks for dimension reduction and pattern recognition, deep neural networks for image or voice recognition. Most of the above types of neural networks can be found in R packages hosted on CRAN but without any warranty about the accuracy or the speed of computation. This is an issue as many poor algorithms are available in the literature and hence poor packages implemented on CRAN.

A neural network algorithm requires complicated calculations to improve the model

control parameters. As with other optimization problems, the gradient of the chosen cost function that indicates the lack of suitability of the model is sought. This lets us improve the model by changing the parameters in the negative gradient direction. Parameters for the model are generally obtained using part of the available data (a training set) and tested on the remaining data. Modern software allows much of this work, including approximation of the gradient, to be carried out without a large effort by the the user.

The training process can generally be made more efficient if we can also approximate second derivatives of the cost function, allowing us to use its curvature via the Hessian matrix. There are a large number of approaches, of which quasi-Newton algorithms are perhaps the most common and useful. Within this group, methods based on the Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm for updating the (inverse) Hessian approximation provide several well-known examples. In conducting this study, we believed that these second-order algorithms would perform better than first-order methods for fit-in-memory datasets.

Regardless of our belief, we wished to be able to conduct a thorough examination of these training algorithms in R. There are many packages, but barely any information to allow comparison. Our work, reported here, aims to provide a framework for benchmarking neural network packages. We restrict our examination to packages for R, and in this report focus on those that provide neural networks of the perceptron type, that is, one input layer, one normalized layer, one hidden layer with a nonlinear activation function that is usually the hyperbolic tangent tanh(), and one output output layer. The criteria used in our benchmark were: (i) the accuracy, i.e. the ability to find the global minima on 13 datasets in a limited number of iterations; (ii) the speed of the training algorithm; (iii) the availability of helpful utilities; (iv) and the quality of the documentation. We restricted our evaluation to regression algorithms applied on the one-hidden layer perceptron and ignored those for classification or other specialized purposes.

Neural Networks: the perceptron

Here, we give a short description of the one hidden layer perceptron. As the "layer" term suggests it, some terms come from the representation of graphs whereas some other terms come from the traditional literature on nonlinear models.

Using the graph description, a one-hidden layer neural network is made of 3 parts: (i) the layer of the input(s), (ii) the hidden layer which consists of independant neurons, each of them performing two operations: a linear combination of the inputs plus an offset, then a nonlinear function applied on this linear combination. (iii) the layer of the output(s) which is a linear combination of the output of the nonlinar functions in the hidden layer.

The nonlinear function used in the hidden layer must have the following four properties: continuous, derivable, monotonic, bounded. The logistic function, the hyperbolic tangent function and the arctangent functions are the usual candidates.

The above description has a simple mathematical equivalence. Let's give two examples.

The model y = a1 + a2 * tanh(a3 + a4 * x) + a5 * tanh(a6 + a7 * x) + a8 * tanh(a9 + a10 * x) describes a neural network with one input, three hidden neurons, one output model where x is the input, tanh() is the activation function, y is the output and a1, ..., a10 are the parameters.

The model y = a1 + a2 * atan(a3 + a4 * x1 + a5 * x2 + a6 * x3 + a7 * x4 + a8 * x5) + a9 * atan(a10 + a11 * x1 + a12 * x2 + a13 * x3 + a14 * x4 + a15 * x5) + a16 * atan(a17 + a18 * x1 + a19 * x2 + a20 * x3 + a21 * x4 + a22 * x5) describes a neural network with five inputs, three hidden neurons, one output model where x is the input, atan() is the activation function, y is the output and <math>a1, ..., a22 are the parameters.

In order to get large gradients at the first steps of the training algorithm, it is recommended to use normalized inputs, normalized outputs, odd functions like the hyperbolic tangent function or the arctangent function and small random values to initialize the param-

eters, for instance extracted from the N(0, 0.1) distribution. Such good practices help find the good local minima and possibly the global minimum.

The dataset used for the training is assumed to have a number of rows much larger than the number of parameters. We agree that « much larger » is subject to discussion but 3 to 5 times are accepted values (In experimental design, some iterative strategies start with a dataset having a number of experiments/lines equal to 1.8 times the number of parameters and then increase the number of experiments to finetune the model).

It is rather clear from the mathematical formula above that neural networks of perceptron type are nonlinear models and require for their parameter estimation some training algorithms that can handle (highly) nonlinear models. Indeed, the intrinsic and parametric curvatures of such models are usually very high and, with so many parameters, the Jacobian matrix might exhibit some colinearities between its columns and become quasi-degenerated. As a result, the appropriate algorithms for such pairs dataset::model are rather limited and well-known. They are the second-order algorithms like BFGS and Levenberg-Marquardt (and Horsehoe?).

Unfortunately, due to some simple literature on the gradient and the hype around "deep neural networks" that manipulate ultra-large models with hundreds or thousands parameters and sometimes more parameters than examples in the datasets, many papers and many R packages emphasize the use of first-order gradient algorithms. In the case of the perceptron, this is an error and the goal of this paper is to demonstrate it.

Methodology

??JN: - In working on material below, I think we need to provide some explanation of goals - What do we mean by RMSE, other measures? Should define here for later use.

Considering regression problems, we measure the quality of our model by the root mean squared error (RMSE): the smaller RMSE the better the fitted model. In addition to the RMSE, two other convergence metrics have been considered: the Mean Absolute Error (MAE) and the Worst Absolute Error (WAE). We recall the definition of the RMSE, the MAE and the WAE in Appendix A. The ranking on MAE and WAE may help distinguish packages with close RMSE values.

- What does "convergence" mean in our context? ??JN: Something like

When training neural networks, we attempt to tune a set of hyperparameters so that the RMSE is minimized. When our method for such adjustment can no longer reduce the RMSE, we say that the given algorithm terminated. It converged when the terminated RMSE value is relatively small. So, we do not choose the MAE neither for overall ranking nor for convergence value as there is no consensus in the literature, see e.g. (Willmott and Matsuura, 2005; Chai and Draxler, 2014).

Furthermore, in practice, some algorithms require that we stop the optimization process in exceptional situations (e.g., a divide by zero), or a pre-set limit on the number of steps or elapsed time is reached.

More precisely, second-order algorithms are all set to a maximum of 200 iterations. On the other hand, first-order algorithms were set to several values, depending on how well and how fast they converged: maxit1storderA=1000 iterations, maxit1storderB=10000 iterations, and maxit1storderC=100000 iterations. The full list of the maximum iteration number per package:algorithm is given in Appendix C.

- What do we mean by "performance"? Other goals? ??JN: perhaps?

We measure performance primarily by relative computing time between methods on a particular computing platform. We could also count measures of iterations, function evaluations or similar quantities that indicate the computing effort. We note that differences in machine architecture and in the attached libraries (e.g., BLAS choices for R) will modify our measures. We are putting our tools on a Github repository so that further evaluation can be made by ourselves and others as hardware and software evolves.

The resulting files in the repository were mostly generated by a Windows system build 10.0.18362.752 with a i7-8750H CPU, a Intel(R) UHD Graphics 630 and NVIDIA GeForce GTX 1060 chip, and 16 GB of RAM.

Our research process was divided into 3 phases.

Phase 1 - Preparation of benchmark datasets

Datasets => NEED TO BE FINISHED??

All the datasets we use cannot generally be modeled using a non-iterative calculation such as Ordinary Least Squares. Varying levels of difficulty in modeling the different data sets are intended to allow us to further classify different algorithms and the packages that implement them. Sonja Surjanovic and Derek Bingham of Simon Fraser University created a useful website from which three of the multivariate datasets were drawn. We note the link, name and difficulty level of the three datasets:

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- http://www.sfu.ca/~ssurjano/fried.html (Friedman - average)
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- http://www.sfu.ca/~ssurjano/detpep10curv.html (Dette medium)
- http://www.sfu.ca/~ssurjano/ishigami.html (Ishigami high)

The other multivariate dataset, Ref153, was taken from ...

Three of the univariate datasets we used were taken from a website of the US National Institute for Standards and Technology (NIST): https://www.itl.nist.gov/div898/strd/nls/nls_main.shtml. (Gauss1 - low; Gauss2 - low; Gauss3 - average)

Univariate datasets Dmod1, Dmod2 are from ...

Dreyfus1 is a pure neural network which has no error. This can make it difficult for algorithms that assume an error exists. Dreyfus2 is Dreyfus1 with errors. NeuroOne from ...

Finally, we also consider a Simon Wood test dataset, used in (Wood, 2011) for benchmarking generalized additive models. Precisely, we consider a generation of Gaussian random variates Y_i , i = 1, ..., n with the mean μ_i defined as

$$\mu_i = 1 + f_0(x_{i,0}) + f_1(x_{i,1}) + f_2(x_{i,2}) + f_3(x_{i,3}) + f_4(x_{i,4}) + f_0(x_{i,5})$$

and standard deviation $\sigma = 1/4$ where f_j are Simon Wood's smooth functions defined in Appendix B, $x_{i,j}$ are uniform variates and n = 20,000.

Packages

Using RWsearch (Kiener, 2020) we sought to automate the process of searching for neural network packages. All packages that have "neural network" as a keyword in the package title or in the package description were included. In May 2020, around 80 packages falls into this category. Packages nlsr, minpack.lm, caret were added because the former 2 are important implementations of second-order algorithms while the latter is the first cited meta package in the CRAN's task view for machine learning, https://CRAN.R-project.org/view=MachineLearning, as well as the dependency for some of the other packages tested. Restricting to regression analysis left us with 49 package::algorithm pairs in 2019 and 60 package::algorithm pairs in 2020.

Phase 2 - Review of packages and development of a benchmarking template

From documentation and example code, we learned that not all packages selected by the automated search fit the scope of our research. Some have no function to generate neural networks. Others were not regression neural networks of the perceptron type or were only intended for very specific purposes. Basically, each package was inspected 3 times.

- 1. The discard/not discard phase: depending on the package, this could be decided as easily as looking at the DESCRIPTION file or having to go through the process of making the code and seeing the results.
- 2. Benchmarking with template that was developed in 2019 and encapsulated in the functions of 2020, keeping notes of whether or not the package was easy to use.

Templates for Testing Accuracy and Speed

As we inspected the packages, we developed a template for benchmarking. The structure of this template (for each package) is as follows:

- 1. Set up the test environment loading of packages, setting working directory and options;
- 2. Summary of tested datasets;
- 3. Loop over datasets:
 - a. setting parameters for a specific dataset,
 - b. selecting benchmark options,
 - c. training a neural network with a tuned functions for each package,
 - d. calculation of convergence metrics (RMSE, MAE, WAE),
 - e. plot each training over one initial graph, then plot the best result,
 - f. add results to the appropriate existing record (*.csv file) and
 - g. clear the environment for next loop.
- 4. Clearing up the environment for the next package. It is optional to print warnings.

To simplify this process, we developed tools in the NNbenchmark package, of which the first version was created as part of GSoC 2019. In GSoC 2020, 3 functions encapsulating the template, that had been made generic with an extensive use of the incredible do.call function, were added:

- 1. In trainPredict_1mth1data a neural network is trained on one dataset and then used for predictions, with several utilities. Then, the performance of the neural network is exported, plotted and/or summarized.
- 2. trainPredict_1data serves as a wrapper function for trainPredict_1mth1data for multiple methods.
- 3. trainPredict_1pkg serves as a wrapper function for trainPredict_1mth1data for multiple datasets.

A function for the summary of accuracy and speed, NNsummary, was also added. The package repository is https://github.com/pkR-pkR/NNbenchmark, with package templates in https://github.com/pkR-pkR/NNbenchmarkTemplates.

3. summarizing or re-reviewing the tested packages utility functions & documentation

Ease of Use Scoring

We define an ease-of-use measure based on what we considered a user would need when using a neural network package for nonlinear regression, namely, utility functions and sufficient documentation.

- 1. Utilities (1 star)
 - a. a predict function exists
 - b. scaling capabilities exist
- 2. Sufficient documentation (2 stars)
 - a. the existence of useful example/vignette = (1 star)
 - clear, with regression = 2 points

- unclear, examples use iris or are for classification only = 1 point
- no examples = 0 points
- b. input/output is clearly documented, e.g., what values are expected and returned by a function = (1 star)
 - clear input and output = 2 points
 - only one is clear = 1 point
 - both are not documented = 0 points

The ease-of-use measure ranges from 0 to 3 stars.

Phase 3 - Collection of and analysis of results

Results collection

Looping over the datasets using each package template, we collected results in the relevant package directories in the templates repository.

Analysis

To rank how well a package converged and its speed, we developed the following method:

- 1. The results datasets are loaded into the R environment as one large list. The dataset names, package:algorithm names and all 10 run numbers, durations, and RMSE are extracted from that list
- 2. For the duration score (DUR), the duration is averaged by dataset. 3 criteria for the RMSE score by dataset are calculated:
 - a. The minimum value of RMSE for each package:algorithm as a measure of their best performance
 - b. The median value of RMSE for each package:algorithm as a measure of their average performance, without the influence of outliers
 - c. The spread of the RMSE values for each package which is measured by the difference between the median and the minimum RMSE (d51)
- Then, the ranks are calculated for every dataset and the results are merged into one wide dataframe.
 - a. The duration rank only depends on the duration.
 - b. For minimum RMSE values, ties are decided by duration mean, then the RMSE median
 - c. For median RMSE values, ties are decided by the RMSE minimum, then the duration mean
 - d. The d51 rank only depends on itself
- 4. A global score for all datasets is found by a sum of the ranks (of duration, minimum RMSE, median RMSE, d51 RMSE) of each package:algorithm for each dataset
- 5. The final table is the result of ranking by the global minimum RMSE scores for each package:algorithm

To rank how easy or not a package was to use (TO BE DISCUSSED FURTHER): - Functionality (util): scaling, input, output, trace - Documentation (docs): examples, structure/functions, vignettes

Results

Table 1 gives the RMSE and time score per package and per algorithm. The full list of score is given in Table 2 in Appendix C.

Tables

(ALSO: THE FOLLOWING IS SIMPLY ALPHABETIC LIST FOR ALL TESTED, I WILL DIVIDE THE TABLE INTO 4: 2nd ORDER always recommended, 1st ORDER recommended, 1st ORDER not recommended, untested packages)

Discussion and Recommendations

The following is a list of packages we included in this study, with brief descriptions.

- 1. AMORE (Limas et al., 2020),
- 2. ANN2 (Lammers, 2020),
- 3. **appnn** (Família et al., 2015),
- 4. autoencoder (Dubossarsky and Tyshetskiy, 2015),
- 5. automl (Boulangé, 2020),
- 6. BNN (Jia, 2018),
- 7. brnn (Rodriguez and Gianola, 2020),
- 8. Buddle (Kim, 2020),
- 9. CaDENCE (Cannon, 2017a),
- 10. cld2 (Ooms, 2018),
- 11. cld3 (Ooms, 2020),
- 12. condmixt (Carreau, 2020),
- 13. DamiaNN (Siniakowicz, 2016),
- 14. **deep** (Mayer, 2019),
- 15. deepdive (Balakrishnan, 2020),
- 16. deepnet (Rong, 2014),
- 17. deepNN (Taylor, 2020),
- 18. DNMF (Jia and Zhang, 2015),
- 19. elmNNRcpp (Mouselimis and Gosso, 2020),
- 20. ELMR (Petrozziello, 2015),
- 21. EnsembleBase (Mahani and Sharabiani, 2016),
- 22. evclass (Denoeux, 2017),
- 23. gamlss.add (Stasinopoulos et al., 2020),
- 24. gcForest (Jing, 2018),
- 25. GMDH (Dag and Yozgatligil, 2016),
- 26. GMDH2 (Dag et al., 2019),
- 27. GMDHreg (Tilve, 2020),
- 28. gnn (Hofert and Prasad, 2020),
- 29. grnn (Chasset, 2013a),
- 30. h2o (LeDell et al., 2020),
- 31. hybridEnsemble (Ballings et al., 2015),
- 32. isingLenzMC (Suzen, 2016),
- 33. keras (Allaire and Chollet, 2020),
- 34. kerasR (Arnold, 2017),
- 35. leabRa (Titz, 2017),
- 36. learNN (Quast, 2015),
- 37. LilRhino (Barton, 2019),
- 38. minpack.lm (Elzhov et al., 2016),
- 39. MachineShop (Smith, 2020),
- 40. monmlp (Cannon, 2017b),
- 41. neural (Nagy, 2014),
- 42. neuralnet (Fritsch et al., 2019),
- 43. NeuralNetTools (Beck, 2018),
- 44. NeuralSens (Portela González et al., 2020),
- 45. NlinTS (Hmamouche, 2020),
- 46. nlsr (Nash and Murdoch, 2019),
- 47. nnet (Ripley, 2020),

 Table 1: Result from Tested Packages

	Individual score			Global score	
Package	Util	Doc	Algorithm	Time	RMSI
	1	3.0	ADAPTgd	10	34
AMORE	1	3.0	ADAPTgdwm	17	25
AMORE	1	3.0	BATCHgd	39	40
	1	3.0	BATCHgdwm	40	39
ANN2	2 2	3.0 3.0	adam	16 14	33 28
AININZ	2	3.0	rmsprop sgd	12	41
	1	3.0	trainwgrad_adam	50	18
automl	1	3.0	trainwgrad_RMSprop	47	26
	1	3.0	trainwpso	57	42
brnn	2	4.0	Gauss-Newton	8	13
	2	3.0	optim(BFGS)	46	10
CaDENCE	2	3.0	pso_psoptim	54	54
	2	3.0	Rprop	56	51
caret	2	3.0	avNNet_nnet_optim(BFGS)	9	22
	2	3.0	adam	32	45
deepdive	2	3.0	gradientDescent	52	58
1	2	3.0	momentum	53	56 52
	2	3.0	rmsProp	34	53
deepnet	1	3.0	BP	23	18
elmNNRcpp	2	3.0	ELM	1	59
ELMR	2	3.0	ELM	2	60
EnsembleBase	1	1.0	nnet_optim(BFGS)	5	12
h2o	2	2.0	first-order	51	11
	2	0.0	adadelta	60	47
	2	0.0	adagrad	58	36
Iranas	2 2	0.0	adam adamax	42 48	35 23
keras	2	0.0	nadam	44	36
	2	0.0	rmsprop	37	52
	2	0.0	sgd	48	43
MachineShop	1	3.0	nnet_optim(BFGS)	6	4
minpack.lm	1	3.5	Levenberg-Marquardt	13	24
	2	3.5	optimx(BFGS)	26	9
monmlp	2	3.5	optimx(Nelder-Mead)	32	46
	1	3.0	backprop	37	48
	1	3.0	rprop-	21	21
neuralnet	1	3.0	rprop+	18	20
	1	3.0	sag	41	38
	1	3.0	slr	31	30
nlsr	1	4.0	NashLM	18	1
nnet	1	3.0	optim (BFGS)	3	3
qrnn	2	3.0	nlm()	28	15
radiant.model	2	2.0	nnet_optim(BFGS)	11	7
rminer	2	3.5	nnet_optim(BFGS)	14	2
	2	3.0	BackpropBatch	43	49
	2	3.0	BackpropChunk BackpropMomentum	26 25	29
	2 2	3.0 3.0	BackpropMomentum BackpropWoightDocay	25 29	30 32
RSNNS	2	3.0	BackpropWeightDecay Quickprop	45	52 57
	2	3.0	Rprop	24	16
	2	3.0	SCG	30	17
	2	3.0	Std_Backpropagation	22	27
	2	2.0	SemiSmoothNewton	7	49
snnR			nnet_optim(BFGS) 4		6
snnR traineR	1	2.5	nnet_optim(BFGS)	4	6
	1	2.5	optim(BFGS)	35	4
traineR	1 1	4.0 4.0	optim(BFGS) optim(CG)	35 59	4 8
	1	4.0	optim(BFGS)	35	4

```
48. nnetpredint (Ding, 2015),
49. nnfor (Kourentzes, 2019),
50. nntrf (Aler and Valls, 2020),
51. nnli2bRcpp (Nikolaidis, 2020),
52. onnx (Tang and ONNX Authors, 2018),
53. OptimClassifier (Perez-Martin et al., 2020),
54. OSTSC (Dixon et al., 2017),
55. pnn (Chasset, 2013b),
56. polyreg (Matloff et al., 2020),
57. predictoR (with contributions from Diego Jimenez A. and D., 2020),
58. qrnn (Cannon, 2019),
59. QuantumOps (Resch, 2020),
60. quarrint (Barthelemy et al., 2016),
61. radiant.model (Nijs, 2020),
62. rasclass (Wiesmann and Quinn, 2016),
63. rcane (Suresh et al., 2018),
64. regressoR (Rodriguez R., 2019),
65. rminer (Cortez, 2020),
66. rnn (Quast and Fichou, 2020),
67. RSNNS (Bergmeir, 2019),
68. ruta (Charte et al., 2019),
69. simpleNeural (Dernoncourt, 2020),
70. snnR (Wang et al., 2017),
71. softmaxreg (Ding, 2016),
72. Sojourn. Data (Hibbing and Lyden, 2019),
73. spnn (Ebrahimi, 2020),
74. TeachNet (Steinbuss, 2018),
75. tensorflow (Allaire and Tang, 2020),
76. tfestimators (Allaire et al., 2018),
77. trackdem (Bruijning et al., 2020),
78. TrafficBDE (Chatzopoulou et al., 2018),
79. tsensembler (Cerqueira et al., 2017),
80. validann (Humphrey, 2017),
81. zFactor (Reyes, 2019).
```

Recommended: 2nd order algorithms

Out of all the algorithms, the following second algorithms generally performed better in terms of convergence despite being set to a much lower number of iterations, to be precise a fifth or even less, than the first-order algorithms.

An important finding is that 11 out of 15 of these package::algorithms use the algorithms included in optim from stats. 2 of them, CaDENCE's BFGS (Cannon, 2017a) and validann's BFGS and L-BFGS-B (Humphrey, 2017), do so with no intermediate package. However, it is not clearly stated in CaDENCE's documentation that optim's BFGS algorithm is used and not one of the other algorithms. Furthermore, the mention of Nelder-Mead in the documentation might lead users to believe that optim's Nelder-Mead is used instead. Speed and variation between results are also not as good as other package's that use optim. This could be because CaDENCE is intended for probabilistic nonlinear models with a full title of "Conditional Density Estimation Network Construction and Evaluation". On the other hand, validann is clearly a package that allows a user to use all optim's algorithms. validann::L-BFGS-B ranks lower than validann::BFGS in just about everything for most runs, despite the former being more sophisticated. This is probably due to our efforts to harmonize parameters under-utilizing the possibilities of the L-BFGS-B algorithm. Both CaDENCE and validann's BFGS are outperformed by nnet, especially in terms of speed.

nnet (Ripley, 2020) differs from the two packages because it uses the C code from optim

(converted earlier from Fortran) instead of calling optim from R. It also only implements the BFGS algorithm. This could be what allows it to be faster. nnet is only beaten by the Extreme Learning Machine (ELM) algorithms in terms of speed. However, there is a larger variation between results (see the RMSEd51.score in Appendix C) in comparison to validann::BFGS. Most likely, the different default values are the cause of this. For instance, nnet uses a range of initial random weights of 0.7 while validann uses a value of 0.5. In spite of these results, the real reason most authors or users are likely to choose nnet is because it ships with base R and is even mentioned as the very first package in CRAN's task view for machine learning.

Our research found that 6 of the 11 packages that use optim do so through nnet. Moreover, 8 packages for neural networks, though not tested, use nnet. The total number of nnet dependencies found through a search through the offline database of CRAN with RWsearch came up with 136 packages, although some might be using nnet for the multinomial log-linear models, not neural networks. As for the ones we tested, there were several similarities and differences. The packages that use nnet for neuralnetworks are often meta packages with a host of other machine learning algorithms. caret (?), also mentioned in the taskview, boasts 238 methods with around 13 different neural network packages with somewhat deceivingly simple name of "Classification and Regression Training". It has many pre-processing utilities available, as well as other tools.

EnsembleBase (Mahani and Sharabiani, 2016) maybe useful for those who wish to make ensembles and test a grid of parameters although the documentation. MachineShop (Smith, 2020) has 51 algorithms, with some additional information about the response variable types in the second vignette, functions for preprocessing and tuning, performance assessment, and presentation of results. radiant.model (Nijs, 2020) has an unchangeable maxit of 10000 in the original package. Perhaps the author thought this was reasonable as source of the algorithm, nnet, is quite fast. We changed this to harmonize the parameters. rminer (Cortez, 2020) is the only package dependant on nnet that ranks above nnet at number 2 for minimum RMSE, and even number 1 in some runs. It also ranks number 1 on the other accuracy measures (median RMSE, minimum MAE, minimum WAE) and is only behind deepdive and minpack.lm in terms of results that are consistent and do not vary (RMSEd51). The difference is probably from the change of maximum allowable weights in rminer to 10000 from 1000 in nnet, which is also probably the reason it its fits are slower. traineR (?) claims to unify the different methods of creating models between several learning algorithms.

Something worth noting is that nnet and validann do not have external normalization, and it is especially recommended for validann . However, some of the packages dependent on nnet do have this utility and it is included in the scoring for ease of use. With NNbenchmark, this is done through setting scale = TRUE in the function prepare.ZZ. Note that scaling might lead to complicating the constraints which is not always worth it. Regardless, users might want to have the utility and most likely want a clear explanation of the method chosen to center the variables. Scaling is one of the things that <code>optimx</code> (?) incorporates in an attempt to make a more useful version of optim that only allows for changing the sign of the function which might not even be considered as scaling (Nash, 2014).

Not Recommended: 2nd order algorithms

Recommended: 1st order algorithms

validann optim CG -slow RSNNS SCG h2o back-propagation RSNNS Rprop ANN2 adam CaDENCE Rprop -SLOW deepnet BP AMORE ADAPTgdwm AMORE ADAPTgd ANN2 sgd automl trainwgrad ANN2 rmsprop RSNNS BackpropChunk RSNNS BackWeightDecay RSNNS Std_Backpropagation RSNNS BackpropMomentum automl trainwpso validann optim NelderMead snnR Semi Smooth Newton RSNNS BackpropBatch validann optim SANN monmlp optimx Nelder Mead

Not recommended: 1st order algorithms <- DISCUSS CUTOFF

By package ELMR, elmNNRcpp - fast ELM algorithms. Unfortunately, can't finetune, does not converge well. neuralnet: a large ammount of iterations, slow, erratic failures tensorflow: NOT EASY TO USE, subsequently keras, tfestimators, ruta ... user needs to understand the language However, advanced users might be able to highly specify a neural network to their needs (customization?)

By algorithm: neuralnet rprop+ neuralnet rprop- neuralnet slr - once ranked well with 100000 iterations AMORE BATCHgd CaDENCE pso psoptim - need to reconfigure? elmN-NRcpp - fast, no iterations RSNNS Quickprop (?) AMORE BATCHgdwm tensorflow MomentumOptimizer tensorflow AdamOptimizer ELMR - fast, no iterations tensorflow GradientDescentOptimizer keras rmsprop keras adagrad keras sgd keras adadelta tensorflow AdagradOptimizer keras adam tensorflow FtrlOptimizer neuralnetwork sag tensorflow AdadeltaOptimizer neuralnet backprop - note, might not actually reflect standings, somehow from template to template the learning rate disappeared. Will fix this in future runs

Untested => TO DO - LIST

Conclusion and perspective

??JN: Can we start to put in some major findings? i.e., important positive findings, big negatives?

Positives (no particular order)

- 1. the existence of algorithms that converge well
- 2. nnet, which uses optim's BFGS, is already often chosen to represent neural networks for packages that are either a collection of independent machine learning algorithms, ensembles, or even applications in a field such as ...
- 3. the wide variety of neural networks available to users of R, from libraries of other programming languages to many different types of algorithms, hyperparameters, and uses

Negatives (no particular order)

- 1. bad documentation
- 2. the lack of packages that expand the number of unique second order algorithms. (Perhaps even the existence of what can be considered as repetitive packages?)
- 3. the lack of clear default values, or bad default values

Future work

As the field of neural networks continue to grow, there will always be more algorithms to validate. For current algorithms in R, our research should be extended to encompass more types of neural networks and their data formats (classifier neural networks, recurrent neural networks, and so on). Different rating schemes and different parameters for package functions can also be tried out.

- The dreamed NN package: Recommendation to package authors
- Conclusion

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Appendix

Appendix A

Consider a set of observations y_i and its corresponding predictions \hat{y}_i for i = 1, ..., n. The three metrics used were:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|, \ RMSE = \frac{1}{n} \sqrt{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}, \ WAE = \frac{1}{n} \max_{i=1,\dots,n} |y_i - \hat{y}_i|.$$

These values represent the absolute, the squared and the maximum norm of residual vectors.

Appendix B

We define three smooth functions for Simon Wood's test dataset

$$f_0 = 5 * \sin(2\pi x), f_1 = exp(3 * x) - 7f_2 = 0.5x^{11} * (10(1 - x))^6 - 10(10 * x)^3 * (1 - x)^{10},$$

$$f_3 = 15 \exp(-5|x - 1/2|) - 6, f_4 = 2 - 1_{(x < = 1/3)}(6 * x)^3 - 1_{(x > = 2/3)}(6 - 6 * x)^3 - 1_{(2/3 > x > 1/3)}(8 + 2\sin(9 * (x - 1/3))^3) = 0.5x^{11} * (10(1 - x))^6 - 10(10 * x)^3 * (1 - x)^{10},$$

Appendix C

Appendix D

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 Table 2: All convergence scores per package:algorithm

Input parameter			Score				
Num	Input format	Maxit	Learn. rate	RMSE median	RMSE d51	MAE	WAE
1	x & y	1000	0.01	24	8	26	19
2	x & y	1000	0.01	22	28	17	26
3	x & y	10000	0.1	37	24	42	31
4	x & y	10000	0.1	33	14	36	27
5	x & y	1000	0.01	27	26	28	23
6	x & y	1000	0.01	26	33	27	22
7	x & y	1000	0.01	36	20	35	28
8	x & y	1000	0.01	20	35	16	19
9	x & y	1000	0.01	31	50	29	38
10	x & y	1000	-	40	49	40	37
11	x & y	200	-	11	9	12	11
12	x & y	200	-	28 56	48	23	39
13 14	x & y	1000 1000	0.01	56 54	56 60	54 52	56 58
15	x & y x & y	200	-	13	30	14	12
	-						
16	x & y	10000	0.4	41	1	37	44
17	x & y	10000	0.8	57	2	57	53
18	x & y	1000	0.8	52	3	53	51
19 20	x & y	1000	0.8 0.8	45 18	4 38	47 24	50 17
	x & y	1000	0.8				
21	x & y	-	-	59	55	59	59
22	fmla & data	-	-	60	54	60	60
23	x & y	200	-	15	33	15	15
24 25	"y" & data	10000	0.01 0.1	7 48	7 27	8 51	8 41
	x & y	10000					
26	x & y	10000	0.1	42	51	41	33
27	x & y	10000	0.1	28	44	30	25
28	x & y	10000	0.1	16	19	20	16
29 30	x & y x & y	10000 10000	0.1 0.1	38 54	58 57	39 55	40 54
	•		0.1				
31 32	x & y fmla & data	10000 200	0.1	44 9	47 20	43 10	43 7
33	full fmla & data	200	_	18	5	19	14
34	x & y	200	_	10	17	9	10
35	x & y	10000	-	46	46	43	47
36	fmla & data	100000	0.001	50	11	48	45
37	fmla & data	100000	-	21	41	22	18
38	fmla & data	100000	-	23	40	21	24
39	fmla & data	100000	-	50	59	46	52
40	fmla & data	100000	-	38	37	38	46
41	full fmla & data	200	-	3	16	3	6
42	x & y	200	-	2	17	2	3
43	x & y	200	-	14	22	7	35
44 45	"y" & data	200 200	-	8 1	32 6	11 1	9 1
	fmla & data		-				
46	x & y	10000	0.1	47	25	50	49
47	x & y	1000	-	34	41	32	34
48	x & y	1000	-	35	38	34	30
49 50	x & y x & y	1000 10000	-	30 58	43 36	33 58	32 57
	-		_				
51	x & y	1000	-	24	51	25	29
52 52	x & y	1000	- 0.1	16	22	18	19
53 54	x & y x & y	1000 200	0.1	32 48	30 13	31 49	36 47
5 4 55	fmla & data	200	-	5	15	6	2
56	x & y	200	_	4	11	4	5
57	x & y x & y	1000	-	6	10	5	4
58	x & y	200	_	12	29	13	12
		10000		43	45	45	41
59	x & y	10000	-				

Table 3: Review of Ommitted Packages

No	Name (package)	Category	Comment
1	appnn	AP	This package provides a feed forward neural network to predict the amyloidogenicity propensity of polypeptide sequences
2	autoencoder	AP	This package provides a sparse autoencoder, an unsupervised
3	BNN	RE*	algorithm that learns useful features from the data its given This package uses a feed forward neural network to perform regression as provided in the examples, however, it is unclear whether it fits the form of perceptron that is the scope of our research. Moreover, it states that it is intended for variable selection. Although how exactly the package would be used to do so isn't accessible in the package, especially considering the source code is based on .c code that users of R might not understand. It's performance is slow, which may have to do with the 100.000 iterations it needs, although quite accurate for simple datasets.
4	Buddle	RE**	(errors)
5	cld2	00 A.D.	
6 7	cld3 condmixt	AP AP	
8	deep	CL	
9	DALEX2	00	removed keyword, included in 2019
10	DamiaNN	RE**	(errors) exported functions, still doesn't work
11	DChaos	??	removed keyword for some reason, need to check out!
12	deepNN	RE**	(errors) I/O weird, ragged vector array
13	DNMF	AP	
14	evclass	CL	
15 16	gamlss.add	RE 00	there is some code but dist not appropriate
17	gcForest GMDH	TS	
18	GMDH2	CL	
19	GMDHreg	RE*	
20	grnn	RE**	
21	hybridEnsemble	??	
22	isingLenzMC	AP	
23 24	leabRa learNN	?? ??	
25	LilRhino	AP	
26	neural	CL	
27	NeuralNetTools	UT	tools for neural networks
28	NeuralSens	UT	tools for neural networks
29	NlinTS	TS	Time Series
30	nnetpredint	UT	confidence intervals for NN
31 32	nnfor nntrf	TS UT	Times Series, uses neuralnet
33	onnx	O I	provides an open source format
34	OptimClassifier		choose classifier parameters, nnet
35	OSTSC		solving oversampling classification
36	passt		
36	pnn		Probabilistic
37	polyreg		polyregression as alternative to NN
38 39	predictoR ProcData		shiny interface, neuralnet
40	QuantumOps		classifies MNIST, Schuld (2018), removed keyword, in 2019
41	quarrint		specified classifier for quarry data
42	rasclass		classifier for raster images, nnet?
43	rcane		
44	regressoR		a manual rich version of predictoR
45	rnn PTautTaala		Recurrent
46 47	RTextTools ruta		
48	simpleNeural		
49	softmaxreg		
50	Sojourn.Data		sojourn Accelerometer methods, nnet?
51	spnn		classifier, probabilistic
52 52	studyStrap		-1:G
53 54	TeachNet		classifier, selfbuilt, slow
54 55	tensorflow tfestimators		
56	trackdem		classifier for particle tracking
57	TrafficBDE	RE*	
58	tsfgrnn		
59	yap		
60	yager	RE*	/ 1119 / (1 1 1
61	zFactor	AP	'compressibility' of hydrocarbon gas