# A Review of R Neural Network Packages (with NNbenchmark): Accuracy and Ease of Use

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#### **Abstract**

In the last three decades, neural networks have evolved from an academic topic to a common scientific computing tool. CRAN currently hosts around 80 packages (May 2020) that involve neural network modeling; some offering more than one algorithm. However, to our knowledge, there is no comprehensive study which tests the accuracy, the reliability, and the ease-of-use of those NN packages.

In this paper, we test a large number of packages against a common set of datasets with varying levels of complexity to benchmark and rank them with statistical metrics.

We restrict our evaluation to single hidden-layer perceptrons that perform regression. We ignore packages for classification and other specialized purposes. This leaves us with approximately 60 package:algorithm pairs to test. The criteria used in our benchmark were: (i) accuracy, i.e. the ability to find the global minima on 13 datasets, measured by the Root Mean Square Error (RMSE) in a fixed number of iterations; (ii) speed of the training algorithm; (iii) availability of helpful utilities; (iv) quality of the documentation.

We have given a score for each evaluation criterion to compare all package:algorithm pairs in a global table. Overall, 15 pairs are considered accurate and reliable and are recommended for daily usage. Other packages are either less accurate, slow, difficult to use, or have poor or zero documentation.

To carry out this work, we developed multiple scripts along with the NNbenchmark package. We have open-sourced our code for reproducibility on a github repository https://github.com/pkR-pkR/NNbenchmarkTemplates as well as outputs per package/dataset at https://theairbend3r.github.io/NNbenchmarkWeb/index.html.

#### Introduction

The R Project for Statistical Computing, as any open-source platform, relies on its contributors to keep it up to date. Neural network, inspired by the brain itself, are a class of models in the growing field of machine learning for which R has a number of packages. Before 2010, neural networks were often considered theoretically instead of pragmatically, partly because the algorithms used were computationally expensive.

The term "neural network" is colloquially used for different model structures and applications. For regression and classification, the term multilayer perceptron is used interchangeably. The term "recurrent neural network" is mainly used in the context of autoregressive time-series while the term "convolutional neural network" is appropriate for dimension reduction and pattern recognition (images/audio/text). Most of the above types of neural networks (NN) can be found in R packages hosted on CRAN but without any study about the accuracy or the speed of computation. This is an issue as many slow or poor algorithms to fit NN are available in the literature and hence bad packages are implemented on CRAN.

In the NN literature, a certain number of benchmark of neural networks have been conducted. (Adolf et al., 2016) propose a reference workloads for modern deep learning methods with a large variety of benchmark tasks and NN types. They analyze the breakdown of execution time by operation type for each workload in order to identify where time is spent. (Tao et al., 2018) propose a benchmark suite for intelligence processors, which consists of two levels of benchmarks: microbenchmarks of single-layer networks and macrobenchmarks of state-of-the-art industrial networks. However (Tao et al., 2018) focus only

various hardware platforms, including CPUs, GPUs, and scenarios are limited to classification/recognition scenario. (Xie et al., 2020) propose another benchmark methodology to evaluate software/hardware co-designs and exemplify it on a selected set of applications from the TensorFlow Model Zoo.

Furthermore, there are also benchmarks with a specific type of application, e.g., (Bianco et al., 2018) for image recognition, (Wang et al., 2020) for crime forecasting, (Witczak et al., 2006) for fault diagnosis.

None of these benchmarks deals with NN <!- Ref 2 - Comment 14 -> implemented in R packages which is the aim of this paper. We follow the general principles of (Prechelt et al., 1994) to conduct our benchmark: validity, reproducibility and comparability when designing our benchmark. Furthermore, we also use from (Prechelt et al., 1994) other rules such as input scaling, error measure, NN naming convention, NN random initialization.

A neural network algorithm requires complicated calculations to improve the model control parameters. As with other optimization problems, the gradient of the chosen cost function indicates the model's lack of suitability. Optimization methods improve the current iterate by changing the parameters in the opposite of the gradient direction generally with an adaptive step. Parameters for the model are generally obtained by using part of the available data (a training set) and tested on the remaining data. Modern software allows much of this work, including approximation of the gradient, to be carried out without a large effort by the user.

The training process can generally be made more efficient if we can also approximate second derivatives of the cost function, allowing us to use its curvature via the Hessian matrix. There are a large number of approaches, of which quasi-Newton algorithms are perhaps the most common and useful. Within this group, methods based on the Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm for updating the (inverse) Hessian approximation provide several well-known examples. In conducting this study, we hypothesize that these second-order algorithms would perform better than the first-order methods for datasets that fit in memory.

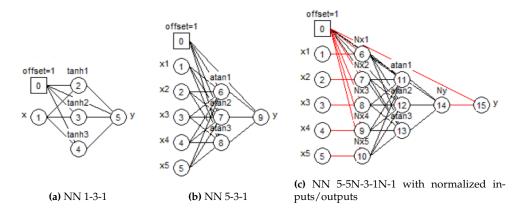
To test our hypothesis, we conduct a thorough examination of these training algorithms in R. There are many packages, but there is a dearth of information that would allow the users to make an informed decision. Our work aims to provide a framework for benchmarking neural network packages. We focus our examination to neural networks of the perceptron type which consist of one input layer, one normalized layer, one hidden layer with a non-linear activation function and one output layer.

Specifically, we focus only on regression-based algorithms. The criteria used in our benchmark were: (i) accuracy, i.e. the ability to find the global minima on 13 datasets, measured by the Root Mean Square Error (RMSE) in a fixed number of iterations; (ii) speed of the training algorithm; (iii) availability of helpful utilities; (iv) quality of the documentation.

# Multilayer perceptron with a single hidden layer

In this section, we briefly describe the single hidden-layer perceptron. As the "layer" term suggests - some terms come from graphs representations while others come from the traditional literature on non-linear models. We refer to (Friedman et al., 2001, Chapter 11), (Izenman, 2008, Chapter 10) (Ripley, 2007) for a general introduction of neural networks.

Using the graph description e.g. Fig 1, a single-hidden layer neural network is made up of 3 parts: (i) layer of the input(s), (ii) hidden layer which consists of independent neurons, each of them performing two operations: a linear combination of the inputs plus an offset followed by a non-linear function, (iii) output layer which is a linear combination of the output of the previous layer. We introduce a generic notation NN a-b-c for a neural network with a inputs, b hidden neurons and c outputs. If inputs or outputs are normalized, we interleave either aN or cN in the notation.



**Figure 1:** Three neural networks using the NN *a-b-c* notation

The non-linear function used in the hidden layer must have the following four properties: continuous, differentiable, monotonic, and bounded. The logistic (invlogit), hyperbolic tangent (tanh) and arctangent (atan) functions are the usual candidates.

The resulting model has the following generic expression

$$y = a_1 + \sum_{j=1}^{d} a_{j,1} \times f(a_{j,2} + \sum_{l=1}^{p} a_{j,2+l} \times x_l),$$

with p inputs, d hidden neurons and f as the activation function. The total number of parameters to be estimated is 1 + d(2 + p) The neural network depicted Fig. 1a corresponds to p = 1, d = 3 and f = anh for a total of 10 parameters, whereas the neural network depicted Fig. 1b corresponds to p = 5, d = 3 and f = anh for a total of 22 parameters.

In practice, modelers also use piecewise differentiable functions with bounded left/right derivatives, such as the Rectified Linear Unit function (called ReLU in softwares). The ReLU activation function is in particular useful for classification problems which are not investigated here.

While the final gradient should be small, we believe it is helpful to have gradients with large values at the first steps of the training algorithm, so the following is recommended: (i) normalized inputs and outputs (Fig. 1c contains Nx nodes after inputs and before outputs), (ii) odd functions like the hyperbolic tangent function or the arctangent function, (iii) small random values to initialize the parameters. A common example of this is to use values extracted from a centered Gaussian  $\mathcal{N}(0,0.1)$  distribution. When normalizing input/outputs, inputs  $x_l$  are replaced by  $F_N(x_l)$  and output by  $F_N^{-1}(y)$  where  $F_N$  and  $F_N^{-1}$  stand respectively for the distribution function and the quantile function of a Gaussian distribution. These practices help us find good local-minima and possibly the global-minima.

The dataset used for the training is assumed to have the number of rows much larger than the number of parameters. While "much larger" is subjective, values of 3 to 5 are generally accepted (in experimental design, some iterative strategies start with a dataset having a number of distinct experiments equal to 1.8 times the number of parameters and then increase the number of experiments to fine tune the model).

It is rather clear from the mathematical formula above that neural networks of perceptron type are non-linear models which require training algorithms that can handle (highly) non-linear models for their parameter estimation. Indeed, the intrinsic and parametric curvatures of such models are usually very high and with so many parameters, the Jacobian matrix might exhibit some co-linearities between its columns and become nearly singular. As a result, appropriate algorithms for such dataset:model pairs are rather limited and well-known. They pertain to the class of second-order algorithms such as the BFGS algorithm which is Quasi-Newton in how it updates the approximate inverse Hessian or the Levenberg-Marquardt algorithm which stabilizes the Gauss-Newton search direction at every iteration,

e.g. (Bonnans et al., 2006; Nocedal and Wright, 2006).

Unfortunately, due to certain educative tools on the backpropagation and recent popularity of "deep neural networks" that manipulate ultra-large models (sometimes more parameters than examples in the datasets), many papers emphasize the use of first-order gradient algorithms.

Therefore, many R packages have implemented such algorithms. In the case of the perceptron, we contend this is an oversight, and provide evidence to that effect in this paper. We refer interested readers to (Tan and Lim, 2019) for a review of second-order algorithms for neural networks and their potential benefits over first-order methods.

# Methodology

#### Convergence and termination

Most of package:algorithm pairs try to minimize the Root Mean Squared Error (RMSE) during the training step. Two exceptions are the **brnn** package which minimizes the RMSE plus the sum of the parameters (hence the name Bayesian Regularized neural network), and the **qrnn** package which performs quantile regression. For all packages, the datasets were learnt as a whole and without any weighting scheme to favor a single part of a dataset. We don't use a validation/test set because the purpose of our study is to verify the ability to reach good minima. This requirement is satisfied by using only a train set.

When training neural networks, we attempt to tune a set of hyperparameters so that the root to minimize the RMSE. When our method for such adjustment can no longer reduce the RMSE, we say that the given algorithm **terminated**. We consider the method to have **converged** when termination is not due to some exceptional situation and the final RMSE value is relatively small<sup>1</sup>. In practice, some algorithms require that we stop the optimization process in exceptional situations (e.g., a divide by zero), or a pre-set limit on the number of steps or a maximum elapsed time is reached.

Specifically, second-order algorithms are all set to a maximum of 200 iterations. On the other hand, first-order algorithms were set to several values, depending on how well and how fast they converged: maxit1storderA=1000 iterations, maxit1storderB=10000 iterations, and maxit1storderC=100000 iterations. The full list of the maximum iteration number per package:algorithm is given in Table 4 in Appendix D. It can be seen that we were unable to completely harmonize the hyperparameters as an appropriate learning rate differed between packages, despite the algorithm being similarly named. Using a manual grid search, we did our best to find the best learning rate and maxit for each package:algorithm, especially for first-order algorithms where different maxit values was used.

## Performance

We measure **performance** primarily by relative computing time between methods on a particular computing platform. We could count the precise number of iterations, function evaluations or similar quantities that indicate the computing effort, but this would have required a large effort in R coding in order to get values that are comparable between NN packages. We note that differences in machine architecture and in the attached libraries (e.g., BLAS choices for R) will modify our performance measure. We are putting our tools on a Github repository so that further evaluation can be made by ourselves and others as hardware and software evolves.

The majority of the resulting files in our repository were generated on a Windows system build 10.0.18362.752. The machine specifications are (i) i7-8750H CPU, (ii) Intel(R) UHD Graphics 630, (iii) NVIDIA GeForce GTX 1060 chip, (iv) 16 GB of RAM.

<sup>&</sup>lt;sup>1</sup>We do not choose the mean absolute error (MAE) for overall ranking nor for convergence testing as there is a lack of consensus in the literature, see e.g. (Willmott and Matsuura, 2005; Chai and Draxler, 2014).

Tests were also performed on other platforms and the computation times were found to be reasonably similar.

# Phase 1 - Preparation of benchmark datasets and selection of packages

#### **Datasets**

A non-iterative calculation such as Ordinary Least Squares cannot generally be used to model all the datasets in our evaluation set. Varying levels of difficulty in modeling the different data sets are intended to allow us to further classify different algorithms and the packages that implement them. As we focus on regression analysis, we select only datasets where the response variable is real-valued.

Sonja Surjanovic and Derek Bingham of Simon Fraser University created a useful website from which three of the multivariate datasets were drawn. We note the link, name and difficulty level of the three datasets:

- http://www.sfu.ca/~ssurjano/fried.html: mFriedman, Friedman's dataset, published in (Friedman, 1991) (average difficulty),
- http://www.sfu.ca/~ssurjano/detpep10curv.html: mDette, Dette's dataset, published in (Dette and Pepelyshev, 2010) (medium difficulty),
- http://www.sfu.ca/~ssurjano/ishigami.html: mIshigami, Ishigami's dataset, published in (Ishigami and Homma, 1990) (high difficulty).

The last multivariate dataset, mRef153, was used to teach neural networks at ESPCI (The City of Paris Industrial Physics and Chemistry Higher Educational Institution, https://www.neurones.espci.fr/) from 2003 to 2013 and is available in the proprietary software Neuro One at http://www.inmodelia.com/software.html. This dataset presents some interesting non-linear features.

uDreyfus1 is a pure neural network which has no error. This can make it difficult for algorithms that assume an error exists. uDreyfus2 is uDreyfus1 with errors. Both are considered to be of low difficulty and used to teach neural networks at ESPCI from 1991 to 2013. uDmod1 and uDmod2 are univariate datasets with few observations but exhibit high non-linear patterns and prove to be very challenging datasets. The parameters are highly correlated and singular Jacobian matrices often appear.

Three of the univariate datasets were taken from the US National Institute for Standards and Technology (NIST) website: https://www.itl.nist.gov/div898/strd/nls/nls\_main.shtml. Namely uGauss1, uGauss2 and uGauss3 published in (Rust, 1996a,b,c, resp.) created by NIST to assess non-linear least squares regressions are of low, low and medium difficulty respectively.

The last univariate dataset, uNeuroOne, was also used to teach the same course and is now available in the proprietary software NeuroOne at http://www.inmodelia.com/software.html. In Table 1, we list some information on each dataset used in the first round of our analysis: the number of neurons and the induced parameter number are available in the last two columns.

Finally, we consider a Simon Wood test dataset, named bWoodN1, used in (Wood, 2011) for benchmarking generalized additive models. Precisely, we consider a generation of Gaussian random variates  $Y_i$ , i = 1, ..., n with the mean  $\mu_i$  defined as

$$\mu_i = 1 + f_0(x_{i,0}) + f_1(x_{i,1}) + f_2(x_{i,2}) + f_3(x_{i,3}) + f_4(x_{i,4}) + f_0(x_{i,5})$$

and standard deviation  $\sigma = 1/4$  where  $f_j$  are Simon Wood's smooth functions defined in Appendix B,  $x_{i,j}$  are uniform variates and n=20,000. bWoodN1 will only be used in the second round of our analysis when the TOP-5 packages will be further analyzed with 5 neurons resulting in 41 parameters.

Input nb. Neuron nb. Row nb. Param, nb. Dataset Multivariate 500 3 26 mDette mFriedman 500 5 5 36 mIshigami 500 10 51 3 mRef153 153 Univariate 51 1 19 uDmod1 uDmod2 51 1 16 uDreyfus1 51 1 3 10 uDreyfus2 51 3 10 uGauss1 250 uGauss2 250 4 13 250 uGauss3 13 uNeuroOne 51 7

Table 1: Datasets' summary

To build the final result table, we selected all four multivariate datasets and 4 out of the 8 univariate datasets so that the overall score does not overly weight the univariate datasets. Note that the 2020 GSoC results are available in Section 1 of the supplementary materials, (Mahdi et al., 2021). Furthermore the 2019 GSoC code uses all 12 datasets. For convenience, all datasets are made available in NNbenchmark, so that anyone can replicate our analysis.

#### **Packages**

Using RWsearch (Kiener, 2020), we sought to automate the process of searching for neural network packages. All packages that have "neural network" as a keyword in the package title or in the package description were included.

As of May 2020, around 80 packages fall into this category. Packages nlsr, minpack.lm, caret were added because the former two are important implementations of second-order algorithms while the latter is the first cited meta package in the CRAN task view for machine learning, *MachineLearning*. It is also a dependency for some of the other packages tested. Restricting to regression analysis left us with 49 package: algorithm pairs in 2019 and 60 package: algorithm pairs in 2020.

## Phase 2 - Review of packages and development of a benchmarking template

All packages were tested 3 times. Each assessment is described in detail below.

#### 1. The decision to exclude or include

From documentation and example code, we learned that not all packages selected by the automated search fit the scope of our research. Some have no function to generate neural networks while others were not regression neural networks of the perceptron type or were only intended for very specific purposes: for instance an R package allows to predict the amyloidogenicity propensity of polypeptide sequences. Depending on the package, this could be decided by looking at the DESCRIPTION file or by trial and error. We refer to Table 5 in Appendix D for the full list of discarded packages.

# 2. Templates for testing accuracy and speed

While inspecting the packages, we slowly developed a template for benchmarking that evolved over time. The final structure of this template (for each package) is as follows:

- 1. Set up the test environment loading of packages, setting working directory and options;
- 2. Summary of tested datasets;
- 3. Loop over datasets:
  - a. setting parameters for a specific dataset,
  - b. selecting benchmark options,
  - c. training a neural network with a tuned function for each package,

- d. calculation of convergence metrics (RMSE, MAE, WAE)<sup>2</sup>,
- e. plot each training over one initial graph, then plot the best result,
- f. add results to the appropriate existing record (\*.csv file) and
- g. clear the environment for next loop.
- 4. Clearing up the environment for the next package. It is optional to print warnings.

To simplify this process, we developed the NNbenchmark package, of which the first version was created as part of GSoC'19, containing testing functions and datasets. In GSoC'20, 3 new functions encapsulating the template were added that have been made generic with the extensive use of the do.call function from the base package:

- 1. In trainPredict\_1mth1data a neural network is trained on one dataset and then used for predictions, with several utilities. Then the performance of the neural network is exported, plotted and/or summarized.
- 2. trainPredict\_1data serves as a wrapper function for trainPredict\_1mth1data for multiple methods.
- trainPredict\_1pkg serves as a wrapper function for trainPredict\_1mth1data for multiple datasets.

For this paper, the training process (3.b to 3.g) is carried out with NNbenchmark's trainPredict\_1pkg using the NNsummary function computing convergence metrics and speed. The package repository is at https://github.com/pkR-pkR/NNbenchmark, with template repository at https://github.com/pkR-pkR/NNbenchmarkTemplates, and outputs per package at https://theairbend3r.github.io/NNbenchmarkWeb/index.html. A usage example trainPredict\_1pkg is given in Appendix C, where nnet is tested on the fifth dataset uDmod1: hyperParams.nnet() sets up hyperparameters, NNtrain.nnet() is a wrapper of the fitting procedure nnet::nnet, NNpredict.nnet() is a wrapper of the predicting function, while NNclose.nnet() terminates the call. Finally, trainPredict\_1pkg is called using these 5 dedicated functions and a list of input parameters.

# 3. Ease of use scoring

We define ease-of-use measures to rate NN packages on their user-friendliness. Based on our understanding of what a user may be required to know or do when using a neural network package, we consider: (i) a measure for the availability of appropriate utility functions (ii) a measure for (non-trivial) examples (iii) a sufficient documentation (well-written manual, vignette(s)) (iv) a measure to rate the clarity of the R call to fit a given neural network.

Our ratings are as follows.

- 1. Utilities in R to deal with NN
  - a. a predict function exists = 1 star
  - b. scaling capabilities exist in the package = 1 star
- 2. Sufficient and reliable documentation
  - a. the existence of useful and relevant example(s)/vignette(s)
    - clear, with regression = 2 stars
    - unclear, examples use iris or are for classification only = 1 star
    - no examples = 0 stars
  - b. input/output is clearly documented, e.g., what values are expected and returned by a function
    - clear input and output = 2 stars
    - only one is clear = 1 star

<sup>&</sup>lt;sup>2</sup>We measure the quality of our model by RMSE, but the mean absolute error (MAE) and the worst absolute error (WAE) may help distinguish packages with close RMSE values. See Appendix A for definition of convergence metrics.

- both are not documented = 0 stars
- 3. User-friendly call to fit a NN
  - a. a single function with arguments passed as character, numeric, boolean or formula; and data as a data.frame or a matrix = 2 stars
  - b. a single function with model specification passed as a list or via a dedicated function; or data converted in a dedicated S3/S4 object = 1 star
  - c. multiple functions for initializing-converting-fitting = 0 star

Hence, the utility rating gives an indication to users if the package includes a predict function and/or a scaling argument. It is worth mentioning many R packages provide scaling, standardizing functions. Indeed, **bdpar**, **binst**, **dataprep**, **discretization**, **helda**, **Pre-Processing**, **preputils**, **recipes** offer general data pre-processing functions, there are many more packages providing topic specific pre-processing. We do not consider in this paper any of these packages and only rate pre-processing functions in the package. Furthermore, to inform users about the usability of packages, the documentation measure ranges from 0 to 4 stars, while the utility and the R call range from 0 to 2 stars.

## Phase 3 - Collection of and analysis of results

## Results collection

Looping over the datasets using each package template, we collected results in the relevant package directories that rests in the templates repository. A large number of runs were carried out in order to obtain the best result for every package.

# **Analysis**

To rank the speed and quality of convergence, we have devised the following method:

- 1. The results datasets are loaded into the R environment as one large list. The dataset names, package:algorithm names and all 10 run numbers, durations, and RMSE are extracted from that list.
- 2. For the duration score (DUR), the duration is averaged by dataset. 3 criteria for the RMSE score by dataset are calculated:
  - a. The minimum value of RMSE for each package: algorithm as a measure of their best performance;
  - b. The median value of RMSE for each package:algorithm as a measure of their average performance, without the influence of outliers;
  - c. The spread of the RMSE values for each package which is measured by the difference between the median and the minimum RMSE (subsequently referred to as RMSE D51).
- 3. Then, the ranks are calculated for every dataset and the results are merged into one wide dataframe.
  - a. The duration rank only depends on the duration;
  - b. For minimum RMSE values, ties are decided by duration mean, then the RMSE median:
  - c. For median RMSE values, ties are decided by the RMSE minimum, then the duration mean;
  - d. The RMSE D51 rank only depends on itself.
- 4. A global score over all datasets is computed by summing the ranks (of duration, minimum RMSE, median RMSE, RMSE D51) of each package:algorithm for each dataset.
- 5. The final table is the result of ranking by the global minimum RMSE scores for each package: algorithm.

Global score Global score Package Algorithm Time RMSE Package Algorithm Time **RMSE** 41. NashLM trainwgrad\_RMSprop nlsr automl rminer 45. nnet\_optim(BFGS) 12 2 10. trainwpso 57 43 nnet 42. optim (BFGS) 3 3 deepnet 20. BP 18 56. optim(BFGS) 35 4 19 21 38. rprop+ 60 8 37. rprop-21 22 57. optim(CG) 58. optim(L-BFGS-B) 15 validann 36 neuralnet 40. slr 31 31 55 59. optim(Nelder-Mead) 45 39. sag 41 38 60. optim(SANN) 20 55 36. backprop 37 50 MachineShop 32. nnet\_optim(BFGS) 6 5 28. adamax 48 23 55. nnet\_optim(BFGS) 4 6 27. adam 42 34 radiant.model 44. nnet optim(BFGS) 10 29. nadam 44 36 9 34. optimx(BFGS) 58 37 26 keras 26. adagrad monmlp 47 35. optimx(Nelder-Mead) 32 25. adadelta 59 40 12. optim(BFGS) 46 10 31. sgd 48 44 **CaDENCE** 37 14. Rprop 56 51 30. rmsprop 52 13. pso psoptim 54 54 2. ADAPTgdwm 16 24 1. ADAPTgd 9 51 11 35 24. first-order h2o **AMORE** 23. nnet\_optim(BFGS) 40 EnsembleBase 5 12 4. BATCHgdwm 39 15. avNNet\_nnet\_optim(BFGS) 17 3. BATCHgd 39 41 caret 13 11. Gauss-Newton 8 14 minpack.lm 33. Levenberg-Marquardt 15 24 6. rmsprop grnn 43. nlm() 28 51. Rprop 24 17 ANN2 13 33 5. adam 52. SCG 30 18 7. sgd 11 42 53. Std\_Backpropagation 22 27 16. adam 32 46 47. BackpropChunk 26 29 19. rmsProp 34 53 RSNNS deepdive 48. BackpropMomentum 25 30 53 56 18. momentum 49. BackpropWeightDecay 29 31 17. gradientDescent 52 58 46. BackpropBatch 49 snnR 54. SemiSmoothNewton 7 48 43 elmNNRcpp 57 59 50. Quickprop 45 21. ELM 1 8. trainwgrad\_adam 50 18 ELMR 22 ELM 2 60 automl

Table 2: Results of Tested Packages (sorted by best RMSE score per package)

Note: Statistics over 10 runs.

## Results, discussion and recommendations

Table 2 gives the RMSE and time score per package and per algorithm. The full list of scores is given in Table 4 in Appendix D. Figure 2 shows the minimum RMSE value per package: algorithm for two particular datasets mIshigami and uDreyfus1, whereas Figure 3 displays the average computation time. The number on the x-level refers to the RMSE overall score of the package: algorithm given in Table 2 (last column), e.g., 8 refers to validann: optim(CG) which is a very slow algorithm as depicted in Fig. 3.

Both figures show that a good overall score does not necessarily imply a good performance on the two datasets under consideration. Furthermore, there is a break between the TOP-10 package:algorithm and others in terms of RMSE value. In Section 1.13 of the supplementary materials, (Mahdi et al., 2021), the score probabilities per package:algorithm also gives some insights how robust is the overall score.

Regarding computation time, we observe that some package:algorithm are very slow and have poor RMSE, e.g. 41 corresponding to AMORE:BATCHgd. In the following, we divide our analysis in two groups: packages implementing second-order algorithms and packages implementing first-order algorithms. Finally, we list the reasons for discarded packages.

## Second-order algorithms

Of all approaches, the following second-order algorithms generally performed better in terms of convergence despite being limited to  $1/5^{th}$  or fewer iterations than the first-order algorithms.

We note that 11 out of 15 of these package: algorithms use optim from stats. 2 of them,

Table 3: Ease of use of Tested Packages

	Individual score			Input allowed					
Package	Util	Doc	Call	Formula	XY	Comments			
AMORE	*	***	*	no	yes	train() needs newff() call for model spec			
ANN2	**	***	**	no	yes	neuralnetwork() needs only character, numeric, boolean but train() needs neuralnetwork()			
automl	*	***	*	no	yes	automl_train_manual() needs a list for model spec			
brnn	**	****	**	yes	yes	brnn() needs only character, numeric, boolean or a formula			
CaDENCE	**	***	*	no	yes	cadence.fit() needs a list, numeric, boolean			
caret	**	***	**	yes	yes	avNNet() needs only character, numeric, boolean or a formula			
deepdive	**	***	**	no	yes	deepnet() needs only character, numeric, boolean			
deepnet	*	***	**	no	yes	nn.train() needs only character, numeric, boolean			
elmNNRcpp	**	***	**	no	yes	elm_train() needs only character, numeric, boolean			
ELMR	**	***	**	yes	yes	OSelm_train.formula() needs a formula, data.frame, but Oselm_training() needs matrix, numeric			
EnsembleBase	*	*	*	yes	no	Regression.Batch.Fit() needs a function for model spec and a formula			
h2o	**	**	*	no	yes	h2o.deeplearning() needs character, boolean, numeric and a dedicated function to convert data in S3			
keras	**	*		no	yes	fit() needs multiple function for model spec keras_model() and initiate model compile()			
MachineShop	*	***	*	yes	yes	fit() needs NnetModel() for model spec and formula / data.frame / recipe			
minpack.lm	*	***	*	yes	no	nlsLM() needs a formula, data.frame and list for control parameter			
monmlp	**	***	**	no	yes	monmlp.fit() needs only character, numeric, boolean			
neuralnet	*	***	**	yes	no	neuralnet() needs formula, data.frame, boolean, character			
nlsr	*	****	*	yes	no	nlxb() needs a formula, data.frame and list for control parameters			
nnet	*	***	**	yes	yes	nnet() needs only character, numeric, boolean or a formula			
qrnn	**	***	**	no	yes	qrnn.fit() needs only character, numeric, boolean			
radiant.model	**	**	**	no	yes	nn() needs only character, numeric, matrix			
rminer	**	***	**	no	yes	fit() needs a formula, data.frame, character and numeric			
RSNNS	**	***	**	no	yes	mlp() needs only character, numeric, boolean			
snnR	**	**	**	no	yes	snnR() needs only character, numeric. Package archived.			
traineR	*	**	**	yes	no	train.nnet() needs a formula, data.frame, numeric, boolean			
validann	*	****	**	no	yes	ann() needs only character, numeric			

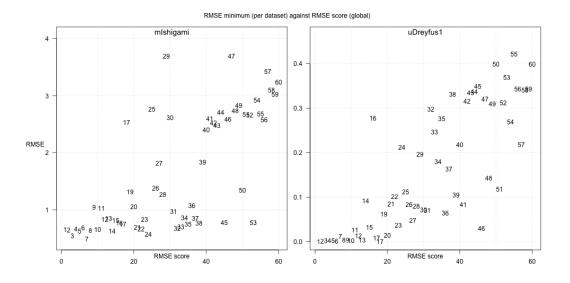


Figure 2: RMSE minimum value per package for mIshigami and uDreyfus1 datasets

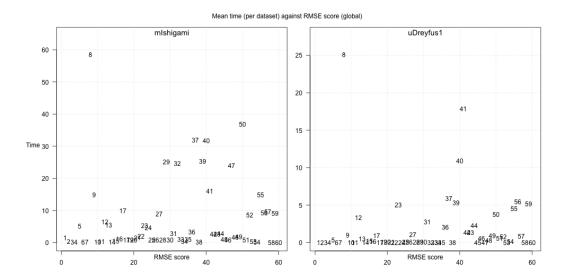


Figure 3: Average time value per package for mIshigami and uDreyfus1 datasets

CaDENCE's BFGS (Cannon, 2017a) and validann's BFGS and L-BFGS-B (Humphrey, 2017), make the call directly. However, it is not clearly stated in CaDENCE's documentation that optim's BFGS method has been chosen rather than one of the other four methods. Furthermore, the mention of Nelder-Mead in the documentation suggests that optim's Nelder-Mead method is used. Speed and variation between results for CaDENCE are also not as good as other packages that use optim. This could be because CaDENCE is intended for probabilistic non-linear models with a full title of "Conditional Density Estimation Network Construction and Evaluation".

By contrast, **validann** is clearly a package that allows a user to use all optim's algorithms. **validann**:L-BFGS-B ranks mostly lower than **validann**:BFGS, despite the former method being more sophisticated. We believe this is due to our efforts to harmonize parameters, thereby under-utilizing the possibilities of the L-BFGS-B algorithm. Both **CaDENCE** and **validann**'s BFGS are outperformed by **nnet**, especially in terms of speed.

**nnet** (Ripley, 2020) differs from the two packages above because it uses the C code for BFGS (vmmin.c) from optim (converted earlier from Pascal) directly instead of calling optim from R. This may be what allows it to be faster, but limits the optimization to the single method. **nnet** is only beaten by the Extreme Learning Machine (ELM) algorithms in terms of speed. However, there is a larger variation between results (see the RMSE D51 in Appendix D) in comparison to **validann**:BFGS. We believe the different default starting values are the cause of this. For instance, **nnet** uses a range of initial random weights of 0.7 while **validann** uses a value of 0.5. In spite of these results, the real reason most authors or users are likely to choose **nnet** is because it is included in the distributed base R and is even mentioned as the very first package in CRAN's task view for machine learning (*MachineLearning*).

Our analysis found that 6 out of 11 packages tested that use optim do so through **nnet**. Moreover, approximately 8 packages for neural networks, though not tested, use **nnet**.

The total number of **nnet** dependencies found through a search through the offline database of CRAN with **RWsearch** is 136 packages, although some might be using **nnet** for the multinomial log-linear models, not neural networks.

The packages that use **nnet** for neural networks are often meta packages with a host of other machine learning algorithms. **caret** (Kuhn, 2020), also mentioned in the task-view, boasts 238 methods with 13 different neural network packages, under a deceivingly simple name of "Classification and Regression Training". It has many pre-processing utilities available, as well as other tools.

EnsembleBase (Mahani and Sharabiani, 2016) may be useful for those who wish to

make model ensembles and test a grid of parameters, although the documentation is rather confusing. **MachineShop** (Smith, 2020) has 51 algorithms, with some additional information about the response variable types in the second vignette, functions for preprocessing and tuning, performance assessment, and presentation of results. **radiant.model** (Nijs, 2020) has an unalterable maxit of 10000 in the original package. We changed this to harmonize the maxit parameter. **rminer** (Cortez, 2020) is the only package dependent on **nnet** that ranks above **nnet** at number 2 for minimum RMSE, and even number 1 in some runs. It also ranks number 1 on the other accuracy measures (median RMSE, minimum MAE, minimum WAE) and is only behind **deepdive** and **minpack.lm** in terms of results that are consistent and do not vary (RMSE D51).

The difference is probably from the change of maximum allowable weights in **rminer** to 10000 from 1000 in **nnet**, which is also probably the reason its fits are slower. **traineR** (Rodriguez R., 2019) claims to unify the different methods of creating models between several learning algorithms.

It is worth noting is that **nnet** and **validann** do not have external normalization, which is especially recommended for **validann**. However, some of the packages dependent on **nnet** do have this capability and it is included in the scoring for ease of use. With **NNbenchmark**, this is done through setting scale = TRUE in the function prepare.ZZ. Note that use of scaling may complicate the application of constraints, so not be worth the effort for some users. Nevertheless, users might want scaling, or at least to have a clear explanation of the method chosen to center the variables. Scaling of both function and parameters is one of the features that **optimx** (Nash and Varadhan, 2020) incorporates, as some optimization algorithms can work significantly better on scaled problems (Nash, 2014).

Of all the packages, only monmlp (Cannon, 2017b) calls optimx. Since the calls are for BFGS and Nelder-Mead, they could do better to call optim directly, though the door is open to other optimization methods in optimx. However, the author, Alex J. Cannon who is also the author of CaDENCE, has created a package meant to fill a certain niche, namely for multi-layer perceptrons with optional partial monotonicity constraints. GAM-style effect plots are also an interesting feature. Another package by Alex Cannon is qrnn (Cannon, 2019) which uses yet another algorithm: nlm, a "Newton-type" algorithm, from stats. Although its performance is at the bottom of second-order algorithms, sometimes even being beaten by first-order algorithms, this could also be because of the intended use of the package compared to the tests here. qrnn is designed for quantile regression neural networks, with several options. Alex Cannon has included automatic scaling for all 3 of his packages, as is clearly documented.

Non-linear least square estimation can be performed via nls from stats, which defaults to an implementation of the second-order algorithm referred to as Gauss-Newton. However, in its documentation, nls warns against "zero-residual" or even small residual problems (Nash, 2014, Section 6.4.1). This was one of the motivations for nslr (Nash and Murdoch, 2019). nlsr uses a variant (Nash, 1977) of the Levenberg-Marquardt algorithm versus the plain Gauss-Newton of nls, and modifies the relative offset convergence criterion to avoid a zero divide when residuals are small and can handle a degenerate Jacobian at the first iteration.

minpack.lm (Elzhov et al., 2016) offers another Marquardt approach. While nlsr is entirely in R, and also allows for symbolic or automatic derivatives (which are not relevant to the present study), minpack.lm uses compiled Fortran and C code for some important computations. Its structure is also better adapted to use features already available in nls that may be important for some uses.

Despite the 2 packages ultimately performing well on all runs (capable of being in the top 3 for RMSE as good as packages using BFGS and not being slow), there are some reasons why users might hesitate to choose them. Firstly, both minpack.lm and nlsr require the full formula of the neural network including variables and parameters. Secondly, they require good starting values to achieve the best convergence. Notice that in Table 2, minpack.lm does not have a high rank. This is because we removed the random Gaussian start values we had originally used; which means that the default start values of minpack.lm were not

appropriate for our datasets.

We suspect nlsr's performance on convergence would have similarly dropped if it was possible to use nlsr with no user-set starting values and the author's chosen default values were inadequate. nls deals with this by suggesting a companion function in stats, selfStart. Furthermore, both packages were able to find better minima when the dataset was scaled. With no starting values and no scaling, minpack.lm:nlsLM fails on uNeuroOne but performance is better on Friedman & Ishigami datasets. On the other hand, with no start values and no scaling, it fails on everything but mFriedman, mIshigami, uDmod2, and the Dreyfus datasets. Similarly, there is also a notable drop in performance for nlsr without scaling on the Gauss datasets and mRef153. To conclude, both packages provide algorithms that are capable of doing well on our datasets, but may not be suitable for less experienced users. The vignettes for nlsr and earlier book (Nash, 2014) may be useful.

brnn (Rodriguez and Gianola, 2020) is an implementation of the Gauss-Newton algorithm in R that does not rely on nls or nlm from stats. Although it is well-documented and has good speed, brnn's implementation of the Gauss-Newton algorithm still ranks below some of the previously mentioned BFGS and Levenberg-Marquardt tools in terms of its global minimum RMSE. We found 2 reasons that we believe to be the cause of this. First, its model uses one parameter fewer than the other algorithms. Only datasets uDreyfus1 and uDreyfus2 which are purely 3 hidden neurons ignore the first term. Second, brnn does not minimize the sum of squares of the errors but the sum of squares of the errors plus a penalty on the parameters. In certain circumstances – especially with an almost singular Jacobian matrix as with mDette, mIshigami, mRef153, uGauss3, and uNeuroOne – this will avoid issues with highly correlated parameters.

The only second-order algorithm which we are unable to recommended from the results of our research is **snnR** (Wang et al., 2017). It ranked among the 10 worst algorithms for minimum RMSE out of all 60 algorithms, but this package, focusing on Sparse neural networks for Genomic Selection in Animal Breeding, might prove useful in that perspective.

#### Lower-order algorithms

Packages with first-order algorithms can be broadly categorized into 2 types: (a) those that allow for one hidden layer (b) those that allow for more than one hidden layer.

## A. One hidden layer

The first category is comprised of either packages that also include second-order algorithms previously discussed or packages that use the Extreme Learning Machine algorithm. Only 2 packages include both second-order algorithms and a lower-order algorithm, that is, monmlp and validann. monmlp has one algorithm besides BFGS, that is, optimx's Nelder-Mead. validann provides the same algorithm but from optim. validann's implementation is slower, as before, but ranks slightly better for minimum RMSE. Both implementations of Nelder-Mead do not rank well in minimum RMSE, around 40 out of 60, with similar ranks for the other criteria. We would also caution users to avoid the other methods in validann from optim. From Table 2 it may appear that validann's implementation of the Conjugate Gradient (CG) algorithm finds reasonable minima and is thus a good option. It consistently ranked in the top 15 with minimum RMSE. However, it is the slowest algorithm of all 60 algorithms tested. Note, this includes algorithms from packages that call external libraries outside R in Python or Java and packages that use as much as 100,000 iterations.

On the other hand, **validann**'s SANN algorithm is relatively worse than other packages as it ranks at number 55 for minimum RMSE although it is in the top one third for speed (rank 20).

Packages that implement the ELMR algorithm are similar to SANN from **validann** in the sense that they are faster but do not converge as well as other package's algorithms. The 2 packages that do so, **elmNNRcpp** (Mouselimis and Gosso, 2020) and **ELMR** (Petrozziello, 2015) are, respectively, number 1 and number 2 in the ranks for time but 59 and 60 (bottom 2) for minimum RMSE. **ELMR** converges slightly worse on all datasets than **elmNNRcpp** 

but has noticeably worse performance on the Gauss datasets, especially uGauss1. Even increasing the number of neurons did not lead to better convergence for those particular datasets.

#### B. More than one hidden layer

Following the trend of "deep learning", the last 9 packages provide the option for more than one layer with a first-order learning algorithm. Our results show that they are often either/both slower or worse at converging than the second-order algorithms with the same number of neurons or layers than their counterparts. We recommend choosing better algorithms over more layers for datasets similar to the ones we used.

Choosing more layers often comes at the expense of speed. An example of this is the implementation of the first-order algorithm in h2o (LeDell et al., 2020). With the same numbers of neurons it already is quite slow - coming in at 51 out of the 60 algorithms.

With a default hidden layer size of 2, each with 200 neurons, it takes around 10 minutes on mFriedman with a minimum RMSE of 0.0022. On the other hand, nnet can find a minima of the error function with a minimum RMSE of 0.0088 in less than a second with fewer neurons and only one layer with 3 neurons. Thus, despite having a ranking of 11 in minimum RMSE in the final run, beating some of the second-order algorithms, users of h2o should be wary of the trade off between performance and speed. Moreover, users might hesitate as it is not actually clear what algorithm is used. The large number of options to choose from seem capable of changing the basic algorithm itself into what is considered a different algorithm by other packages (example: "adaptive\_rate: Specify whether to enable the adaptive learning rate (ADADELTA). This option is enabled by default." in link, set to false in latest run). Some users also might not want to setup Java, which is needed, although it is not as painful to setup as some external libraries.

By far, the hardest package to set up which called external libraries was **tensorflow** (Allaire and Tang, 2020) and its derivatives. In the summer of 2019, it took quite some time to figure out how things worked. Then the latest TensorFlow 2.2.0 became available and we hoped to be able to use the Eager Execution provided to avoid the R Session crashing in the summer of 2020. Unfortunately, this led to different problems with the translation between R and Python so we could not use the 2019 code. **tfestimators** (Allaire et al., 2018) had also similar issues and is even less supported. **kerasR** (Arnold, 2017), which provides a consistent interface to Keras, a Python API which provides an easier use interface to TensorFlow, had the same issue. In the end, we tested the algorithms in **keras** (Allaire and Chollet, 2020) with the hope that it would be able to represent the performance of the other packages.

keras has the second-most number of algorithms, a total of 7, with most of them being "adaptive" algorithms. The highest ranking algorithm for minimum RMSE is adamax at 23 and the highest ranking algorithm for speed was rmsprop at 37 (quite slow). However, these results were achieved with a reasonable GPU so users might want to decide on whether to use keras based on their own hardware specifications. Other algorithms did not perform well in terms of minimum RMSE and the spread of RMSE represented by RMSE D51. As keras has also many options available, including a convolutional layer for CNNs, more experienced users may prefer it. On the other hand, just deciding the learning rate (the default was not appropriate for our datasets) can be a real challenge.

The default learning rates in RSNNS (Bergmeir, 2019) were more appropriate to use directly. RSNNS is an example of a package that directly wraps around an external library, the Stuttgart neural network Simulator (SNNS), to provide an easy-to-use interface. This library is rather large with many implementations of neural networks. It contains the biggest number of algorithms tested at a total of 8. Algorithms Rprop and SCG, the best for minimum RMSE, rank at 16 and 17 respectively which is pretty good for a first-order algorithm. Speed for Rprop is better but SCG's results vary less.

#### Other packages

**AMORE** (Limas et al., 2020): Unfortunately, the focus of the paper behind this package, its unique point, is not explained or documented well enough.

An addition of some examples using the TAO option as the error criterion would be

helpful for using the TAO-robust learning algorithm, since this type of error measure is most useful for data with outliers. The function for creating a dot file to use with <a href="http://www.graphviz.org">http://www.graphviz.org</a> is also interesting. ADAPT algorithms appear to perform better than the BATCH algorithms with the parameters used in this research.

ANN2 (Lammers, 2020): This package's implementation of adam or rmsprop consistently ranked in the top half for minimum RMSE which is not bad for a first-order algorithm. It is not as accurate as second-order algorithms but all its algorithms are quite fast. C++ code was used to enhance the speed. Functions for autoencoding are included with anomaly detection in mind.

automl (Boulangé, 2020): It would be easier to use the algorithms in this package if they did not rely on the beta parameters and instead had an argument of their own. However, it is nice that there are notes on what parameters have a higher tuning priority. The package is rather slow (highest ranking algorithm for speed is RMSprop at 47) with good enough convergence (highest ranking is adam at 18).

**deepdive** (Balakrishnan, 2020): All algorithms are very good in terms of little variance between results (see its RMSE D51 score). However, the results on convergence by minimum RMSE score are not as good with the worst being gradientDescent which ranks 3rd from the bottom. There are few exported functions. The novelty of this package is apparently in the deeptree and deepforest functions it provides.

**deepnet** (Rong, 2014): This is one of the better performing implementations of the first-order algorithms back-propagation, ranking at 18 for minimum RMSE. It is relatively fast, ranking at 23 for speed.

**neuralnet** (Fritsch et al., 2019): Considering that this is the only package that uses 100000 iterations as its maxit parameter (excluding BNN which is not included in the official ranks), it can be considered as not recommended. Nonetheless, the default algorithm, rprop+ and the similar rprop-, managed to rank 20 and 21 respectively, out of 60 algorithms for minimum RMSE. These two also do not do badly in terms of speed. Following, in order, are slr, sag, and traditional backprop as the worst at rank 48 out of 60 for minimum RMSE. Notes on documentation show that is rather difficult to configure this package, and it should probably not be a dependency for other packages that wish to be more certain of the results. For simple datasets, it is less of an issue.

## Untested packages

A certain number of packages have been discarded from this study for at least one of the following reasons:

- 1. For regression but unsuitable for the scope of our research, coded RE in Table 5.
- 2. For time series, coded TS in Table 5.
- 3. For classification, coded CL in Table 5.
- 4. For specific application purpose, coded AP in Table 5.
- 5. For tools to complement NN's by other packages, coded UT in Table 5.
- 6. Not actually neural networks and other reasons, coded XX in Table 5.

The full list of untested packages is given in Table 5 in Appendix D.

# Further analysis of TOP-5 packages

We perform a second round of analysis with a larger dataset and a focus on the TOP-5 packages given in Table 2. That is, we consider packages **nlsr**, **rminer**, **nnet**, **validann** with algorithm BFGS and **MachineShop**. We fit the NN packages on Simon Wood's Gaussian dataset, see bWoodN1 in dataset description, which contains 20,000 rows with 6 inputs valued in [0,1] for a (single) numeric output. Due to the non-linear functions considered, see Appendix B, the link between the output and each explanatory variable is highly non-linear

validann

RMSE median RMSE min RMSE D51 MAE median Package Algorithm WAE median Time median MachineShop 32. nnet\_optim 3 547 4 756 1 2100 3 901 16.02 3 40 3.548 4.706 1.1570 3.801 76.73 41. NashLM 16.56 nnet 42. optim 3.550 4.706 1.1560 3.801 16.57 3.38 45. nnet optim 3.366 0.3218 2.956 15.43 11.07 rminer 3.688

1.1370

3.711

15.89

140.80

**Table 4:** Performance on bWoodN1 dataset

Note: statistics taken over 20 runs; time in seconds.

3.360

56. optim

which greatly affects the fitting time. Table 3 gives the metric performance over 20 runs of these TOP-5 five packages on bWoodN1.

4.497

We observe that the minimum RMSE (over 20 runs) is very similar for all packages, yet **rminer** and **validann** are a little ahead of the others. The metrics median RMSE and RMSE D51 reveal how consistent **rminer**'s results are in comparison to other packages. This is further proved by the other metric norms: WAE and MAE. However, regarding computation time **rminer** is the 3rd slowest with **nlsr** being the 2nd slowest and **validann** being the slowest of all. The best two in terms of speed in this class are **nnet** and **MachineShop**. Nevertheless, these TOP-5 packages performs generally better than other packages, see Section 2.1 of the supplementary materials, (Mahdi et al., 2021). In Section 2.1 of the supplementary materials, we observe that only 2 packages (in the TOP10) have a RMSE minimum close to the RMSE of TOP5 packages: CaDENCE and traineR. Hence, other non-TOP10 packages will be far worse on the bWoodN1 dataset.

Figures in Section 2.2 of the supplementary materials, (Mahdi et al., 2021), provides some insights where a package performs reasonably well with respect to one explanatory variable and where the fit misses the correct behavior of an explanatory variable.

# Conclusion and perspective

This paper focuses on benchmarking neural network packages available on CRAN to recommend or advise against some packages. Based on **RWsearch**'s outputs in 2019-2020, we selected 26 appropriate packages to analyze in-depth and discarded the other 63 packages. Using **NNbenchmark**, we ranked 60 package: algorithm pairs and are happy to note that most of them converge well enough within a reasonable time. Packages reviewed appear to offer essentially the same methods, and second-order algorithms perform generally better than first-order algorithms.

**nnet**, the most recommended package of our study, ranked third in terms of minimum RMSE, and is probably the most efficient package. **nnet** is notably used by many other packages, such as **MachineShop** and **rminer** respectively ranked fifth and second. **MachineShop** and **rminer** are also very good challengers in our benchmark, in particular when considering a larger dataset. Other packages in the TOP-5, **nlsr** (the best in terms of RMSE minimum) and **validann** are efficient packages but a little bit slower in our analysis.

However, we are disappointed that many of the packages we reviewed had poor documentation, notably **EnsembleBase** and **keras**. We often found it difficult to discover what default starting values were used for model parameters and/or to understand how to change the hyper-parameters.

As the field of neural networks continues to grow, there will always be more algorithms to validate. For current algorithms in R, our research should be extended to encompass more types of neural networks and their data formats (classifier neural networks, recurrent neural networks, and so on). Different rating schemes and different parameters for package functions can also be tried out.

Our work is available online through https://theairbend3r.github.io/NNbenchmarkWeb/index.html and is entirely reproducible thanks to **NNbenchmark**. We hope users and package maintainers find our work useful and will provide any necessary feedback. In the future, we plan to use a larger list of benchmark datasets, such as the OpenML-CC18 database from

https://www.openml.org/available in R thanks to the OpenML package. Ideally, we hope to generate such a benchmark on a regular basis as packages get updated.

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# **Appendix**

# Appendix A

Consider a set of observations  $y_i$  and its corresponding predictions  $\hat{y}_i$  for i = 1, ..., n. The three metrics used were:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|, \ RMSE = \frac{1}{n} \sqrt{\sum_{i=1}^{n} (y_i - \hat{y}_i)^2}, \ WAE = \frac{1}{n} \max_{i=1,\dots,n} |y_i - \hat{y}_i|.$$

These values represent the absolute, the squared and the maximum norm of residual vectors.

#### Appendix B

We define five smooth functions for Simon Wood's test dataset

$$f_0 = 5\sin(2\pi x), \ f_1 = \exp(3x) - 7,$$
 
$$f_2 = 0.5 \times x^{11}(10(1-x))^6 - 10(10x)^3(1-x)^{10}, \ f_3 = 15\exp(-5|x-1/2|) - 6,$$
 
$$f_4 = 2 - 1_{(x<=1/3)}(6x)^3 - 1_{(x>=2/3)}(6-6x)^3 - 1_{(2/3>x>1/3)}(8+2\sin(9(x-1/3)\pi)).$$

# Appendix C

An example of our template for the package nnet:

```
library(NNbenchmark)
nrep <- 3
odir <- tempdir()

library(nnet)
nnet.method <- "BFGS"
hyperParams.nnet <- function(...) {
    return (list(iter=200, trace=FALSE))
}
NNtrain.nnet <- function(x, y, dataxy, formula, neur, method, hyperParams, ...) {</pre>
```

# uDmod1\_nnet::nnet\_BFGS

# uDmod1\_nnet::nnet\_BFGS

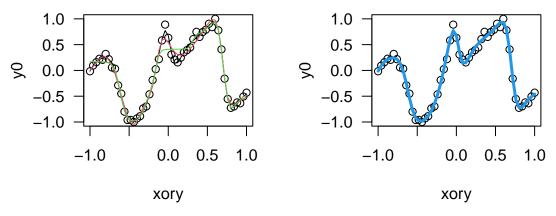


Figure 4: Example of nnet on uDmod1

# Appendix D

Table 6: Review of Discarded Packages

Package	Category	Reason to Discard (File(s) and/or function(s))
appnn	AP	Provide a feed forward neural network to predict the amyloidogenicity propensity of polypeptide sequences (DESCRIPTION file)
autoencoder	AP	Provide a sparse autoencoder, an unsupervised algorithm that learns useful features from the data its given (::autoencode)
BNN	RE*	Use a feed forward neural network to perform regression. It is unclear whether it fits the form of perceptron in the scope. It states that it is intended for variable selection, although how exactly the package would be used to do so is missing. Also the source code is written in C that users of R might not understand. Performance is slow: need 100.000 iterations. (::BNNsel-examples & abstract of paper)
Buddle	CL	Did not include regression in 2019. Unfortunately, the version we tested in 2020 could not be used properly for regression either. See the examples (::TrainBuddle)
cld2	XX	Provide bindings to Google's C++ library CLD2, which detects languages using a Naïve Bayesian classifier. CLD3, which does use neural networks, is mentioned in the description (DESCRIPTION file & link to github)
cld3	AP	Bindings to Google's C++ library CLD3, which detects languages using a neural network with an experimental algorithm (DESCRIPTION file)
condmixt	AP	Use neural networks to predict parameters of mixture models (DESCRIPTION file)
DamiaNN	RE	Was designed specificly for training datasets from Numerai, <a href="https://numer.ai/">https://numer.ai/</a> . We were unable to adapt it to our datasets even after exporting functions from the interactive interface (DESCRIPTION file, help pages)
deep	CL	Seem to implement a perceptron to classify data (implicitly known from choice of iris as example and in source code)

 Table 6: Review of Discarded Packages (continued)

Package	Category	Reason to Discard (File(s) and/or function(s))					
deepNN	RE	Another implementation of deep learning. Its input format of lists of vectors is not standard require users to understand how to use lapply or other functions to convert the format of their data. Univariate datasets can't be used with the functions and we could not manage to adapt it to 2020 code (::train).					
DNMF	XX	Help extract features that enforce spatial locality with separability between classes in a discriminant manner (DESCRIPTION file)					
evclass	CL	Provide an evidential neural network that outputs Dempster-Shafer mass functions (DESCRIPTION file)					
gamlss.add	UT	Allow users to use nnet with a variety of Generalized Additive Models for Location Scale					
gcForest	XX	and Shape (::nn). It is not particularly appropriate for all our datasets.  Based on an article with "Towards an Alternative to Deep Neural Networks" in its title (DESCRIPTION file)					
GMDH	TS	Provide GMDH type neural network algorithms for short term forecasting on a univariate time series (DESCRIPTION file)					
GMDH2	CL	Provide GMDH type neural network algorithms for performing binary classification (DESCRIPTION file)					
GMDHreg	RE*	Regression using GMDH algorithms. We only managed to tested the COMBI algorithm (th most basic and first in the vignette) on the multivariate datasets. It is strangely slow on the "easy" datasets, mFriedman and mRef153. The convergence is relatively not good					
gnn	AP	considering the ammount of layers (Title in DESCRIPTION file)  Out of scope: Generative moment matching networks (GMMNs) are introduced for generating quasi-random samples from multivariate models (article abstract)					
grnn	RE	Provide an implementation of Specht's General Regression Neural Network in 1991 (DESCRIPTION file). We could not manage to make the functions work on the multivariate datasets. ::guess, the function for predicting, only allows for 1 data at a time. Performance of General Regression Neural Networks can be seen from package yager instead.					
hybridEnsemble	RE	Hybrid ensemble of eight different sub-ensembles (DESCRIPTION file)					
image.libfacedetection	AP	Face detection with CNNs (DESCRIPTION file)					
isingLenzMC	AP	Out of scope: This package provides utilities to simulate one dimensional Ising Model with Metropolis and Glauber Monte Carlo (DESCRIPTION file)					
kerasR	RE	See section on keras					
leabRa	RE	Provide the local error driven and associative biologically realistic algorithm (Leabra) from O'Reilly 1996. It combines supervised and unsupervised learning, so out of scope (DESCRIPTION file).					
learNN	CL	Implement some basic neural networks from \url{http://qua.st/} (DESCRIPTION file). Examples seem to focus on binary classification (::learn_gd, ::learn_bp).					
LilRhino	AP	Provide binary neural networks meant for reducing data (DESCRIPTION file), a random forest style collection of neural networks for classification (::Random_Brains), and code for even more purposes. Documentation is satisfyingly clear for a package for applications: a 3 layer network with an adam optimizer, with an explanation of its activation functions (::Binary_Network)					
neural	CL	An implementation of "a simple MLP neural network that is suitable for classification tasks (::mlptrain)					
NeuralNetTools	UT	Out of scope: Functions are available for plotting, quantifying variable importance, conducting a sensitivity analysis, and obtaining a simple list of model weights (DESCRIPTION file and Help Pages titles)					
NeuralSens	UT	A greater focus on sensitivity, with additional functions (DESCRIPTION file)					
NlinTS	TS	A non-linear version of a causality test with feed forward neural networks and a Vector Auto-Regressive Neural Network (VARNN) for non-linear time series analysis models (DESCRIPTION file)					
nnetpredint	UT	Out of scope: Computing prediction intervals of neural network models at certain confidence level (DESCRIPTION file)					
nnfor	TS	Automatic to fully manual time series modelling with neural networks (DESCRIPTION file					
nnlib2Rcpp	CL	Provide a collection of neural networks, but examples seem to indicate classification and testing our code with the functions provided led to error. Using the RcppClass might be					
nntrf	AP	confusing for less experienced R users (::NN-class)  Provide useful pre-processing for Machine Learning tasks through data transformation in a non-linear, supervised way with a perceptron (DESCRIPTION file)					
onnx	UT	Aims to provide an open source format for neural networks, with definitions of an extensible computation graph model, built-in operators, and standard data types (DESCRIPTION file)					
OptimClassifier	UT	Search for the best amount of neurons for binary classification neural networks, among other types of binary classifiers (based on how Optim.NN works & DESCRIPTION file)					
OSTSC	UT	A tool to solve imbalanced data for univariate time series classification with oversampling using integrated ESPO and ADASYN methods (DESCRIPTION file) thus improving the performance of RNN classifiers (vignette)					

 Table 6: Review of Discarded Packages (continued)

Package	Category	Reason to Discard (File(s) and/or function(s))					
passt	AP	This package provides implementation of the Probability Associator Time (PASS-T) model, a memory model based on a simple competitive artificial neural network which imitates human judgment of frequency and duration (DESCRIPTION file)					
pnn	CL	This package provides implementation of the Specht algorithm, 1990, for classification with four functions: learn, smooth, perf, and guess (DESCRIPTION file)					
polyreg	XX	Polyregression as alternative to NN (DESCRIPTION file)					
predictoR	RE	A shiny interface for supervised learning with very minimal documentation. Users may be additionally confused when opening the application only to find that it's default language is Espanol, although this can be changed in the Idioma section. (DESCRIPTION file & ::init_predictor)					
ProcData	AP	Provide tools for exploratory process data analysis via functions: reading, process manipulation, action sequence generators, feature extraction and prediction (link + DESCRIPTION file)					
quarrint	AP	Out of scope: provide two indexes for interaction prediction between groundwater and quarry extension, one of which is an artificial neural network; specified classifier for quarry data (help page - quarrint-package and DESCRIPTION file)					
rasclass	CL	Provide neural networks as one of the five supervised classification algorithms for raster images with a design meant to facilitate land-cover analysis (DESCRIPTION file)					
rcane	RE	Provide parameter estimation for linear regression, which was not appropriate for the relationships in our data. (DESCRIPTION file)					
regressoR	RE	A manual rich version of predictoR					
rnn	AP	Implementations of the vanilla Recurrent Neural Network, Long Short-Term Memory (LSTM), and Gated Recurrent Unit (GRU) in native R (DESCRIPTION file)					
RTextTools	AP	Out of scope: A machine learning package for automatic text classification (DESCRIPTION file)					
ruta	AP	unsupervised neural networks (DESCRIPTION file)					
simpleNeural	CL	Neural networks for multi-class or binary classification (DESCRIPTION file)					
softmaxreg	CL	Out of scope: Implementation of 'softmax' regression and classification models with multiple layer neural network (DESCRIPTION file)					
Sojourn.Data spnn	AP CL	Stores some neural networks used for Sojourn Accelerometer methods (DESCRIPTION file) Out of scope: Scale invariant version of the original PNN with the added functionality of allowing for smoothing along multiple dimensions while accounting for covariances within the data set (DESCRIPTION file)					
studyStrap	AP	Implements multi-study learning algorithms such as merging, the study-specific ensemble the study strap, the covariate-matched study strap, covariate-profile similarity weighting, and stacking weights with single-study learners from caret (DESCRIPTION file)					
TeachNet	CL	Provide neural networks with up to 2 hidden layers, 2 different error functions, and a weight decay for 2 class classification: it is slow. (DESCRIPTION file & ::TeachNet)					
tensorflow	RE	See section on keras					
tfestimators	RE	See section on keras					
trackdem	AP	An artificial neural network can be trained for filtering false positives present in video materials or image sequences (DESCRIPTION file)					
TrafficBDE	RE*	Use caret for a grid of parameters for 3 layers combined with neuralnet. Is very slow. Out of scope to test one layer perceptrons. We recommend the author to use other packages and lessen the number of layers. Datasets in Traffic Status Prediction and Urban Places are similar in nature to ours (TrainCR.R, DESCRIPTION file)					
tsfgrnn	TS	Out of scope: A general regression neural network (GRNN) is a variant of a Radial Basis Function Network. Allow you to forecast time series using an autoregressive GRNN model (DESCRIPTION file)					
yager	RE*	This package provides a neural network that behaves differently from a perceptron. Results indicate that predictions are quite close to the real values, however this comes at the cost of a large number of weights. With less weights or insufficient training data, the performance isn't as great. (::grnn.fit)					
yap	CL	Yet another PNN, with a N-level response, where N > 2 (DESCRIPTION file)					
zFactor	AP	Computational algorithms to solve equations and find the 'compressibility' factor ' $z$ ' of hydrocarbon gases (DESCRIPTION file)					

Note: AP=Application, CL=Classification, RE=Regression, RE\*=?, TS=Time serie, UT=Utility, XX=Other.

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 $\textbf{Table 5:} \ All \ convergence \ scores \ per \ package: algorithm \ sorted \ by \ minimum \ RMSE$ 

Name			Inpu	RMSE Score		Other score			
miner	ckage	Algorithm	Input format	Maxit	Maxit Learn. rate		D51	MAE WA	
miner	r	41. NashLM	full fmla & data	200	_	3	16	3	6
Name									
Se optim(BFCS)	iner	45. nnet_optim(brG5)	imia & data		-				1
S7. optim(CG)	et	42. optim (BFGS)	x & y	200	-	2	17	2	3
S8. optim(L-BFGS-B)			•		-				5
59. optimi(SAINY)		-			-				4
60. optim(SANN)	ıdann	•			-				13 42
MachineShop   32   nnet_optim(BFCS)   fmla & data   200   -   9   22   9		•							55
	1: 01		<u> </u>						
Additional analysis	cnineSnop	32. nnet_optim(BFGS)			-				7
Manumalp   34. optimx(BFCS)	ineR	55. nnet_optim(BFGS)	fmla & data	200	-	5	15	6	2
Cade	iant.model	44. nnet_optim(BFGS)	"y" & data	200	-	8	32	12	10
S. Optimi(Nicolaci-visical)   X & Y   1000   -   47   45   45   45	nmln	34. optimx(BFGS)	x & y	200	-	10	18	9	11
Cade Name         14. Ryrop         x & y         1000         0.01         54         60         52           12.0         24. first-order         "y" & data         10000         0.01         7         7         8           EnsembleBase         23. nnet_optim(BFGS)         x & y         200         -         15         34         15           caret         15. avNNet_nnet_optim(BFGS)         x & y         200         -         10         21         11           brnn         11. Gauss-Newton         x & y         200         -         12         9         13           qrm         43. nlm()         x & y         200         -         14         25         7           Fine Rynn         x & y         200         -         14         25         7           Fine Rynn         x & y         1000         -         23         52         25         36         36	шпр	35. optimx(Nelder-Mead)	x & y	10000	-	47	45	44	47
13, pso_psoptim		12. optim(BFGS)	x & y						40
No.   Process	DENCE		•						58
EnsembleBase   23. nnet_optim(BFGS)		13. pso_psoptim	x & y	1000	-	56	56	54	56
15. avNNet_nnet_optim(BFCS)   x & y   200   -   10   21   11	)	24. first-order	"y" & data	10000	0.01	7	7	8	8
The component   The componen	sembleBase	23. nnet_optim(BFGS)	x & y	200	-	15	34	15	15
The color of the	et	15. avNNet_nnet_optim(BFGS)	x & y	200	-	10	21	11	9
	ın	11. Gauss-Newton	x & y	200	-	12	9	13	12
S2. SCG	าท	43. nlm()	x & y	200	-	14	25	7	36
S2. SCG		51. Rprop	x & v	1000	_	23	52	25	28
S3. Std_Backpropagation					_				19
RSNNS  47. BackpropChunk  48. BackpropMomentum  x & y 1000 - 35 39 35  49. BackpropMeightDecay  x & y 1000 - 30 43 33  46. BackpropBatch  x & y 1000 0.1 48 27 50  50. Quickprop x & y 1000 0.1 48 27 50  50. Quickprop x & y 1000 0.1 20 35 16  automl  8. trainwgrad_adam  x & y 1000 0.01 20 35 16  automl  9. trainwgrad_RMSprop  x & y 1000 0.01 31 50 29  10. trainwpso x & y 1000 - 41 49 41  deepnet  20. BP  x & y 1000 0.8 18 38 24  40. SIR  38. rprop+  fmla & data 100000 - 23 40 23  37. rprop-  fmla & data 100000 - 21 42 21  40. SIR  40. SIR  40. SIR  fmla & data 100000 - 39 37 39  39. sag fmla & data 100000 - 39 37 39  39. sag fmla & data 100000 - 39 37 39  39. sag fmla & data 100000 0.001 51 10 49  40. SIR  28. adamax  x & y 1000 0.1 18 20 20  27. adam  x & y 1000 0.1 28 44 30  29. nadam  x & y 1000 0.1 28 44 30  29. nadam  x & y 1000 0.1 28 44 30  30. rmsprop  x & y 1000 0.1 35 19 34  31. sgd  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  x & y 1000 0.1 35 19 34  31. sgd  x & y 1000 0.1 35 19 35  31. sgd  31. sgd  x & y 1000 0.1 35 15 30  32. sgd  33. sgd  34. sgd  34. sgd  35. sgd  36. sgd  37. sgd  x & y 1000 0.1 35 15  38. sgd  39. sgd			. *		0.1				36
A8. BackpropMomentum	NINIC		. *	1000	-	34	41	32	34
46. BackpropBatch   x & y   10000   0.1   48   27   50	NNS			1000	-	35	39	35	30
Solution		49. BackpropWeightDecay	x & y	1000	-	30	43	33	31
8. trainwgrad_adam		46. BackpropBatch	x & y	10000	0.1	48	27	50	48
automl         9. trainwgrad_RMSprop         x & y         1000         0.01         31         50         29           10. trainwpso         x & y         1000         -         41         49         41           deepnet         20. BP         x & y         1000         0.8         18         38         24           neuralnet         38. rprop+         fmla & data         100000         -         23         40         23           37. rprop-         fmla & data         100000         -         21         42         21           40. slr         fmla & data         100000         -         39         37         39           39. sag         fmla & data         100000         -         49         59         47           36. backprop         fmla & data         100000         -         49         59         47           36. backprop         fmla & data         100000         0.01         18         20         20           27. adam         x & y         10000         0.1         18         20         20           27. adam         x & y         10000         0.1         33         53         42		50. Quickprop	x & y	10000	-	58	36	58	57
10. trainwpso	_	-	. *						20
A	automl								39
38. rprop+		10. trainwpso	x & y	1000	-	41	49	41	38
37. rprop-   fmla & data   100000   -   21   42   21	epnet	20. BP	x & y	1000	0.8	18	38	24	17
Neuralnet		* *			-				24
39. sag fmla & data 100000 - 49 59 47 36. backprop fmla & data 100000 0.001 51 10 49 49 49 59 47 36. backprop fmla & data 100000 0.001 51 10 49 49 49 49 49 49 49 49 49 49 49 49 49					-				18
28. adamax	ıralnet				-				46
28. adamax		-							52
27. adam		36. backprop	fmla & data	100000	0.001	51	10	49	45
29. nadam		28. adamax	x & y	10000	0.1	18	20	20	16
keras       26. adagrad       x & y       10000       0.1       43       53       42         25. adadelta       x & y       10000       0.1       35       19       34         31. sgd       x & y       10000       0.1       45       47       45         30. rmsprop       x & y       10000       0.1       55       57       55         AMORE       1. ADAPTgdwm       x & y       1000       0.01       22       29       16         4. BATCHgdwm       x & y       1000       0.01       25       8       26         4. BATCHgdwm       x & y       10000       0.1       33       14       37         3. BATCHgd       x & y       10000       0.1       38       24       42         minpack.lm       33. Levenberg-Marquardt       full fmla & data       200       -       16       5       19         ANN2       5. adam       x & y       1000       0.01       25       33       27         7. sgd       x & y       1000       0.01       27       27       28         7. sgd       x & y       1000       0.01       37       22       36			•					30	25
25. adadelta			•					40	41
31. sgd	ras		•					42	35
30. rmsprop			•						33
AMORE  2. ADAPTgdwm  2. ADAPTgd  3. ADAPTgd  4. BATCHgdwm  3. BATCHgd  3. BATCHgd  4. Comparison of the property of the proper		~	•						43
AMORE  1. ADAPTgd			x & y					- 33	54
AMORE  4. BATCHgdwm		- C	•					16	26
4. BATCHgdwm	<b>IORE</b>	O	•						21
Minpack.lm   33. Levenberg-Marquardt   full fmla & data   200   -   16   5   19	<u>-</u>	-	•						27 31
ANN2 6. rmsprop	1 1								
ANN2 5. adam x & y 1000 0.01 27 27 28 7. sgd x & y 1000 0.01 37 22 36  16. adam x & y 1000 0.4 42 1 38 19. rmsProp x & y 1000 0.8 46 4 48 18. momentum x & y 1000 0.8 52 3 53	праск.Іт								14
7. sgd x & y 1000 0.01 37 22 36  16. adam x & y 1000 0.4 42 1 38  19. rmsProp x & y 1000 0.8 46 4 48  18. momentum x & y 1000 0.8 52 3 53	JNI2		•					27	23 21
deepdive     16. adam     x & y     10000     0.4     42     1     38       19. rmsProp     x & y     1000     0.8     46     4     48       18. momentum     x & y     1000     0.8     52     3     53	AININ2		•					28 36	21 29
deepdive     19. rmsProp     x & y     1000     0.8     46     4     48       18. momentum     x & y     1000     0.8     52     3     53									44
18. momentum x & y 1000 0.8 52 3 53			•						50
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snnR 54. SemiSmoothNewton x & y 200 - 49 13 50	nR	54. SemiSmoothNewton	x & y	200	-	49	13	50	48
elmNNRcpp 21. ELM x & y 59 55 59	nNNRcpp	21. ELM	x & v	-	-	59	55	59	59
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ELMR 22. ELM fmla & data 60 53 60	IVIK	ZZ. ELIVI	rmia & data	-	-	60	53	60	60

Note: TOP5 are nlsr:NashLM, rminer:nnet\_optim(BFGS), nnet:optim (BFGS), validann:optim(BFGS), MachineShop:nnet\_optim(BFGS).