

9. mathematics

letters M, A, T, H, E, M, A, T, I, C, S

Vowels = A, E, A, I

Consonants : M, T, H, M, T, C, S

Total letters = 11

$$\frac{8!}{2! \cdot 2!} \times \frac{4!}{2!} = \frac{40320}{4} \times \frac{24}{2} = 10080 \times 12 = 120960$$

10. OPTICAL

Vowels = O, I, A

Vowel \Rightarrow 5 units

$$5! = 120$$

$$3! = 6$$

$$120 \times 6 = 720$$

$$11. \quad n(n-1)/2 = \frac{30 \times 20}{2} = 435$$

12. LOGARITHMS

No of 4-letters = $P(10, 4) =$

$$\frac{10!}{(10-4)!} = 10 \times 9 \times 8 \times 7 = 5040$$

14. 3 girls, 2 days

3 boys, 2 girls

2 boys from 2 girls.

$$\text{Boys: } C(2, 2) = 1$$

$$\text{Girls: } C(2, 2) = 1$$

Total

4. 6 men, chosen in $8C_6$ ways and 4 women a
be chosen in $10C_4$ ways

$$8C_6 \times 10C_4 = \frac{8!}{2! \times 6!} \times \frac{10!}{4! \times 6!} = 5880 \text{ ways}$$

5. Cost of brown = x

Cost of black = $3x$

no. of black = 5

no. of brown = b

$$5 \times 3x + b \times x = 15x + bx$$

$$3bx + 5x = 30x + 2bx$$

$$bx = 25x$$

$$b = 25$$

6. Let total people = n

let total handshakes = 24

total ways - handshakes

$$= \frac{n(n-1)}{2} = 24$$

7. 5 tasks, 5 persons

$T_1 \neq P_1$ or $P_2 \rightarrow$ can go to P_3, P_4, P_5

$T_2 =$ only P_3 or $P_4 \rightarrow 2$ options. $\rightarrow 3$ persons

3 tasks to remaining 3 people - $3! = 6$

$$(3 \times 2 - 1) \times 6 = (6 - 1) \times 6 = 5 \times 6 = 30$$

$$= 30$$

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permutation & combination

1. Committee of 5 men & 6 women from 8 men & 10 women

$${}^8C_5 \times {}^{10}C_6 = 56 \times 210 = 11760$$

2. 3 men, 2 women = ${}^7C_3 \times {}^6C_2$

4 men, 1 woman = ${}^7C_4 \times {}^6C_1$

5 men, 0 women = 7C_5

$$35 \times 15 = 525$$

$$35 \times 6 = 210$$

$$= 21$$

$$525 + 210 + 21 = 756$$

3. D, E, T, A, I, L

→ 6 Letter

Odd positions → 3 positions

E A I → 3 vowels

no. of ways to arrange vowels in odd position = $3! = 6$

no. of ways to arrange in remaining

3 position = $3! = 6$

$$6 \times 6 = 36$$