

DATA STRUCTURES

1) LINKED LISTS

→ Physical DS

- if in Stack, programmer needs to hard code size of array.
- if in Heap, size needs to be pre-decld. before working with array. **imp**

Static DS → Array [we can't extend the size of same array]

* Linked List	memory efficient (oper^n depend)	Array
- uses more space	- less space	
- only in Heap	- stack / heap	
- dynamic	- static	

[Efficiency of Array / LL depends on oper]

(i) Singly linked list

struct node

{

int data;

struct node * next;

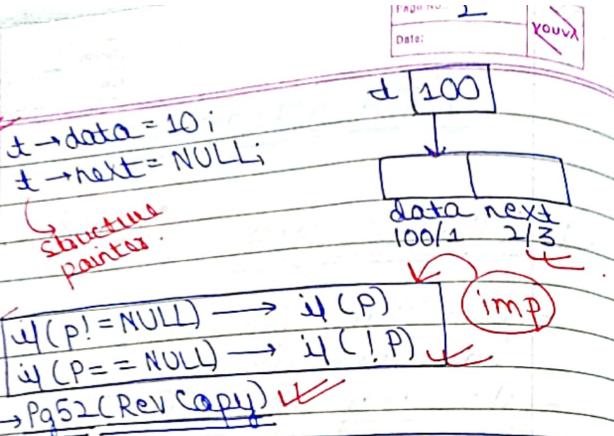
}

Singly referential Structure

struct node * t;

t = new node;

t = (struct node *) malloc (sizeof (struct node))



eg → Pg 112 (Display of SLL) ① → iterative
 recursive

eg → Pg 54 [max] ←
 int fun(struct node *p)
 {
 int x = 0;
 if (p)
 x = fun(p->next);
 if (p->data > x)
 p->data = x;
 return x;
}

② * Search: [Linear Search] → $O(n)$ time

eg → Pg 117 [run code & check] ✅
 [rep around items to first]

③ Reverse [use 3 pointers trailing] imp
 ⇒ reversing/modifying links is much faster & cheaper than data movement
 [Time: $O(n)$]

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jmp

eg → Pg 120 (Recursive Reverse) [Trace & See] ✅

(i) ↗ $O(1)$
 Insert before Head: 1 Pointer

(ii) Insert node at given Position:
 2 Pointers
 $O(n)$ Time

(iii) Appending node at last Position.
 while ($p \rightarrow \text{next} \neq \text{NULL}$)
 {
 p = p->next;
}

\times $p \rightarrow \text{next} = \text{newnode};$
 \times $p = p \rightarrow \text{next};$
 \times $p \rightarrow \text{next} = \text{NULL};$

reached last node.

* DELETION IN SLL:

(i) delete first node: 1 Pointer

(ii) delete any node:
 ↓
 6 → 4 → q → 8 → 7 → NULL
 ↑
 p
 node to be deleted.

$p \rightarrow \text{next} = q \rightarrow \text{next};$
 $\text{free}(q);$ jmp

2 Pointers

[or use memory leak]

↓
 $p \rightarrow \text{next} = p \rightarrow \text{next} \rightarrow \text{next}$

Scanned with CamScanner

(ii) Find DLL

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- If p is pointing to same node in LL & we want to delete that node.

imp Time $\rightarrow O(n)$ **[in SLL]**
→ We must go till Prev.

→ Binary Search not quite efficient in linked list [in Array, it is].

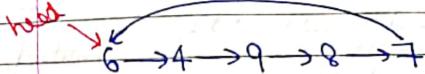
[eg] → Pg 59 (Detect loop in LL) **[imp]**

$p \rightarrow 1$ step
 $q \rightarrow 2$ steps

2 Pointers req.

$O(n)$

(iii) Circular linked list



① Display → $p = \text{head}$;

```

    do
        printf("%d", p->data);
        p = p->next;
    } while (p != head);
  
```

② Insertion

(i) before head : **1 pointer** [$O(n)$]

(ii) after given position : **2 pointers**
(Same as SLL)

[eg] → Pg 61 (Rev copy) **[imp]**

③ Deletion:

- delete any node → **2 pointers**
- delete head node → **1 pointer**
- delete last node → **1 pointer**

$O(n)$ Time **[imp]**

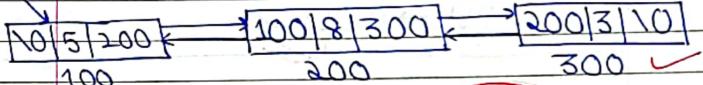
[eg] → Pg 62 (Rev copy) [Linked Circular Queue] **[imp]**

(iv) Doubly linked list

- cost increases, but flexibility increases

Head

[100]



[eg]

→ Pg 131 (using flags) **[imp]**

[imp] Flags can be used to detect loops in $O(n)$ Time. **[no need to take 2 pointers]**

① Insertion:

② Start : **1 pointer** $\rightarrow O(1)$ time.

(ii) after given position:
 Eg → Pg 64 (Rev Copy)
 (Links modified) → 4
 imp
 2 pointers
 $O(n)$ Time.

* If p points to any element in DLL, &
 we need to delete that element

→ $O(1)$ time
 node *t = p → pprev;
 $t \rightarrow next = p \rightarrow next;$
 $p \rightarrow next \rightarrow pprev = t;$
 delete(p) ✓
 imp
 [using 1 extra
 pointer]

For Concatenation:

SLL → $O(n)$

C-SLL → $O(n)$

DLL → $O(n)$

C-DLL → $O(1)$ → most used LL

* Circular doubly linked list is the most
 efficient linked list used

[used in Undo operation]

2) STACK → Logical DS

Stack is an ADT
 [Array, LL] = Physical DS
 [Stack, Queue, tree, Graphs] = Logical DS
 vimp

Logical DS are implemented using
 physical DS.

* Stack works on LIFO
 Definition of new data type
 = ADT → Space, top V.

{ Stack → push(x), pop(), peek (pos),
 stackTop(), isFull(). } ✓

* Implementation of Stack using Array

```

(i) Initial : top = -1
(ii) Empty : if(top == -1);
(iii) Full : if (top == size-1);
(iv) void push (int x)
{
    if (top == size-1)
        printf("Stack overflow");
    else
    { top++; stack[top] = x; } or, stack[+top] = x;
}
    
```

O(1)

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(v) int pop()

```

    {
        int x = 0;
        if (top == -1)
            pf("Stack Underflow");
        else
            x = s[top];
            top--;
    }
    return x;
}

```

will be mentioned in ADT.

(vi) Peek: returns the element, if push entered.

index = (top - position) + 1 (imp)

eg → Pg 67 (Peek eg) (Rev Copy) 4

Stack.push(stack S, int n)
Stack.pop (Stack S)

→ takes Stack & element as argument, pushes the element, & returns Stack.

* Stack implementation using 1 Array

Test

S	1	8	7	4	3	6	1	1	2	3
---	---	---	---	---	---	---	---	---	---	---

empty: if ($t_1 == -1$) && ($t_2 == -1$)

full: if ($t_1 == t_2 - 1$)

eg → Pg 142 (Imp Q) 4

3 Top
4 bound

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* Valid Permutation Problem

[eg] → Stack Q3 & Q5 [Pg 143]

no. of diff. 8 Ts
formed
in insertion

No. of Valid Permutations = $\frac{2^n}{n+1}$ (imp)

* Avg. lifetime of element in Stack

[eg] → Pg 145 (Gate Q)

Vimp

* INFIX TO POSTFIX

Infix: a * b
Prefix: * a b
Postfix: a b *

during operator stack

Infix: a + b * c

Postfix: (a + (b * c))

$\rightarrow a + [bc *]$

$\rightarrow abc * +$ X

Prefix: (a + (b * c))

$\rightarrow a + [* bc]$

$\rightarrow + a * bc$ X

* Compiler converts every infix exp to

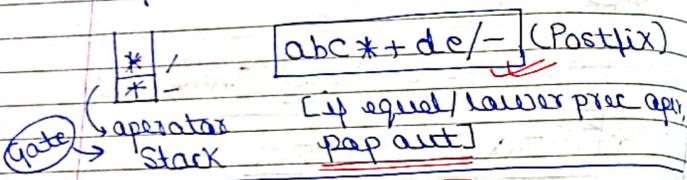
Postfix exp & then evaluate it.

(reduces no. of row for compiler
& therefore reduces time)

eg	Pg 148 [Q 4]	Open	Prece	Assoc.
		+,-	3	LR
		*,/	2	LR
		()	1	LR

① * Infix to Postfix using Stack

Infix: $a+b*c-d/e$. operator stack

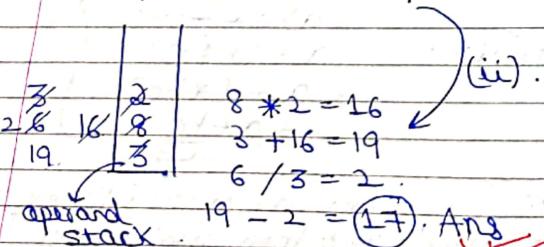


- Express n char conversion (infix to postfix) = $O(n)$

② * Evaluation of Postfix exp

Infix: $3+8*2-6/3$. operator stack

Postfix: $382*+63/-$.



∴ 2 Scans To achieve result (i) & (ii)
 $O(n) + O(n) = \underline{O(n)}$

- Order of execution depends on compiler, we can't predict it.

$$\begin{aligned} 1. ((a+b)+c)+d &\rightarrow ab+c+d+ \quad [LR] \\ 2. (a=b=c=d=5)) &\rightarrow abcde5==== [RL] \\ 3. a^b^c = abc \quad \text{imp} &\rightarrow (RL) \end{aligned}$$

* Unary Operators

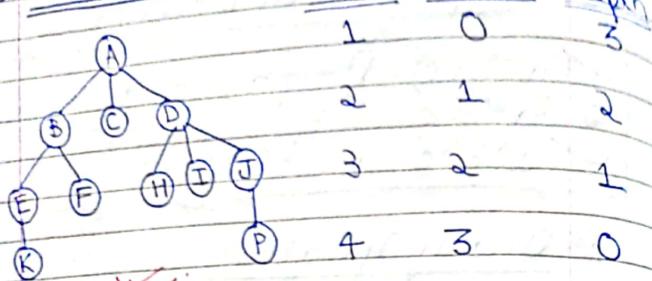
()	imp [Unary oper]
! log -	[CRL]
^	[CRL]
*, /	[LLR]
+, -	[LR]

precedence.

eg → Pg 72 (Rev Copy) imp

* But DS to check balanced Parenthesis exp is Stack

4.3 TREES



EBA: ancestors of K

HJP: descendants of D

$\deg(D)=3$ (imp) [Tree]

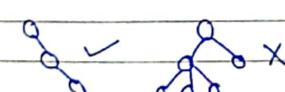
$\Rightarrow \deg=0$ (leaf) / terminal / external

$\deg>0$ (non-terminal / internal)
[Branch].

NOTE: If deg of tree = n, it can have max n children. (imp)

① BINARY TREES $\rightarrow \deg=2$

- atmost 2 children



(ii) Unlabelled Nodes

If n unlabelled nodes, no. of different binary trees formed / diff shapes are:

(imp)

$$T(n) = 2^n C_{n+1}$$

can also start from 1
(depend on A);

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(imp)

* If n unlabelled nodes, no. of trees drawn with max height:

$$T(n) = 2^{n-1}$$

$$T(n) = \sum_{k=1}^n T(k-1)T(n-k)$$

[eg] \rightarrow Pg 2 (Rev Copy) ($n=3$)

\star	n	0	1	2	3	4	5
	$T(n)$	1	1	2	5	14	42

Gate

$$T(5) = 1 \cdot 1 + 1 \cdot 5 + 2 \cdot 2 + 5 \cdot 1 + 14 \cdot 1$$

[Recursive Reln]

(iii) Labelled Nodes \rightarrow A B C

: [3 lab Nodw $\rightarrow 30$]

$$\text{Total BTs} = 2^n C_n * n!$$

$\underbrace{n+1}_{\text{Shapes}}$ $\underbrace{n!}_{\text{Permutn in 1 Shape}}$

* HEIGHT v/s NODES

Substitute
 $h=2 \rightarrow n=7$

① If height (h) is given ($h \geq 0$)

$$h=2, n=7.$$

$$\begin{aligned} \text{min nodes} &= h+1 \\ \text{max nodes} &= 2^{h+1}-1 \end{aligned}$$

② If 'n' nodes are given ($n \geq 0$)

$$\text{min } h = \log_2(n+1)-1$$

$$\text{max } h = n-1$$

$$n=3, h=1$$

$L=3, n=4$

max nodes in level $L = 2^{L-1}$
min nodes in level $L = 1$

e.g. Pg 4 (Rev Copy) (Derivation)

(*) Strict BT

(**) Complete Binary Tree

- every node have exactly 2 children.

$$e = i+1 ; n = i \cdot e \quad (\text{imp})$$

In CBT = no. of nodes must be odd

e.g. Pg 182 [20 nodes]

* In a not complete Binary Tree:

$$\deg(0) = \deg(2) + 1 \quad (\text{imp})$$

(*) n-Ary Tree

atmost n children.

* Complete n-Ary Tree

if $n=3 \rightarrow$ exactly 3 children.

$$e = (n-1)i + 1 \quad [\text{Complete } n\text{-Ary tree}]$$

e.g. Pg 185 [2n+1/3]

* Representation of BT

- ① → Array
- ② → Linked

i) node at index i
left = $2i$
right = $2i + 1$
parent = $\lfloor i/2 \rfloor$

e.g. Pg 187 [Q2]

(*) Linked Representation,

struct node

{ struct node *lchild;

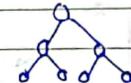
int data;

struct node *rchild;

(imp)

$$n \text{ nodes} = (n+1) \text{ Null Pointers}$$

(*) Full Binary tree



Given height h .

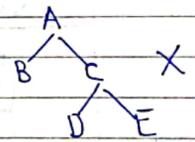
$$\max n = 2^{h+1} - 1$$

(*) Almost complete Binary tree

- In array: No Gaps

- In last level, elements

will be inserted from left to right; & full BT till previous level.



* TREE TRAVERSALS

- DFS
- Preorder: visit(node), pre(left), pre(right)
 - Inorder: in(left), visit(node), in(right)
 - Postorder: post(left), post(right), visit(node)

eg → Pg 8 [Rev Copy] ✗

Given a traversal, 1 shape can be filled in just 1 way. imp

In labelled nodes,

No. of Binary trees, given a preorder traversal, we can generate total of

imp $\left[\frac{2^n C_n}{n+1} \right]$ BTS.

If no traversal: $2^n C_n * n!$

* Generating Binary tree from Traversal [O(n^2)]

We need 2 traversals & one must be Inorder imp

pre: left → right
post: right → left

eg → Pg 194 ✗

Time taken for generating tree from traversal = $O(n^2)$ binary

Time = $O(n)$
Space = $O(n)$

Preorder
Postorder

eg → Pg 10 [Rev copy] ✗

n nodes

$n+1$ NULLP

$(2n+1)$ funct calls

0(n) = Time

void MyInorder(Start node * p)
{ if (p == NULL) return;

MyInorder(p → rchild);
printf("./c", p → data);
MyInorder(p → lchild);
printf("./c", p → data);

} } ↴ GGCFFCAFEFDDBA

eg → Pg 197 [Postorder count] order $(2n+1)$ fun
[Vimp] ✗ : $O(n)$

eg → Pg 198 [Counting] ✗ Vimp

eg → Pg 199 (Practice) ✗

Inorder / Preorder / Postorder traversal counting $\rightarrow O(n)$
 $\because (2n+1)$ funct calls.

BINARY SEARCH TREE

- Distinct Set of Elements, where value of item is greater than all elements in left ST & smaller than right ST.

Search time depends upon ht of tree

eg → Pg 12 (Rev Copy) (Keys 1 → 100)

* Inorder of BST → always sorted order of elements. (imp)

Generating BST from Traversal

→ 1 traversal sufficient to create BST [Pre/Post]

eg → Pg 203. [Can this be preorder of BST?]

(Gate)

* Also to create BST from pre/post: $O(n)$
Also to create BT from pre/post: $O(n^2)$

(imp)

NOTE: Preorder can't tell you, whether its BST or not [only inorder says!]

(imp)

imp

* If n labelled Nodes,
No. of BST possible = $2^n C_m / n+1$

∴ each structure labelled in 1 way (\because inorder given).

Operations on BST

① Insert:

- depends upon height of tree

- $O(h) = O(\log n)$

[best case]

② Create BST

eg → Pg 206. ✓

③ Deletion:

(imp) [Text]

- Replace with inorder predecessor Successor.

eg → Pg 14 (Rev Copy) ✓

Drawback of BST

∴ Height of BST depends upon order of insertion of elements.

$$\begin{aligned} h > 0 \rightarrow \min h &= \lceil \log(n+1) \rceil [\text{full}] \\ &\max h = n [\text{skewed}] \end{aligned}$$

⑦ HEIGHT BALANCED / AVL TREES

Balance \rightarrow ht of left - ht of right
 factor SubTree SubTree

if balanced \rightarrow $Bf = \{-1, 0, 1\}$ (imp)
 if not balanced $\rightarrow |Bf| > 1$ ✓.

eg Pg 211 [LL, LR, RR, RL rotation] ✓

AVL tree is made step by step using rotations, it's not that, you get a skewed tree & you make AVL tree.

eg Pg 216 (Example) ✓

* Height v/s Nodes in AVL Tree

\Rightarrow If height 'h' is given: ($h \geq 1$)

$$\min h = \text{Table}$$

$$\max n = 2^h - 1$$

\Rightarrow If n nodes are given:

$$\min h = \lceil \log_2(n+1) \rceil$$

$$\max h = \text{Table}$$

Height h	0	1	2	3	4	5	6	7	8	9	10
Nodes n	0	1	2	4	7	12	20	33	54	88	143

like
Fibonacci

\hookrightarrow 5 ht. AVL tree ke
lie min 12 nodes
12 nodes ke lie
max ht = 5.

cg Pg 218 (Q2/Q3)

v. imp

imp

for 12 nodes

ht = 5

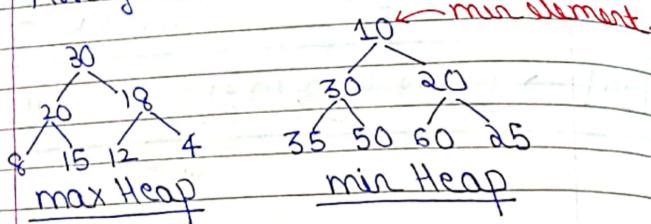
nodes = 12

Huffman Coding, dijkstra
Tab Sequencing, use
Heap.

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4) HEAP

- Every heap is almost complete BT, there must not be any Gaps in Array.



eg → Pg 220 [Which one is heap] ✓

Height of heap = $\lceil \log n \rceil$ ✓ [imp]

Height of BST = $\log n \leq h \leq n$

Height of AVL = $\log n \leq h \leq \text{Table}$

* Operations of Heap:

① Insert

- Insert the element & heapify.

$O(\log n)$

$O(\log n)$

$O(1)$

replace with left child

② Delete: delete the root, & heapify.

$O(1)$

largest stem → max Heap
smallest stem → min Heap

∴ $O(\log n)$ [Contributed by heapify].

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[imp]

eg → Pg 25 [Rev Copy] ✓

③ Create Heap = $O(n)$ ✓

$n + n * \log n$

④ Heap Sort →

• Create heap: $O(n)$

• delete element

one by one &

heapify: $O(n \log n)$

$T = O(n \log n)$

In Place Sorting ↗ [No auxiliary array]

eg → Pg 19 [2015] ✓

In a max heap, smallest element must be in lowest level, ∵ it must not have children.

eg → Pg 20 [Rev Copy] [7th ele] ✓

eg → Pg 21 [Both Qs] ✓

[imp]

Max Heapify = $O(\log n)$ ✓
Build max Heap = $O(n)$ ✓

Create Heap: $O(n)$ ✓

[imp]

Heapify: $O(\log n)$ ✓

Delete min stem from max Heap: $O(n)$

max Heap → min Heap: $O(n)$ ✓

delete: $O(\log n)$

Search: $O(n)$ // find

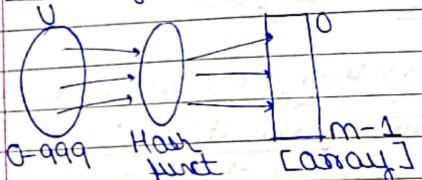
delete 7th stem: $O(\log n)$ ↗ [imp]

5) HASHING

Invert DS, Search time is costly
 $[LL \rightarrow O(n), BT \rightarrow O(n), BST \rightarrow O(n) \text{ [sk]}, AVL BST \rightarrow O(\log n)]$ $O(\log n)$.

But, Hashing $\rightarrow O(1)$ imp

* Hashing



eg: Keys $\rightarrow (121, 145, 132, 999)$
 $0 \quad 1 \quad 2 \quad 3 \quad 4 \quad 5 \quad 6 \quad 7 \quad 8 \quad 9$

121	132	145		999					
-----	-----	-----	--	-----	--	--	--	--	--

 $hf = \text{modulo}$

Insertion = $O(1)$ imp : $m=10$
Search = $O(1)$ imp

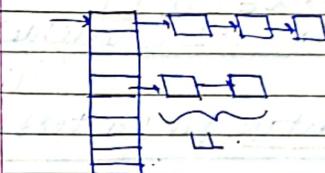
* Problem: Collision

When more than 1 element map to same space.

Solution to collision

- 1) Coming up with better hash functions
2) Chaining
3) Open Addressing
→ Linear Probing
→ Quadratic Probing
→ Double Hashing. ✓

* CHAINING



Insertion = $O(1)$
Search = $O(n)$
Deletion = $O(n)$

all item might map to single entry in a list.

Load (α) = n/m ✓ $n \rightarrow \text{elem. in HT}$.
Vector m $m \rightarrow \text{size of HT}$.

To uniform dist funct, Avg length of list = α .

Avg search = $\theta(1)$
Avg deletion = $\theta(1)$

(Vimp)

NOTE: For deletion, chaining is much better than OA; most open is $O(1)$.

disadv: stored outside table (not space efficient). ✓

eg: Pg 5 (Ravi) [LF = avg. L of list] ✓

imp

- [eg] → Pg 6 ($97/100$)³ [Probab.] ✓ (Opt.)
- [eg] → Pg 6 [Q1] (Vimp) ✓ (Imp)

3) OPEN ADDRESSING

- We can visit more elements than table size.

$\alpha = n/m$ OA $\rightarrow \alpha \in [0, 1]$
 Chain $\rightarrow \alpha > 1$ (possible) ✓ (Imp)

Adv: No Space Wastage for Pointers.

(*) Linear Probing

- Probing in a linear manner.

($1, 2, 3, \dots, m-1, 0$) probe sequence
 (2, 3, 4, ..., m-1, 0, 1) probe sequence
 No. of probe sequences possible = m

Note: If n elements map to same initial index & follow the same Probe Sequence.
 ⇒ Secondary Clustering

If a run of elements filled up, prob of next slot to be filled up is very high: Primary clustering

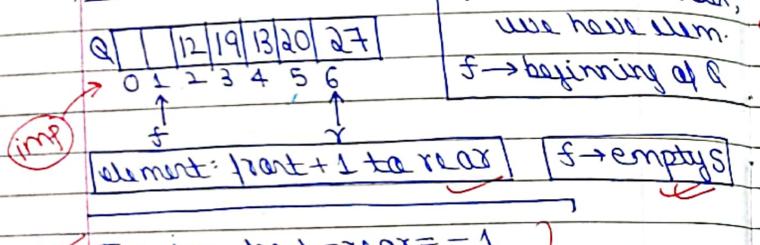
- (Imp) [due to Primary Clust.]
- Search time = $O(n)$ [Avg]
- [eg] → Pg 12 (Gate 2008) ✓
- [eg] → Pg 13 [Q1: Just Prob]
 Q2: ($i > 10$) ✓ Primary clustering
- [eg] → Pg 14 [Gate 2010] (Vimp) ✓ (Imp) [PnC]

QUEUE

- Works on FIFO.
- Elements are inserted from rear and deleted from front.
- Implemented as ADT.

① Queue using Array

② Linear Queue



- ✓ Initially: $\text{front} = \text{rear} = -1$
- ✓ Empty: $\text{if } (\text{front} == \text{rear})$
- ✓ Full: $\text{if } (\text{rear} == \text{size} - 1)$

Code → Pg 74 (Rev Copy) [Enqueue & Dequeue]

* Drawback of Linear Queue: $\text{front} + \text{rear} + \text{(by arr)}$

- empty Space can't be used, if rear is already pointing to last element.

→ Resetting Pointers

* Solutions → Circular Queue.

* Resetting Pointers: at any point, if Q becomes empty, reset front & rear to -1.

③ Circular Queue

- front & rear moves in circular fashion.

0 1 2 3 4 5 6

4 | 6 | 12 | 9 | 13 | 8 |

some
of time

r
f

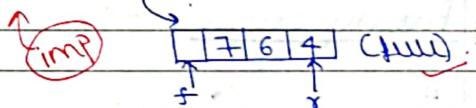
element: front + 1 to rear f → empty S

* If size of array is n, we can store n-1 elements.

✓ Initially: $\text{front} = \text{rear} = 0$.

✓ Empty: $\text{if } (\text{front} == \text{rear})$

✓ Full: $\text{if } (\text{rear} + 1 / \text{size} == \text{front})$



Code → Pg 76 (Rev Copy) [Enqueue & Dequeue]

Circular Queue: always used.
Linear Queue: Space wastage

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② Queue using linked list (IMP)

Initially: $\text{front} = \text{rear} = \text{NULL}$; [When first node created, $\text{front} = \text{rear} = +1$]

Empty: if ($\text{front} == \text{NULL}$) $O(1)$

Code → Pg 162 [Enqueue & Dequeue] ✓

(iii) Double Ended Queue

Queue:		DE-Queue			
1	insert	delete	2	insert	delete
front	X	✓	front	✓	✓
rear	✓	X	rear	✓	✓

If restricted: $\text{insertion} = \text{rear}$, $\text{deletion} = \text{front}$ (IMP)

(iv) Priority Queue

fixed no. of priorities [OS] → Insert: $O(n)$, delete: $O(1)$ (IMP)

unlimited no. of priorities → Insert: $O(1)$, delete: $O(n)$ (IMP)

→ **Heap is best DS to implement Priority Queue** → Insert: $O(\log n)$, delete: $O(\log n)$ (IMP)

→ In Priority Queue, Priority of every element must be distinct. (Gate)

[eg] → Pg 166 [Reversing Queue] ✓ (IMP)

[eg] → Pg 168 [Q1 & Q2] ✓ (IMP)

* Implementing Queue using 2 Stacks

[eg] → Pg 78 [Rev Copy] ✓ (IMP)

S1 → used for enqueue Concept.

S2 → used for dequeue.

→ Pg 169 [Enq & Deq] ✓ (IMP)

→ Pg 171 [Imp Q] ✓ (IMP)

Application

Test → Engine: $O(1)$, Deque: $O(n)$ (or vice-versa)

(Max Heap)

[But max element: $O(\log n)$]

Min element: $O(n)$]

So use Min-Max Heap

max: $O(\log n)$, min: $O(\log n)$

PREV YEAR PAPERS

TREES

* Inserion of an element if it is not already present in the Set

→ find element

→ if not found, insert

Heap : $O(n) + O(\log n) = O(n)$

Balanced BST : $O(\log n)$

[AVL]

imp

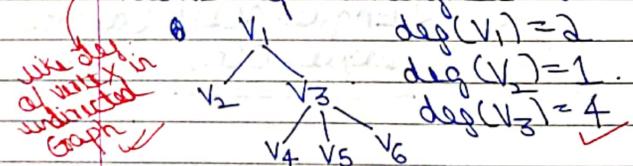
* Cost of Search / insertion / deletion in a complete binary tree : $\Theta(n)$

Cost of Search in AVL / Balanced

BST : $\Theta(\log n)$

Cost of Search in BST : $O(n)$

* If degree of node is defined as the number of its neighbours



* Q. 5.48 → Imp q on PnC & BST.

Q. 5.79 → [How many diff orders are possible?]

2 choices at each level.

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* In order to count the no. of nodes / number of subtrees having exactly 4 nodes : Preorder / Postorder traversal needed

→ $O(n)$

: $(2n+1)$ junction cells

* Travers Traversal of a Ternary tree :
left → root → middle → right

HASHING

already in Notes

* Q. 7.11 → PnC & Hashing

QUEUES

* In a Priority Queue / Heap, 2 elements can have same priority.

* Reverse Polish → Postfix form expression

* Linked list is not Suitable in Binary Searches [BS not quite efficient in LL]

←

Scanned with CamScanner

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- * Compact single dimensional array representation for lower triangular matrix \rightarrow Q2.1.
 $(j) + i(i-1)/2$ ✓
- * 2D array \rightarrow Address rotations.
 Q2.11 - Gate 2015 (Set A)
 (imp)
- * Queue implemented as 1 Stack.
 Enqueue: ~~insert~~, push, ~~insert~~
 dequeue: pop ✓ (imp)

GRAPHS

$G = (V, E)$ represented as:

- adjacency matrix: $O(V^2) / O(n^2)$
- adjacency list: $O(|V| + |E|) = O(n)$.
 (imp)

* Graph Traversal Method → BFS → DFS.

(*) Breadth first Search: If you visit a node, visit it completely (all its neighbours) before exploring some other node.
 → Queue DS is used
 eg] → Pg 55 [Vari] ✓ (imp)

In BFS Spanning tree: dep maintained
 overall steps: n to $n+1$ level
 (or same level). ✓

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eg] → Pg 55 [All 5 Qs] (Valid BFS Order) ✓

(*) Depth first Search: start visit. Once a new vertex w is visited, suspend it into Stack, & start exploring w (neighbours).
 (imp)

* Back edge: any level-level
 eg] → Pg 56 [DFS spanning tree] ✓

eg] → Pg 292 [2 qn] ✓ (Ht of a tree must be \leq no. of nodes, if tree → articulation point)
 (Present). Gate 2 (imp)

eg] → Pg 293 [Discovery & Finish] ✓

eg] → Pg 20 [Self Notes] ✓
 (Most imp → BFS, DFS tree).

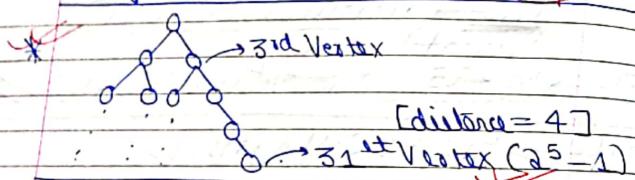
PREVIOUS YEARS.

* The most efficient algo for finding all connected components \rightarrow BFS/DFS $O(m+n)$ ✓ → (H with adjacency)

* In a sorted doubly linked list:
 delete $\rightarrow O(1)$
 Insert $\rightarrow O(n)$
 Find $\rightarrow O(n)$
 delete key $\rightarrow O(n)$ [Vimp]

	insert	find	insert	delete	data	db	know
Unsorted Array	$O(n)$	$O(1)$	$O(1)$	$O(1)$			
Min Heap	$O(n)$	$O(n)$	$O(\log n)$	$O(\log n)$			
Sorted Array	$O(n \log n)$	$O(n)$	$O(n)$	$O(n)$			
Sorted Doubt Linked List	$O(n)$	$O(n)$	$O(n)$	$O(1)$			

* Depth First Search requires $O(V+E)$ time, if implemented with adjacency list & $O(V^2)$ time, if with an adjacency matrix. \checkmark (imp)



* Tree edges: edges that appear in the final DFS tree.

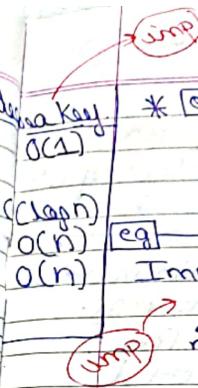
$$G = \begin{array}{c} \square \\ \Delta \\ \triangle \end{array} \quad n=10 \quad K=4+2+1=7$$

connected - $n-K$ components

(tree edges)

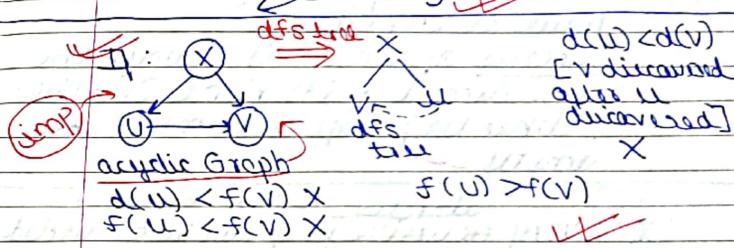
* So, any Graph with minimum cycle length 3, will have at least 3 spanning trees. \checkmark (imp)

$$K_3 \rightarrow n-2 = 3^1 - 3$$



* eq \rightarrow 6.5 [Group \rightarrow GO Sol] - computes whether subGraph is connected / net.

eq \rightarrow 6.10 \checkmark . Imp Q for discovery / finish time. {arrange discovery & finish times.}



* If a node is a leaf in the DFS tree, and deg v in Graph, (at least 2). Then definitely, it has to be in a cycle. \checkmark (Gate)

* In undirected connected Graph, only back edges possible in DFS tree (cross edge not poss.)

* In a BFS tree, if UV edge, $U \rightarrow$ depth i , $V \rightarrow$ depth j . $|i-j| \leq 1$. \checkmark (cross edge)

(it can't be > 1)

TEST - 2019 (Subject Wise)

* In a BST, the insertion/deletion operation is not commutative.

* Predecessor of a node (in its inorder traversal), is always the max. element of its left SubTree.
either a leaf / its right child must be empty.

Success: a) a node is always the min. element of its right subtree.
either left / right child must be empty.

* Every recursive program can be converted to iterative program [and vice-versa]

If tail recursion \longleftrightarrow loop.
[similar stack Space] ✓

```

char (*(*x())[])(); // Vimle
char x1(); // function returning char
char (*x2[])(); // array of pointers
                // to function returning
                // char
{
    char (*(*x1())[])()); // function returning
                           // pointer to above
}

```

imp

- * strlen(): counts length of string
(excludes NULL)
- * sizeof(str): counts length of string
(includes NULL) ✅

* Consider a 2D Array, $A[40 \times 95]$,
 $40 \times 95] \rightarrow$ Lower triangular matrix.
 $BA = 1000$, add of $A[66 \times 50]$

$$\#) \text{ To reach row } 66 = (66 - 40) = 26 \\ \text{rows covered}$$

$$\rightarrow \text{To many to cat. 50}$$

⇒ To move to col. 50

$$\rightarrow (50 - 40) = 10 \text{ elements carried.}$$

$$1000 + 351 + 10 = \underline{\underline{1361}} \quad \times$$

* ~~int S[6] = {128, 256, 512, 1024, 2048, 4096};~~

$\text{int} * y = (\text{int} *) (\& s + 1)$;

`n=2024` → [& array object]

* If we are provided with a pointer to the node which is to be deleted in SLL, it will work in all cases like (if its last node) only

- * Given Linked List is palindrome/not
- first identify mid element
 - reverse second half.
 - compare first half with second half
 $O(n) + O(n) + O(n)$

$$\boxed{T = O(n)}$$

$$S = O(1)$$

[No extra Array]

eg

→ Q31 [Addition corresponding to
 $A[100] \text{ [55]}$ if ; elements in
 Z representation].

$$(100-1) \quad (55-1) \quad 99 + 99 + 545 + 1000 = 1252$$

✓

- * In BST, time taken to find a non-existent element 'x' in the bst
 case ii: $O(1)$

15

- * In minHeap, time taken to find a
non-existent element in the bst case
 ii: $O(1)$

: [smallest element at root; if
 $K < \text{root} \rightarrow O(1) : (\text{not found})]$