A review of R neural network packages (with NNbenchmark): accuracy and ease of use

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Abstract

For the last 30 years, neural networks have evolved from an academic topic to a common tool in scientific computing. Following this trend, CRAN has chosen to host many packages that claim to provide neural network modeling. Our count in May 2020 is roughly 70 packages. How accurate and reliable are these packages and their documentation? Are there packages that perform better in terms of accuracy? Are some better suited to beginners while others require expert knowledge? Do these packages provide the features found in some dedicated proprietary software?

This paper is, to our knowledge, the first attempt to test this rather large number of packages against a few datasets with different levels of complexity, and to benchmark and rank them with certain metrics. We have restricted our evaluation to regression algorithms applied on the one-hidden layer perceptron and ignored those for classification or other specialized purposes. This left us with 49 package::algorithm pairs in 2019 and 60 package::algorithm pairs in 2020. The criteria used in our benchmark were: (i) the accuracy, i.e. the ability to find the global minima on 13 datasets, measured by the Root Mean Square Error (RMSE) in a limited number of iterations; (ii) the speed of the training algorithm; (iii) the availability of helpful utilities; (iv) and the quality of the documentation.

All package::algorithm pairs were given a score for each criterion and ranked in a global table. Overall, 15 package::algorithm pairs are considered accurate and reliable and can be recommended for daily usage. 45 algorithms should be avoided as they are either less accurate, slow, difficult to handle, or have poor or no documentation.

Our codes, templates, and the NNbenchmark package used to test each package::algorithm pair are publicly available at the address https:://github.com/pkR-pkR/NNbenchmark. These can be used by the package authors and others to verify the metrics and eventually improve their own package or code. Finally, we provide some hints and features to guide the development of an idealized neural network package for R.

Introduction

(PK) For the last 30 years, neural networks have evolved from an academic topic to a common tool in scientific computing. As a convenience in the general conversation, the same term is used in a generic manner (for a shortcut to) for different model structures and applications: multilayer perceptron for regression, multilayer perceptron for classification, multilayer perceptron for specialized applications (mixture of models, conditional distribution, etc), recurrent neural network for autoregressive time series (NARMAX models), convolutional neural networks for dimension reduction and pattern recognition, deep neural networks for image or voice recognition.

Most of the above types of neural networks can be found in R packages hosted on CRAN but without any warranty about the quality or the accuracy of the calculation, since CRAN has no tools to check them. Package users have to believe package authors who are assumed to have selected the best algorithms and tuned them with the appropriate hyperparameters. This is rather problematic with neural networks as many poor algorithms have been mentioned in the literature, and are probably implemented in a few packages.

The goal of this paper is to verify the accuracy and the ease of use (including the quality of the documentation) of the packages hosted on CRAN that supply the most common neural network structure + algorithm, i.e. the multilayer perceptron for regression purpose.

(SB) The R Project for Statistical Computing (www.r-project.org), as any opensource platform, relies on its contributors to keep it up to date. Neural networks, based on the brain's own connections system, are a class of models in the growing field of machine learning forwhich R has a number of tools. Previously, neural networks could be considered more theory than practice, partly because the algorithms used are computationally demanding.

A neural network algorithm requires complicated calculations to improve the model control parameters. As with other optimization problems, the gradient of the chosen cost function that indicates the lack of suitability of the model is sought. This lets us improve the model by changing the parameters in the negative gradient direction. Parameters for the model are generally obtained using part of the available data (a training set) and tested on the remaining data. Modern software allows much of this work, including approximation of the gradient, to be carried out without a large effort by the the user.

This process can generally be made more efficient if we can also approximate second derivatives of the cost function, allowing us to use its curvature via the Hessian matrix. There are a large number of approaches, of which quasi-Newton algorithms are perhaps the most common and useful. Within this group, methods based on the Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm for updating the Hessian approximation (or its inverse) provide several well-known examples. In conducting this study, we believed that these second-order algorithms would perform better than first-order methods.

Regardless of our belief, we wished to be able to conduct a thorough examination of these training algorithms in R. There are many packages, but barely any information to allow comparison. Our work, reported here, aims to provide a framework for benchmarking neural network packages. We restrict our examination to packages for R, and in this report focus on those that provide neural networks of the perceptron type, that is, one input layer, one normalized layer, one hidden layer with a nonlinear activation function that is usually tanh(), and one output output layer.

Methodology

??IN: **************

In working on material below, I think we need to provide some explanation of goals - What does "convergence" mean in our context? - What do we mean by RMSE, other measures? Should define here for later use. - What do we mean by "performance"? Other goals?

Our research process was divided into 3 phases.

Phase 1 - Preparation

Datasets => NEED TO BE FINISHED??

All the datasets we use cannot generally be modeled using a non-iterative calculation such as Ordinary Least Squares. Varying levels of difficulty in modeling the different data sets are intended to allow us to further classify different algorithms and the packages that implement them. Sonja Surjanovic and Derek Bingham of Simon Fraser University created a useful website from which three of the multivariate datasets were drawn. We note the link, name and difficulty level of the three datasets:

- http://www.sfu.ca/~ssurjano/fried.html (Friedman average)
- http://www.sfu.ca/~ssurjano/detpep10curv.html (Dette medium)
- http://www.sfu.ca/~ssurjano/ishigami.html (Ishigami high)

The other multivariate dataset, Ref153, was taken from ...

Three of the univariate datasets we used were taken from a website of the US National Institute for Standards and Technology (NIST): https://www.itl.nist.gov/div898/strd/

nls/nls_main.shtml. (Gauss1 - low; Gauss2 - low; Gauss3 - average)

Univariate datasets Dmod1, Dmod2 are from ...

Dreyfus1 is a pure neural network which has no error. This can make it difficult for algorithms that assume an error exists. Dreyfus2 is Dreyfus1 with errors. NeuroOne from

• • •

Wood ...

Packages

Using **RWsearch** (Kiener, 2020) we sought all were able to automate the process. All packages that have "neural network" as a keyword in the package title or in the package description were included. Packages **nlsr**, **minpack.lm**, **caret** were added because ...

Phase 2 - Review of packages and development of a benchmarking template

From documentation and example code, we learned that not all packages selected by the automated search fit the scope of our research. Some have no function to generate neural networks. They are simply meta-packages. Others were not regression neural networks of the perceptron type or were only intended for very specific purposes.

Template => TO REVISE AFTER 2020 CODE

As we inspected the packages, we developed a template for benchmarking. The structure of this template (for each package) is as follows:

- (1) Set up the test environment loading of packages, setting working directory and options;
- (2) Summary of datasets;
- (3) Loop over datasets: (a) setting parameters for a specific dataset (b) selecting benchmark options (c) training a neural network with a tuned functions for each package (d) calculation of RMSE and MAE (??definition, reference) (e) plot each training over one initial graph, then plot the best result (f) add results to the appropriate existing record (*.csv file) and (g) clear the environment for next loop; and
- (4) Clearing up the environment for the next package. (5) It is optional to print warnings.

To simplify this process, we developed tools in the NNbenchmark package, of which the first version was created as part of the 2019 GSoC activity and later refined in the 2020 initiative. The package repository is https://github.com/pkR-pkR/NNbenchmark, with package templates in https://github.com/pkR-pkR/NNbenchmarkTemplates).

Phase 3 - Collection of and analysis of results

Results collection

Looping over the datasets using each package template, we collected results in the relevant package directories in the templates repository.

Analysis

To rank the how well a package converged and its speed, we developed the following method:

- 1. The results datasets are loaded into the R environment as one large list. The dataset names, package:algorithm names and all 10 run numbers, durations, and RMSE are extracted from that list
- 2. For the duration score (DUR), the duration is averaged by dataset. 3 criteria for the RMSE score by dataset are calculated:
- a. The minimum value of RMSE for each package:algorithm as a measure of their best performance

- b. The median value of RMSE for each package:algorithm as a measure of their average performance, without the influence of outliers
- c. The spread of the RMSE values for each package which is measured by the difference between the median and the minimum RMSE (d51)
- 3. Then, the ranks are calculated for every dataset and the results are merged into one wide dataframe.
- a. The duration rank only depends on the duration.
- b. For minimum RMSE values, ties are decided by duration mean, then the RMSE median
- c. For median RMSE values, ties are decided by the RMSE minimum, then the duration mean
- d. The d51 rank only depends on itself
- 4. A global score for all datasets is found by a sum of the ranks (of duration, minimum RMSE, median RMSE, d51 RMSE) of each package:algorithm for each dataset
- 5. The final table is the result of ranking by the global minimum RMSE scores for each package:algorithm
- 6. In addition to the previous metrics, two other convergence metrics have been considered: the Mean Absolute Error (MAE) and the Worst Absolute Error (WAE), see Appendix. The ranking on those two metrics may help distinguish packages with close RMSE values. However, we do not choose the MAE for overall ranking as there is no consensus in the literature, see e.g. (Willmott and Matsuura, 2005; Chai and Draxler, 2014).

To rank how easy or not a package was to use (TO BE DISCUSSED FURTHER): - Functionality (util): scaling, input, output, trace - Documentation (docs): examples, structure/functions, vignettes

Results

Tables (NOTE: FINAL MEASURE FOR CONVERGENCE - RMSE RANKS? OR A COMBINATION OF OTHER MEASURES? As in Christophe's recent email: L1 MAE(), L2 RMSE(), Linfinity (WAE)) -> see Appendix

(ALSO: THE FOLLOWING IS SIMPLY ALPHABETIC LIST FOR ALL TESTED, I WILL DIVIDE THE TABLE INTO 4: 2nd ORDER always recommended, 1st ORDER recommended, 1st ORDER not recommended, untested packages)

Table 1: Review of Tested Packages

validann::

No	Package::Function	Algorithm	RMSE	DUR	UTIL	DOCS
1	AMORE	1. ADAPTgd	TUVIOL	Den	CIL	2000
	::train	2. ADAPTgdwm				
		3. BATCHgd				
		4. BATCHgdwm				
2	ANN2	5. adam				
	::neuralnetwork	6. rmsprop				
		7. sgd				
3	automl	8. trainwgrad.adam				
	::automl_train_manual	9. trainwgrad.RMSprop				
		10. trainwpso				
4	brnn::brnn	11. Gauss-Newton				
5	CaDENCE	12. optim(BFGS)				
	::cadence.fit	13. pso::psoptim				
-	A NINI (14. Rprop				
6	caret::avNNet	15. nnet::optim(BFGS)				
7	deepdive	16. adam17. gradientDescent				
	::deepnet	18. momentum				
		19. rmsProp				
8	deepnet::nn.train	20. BP				
9	elmNNRcpp::elm_train	21. ELM				
10	ELMR::OSelm_train.formula	22. ELM				
11	EnsembleBase::Regression.Batch.Fit	23. nnet::optim(BFGS)				
12	h2o::deeplearning	24.				
13	keras	25. adadelta				
	::fit	26. adagrad				
		27. adam				
		28. adamax				
		29. nadam				
		30. rmsprop				
		31. sgd				
14	MachineShop::fit	32. nnet::optim(BFGS)				
15	minpack.lm::nlsLM	33. LM				
16	monmlp::fit	34. BFGS				
17	monmlp::fit neuralnet::	35. Nelder-Mead				
17	::neuralnet::	36. backprop 37. rprop-				
	ieuraniet	38. rprop+				
		39. sag				
		40. slr				
18	nlsr::nlxb	41. NashLM				
19	nnet::nnet	42. optim(BFGS)				
20	qrnn::qrnn.fit	43. nlm()				
21	radiant.model::radiant.model	45. nnet::optim(BFGS)				
22	rminer::fit	46. nnet::optim(BFGS)				
23	RSNNS::	47. BackpropBatch				
	RSNNS::	48. BackpropChunk				
	RSNNS::	49. BackpropMomentum				
	RSNNS::	50. BackpropWeightDecay				
	RSNNS::	51. Quickprop				
	RSNNS::	52. Rprop 53. SCG				
	RSNNS:: RSNNS::	54. Std-Backpropagation				
24	snnR	55.				
25	traineR	55.				
26	validann::	56. BFGS				
_3	validann::	57. CG				
	validann::	58. L-BFGS-B				
The R	Journal XX/YY, AAAA	59. Nelder-Mead	ISSN 20	73-4859		
	validann	60 SANNI				

60. SANN

(THE FOLLOWING IS JUST AN ALPHABETICALLY ORDERED LIST OF CURRENTLY UNTESTED PACKAGES)

Table 2: Review of Ommitted Packages

No	Name (package)	Category	Comment			
1	appnn	AP	This package provides a feed forward neural network to predict the amyloidfogenicity propensity of polypeptide sequences			
2	autoencoder	AP	are unity to take of persons of persons are sequences			
3	BNN	RE*				
4	Buddle	RE**	(errors) even performance on examples is bad			
5	cld2	00				
6	cld3	AP				
7	condmixt	AP				
8	deep	CL				
9	DALEX2	00 DE##	removed keyword, included in 2019			
10	DamiaNN	RE**	(errors) exported functions, still doesn't work			
11 12	DChaos	?? RE**	removed keyword for some reason, need to check out!			
13	deepNN DNMF	AP	(errors) I/O weird, ragged vector array			
14	evclass	CL				
15	gamlss.add	RE	there is some code but dist not appropriate			
16	gcForest	00				
17	GMDH	TS				
18	GMDH2	CL				
19	GMDHreg	RE*				
20	grnn	RE**				
21	hybridEnsemble	??				
22	isingLenzMC	AP				
23	leabRa	??				
24	learNN	??				
25	LilRhino	AP				
26	neural	CL	tools for a small and the			
27	NeuralNetTools	UT	tools for neural networks			
28	NeuralSens NlinTS	UT	tools for neural networks			
29 30		TS UT	Time Series confidence intervals for NN			
30 31	nnetpredint nnfor	TS	Times Series, uses neuralnet			
32	nntrf	UT	Times octios, uses neuralitet			
33	onnx	- 1	provides an open source format			
34	OptimClassifier		choose classifier parameters, nnet			
35	OSTSC		solving oversampling classification			
36	passt					
36	pnn		Probabilistic			
37	polyreg		polyregression as alternative to NN			
38	predictoR		shiny interface, neuralnet			
39	ProcData					
40	QuantumOps		classifies MNIST, Schuld (2018), removed keyword, in 2019			
41	quarrint		specified classifier for quarry data			
42	rasclass		classifier for raster images, nnet?			
43	rcane		a manual righ vargion of prodictoD			
44 45	regressoR		a manual rich version of predictoR Recurrent			
45 46	rnn RTextTools		Necurrent			
40 47	ruta					
48	simpleNeural					
49	softmaxreg					
50	Sojourn.Data		sojourn Accelerometer methods, nnet?			
51	spnn		classifier, probabilistic			
52	studyStrap		-			
53	TeachNet		classifier, selfbuilt, slow			
54	tensorflow					
55						
	The R Jarackdewn XX/YY, AAAA classifier for particle tracking ISSN 2073-4859					
57 5 0	TrafficBDE	RE*				
58	tsfgrnn					

Discussion and Recommendations

The following is a list of packages we included in this study, with brief descriptions.

- 1. AMORE (Limas et al., 2020),
- 2. ANN2 (Lammers, 2020),
- 3. **appnn** (Família et al., 2015),
- 4. autoencoder (Dubossarsky and Tyshetskiy, 2015),
- 5. automl (Boulangé, 2020),
- 6. BNN (Jia, 2018),
- 7. brnn (Rodriguez and Gianola, 2020),
- 8. Buddle (Kim, 2020),
- 9. CaDENCE (Cannon, 2017a),
- 10. cld2 (Ooms, 2018),
- 11. cld3 (Ooms, 2020),
- 12. condmixt (Carreau, 2020),
- 13. DamiaNN (Siniakowicz, 2016),
- 14. deep (Mayer, 2019),
- 15. deepdive (Balakrishnan, 2020),
- 16. deepnet (Rong, 2014),
- 17. deepNN (Taylor, 2020),
- 18. **DNMF** (Jia and Zhang, 2015),
- 19. elmNNRcpp (Mouselimis and Gosso, 2020),
- 20. ELMR (Petrozziello, 2015),
- 21. EnsembleBase (Mahani and Sharabiani, 2016),
- 22. evclass (Denoeux, 2017),
- 23. gamlss.add (Stasinopoulos et al., 2020),
- 24. gcForest (Jing, 2018),
- 25. GMDH (Dag and Yozgatligil, 2016),
- 26. GMDH2 (Dag et al., 2019),
- 27. GMDHreg (Tilve, 2020),
- 28. gnn (Hofert and Prasad, 2020),
- 29. grnn (Chasset, 2013a),
- 30. **h2o** (LeDell et al., 2020),
- 31. hybridEnsemble (Ballings et al., 2015),
- 32. isingLenzMC (Suzen, 2016),
- 33. keras (Allaire and Chollet, 2020),

- 34. kerasR (Arnold, 2017),
- 35. leabRa (Titz, 2017),
- 36. learNN (Quast, 2015),
- 37. LilRhino (Barton, 2019),
- 38. minpack.lm (Elzhov et al., 2016),
- 39. MachineShop (Smith, 2020),
- 40. monmlp (Cannon, 2017b),
- 41. neural (Nagy, 2014),
- 42. neuralnet (Fritsch et al., 2019),
- 43. NeuralNetTools (Beck, 2018),
- 44. NeuralSens (Portela González et al., 2020),
- 45. NlinTS (Hmamouche, 2020),
- 46. nlsr (Nash and Murdoch, 2019),
- 47. nnet (Ripley, 2020),
- 48. nnetpredint (Ding, 2015),
- 49. nnfor (Kourentzes, 2019),
- 50. nntrf (Aler and Valls, 2020),
- 51. nnli2bRcpp (Nikolaidis, 2020),
- 52. onnx (Tang and ONNX Authors, 2018),
- 53. OptimClassifier (Perez-Martin et al., 2020),
- 54. OSTSC (Dixon et al., 2017),
- 55. pnn (Chasset, 2013b),
- 56. polyreg (Matloff et al., 2020),
- 57. predictoR (with contributions from Diego Jimenez A. and D., 2020),
- 58. qrnn (Cannon, 2019),
- 59. QuantumOps (Resch, 2020),
- 60. quarrint (Barthelemy et al., 2016),
- 61. radiant.model (Nijs, 2020),
- 62. rasclass (Wiesmann and Quinn, 2016),
- 63. rcane (Suresh et al., 2018),
- 64. regressoR (Rodriguez R., 2019),
- 65. rminer (Cortez, 2020),
- 66. rnn (Quast and Fichou, 2020),
- 67. RSNNS (Bergmeir, 2019),
- 68. ruta (Charte et al., 2019),

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69. simpleNeural (Dernoncourt, 2020),
70. snnR (Wang et al., 2017),
71. softmaxreg (Ding, 2016),
72. Sojourn. Data (Hibbing and Lyden, 2019),
73. spnn (Ebrahimi, 2020),
74. TeachNet (Steinbuss, 2018),
75. tensorflow (Allaire and Tang, 2020),
76. tfestimators (Allaire et al., 2018),
77. trackdem (Bruijning et al., 2020),
78. TrafficBDE (Chatzopoulou et al., 2018),
79. tsensembler (Cerqueira et al., 2017),
80. validann (Humphrey, 2017),
81. zFactor (Reyes, 2019).
82.
83.
84.
85.
86.
87.
88.
```

A. Recommended: 2nd order algorithms Out of all the algorithms, these second algorithms generally performed better in terms of convergence despite being set to a much lower number of iterations, 200, than the first-order algorithms. Moreover, they performed better in terms of speed. The best in this class were. minpack.lm and. nlsr, tied at rank number 1. The Levenberg-Marquardt (LM) algorithm used is fast and converges well. stats::nls() is used. However, these packages require a handwritten formula that may not be ideal for certain situations. A more popular package for neural networks is nnet. This might be because it is part of base R. It implements the BFGS algorithm with stats::optim().

Ranked directly after are some packages that depend on nnet or use the same functions. They differ in how well they decide initial parameters. rminer (rank 4), MachineShop (rank 5), and radiant.model (rank 7) use nnet. Note, radiant.model has its iterations set to 10000, which originally made it slower yet converge better. We used a modified version of the package. At rank 6 is validann's BFGS algorithm using stats::optim(). Its use of optim's L-BFGS-B ranked at number 9 with CaDENCE's use of optim's BFGS... monmlp, from the same author as CaDENCE (Alex Cannon), uses the package. optimx's BFGS (Nash and Varadhan, 2020).

Alex Cannon also implemented a quantile regression neural network in qrnn with stats::nlm(). It requires more iterations and is not as fast compared to the other second-order algorithms. However, it is a valuable implementation of quantile regression. Last but not least is brnn's Gauss Newton algorithm which ranks at number 8. brnn is easy to use but does not converge as well due to a hidden constraint: a missing first parameter. Furthermore, brnn's algorithm minimizes the sum of squared errors and a penalty on parameters instead

of just the sum of squared errors. This may prevent parameters to get highly correlated, especially with an almost degenerated Jacobian matrix.

B. Recommended: 1st order algorithms validann optim CG -slow RSNNS SCG h2o back-propagation RSNNS Rprop ANN2 adam CaDENCE Rprop -SLOW deepnet BP AMORE ADAPTgdwm AMORE ADAPTgd ANN2 sgd automl trainwgrad ANN2 rmsprop RSNNS BackpropChunk RSNNS BackWeightDecay RSNNS Std_Backpropagation RSNNS BackpropMomentum automl trainwpso validann optim NelderMead snnR Semi Smooth Newton RSNNS BackpropBatch validann optim SANN monmlp optimx Nelder Mead

C. Not recommended: 1st order algorithms <- DISCUSS CUTOFF By package ELMR, elmNNRcpp - fast ELM algorithms. Unfortunately, can't finetune, does not converge well. neuralnet: a large ammount of iterations, slow, erratic failures tensorflow: NOT EASY TO USE, subsequently keras, tfestimators, ruta ... user needs to understand the language However, advanced users might be able to highly specify a neural network to their needs (customization?)

By algorithm: neuralnet rprop+ neuralnet rprop- neuralnet slr - once ranked well with 100000 iterations AMORE BATCHgd CaDENCE pso psoptim - need to reconfigure? elmN-NRcpp - fast, no iterations RSNNS Quickprop (?) AMORE BATCHgdwm tensorflow MomentumOptimizer tensorflow AdamOptimizer ELMR - fast, no iterations tensorflow GradientDescentOptimizer keras rmsprop keras adagrad keras sgd keras adadelta tensorflow AdagradOptimizer keras adam tensorflow FtrlOptimizer neuralnetwork sag tensorflow AdadeltaOptimizer neuralnet backprop - note, might not actually reflect standings, somehow from template to template the learning rate disappeared. Will fix this in future runs

D. Untested => TO DO - LIST

Conclusion => TO DO AFTER 2020 CODE

??JN: Can we start to put in some major findings? i.e., important positive findings, big negatives?

Positives (no particular order)

- 1. the existence of algorithms that converge well
- 2. nnet, which uses optim's BFGS, is already often chosen to represent neural networks for packages that are either a collection of independent machine learning algorithms, ensembles, or even applications in a field such as ...
- 3. the wide variety of neural networks available to users of R, from libraries of other programming languages to many different types of algorithms, hyperparameters, and uses

Negatives (no particular order)

- 1. bad documentation
- 2. the lack of packages that expand the number of unique second order algorithms. (Perhaps even the existence of what can be considered as repetitive packages?)
- 3. the lack of clear default values, or bad default values

Future work

As the field of neural networks continue to grow, there will always be more algorithms to validate. For current algorithms in R, our research should be extended to encompass more types of neural networks and their data formats (classifier neural networks, recurrent neural networks, and so on). Different rating schemes and different parameters for package functions can also be tried out.

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Bibliography

- R. Aler and J. Valls. *nntrf: Supervised Data Transformation by Means of Neural Network Hidden Layers*, 2020. URL https://CRAN.R-project.org/package=nntrf. R package version 0.1.3. [p9]
- J. Allaire and F. Chollet. *keras: R Interface to 'Keras'*, 2020. URL https://CRAN.R-project.org/package=keras. R package version 2.3.0.0. [p8]
- J. Allaire and Y. Tang. tensorflow: R Interface to 'TensorFlow', 2020. URL https://CRAN.R-project.org/package=tensorflow. R package version 2.2.0. [p10]
- J. Allaire, Y. Tang, K. Ushey, and K. Kuo. tfestimators: Interface to 'TensorFlow' Estimators, 2018. URL https://CRAN.R-project.org/package=tfestimators. R package version 1.9.1. [p10]
- T. Arnold. *kerasR: R Interface to the Keras Deep Learning Library*, 2017. URL https://CRAN.R-project.org/package=kerasR. R package version 0.6.1. [p9]
- R. Balakrishnan. *deepdive: Deep Learning for General Purpose*, 2020. URL https://CRAN.R-project.org/package=deepdive. R package version 1.0.1. [p8]
- M. Ballings, D. Vercamer, and D. Van den Poel. *hybridEnsemble: Build, Deploy and Evaluate Hybrid Ensembles*, 2015. URL https://CRAN.R-project.org/package=hybridEnsemble. R package version 1.0.0. [p8]
- J. Barthelemy, T. Carletti, L. Collier, V. Hallet, M. Moriame, and A. Sartenaer. *quarrint: Interaction Prediction Between Groundwater and Quarry Extension Using Discrete Choice Models and Artificial Neural Networks*, 2016. URL https://CRAN.R-project.org/package=quarrint. R package version 1.0.0. [p9]
- T. Barton. LilRhino: For Implementation of Feed Reduction, Learning Examples, NLP and Code Management, 2019. URL https://CRAN.R-project.org/package=LilRhino. R package version 1.2.0. [p9]
- M. W. Beck. *NeuralNetTools: Visualization and Analysis Tools for Neural Networks*, 2018. URL https://CRAN.R-project.org/package=NeuralNetTools. R package version 1.5.2. [p9]
- C. Bergmeir. RSNNS: Neural Networks using the Stuttgart Neural Network Simulator (SNNS), 2019. URL https://CRAN.R-project.org/package=RSNNS. R package version 0.4-12. [p9]
- A. Boulangé. *automl: Deep Learning with Metaheuristic*, 2020. URL https://CRAN.R-project.org/package=automl. R package version 1.3.2. [p8]
- M. Bruijning, M. D. Visser, C. A. Hallmann, and E. Jongejans. *trackdem: Particle Tracking and Demography*, 2020. URL https://CRAN.R-project.org/package=trackdem. R package version 0.5.2. [p10]
- A. J. Cannon. *CaDENCE: Conditional Density Estimation Network Construction and Evaluation*, 2017a. URL https://CRAN.R-project.org/package=CaDENCE. R package version 1.2.5. [p8]
- A. J. Cannon. *monmlp: Multi-Layer Perceptron Neural Network with Optional Monotonicity Constraints*, 2017b. URL https://CRAN.R-project.org/package=monmlp. R package version 1.1.5. [p9]

- A. J. Cannon. *qrnn: Quantile Regression Neural Network*, 2019. URL https://CRAN.R-project.org/package=qrnn. R package version 2.0.5. [p9]
- J. Carreau. condmixt: Conditional Density Estimation with Neural Network Conditional Mixtures, 2020. URL https://CRAN.R-project.org/package=condmixt. R package version 1.1. [p8]
- V. Cerqueira, L. Torgo, and C. Soares. Arbitrated ensemble for solar radiation forecasting. International Work-Conference on Artificial Neural Networks, pages 720–732, 2017. The R package tsensembler has been archived as of July 2020 because it has not been maintained. [p10]
- T. Chai and R. R. Draxler. Root mean square error (rmse) or mean absolute error (mae)?—arguments against avoiding rmse in the literature. *Geoscientific model development*, 7(3): 1247–1250, 2014. [p4]
- D. Charte, F. Charte, and F. Herrera. *ruta: Implementation of Unsupervised Neural Architectures*, 2019. URL https://CRAN.R-project.org/package=ruta. R package version 1.1.0. [p9]
- P.-O. Chasset. grnn: General regression neural network, 2013a. URL https://CRAN.R-project.org/package=grnn. R package version 0.1.0. [p8]
- P.-O. Chasset. *pnn: Probabilistic neural networks*, 2013b. URL https://CRAN.R-project.org/package=pnn. R package version 1.0.1. [p9]
- A. Chatzopoulou, K. Koupidis, and C. Bratsas. *TrafficBDE: Traffic Status Prediction in Urban Places using Neural Network Models*, 2018. URL https://CRAN.R-project.org/package=TrafficBDE. R package version 0.1.0. [p10]
- P. Cortez. rminer: Data Mining Classification and Regression Methods, 2020. URL https://CRAN.R-project.org/package=rminer. R package version 1.4.5. [p9]
- O. Dag and C. Yozgatligil. *GMDH: Short Term Forecasting via GMDH-Type Neural Network Algorithms*, 2016. URL https://CRAN.R-project.org/package=GMDH. R package version 1.6. [p8]
- O. Dag, E. Karabulut, and R. Alpar. *GMDH2: Binary Classification via GMDH-Type Neural Network Algorithms*, 2019. URL https://CRAN.R-project.org/package=GMDH2. R package version 1.5. [p8]
- T. Denoeux. evclass: Evidential Distance-Based Classification, 2017. URL https://CRAN.R-project.org/package=evclass. R package version 1.1.1. [p8]
- D. Dernoncourt. *simpleNeural: An Easy to Use Multilayer Perceptron*, 2020. URL https://CRAN.R-project.org/package=simpleNeural. R package version 0.1.3. [p10]
- X. Ding. *nnetpredint: Prediction Intervals of Multi-Layer Neural Networks*, 2015. URL https://CRAN.R-project.org/package=nnetpredint. R package version 1.2. [p9]
- X. Ding. softmaxreg: Training Multi-Layer Neural Network for Softmax Regression and Classification, 2016. URL https://CRAN.R-project.org/package=softmaxreg. R package version 1.2. [p10]
- M. Dixon, D. Klabjan, and L. Wei. *OSTSC: Over Sampling for Time Series Classification*, 2017. URL https://CRAN.R-project.org/package=OSTSC. R package version 0.0.1. [p9]
- E. Dubossarsky and Y. Tyshetskiy. *autoencoder: Sparse Autoencoder for Automatic Learning of Representative Features from Unlabeled Data*, 2015. URL https://CRAN.R-project.org/package=autoencoder. R package version 1.1. [p8]
- R. Ebrahimi. *spnn: Scale Invariant Probabilistic Neural Networks*, 2020. URL https://CRAN.R-project.org/package=spnn. R package version 1.2.1. [p10]

- T. V. Elzhov, K. M. Mullen, A.-N. Spiess, and B. Bolker. *minpack.lm: R Interface to the Levenberg-Marquardt Nonlinear Least-Squares Algorithm Found in MINPACK, Plus Support for Bounds*, 2016. URL https://CRAN.R-project.org/package=minpack.lm. R package version 1.2-1. [p9]
- C. Família, S. R. Dennison, A. Quintas, and D. A. Phoenix. *appnn: Amyloid Propensity Prediction Neural Network*, 2015. URL https://CRAN.R-project.org/package=appnn. R package version 1.0-0. [p8]
- S. Fritsch, F. Guenther, and M. N. Wright. *neuralnet: Training of Neural Networks*, 2019. URL https://CRAN.R-project.org/package=neuralnet. R package version 1.44.2. [p9]
- P. R. Hibbing and K. Lyden. *Sojourn.Data: Supporting Objects for Sojourn Accelerometer Methods*, 2019. URL https://CRAN.R-project.org/package=Sojourn.Data. R package version 0.1.0. [p10]
- Y. Hmamouche. *NlinTS: Models for Non Linear Causality Detection in Time Series*, 2020. URL https://CRAN.R-project.org/package=NlinTS. R package version 1.4.2. [p9]
- M. Hofert and A. Prasad. *gnn: Generative Neural Networks*, 2020. URL https://CRAN.R-project.org/package=gnn. R package version 0.0-2. [p8]
- G. B. Humphrey. *validann: Validation Tools for Artificial Neural Networks*, 2017. URL https://CRAN.R-project.org/package=validann. R package version 1.2.1. [p10]
- B. Jia. *BNN: Bayesian Neural Network for High-Dimensional Nonlinear Variable Selection*, 2018. URL https://CRAN.R-project.org/package=BNN. R package version 1.0.2. [p8]
- Z. Jia and X. Zhang. *DNMF: Discriminant Non-Negative Matrix Factorization*, 2015. URL https://CRAN.R-project.org/package=DNMF. R package version 1.3. [p8]
- X. Jing. gcForest: Deep Forest Model, 2018. URL https://CRAN.R-project.org/package=gcForest. R package version 0.2.7. [p8]
- P. Kiener. RWsearch: Lazy Search in R Packages, Task Views, CRAN, the Web. All-in-One Download, 2020. URL https://CRAN.R-project.org/package=RWsearch. R package version 4.8.0. [p3]
- J. Kim. Buddle: A Deep Learning for Statistical Classification and Regression Analysis with Random Effects, 2020. URL https://CRAN.R-project.org/package=Buddle. R package version 2.0.1. [p8]
- N. Kourentzes. *nnfor: Time Series Forecasting with Neural Networks*, 2019. URL https://CRAN.R-project.org/package=nnfor. R package version 0.9.6. [p9]
- B. Lammers. *ANN2: Artificial Neural Networks for Anomaly Detection*, 2020. URL https://CRAN.R-project.org/package=ANN2. R package version 2.3.3. [p8]
- E. LeDell, N. Gill, S. Aiello, A. Fu, A. Candel, C. Click, T. Kraljevic, T. Nykodym, P. Aboyoun, M. Kurka, and M. Malohlava. *h2o: R Interface for the 'H2O' Scalable Machine Learning Platform*, 2020. URL https://CRAN.R-project.org/package=h2o. R package version 3.30.0.1. [p8]
- M. C. Limas, J. B. O. Mere, A. G. Marcos, F. J. M. de Pison Ascacibar, A. V. P. Espinoza, F. A. Elias, and J. M. P. Ramos. *AMORE: Artificial Neural Network Training and Simulating*, 2020. URL https://CRAN.R-project.org/package=AMORE. R package version 0.2-16. [p8]
- A. S. Mahani and M. T. Sharabiani. EnsembleBase: Extensible Package for Parallel, Batch Training of Base Learners for Ensemble Modeling, 2016. URL https://CRAN.R-project.org/package=EnsembleBase. R package version 1.0.2. [p8]

- N. Matloff, X. Cheng, P. Mohanty, B. Khomtchouk, M. Kotila, R. Yancey, R. Tucker, A. Zhao, and T. Jiang. *polyreg: Polynomial Regression*, 2020. URL https://CRAN.R-project.org/package=polyreg. R package version 0.6.7. [p9]
- B. L. Mayer. *deep: A Neural Networks Framework*, 2019. URL https://CRAN.R-project.org/package=deep. R package version 0.1.0. [p8]
- L. Mouselimis and A. Gosso. *elmNNRcpp: The Extreme Learning Machine Algorithm*, 2020. URL https://CRAN.R-project.org/package=elmNNRcpp. R package version 1.0.2. [p8]
- A. Nagy. *neural: Neural Networks*, 2014. URL https://CRAN.R-project.org/package=neural. R package version 1.4.2.2. [p9]
- J. C. Nash and D. Murdoch. *nlsr: Functions for Nonlinear Least Squares Solutions*, 2019. URL https://CRAN.R-project.org/package=nlsr. R package version 2019.9.7. [p9]
- J. C. Nash and R. Varadhan. *optimx: Expanded Replacement and Extension of the 'optim' Function*, 2020. URL https://CRAN.R-project.org/package=optimx. R package version 2020-4.2. [p10]
- V. Nijs. radiant.model: Model Menu for Radiant: Business Analytics using R and Shiny, 2020. URL https://CRAN.R-project.org/package=radiant.model. R package version 1.3.10. [p9]
- V. Nikolaidis. nnlib2Rcpp: A Collection of Neural Networks, 2020. URL https://CRAN.R-project.org/package=nnlib2Rcpp. R package version 0.1.4. [p9]
- J. Ooms. *cld2: Google's Compact Language Detector* 2, 2018. URL https://CRAN.R-project.org/package=cld2. R package version 1.2. [p8]
- J. Ooms. cld3: Google's Compact Language Detector 3, 2020. URL https://CRAN.R-project.org/package=cld3. R package version 1.3. [p8]
- A. Perez-Martin, A. Perez-Torregrosa, M. Vaca-Lamata, and A. J. Verdu-Jover. *OptimClassifier:* Create the Best Train for Classification Models, 2020. URL https://CRAN.R-project.org/package=OptimClassifier. R package version 0.1.5. [p9]
- A. Petrozziello. *ELMR: Extreme Machine Learning (ELM)*, 2015. URL https://CRAN.R-project.org/package=ELMR. R package version 1.0. [p8]
- J. Portela González, A. Muñoz San Roque, and J. Pizarroso Gonzalo. *NeuralSens: Sensitivity Analysis of Neural Networks*, 2020. URL https://CRAN.R-project.org/package=NeuralSens. R package version 0.2.1. [p9]
- B. Quast. *learNN: Examples of Neural Networks*, 2015. URL https://CRAN.R-project.org/package=learNN. R package version 0.2.0. [p9]
- B. Quast and D. Fichou. rnn: Recurrent Neural Network, 2020. URL https://CRAN.R-project.org/package=rnn. R package version 1.4.0. [p9]
- S. Resch. QuantumOps: Performs Common Linear Algebra Operations Used in Quantum Computing and Implements Quantum Algorithms, 2020. URL https://CRAN.R-project.org/package=QuantumOps. R package version 3.0.1. [p9]
- A. R. Reyes. *zFactor: Calculate the Compressibility Factor 'z' for Hydrocarbon Gases*, 2019. URL https://CRAN.R-project.org/package=zFactor. R package version 0.1.9. [p10]
- B. Ripley. nnet: Feed-Forward Neural Networks and Multinomial Log-Linear Models, 2020. URL https://CRAN.R-project.org/package=nnet. R package version 7.3-14. [p9]
- P. P. Rodriguez and D. Gianola. brnn: Bayesian Regularization for Feed-Forward Neural Networks, 2020. URL https://CRAN.R-project.org/package=brnn. R package version 0.8. [p8]

- O. Rodriguez R. regressoR: Regression Data Analysis System, 2019. URL https://CRAN.R-project.org/package=regressoR. R package version 1.1.9. [p9]
- X. Rong. deepnet: deep learning toolkit in R, 2014. URL https://CRAN.R-project.org/package=deepnet. R package version 0.2. [p8]
- D. Siniakowicz. *DamiaNN: Neural Network Numerai*, 2016. URL https://CRAN.R-project.org/package=DamiaNN. R package version 1.0.0. [p8]
- B. J. Smith. *MachineShop: Machine Learning Models and Tools*, 2020. URL https://CRAN.R-project.org/package=MachineShop. R package version 2.5.0. [p9]
- M. Stasinopoulos, B. Rigby, V. Voudouris, and D. Kiose. *gamlss.add: Extra Additive Terms for Generalized Additive Models for Location Scale and Shape*, 2020. URL https://CRAN.R-project.org/package=gamlss.add. R package version 5.1-6. [p8]
- G. Steinbuss. *TeachNet: Fits Neural Networks to Learn About Backpropagation*, 2018. URL https://CRAN.R-project.org/package=TeachNet. R package version 0.7.1. [p10]
- A. Suresh, S. Acharekar, H. Chao, and S. Y. Biradar. *rcane: Different Numeric Optimizations to Estimate Parameter Coefficients*, 2018. URL https://CRAN.R-project.org/package=rcane. R package version 1.0. [p9]
- M. Suzen. *isingLenzMC: Monte Carlo for Classical Ising Model*, 2016. URL https://CRAN.R-project.org/package=isingLenzMC. R package version 0.2.5. [p8]
- Y. Tang and ONNX Authors. *onnx: R Interface to 'ONNX'*, 2018. URL https://CRAN.R-project.org/package=onnx. R package version 0.0.2. [p9]
- B. Taylor. *deepNN: Deep Learning*, 2020. URL https://CRAN.R-project.org/package=deepNN. R package version 1.0. [p8]
- M. V. Tilve. *GMDHreg: Regression using GMDH Algorithms*, 2020. URL https://CRAN.R-project.org/package=GMDHreg. R package version 0.2.1. [p8]
- J. Titz. leabRa: The Artificial Neural Networks Algorithm Leabra, 2017. URL https://CRAN.R-project.org/package=leabRa. R package version 0.1.0. [p9]
- Y. Wang, P. Lin, Z. Chen, Z. Bao, and G. J. M. Rosa. snnR: Sparse Neural Networks for Genomic Selection in Animal Breeding, 2017. URL https://CRAN.R-project.org/package=snnR. R package version 1.0. [p10]
- D. Wiesmann and D. Quinn. *rasclass: Supervised Raster Image Classification*, 2016. URL https://CRAN.R-project.org/package=rasclass. R package version 0.2.2. [p9]
- C. J. Willmott and K. Matsuura. Advantages of the mean absolute error (mae) over the root mean square error (rmse) in assessing average model performance. *Climate research*, 30(1): 79–82, 2005. [p4]
- O. R. R. with contributions from Diego Jimenez A. and A. N. D. *predictoR: Predictive Data Analysis System*, 2020. URL https://CRAN.R-project.org/package=predictoR. R package version 1.1.3. [p9]
 - The dreamed NN package: Recommendation to package authors
 - Conclusion
 - Acknowledgments

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Appendix A

Consider a set of observations y_i and its corresponding predictions \hat{y}_i for i = 1, ..., n. The three metrics used were:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|, \ RMSE = \frac{1}{n} \sqrt{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}, \ WAE = \frac{1}{n} \max_{i=1,...,n} |y_i - \hat{y}_i|.$$

These values represent the absolute, the squared and the maximum norm of residual vectors.

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