When solving the initial value problem y' = f(x, y) with the initial condition $y(x_0) = y_0$, we can use the following multi-point methods:

Adams-Bashforth (explicit method)

•
$$y_{i+1} = y_i + \frac{h}{2} \left[3f_i - f_{i-1} \right] + O(h^2)$$
 2-point

•
$$y_{i+1} = y_i + \frac{h}{12} \left[23f_i - 16f_{i-1} + 5f_{i-2} \right] + O(h^3)$$
 3-point

•
$$y_{i+1} = y_i + \frac{h}{24} \left[55f_i - 59f_{i-1} + 37f_{i-2} - 9f_{i-3} \right] + O(h^4)$$
 4-point

•
$$y_{i+1} = y_i + \frac{h}{720} \left[1901f_i - 2774f_{i-1} + 2616f_{i-2} - 1274f_{i-3} + 251f_{i-4} \right] + O(h^5)$$
 5-point

Adams-Moulton (implicit method)

•
$$y_{i+1} = y_i + \frac{h}{12} \left[5f_{i+1} + 8f_i - f_{i-1} \right] + O(h^3)$$
 2-point

•
$$y_{i+1} = y_i + \frac{h}{24} \left[9f_{i+1} + 19f_i - 5f_{i-1} + f_{i-2} \right] + O(h^4)$$
 3-point

•
$$y_{i+1} = y_i + \frac{h}{720} \left[251f_{i+1} + 646f_i - 264f_{i-1} + 106f_{i-2} - 19f_{i-3} \right] + O(h^5)$$
 4-point

where $f_i = f(x_i, y_i)$.