

DAY 03 INTERVIEW QUESTIONS - Types of Sampling Methods, Standard Error

Q1) What do you mean by sample and sampling error? or Variation due to sampling?

Ans - Sample → A sample is a selection of objects or observations taken from the population of interest.

Example of sample → A population might be all citizens of India at a given time. We wish to measure investment by all the citizens.

So now suppose we find sample mean of number of investments.

Batch 1 = 4 (East India), Batch 2 = 6 (West India), Batch 3 = 2 (North India)

Batch 4 = 5 (South India)

Difference in sample mean (batches) is called Sampling Error / Variation due to sampling.

→ So whenever we estimate of population based on samples, we should not say equal / give exact values rather we should say lies between.

For ex, number of investment lies between (,) with Confidence Interval

Q2) What is standard Error? Give an example

Ans - standard Error is a measure of uncertainty in sample mean. Higher the standard error, lesser we are confident.

Standard Error,

$$SE(\bar{x}) = \frac{s}{\sqrt{n}}$$

s → standard deviation

n → number of samples

In one term, Standard Error \Rightarrow Population mean \neq Sample mean.

Example, we want to know the average age of Fixed Deposit Investment.

Let's take 500 random sample, average mean = 56. Confidence → little bit.

Let's take 5000 random samples, avg mean (age) = 59. Confidence → more than last.

Finally, 50,000 random samples, avg mean (age) = 60. Confidence → Good.

So, higher the observation, confidence go up and standard error will decrease.

Therefore after all calculation we can sum up, we are 95% confident that average age of Fixed Deposit investment is in range of (59 to 60) / (59, 60).

Q3) What are Sampling techniques?

Ans - Sampling techniques are mainly grouped in 2 categories -

- i) Probability sampling
- ii) Non probability sampling

i) Probability sampling (Randomized Sampling)

- It uses randomization to make sure every element of population get equal chance to be part of sample. Also known as Random Sampling.

Types in Probability Sampling -

- i) Simple random sampling
- ii) Stratified sampling
- iii) Reservoir sampling.

1) Simple Random Sampling →

- Every element has an equal chance of getting selected to be part of sample.
- It is used when we don't have any kind of prior information about target population.
- For eg → Random select 20 students out of 50. $P(\text{student}) = 1/50$.

ii) Stratified sampling →

- Every element has an equal chance of getting selected, but this technique first divides the element of population into small group or strata based on similarity.
- We need to have prior information about population to create subgroups.
- For eg → Strata can be identified such as age, sex, location etc.

iii) Reservoir sampling →

- Reservoir sampling is a randomized algorithm that is used to select K out of n samples where n is very large or unknown. This algorithm select K elements with uniform probability.

2) Probability Non-Probability Sampling (Non-Randomization) →

- Does not rely on randomization. Outcomes may be bias.

Types - i) Convenience Sampling ii) Purposive Sampling iii) Quota Sampling

- i) Convenience Sampling → Samples are selected based on availability. It is costly.
- ii) Purposive Sampling → Only those elements will be chosen/selected from population which suits best for purpose of study.

- iii) Quota Sampling → Elements are selected until exact properties of certain types of data is obtained or sufficient data in different categories is collected. For eg - we need more sample of women than men in a survey.

3) How to check if the sample is adequate or not?

Ans - Kaiser-Meyer-Olkin (KMO) test measures sampling adequacy for each variable in the model. It is mostly used in Factor Analysis. The statistics is a measure of the proportion of variance among variable might be common variance.

- KMO return values from 0 and 1. We can interpret like

0.8 to 1 indicates the sampling is adequate. (very good for factor analysis)
0.5 to 0.8 Indicates sampling is not adequate, use some remedies.
0 to 0.5 indicates samples are unacceptable. There are widespread of correlations.

Q) What is appropriate sample size of my study? Criteria, Methods

Ans - Answers depend on number of factors including

- 1) Purpose of study
- 2) Population size
- 3) Risk of selecting bad sample
- 4) Allowable sampling error

Sample size criteria -

- 1) Level of precision
- 2) Level of confidence/risk
- 3) Degree of variability in the attributes being measured

1) **Level of precision** - Also known as **Sampling Error / Margin of error**.

- It is the **range** in which **true value of population** is **estimated to be**
- This range is often **expressed in percentage** (eg $\pm 5\%$)

Example, if a researcher finds 70% of student in sample has adopted a recommended practise of submitting the assignment with a precision rate of $\pm 5\%$, then he/she can conclude that between 65% to 75% of students in the population have adopted the practise.

2) **Confidence Interval** - Also known as **Risk level**.

- Based on **Central Limit Theorem**, which means when a population is repeatedly sampled, the average value of attribute obtained by those samples is equal to true population value.
- This is **expressed in percentage** (eg 95%)

Example, if a 95% confidence level is selected, 95 out of 100 samples will have true population value within range of precision specified earlier

3) **Degree of Variability** - Refers to the **distribution of attributes in population**.

- **More heterogeneous (large variance)** a population, **large sample size required**
- **Less variable (more homogeneous)** less variance, **small sample size required**

A proportion of 50% indicates we need large sample size because 50-50. In case 20% or 90% indicates we need small sample size because remaining 80% (in case of 20%) and 90%, large population is on one side (less variance).

Methods used - 1) Cochran formula 2) Yamane formula.

1) **Cochran formula**, $n_0 = \frac{Z^2 pq}{e^2}$, $n_0 \rightarrow$ Sample size
part 1 - Infinite population $Z \rightarrow$ Z value at given confidence interval
 $p \rightarrow$ proportion of attribute present in population
 $q \rightarrow 1-p$
 $e \rightarrow$ desired level of precision

Example - Assume there is **large population** and we **don't know variability** in population. Therefore we assume, $p = 0.5$ (maximum variability). Furthermore, we desire a confidence level of 95% and precision of $\pm 5\%$ precision. Resulting sample size is:

$$n_0 = \frac{(1.96)^2 (0.5)(0.5)}{(0.05)^2} = 385$$

sample size

1.96 \rightarrow Z value at 95% confidence interval

$$p = 0.5 \quad q = 1-p = 0.5$$

$$e = 5\% = 0.05$$

part 2 - Finite population

$$n = \frac{n_0}{1 + \frac{(n_0 - 1)}{N}}$$

$n_0 \rightarrow$ Initial sample size calculated as per larger population criterion.

$N \rightarrow$ population size.

example - Assume our last example, our evaluation of student adoption of the recommended practice will only affect 5,000 students.

$$n = \frac{385}{1 + \frac{(385 - 1)}{5000}} = 358 \text{ students.}$$

② Yamane Formula \rightarrow simplified formula to calculate sample size in case of finite population

$$n = \frac{N}{1 + N(e)^2}$$

$n =$ Sample size $e =$ level of precision.
 $N =$ Population size

example - Take above question of 5000 students, $n = \frac{5000}{1 + 5000(0.05)^2} = 371$ students.
 $e =$ precision $= 5\% = 0.05$