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Saturday~~

classmate

Date

Page

1

LECTURE 1

- storing data of any application is must.
- we had file organi. for data storage.
 - Problem:
- we were missing data abstraction.
[hiding all internal details]

→ Any piece of data is stored in files only, but DBMS gives flexibility to store in (words) tables.

(
→ during which data gets stored,
but user can still fetch it : data abstr
provided in PB .

→ DBMS: facilitate the user to store, manage & access data from DB.

→ developed in 3 diff ways : [implemented]

- hierarchical DBMS
- network DBMS
- relational DBMS

→ most widely used.

eg: Oracle, MySQL,
SSMS

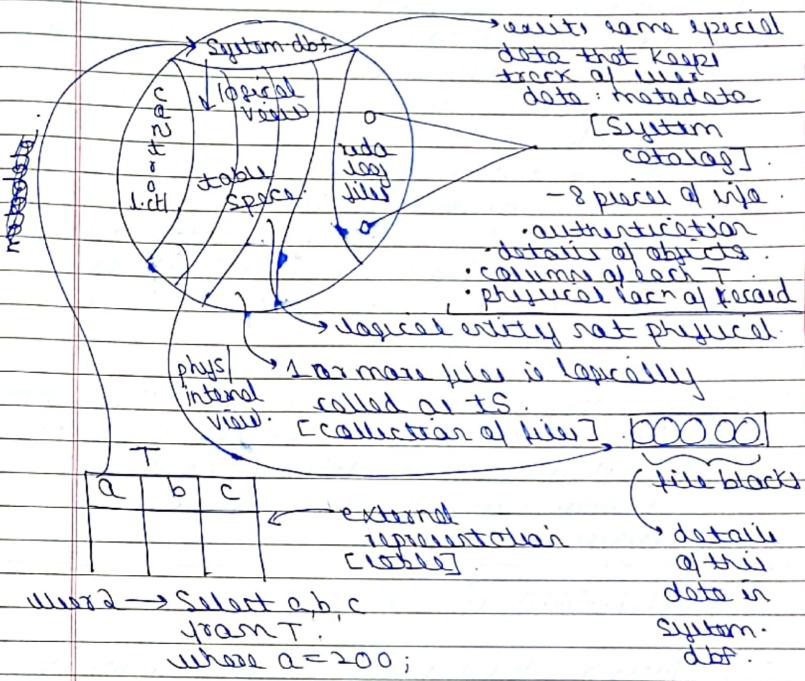
* DBMS	RDBMS
- had been a concept/ hypothesis.	implemented as RDBMS. It's a S/W.

- Date _____
Page _____ 2
- In file System, we know the exact folder & drive, we need full physical path to access data. [data abt X]
 - In RDBMS, data abt get implemented in 3 views:
 - external view.
 - logical/conceptual.
 - physical/internal view.

- * data: collection of related information.
- * collection of related data in an organised manner is called database.
- * DBMS is a concept that facilitates the users while they store the data in the database, access the data from the database and manage the data of the database.
- * DBMS provides the data abstraction feature.
- * RDBMS is one of the implemented version of DBMS which extends the data abstraction to 3 levels:
 - External / representational view.
 - logical / conceptual view.
 - Physical / internal view.

Date _____
Page _____ 3

eg: Oracle Architecture [Oracle DB]



- * As per COdd rules of rdbms, each and every rdb consists of some Special data that keeps track of all the details about the user data. Such Special data is called metadata.
- * In every RDB, metadata will get stored in a separate location from the user data.

- * Contents of Metadata:
- 1. The user credential information
- 2. All the list of objects that are accessed by each and every user.
- 3. The list of columns in each and every object.
- 4. Logical location of the data.
- 5. Physical location of the data.
- 6. List of all the enforced integrity constraints.
- 7. The details of all the useful indexes.
- 8. The permission details of different users on different objects.

NOTE: We query (external view) hits the System dbs, gets converted to logical view & then to physical view, fetches the data & finally provides user with the representational view.

* INTEGRITY CONSTRAINTS

These are the set of rules for maintaining the correctness of data in database.

[Integrity]

There exists 2 types of integrity constraints:

- (i) data integrity constraints.
- (ii) referential integrity constraints.

(i) data integrity constraints

These constraints will validate the correctness of data with its value.

e.g.: unique constraint.

• Not NULL constraint —

• check constraint —

• primary key constraint —

→ [NULL → neither 0 nor blank].

↳ according to Codd's rule of RDBMS:
NULL V. ⇒ not assigned / not deleted / not known value.

e.g.: unique constraint defined on col A

A	B	Salary
✓ 100	xyz	
X 100	xyz	
✓ NULL		5 L X

Want
to
be
able
to
check
NULL/
not

can't
check
whether
unique/
not.

[Comb of Unique & Not Null c → Primary Key]

NOTE: 1. Unique constraint will be able to validate whether the value is unique or not, but it can't validate whether the value is null or not NULL.

2. Not Null constraint can validate whether the value is null/not null; but it cannot validate whether it is unique or not.

* Functional dependencies → to understand keeps.

- FD in RDB consists of determinant & dependent.
- The set of attribute/attributes that exist on the LHS of FD is called determinant.
- The set of attribute/attributes that exist on the RHS of FD is called dependent.
- As per the concept of FD, the value of the dependent gets determined by the determinant i.e. (determinant derives the value of dependent)



Eg:

roll no → name
drives ✕

- ① If deter gets duplicated, value of dep also gets duplicated.

roll no	→ name
100	wyz
200	pqr
300	wyz
400	wyz

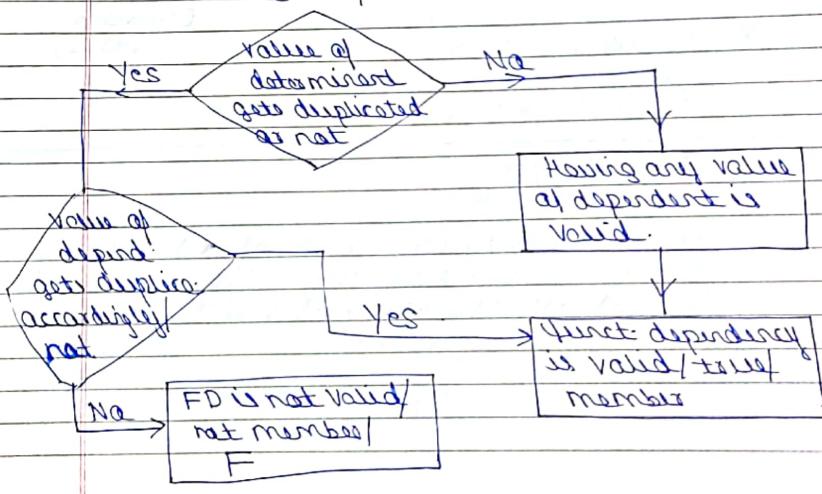
duplicated.

- ② In case det is unique, depend. can have any value.
→ Membership Test ↴

Eg: Instance of relation is as follows:

A	B	C
1	2	3
2	2	3
3	3	2
4	2	3
5	3	2
6	2	3

③ $A \rightarrow B$ T / F
Valid / not
member / not member.



* All possible FDs.

$\{A \rightarrow A, A \rightarrow B, A \rightarrow C, B \rightarrow A, B \rightarrow B, B \rightarrow C, C \rightarrow A, C \rightarrow B, C \rightarrow C\}$

$\{AB \rightarrow A, AB \rightarrow B, AB \rightarrow C, BC \rightarrow A, BC \rightarrow B, BC \rightarrow C, AC \rightarrow A, AC \rightarrow B, AC \rightarrow C\}$

$\{ABC \rightarrow A, ABC \rightarrow B, ABC \rightarrow C\}$

$\because A$ is unique, $AB =$ unique; $AC =$ unique

(2) * decomposition axioms

If $A \rightarrow BC$ &

$\Rightarrow A \rightarrow B$ and $A \rightarrow C$.

$BC \rightarrow BC$ is valid
 $BC \rightarrow B$ and
 $BC \rightarrow C$
 [must be valid].

(3) * Transitive axiom.

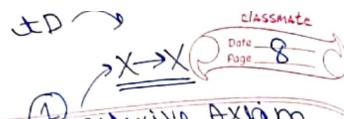
If $A \rightarrow B$ & $B \rightarrow C$ is valid

$\Rightarrow A \rightarrow C$, is also valid.

* SUPER KEYS

An attribute / combination of attributes of the relation is called Super Key if and only if all the attributes of the relation are derived by them.

$\{A, AB, AC, ABC\}$ (derives all attr)



classmate
Date _____
Page _____

relation = Table
attribute = column

- 1: SK can either be simple / composite.
 \downarrow
 $A: \{AB, AC, ABC\}$
- 2: A relation can have more than 1 Super Key.

* CANDIDATE KEY

An attribute / comb of attributes is defined as candidate key if and only if:

- (1) They derive all the attributes of the relation.
- (2) They are the minimal subset of Super Key.

level of subset (not based on no. of attributes).

$ABC \rightarrow \{\emptyset, \{A\}, \{B\}, \{C\}, \{AB\}, \{BC\}, \{AC\}, ABC\}$

proper
Subsets.

CKX	CKX	CK
ABC	AC	A
\emptyset	\emptyset	\emptyset
A	A	A
B	B	
C	C	
AB	AB	
AC		
BC		
ABC	AB	

in PS, A is not
candidate.

in PS of AB , A can
derive all attrib

C: there is further
min level of
subset].

- (1) Candidate Key could either be Simple / composite.
 (2) A relation can have more than 1 candidate key.
 (3) Minimal Subkey is always validated on the level of Subkey & not on the no. of attributes.

* NORMALIZATION

→ to reduce degree of redundancy.

- S1: find out the highest NF. NF ↑ dependency ↓
 S2: decompose table into higher NF.

* Redundancy

Name	FCP	3NF
X	Sachin	
Y		
Z	Sachin	
⋮		
Sachin		

repetition of data.

- 2) Rollno name email contact course dues fees
 100 X - - circle 60⁹⁰ 10K
 200 Y - - circle 60⁹⁰ 10K
 300 Z - - circle 60⁹⁰ 10K
- course → duration
 → fees.
- redundancy can cause many problems:
- wastage of memory
 - update anomaly
 - insertion anomaly
 - deletion anomaly
 - data redundancy would potentially cause the following problems:

* NORMALIZATION

- It is the systematic process applied on the relations to reduce the degree of redundancy.
- Normalization process always guarantees the following properties:
 - lossless decomposition
 - dependency preservation

* NORMAL FORM

- It is the property of relation which indicates the amount of redundancy present in it.

- Normal form & degree of redundancy are inversely proportional
- When normalization process gets applied on the relation, it performs the following steps of action:
 - (1) Find out the highest Normal Form of the given relation.
 - (2) Decompose the relation from its existing Normal form to higher Normal form.

** Procedure for finding highest NF of any Given relation:

Step 1: Find out all the possible candidate keys of the given relation.

Step 2: Identify all the existing prime/ key attributes and Non-prime/ non-key attributes of the relation.

Step 3: Find out all the existing full dependencies, partial dependencies, transitive dependencies and the overlapping candidate key dependencies.

Step 4: Refer to the definitions and the hierarchy of Normal forms for finding the highest Normal form for given relation.

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CLASSEMAIL
Date _____
Page 12

CLASSEMAIL
Date _____
Page 13

Q. R(A, B, C, D)

$$\begin{matrix} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow D \\ D \rightarrow A \end{matrix}$$

Procedure to find out CK

CK:

$$-(A)^+ = \{A, B, C, D\}$$

where A, B, C alone as AB, AC, BC derive any new attribute add it

$$-(B)^+ = \{B, C, D, A\}$$

$$-(C)^+ = \{C, D, A, B\}$$

$$-(D)^+ = \{D, A, B, C\}$$

Q. R(Sno, Pno, city, status, City)

$$\begin{matrix} Sno \rightarrow City \\ Sno \rightarrow Status \\ City \rightarrow Status \\ Sno, Pno \rightarrow City \end{matrix}$$

}

- $(Sno)^+ = \{Sno, city, status\}$ ✓
- $(City)^+ = \{city, status\}$ decomposition

SK. $(Sno, pno)^+ = \{Sno, pno, city, status, City\}$

CK

S_{No}, P_{No} can't derive all attributes.

* Prime/Key Attributes

The attributes of the relation that exist in at least one of the possible candidate keys of the relation are called Prime/Key attributes.

* Non-Prime/non-Key attributes

The attributes of the relation which doesn't exist in any of the possible candidate keys are called non-prime/non-key attributes.

NOTE: In order to identify whether an attribute of the relation is Prime/non-prime, we must find out all the possible CKs of that relation as the pre-requisite.

R(C, S, Z).

{CS} $\xrightarrow{1^-}$ check dependencies.

[if not CS/ part of CS = only 1 CK]

Z $\xrightarrow{2^-}$

C $\xrightarrow{3^-}$ part of CS \therefore more than 1 CK

possible

replaced by can determine.

(CS)⁺ $\rightarrow \{C, S, Z\}$

C $\xrightarrow{1^-}$ CK
S $\xrightarrow{2^-}$

(ZS)⁺ $\rightarrow \{Z, S, C\}$

2 CKs

: {CS, ZS}

Date: 14
Page:

S_{No} \rightarrow City
S_{No} \rightarrow State
City \rightarrow State
S_{No} \rightarrow City

Date: 15
Page:

: {S_{No}, P_{No}} are P/K attributes

P P NP/NK NP/NK NP/NK
R(S_{No}, P_{No}, City, State, City)

P P P
R(C, S, Z) \therefore 0 non-Prime.

Q R(S_{No}, P_{No}, City, State, City)

Unique & Not Null

S _{No}	P _{No}	City	State	City
S1	P1	Bang.	100	1000
S1	P2	Bang.	100	1000
S1	P3	Bang.	100	50,000

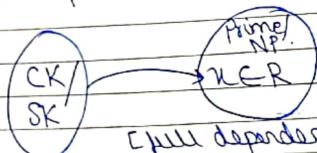
Deletion anomaly \rightarrow S₂ \square pure 100 \square \rightarrow cont insert part of raw.

Deletion \rightarrow S₂ \square pure 100 10000 \rightarrow cont delete part of raw, \therefore CK becomes NULL.

Step 3: FULL DEPENDENCY

If an attribute x belongs to relation R , gets derived by either a CK or a SK, then such dependency is defined as full dependency.

$x \in R$

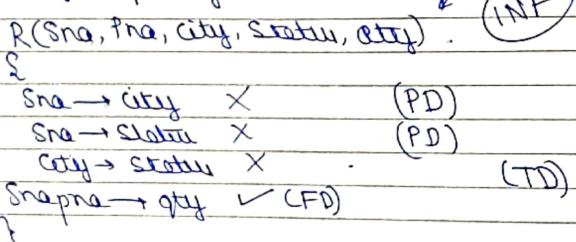


[full dependency]

If the determinant is CK / SK, I don't care abt dependent, that dependency is FD.

* diagram representing FD:

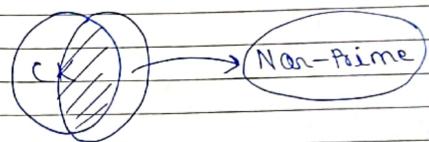
NOTE: While identifying the full dependency, we must validate the determinant of the functional dependency is either candidate key / Super Key.



2) Full dependency will never cause redundancy and hence, normalization process need not eliminate them.

* PARTIAL DEPENDENCY

If in case, a non-Prime/ non-Key attribute of the relation gets derived by only one part of the candidate key, then such dependency is defined as partial dependency.



2 things to be ensured:

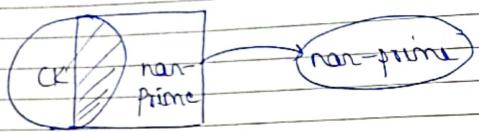
- 1) While identifying partial dependency, we must validate the determinant is part of the candidate key & dependent is non-prime attribute.
- 2) Partial dependencies could cause redundancy in the relation hence Normalization process would try to eliminate them.
- 3) If there exists a relation whose property is having simple candidate keys only, then such relations would never consist of partial dependencies.

* TRANSITIVE DEPENDENCY

- If a non-prime attribute of the relation gets derived by either another non-prime attribute / combination of part of the CK

Date _____
Page _____

along with a non-prime attribute, then such dependency is defined as transitive dependency.



1. While identifying the transitive dependency, we must verify that dependent is a non-prime attribute & the determinant is either a non-prime attribute / the comb. of part of the CK along with a non-prime attribute.

2. Transitive dependency could cause redundancy in the relation & hence normalisation process tries to eliminate them.

3. If there exists a relation which has only prime attributes, then total partial & transitive dependencies in such relations are always 0.

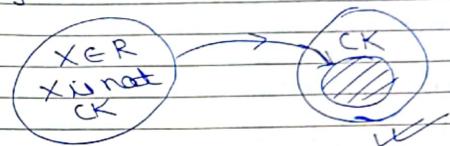
* OVERLAPPING CANDIDATE KEY DEPENDENCY

CLASSTIME
Date 19
Page _____

$R(C, S, Z)$

$$\left\{ \begin{array}{l} CS \rightarrow Z \\ Z \rightarrow C \end{array} \right.$$

}

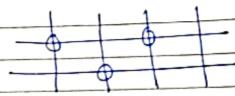


(1) If in case, atleast one of the possible candidate key of the relation is composite and if the part of the candidate key gets derived by another attribute combination $X \in R$ and X is not the candidate key (X is allowed to be part of the candidate key), such dependency would cause the CK to be overlapped. Hence, it is defined as OCD.

Step 4

1] 1NF

- A relation is said to be in 1NF if and only if all the values in the relation are atomic.
- According to Codd's rule of RDBMS, each & every relation must be in 1NF minimum in the relational DB.
- no multivalued attribute allowed here.



2] 2NF

- A relation is said to be in 2NF if and only if:
 - It exists in 1NF.
 - there are no Partial dependencies.

Note: 2NF eliminates all the Partial dependencies & the redundancy caused by the Partial dependencies.

3] 3NF

- A relation is said to be in 3NF if & only if:
 - It exists in 2NF.
 - It doesn't have any transitive dependencies.

Date _____
Page _____

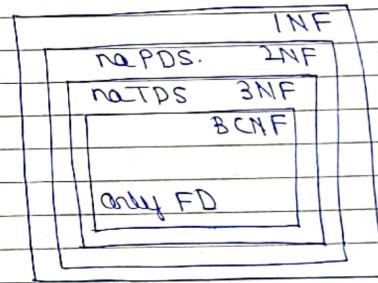
CLASSMATE
Date _____
Page 21

NOTE: 3NF eliminates both Partial & transitive dependencies hence, the redundancy caused by them.

4] BCNF

- Boyce-Codd Normal Form.
- A relation is said to be in BCNF if & only if:
 - it exists in 3NF.
 - it does not have OCD.

Note: BCNF will allow only the full dependencies.



Hierarchy of Normal forms.

- No SQL DB → Big Data → Volume
- Structured data managed by RDBMS → Variety
- Structured / Semistructured [photos / videos] → Velocity.

- People switching N_o SQL DB
 w concept of Normalization

GATE 2005

P P NP NP NP
 R(F₁, F₂, F₃, F₄, F₅)

{
 $F_1 \rightarrow F_3$ PD
 $F_2 \rightarrow F_4$ PD
 $F_1, F_2 \rightarrow F_5$ FD.
 }

$(F_1)^+ = \{F_1, F_3\}$ PD

$(F_2)^+ = \{F_2, F_4\}$ PD

$(F_1, F_2)^+ = \{F_1, F_2, F_3, F_4, F_5\}$ FD

CK

INF

GATE 2005 R(S_{no}, Sname, P_{no}, qty)

{
 $S_{no} \rightarrow Sname$ PD OCD
 $Sname \rightarrow S_{no}$ PD OCD
 $S_{no} P_{no} \rightarrow qty$ FD FD

1) Total no. of existing Partial & transitive dependencies are:

Date _____
 Page 22

Date _____
 Page 23

- (a) (1, 1)
- (b) (1, 0)
- (c) (0, 1)
- (d) (0, 0)

. (2) Highest NF of the relation is : INF 3NF

$(S_{no})^+ = \{S_{no}, Sname\}$
 $(Sname)^+ = \{Sname, S_{no}\}$
 $(S_{no} P_{no})^+ = \{S_{no}, P_{no}, Sname, qty\}$

CK.
 $\boxed{(S_{no}, P_{no}), (Sname, P_{no})}$ HF

(0, 0) ✓

GATE 2005 R(A, B, C, D, E, F, G, H)

$AB \rightarrow CDEF$ FD
 $F \rightarrow G$
 $G \rightarrow H$ } TD
 $B \rightarrow A$ FD
 $C \rightarrow D$
 $D \rightarrow E$
 $E \rightarrow F$ } TD

NO PD.

} Non-prime.

Q) Choose the correct statement w.r.t to candidate key:

- (a) AB is the only possible CK.
- (b) Along with AB there are more CK.
- (c) Along with AB there are 2 more CK.
- (d) None.

(2) Highest NF of the relation is: 2NF

- (a) 1NF
- (b) 2NF
- (c) 3NF
- (d) BCNF

~~Find 1NF~~

① $(AB)^+ = \{A, B, C, D, E, F, G, H\}$ ✓

$(F)^+ = \{F, G, H\}$

$(G)^+ = \{G, H\}$

② $(B)^+ = \{B, A, C, D, E, F, G, H\}$ ✓

$(C)^+ = \{C, D, E, F, G, H\}$

$(D)^+ = \{D, E, F, G, H\}$

$(E)^+ = \{E, F, G, H\}$

~~classless~~

Q) R(A, B, C, D, E, F)

$$\begin{array}{l} A \rightarrow B \quad PP \\ B \rightarrow C \\ C \rightarrow D \\ D \rightarrow E \\ F \rightarrow E \quad PD \end{array}$$

}

(1) Choose the correct one w.r.t to candidate key:

- (a) There is no CK
- (b) insufficient data for finding CK
- (c) A is the CK
- (d) None

(2) Highest NF of the relation is: 2NF.

$(A)^+ = \{A, B, C, D, E\}$

$(B)^+ = \{B, C, D, E\}$

$(C)^+ = \{C, D, E\}$

$(D)^+ = \{D, E\}$

$(E)^+ = \{F, E\}$

choose the best
closure & combine
the missing
attribute.

(AF).

[AF]

→ Only 2 entities in DB → Strong & Weak.
→ Each & every design must have Primary Key.

* PK
- Out of n,
only 1 will
be declared
as 1 PK

~~-4 ncks~~ CK

→ every relation must have at least 1 CK

I GATE 2004

R (Name, calling, cause name, grade)
S

04 Name → zollne

~~QCD~~ rolling → name

name, common name → gree

12) saline, ammonium → grade + 1.

—

$(\text{Name})^+ = \{\text{Name}, \text{all na}\}$

$$(\text{relname})^+ = \{\text{rname}, \text{name}\}$$

$\text{C} \models (\text{name}, \text{name})^+ = \{\text{name}, \text{name}, \text{grads}, \text{tallness}\}$

~~U: (rollno, name)+ = { name, name, grade, name }~~

B^{NP} → $\text{Na PD}, \text{Na TD}$

~~$R(N, R, C, T, Z)$~~

2

$N \rightarrow RCT$ FD
 $RCT \rightarrow Z$ TD
 $Z \rightarrow CT$ TD.

~~(N) + → { R, C, T, Z, N }~~

$(RCT)^+ \rightarrow \{ R, C, T, \succ \}$

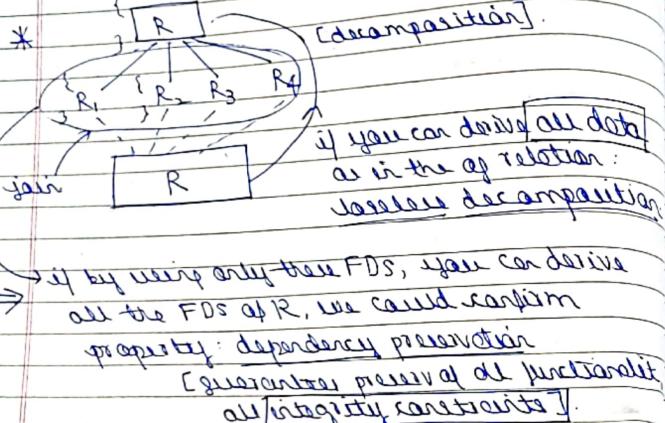
$$(z^+) \rightarrow \{z, c, T\}$$

$\angle C$

6/10/19
Sunday

Date
Page 28

Lecture 2



* lossless decomposition

There exists relation R, that got decomposed into set of relations: R₁, R₂, R₃... By applying join on those relations if we could derive all the data as in the original relation, the property is defined as lossless decomposition.

* Dependency Preservation

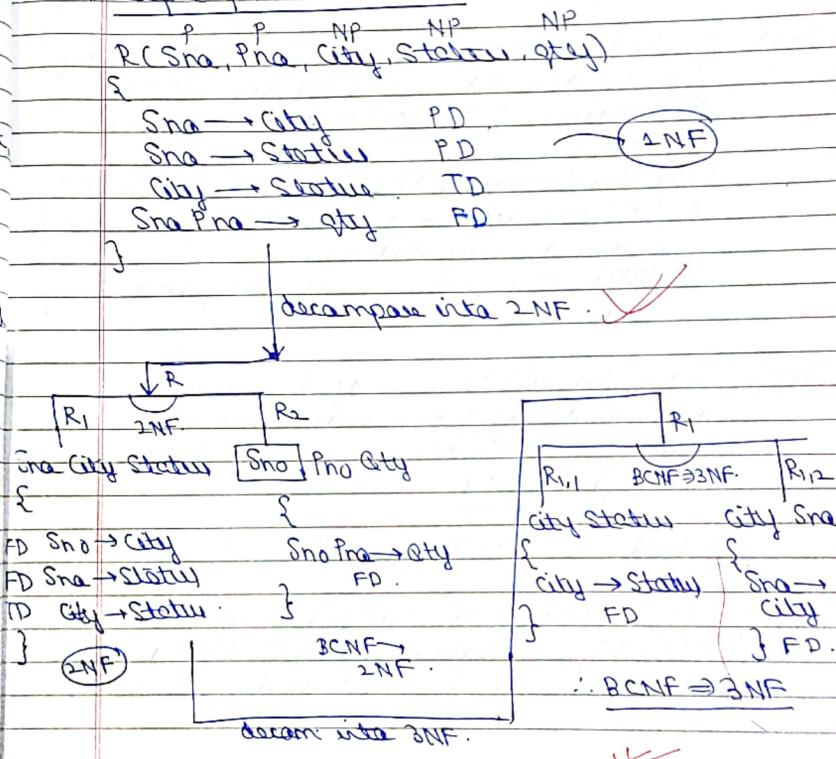
Relation R gets decomposed into set of relations R₁, R₂, R₃... by making use of all the projected functional dependencies if we

classmate
Date 29
Page 29

could derive all the FDs of the given relation. Then it is dependency preservation.

NOTE: 1: lossless decomposition guarantees the availability of all the data & dependency preservation guarantees the availability of all the integrity constraints.

* Step 2 of normalization



$D(\text{city Sna} / \text{city status} / \text{Sna Pna City})$

(decomposition
lossless/not?)

Step 1(a)

* Procedure for finding whether the given decomposition is lossless or not.

Step 1: Create the instance of the given relation by taking the attributes of the relation as columns & the given decomposition as rows.

Fill the values of the instance with X & Y. X value if the attribute is present in the decomposition.

We place the Y value along with row & column nos.

Step 2: Make sure all the FDs of the given relation are valid for the instance we prepared.

During the validation, we could observe:

$$Y \rightarrow Y$$

$$Y \rightarrow X$$

but, $X \rightarrow Y$ (X) [Wrong]

Step 3: Either during the validation of FDs or after the validation of FDs, check if there exists atleast one row with all the X values.

- If such row does exist, the given decomposition is lossless decomposition.

	Sna	Pna	city	status	city
sna city	X	Y_{12}	X	Y_{14}	Y_{15}
city status		Y_{21}	Y_{22}	X	Y_{25}
sna Pna City	X	X	Y_{33}	Y_{34}	X

Check the FDs:

$$\text{sna} \rightarrow \text{city} \quad \checkmark$$

$$\text{sna} \rightarrow \text{status} \quad \checkmark$$

$$\text{city} \rightarrow \text{status} \quad \checkmark$$

all X in

row

: lossless

[no need to
check further]

* Procedure for Validating the dependency
Preservation Property.

Step 1: Generate all the possible FDs by finding the classes of determinants of FDs of the given relation.

Step 2: Apply the projection on all the applicable FDs for finding the members of each decomposition.

Step 3: Make use of only such projected FDs and check whether all the FDs of the original

relation could get derived or not.
If they gets derived, dependencies are preserved.

$$(Sno) = \{Sno, city, Status\} \quad Sno \rightarrow Sno$$

$$Sno \rightarrow city$$

$$Sno \rightarrow Status \times$$

$$(city)^+ = \begin{matrix} city \rightarrow city \\ city \rightarrow Status \end{matrix}$$

$$(Sno, Pno)^+ = \begin{matrix} Sno, Pno \rightarrow Sno \\ Sno, Pno \rightarrow Pno \\ Sno, Pno \rightarrow city \times \\ Sno, Pno \rightarrow Status \times \\ Sno, Pno \rightarrow Qty \end{matrix}$$

city Sno	city Status	Sno, Pno Qty
{	{	{
Sno \rightarrow Sno	city \rightarrow city	Sno \rightarrow Sno
Sno \rightarrow city	city \rightarrow city	Sno, Pno \rightarrow Sno
city \rightarrow city	city \rightarrow Status	Sno, Pno \rightarrow Pno
		Sno, Pno \rightarrow Qty

from
decomp.

(using these FDS,
can you derive the FDS of
a relation.)

$$\begin{matrix} na \rightarrow city & \checkmark \\ ns \rightarrow Status & \checkmark [From] \\ city \rightarrow Status & \checkmark \\ afra \rightarrow qty & \checkmark \end{matrix} \quad \begin{matrix} dependency \\ preservation \end{matrix}$$

* ~~BCNF ALGORITHM~~

These algorithm can be used for decomposing any given relation directly into BCNF

- These also gives guarantee for:

- 1: The first BCNF decomposition.
- 2: The last BCNF decomposition.

These also fail to give guarantee for dependency preservation also. (sometimes it will, sometimes it won't)

• It will identify the dependencies, which are not full dependencies \times

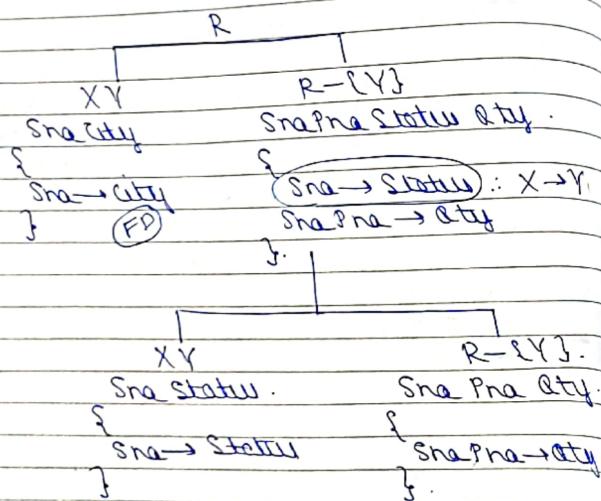
Step 1: Identify the functional dependencies that are not full dependencies.
Consider them as $X \rightarrow Y$.

Step 2: Start decomposing the relation R using any of such $X \rightarrow Y$ into XY and $R - \{Y\}$.

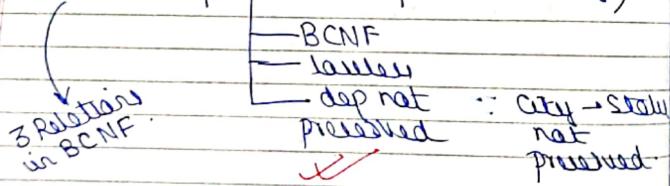
Step 3: Identify both the decompositions in BCNF or not.
If not, apply the algorithm on the decomposition which is not in BCNF.

$R(Sna, Pna, City, State, Atty)$

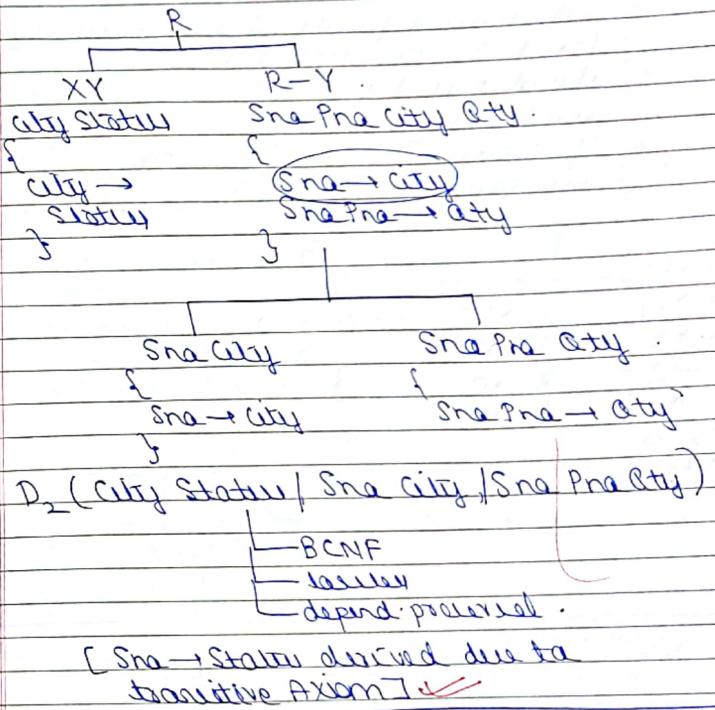
$\{$
 $Sna \rightarrow City$. $X \rightarrow Y$ PD.
 $Sna \rightarrow State$ PD.
 $City \rightarrow State$ TD.
 $Sna Pna \rightarrow Atty$ FD.



$\therefore P_1(Sna City | Sna State | Sna Pna Atty)$



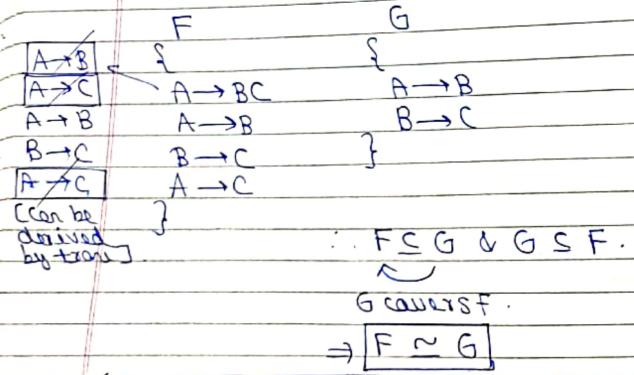
But, if perform alpha on $City \rightarrow State$



NOTE: Though BCNF gives guarantee for zero redundancy, it is not the preferred normal form practically as it is uncertain during the dependency preservation.

* COVER

- There exists 2 functional dependency sets
For e.g. we could define G covers F if and only if all the FDs of F are implied by G.
- In case, F covers G & G covers F, then we could define F & G are equivalent.



* 3NF DECOMPOSITION ALGO

- This algo is used for decomposing any given relation to 3NF directly.
 - This algo gives guarantees for:
 - the final 3NF decomposition.
 - dependency preserving decomposition.
 - Jarvis decomposition.
- due to cover.

Step 1: Find out the cover of functional dependency set of the given relation.

Step 2: Decompose the relation according to the cover we get in Step (1).

Step 3: Verify if the decomposition is Jarvis or not; if not add the candidate key of the given relation as a separate decomposition.

* There exists 2 types of covers:

- Minimal cover.
- Canonical cover.

Procedure for finding Minimal cover:

Step 1: Apply the decomposition axiom on all the functional dependencies to make that dependent of each FD has only 1 attribute.

Step 2: Eliminate the unnecessary attributes that exist on determinant side of functional dependencies.

Scenarios for applying Step 2:

$AB \rightarrow CB$ \downarrow $AB \rightarrow C$	$A(B) \rightarrow C$ $A \rightarrow C$	$\cancel{AB} \rightarrow C$ $B \rightarrow C$	$B \rightarrow C$ $B \rightarrow A$
			$B \rightarrow C$ $BA \rightarrow C$: A $BA \rightarrow C$ and $BA \rightarrow A$.

Step 3: eliminate the unnecessary FD which could be either redundant FD / transitive FDs.

* Procedure for finding canonical cover.

Step 1: Change the FDs whose determinant is same.

Step 2: Eliminate the unnecessary attributes that exist on ~~dependent~~ side of FD
detum

Scenarios discussed during the minimal cover are applicable in canonical cover procedure also.

Step3: Eliminate the unnecessary attributes that exist on dependent side of FD.

Scenarios for Applying S3

$\begin{array}{l} AB \rightarrow C \\ AB \rightarrow D \\ C \rightarrow D \end{array}$	$\begin{array}{l} AB \rightarrow C \\ AB \rightarrow D \\ C \rightarrow D \\ A \rightarrow C \end{array}$	$\begin{array}{l} AB \rightarrow C \\ AB \rightarrow D \\ C \rightarrow D \\ A \rightarrow C \end{array}$
--	---	---

$$\begin{array}{l} AB \rightarrow CD \quad (AB)^+ = \{A, B, C, D\} \\ BC \rightarrow D \quad (AC)^+ = \{A, B, C, D\} \\ \\ (BC)^+ = \{B, C, D\} \\ (AB)^+ = \{A, B, C, D\}. \end{array}$$

Step 4: eliminate the unnecessary FDS

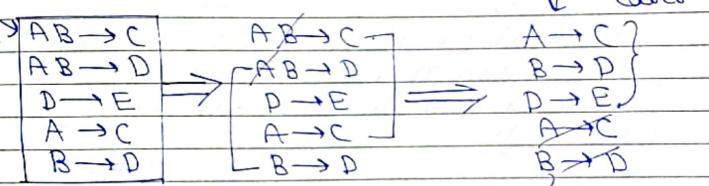
~~P P NP NP NP~~
~~Q R(A,B,C,D,E)~~

$AB \rightarrow CD$	FD
$D \rightarrow E$	TD
$A \rightarrow C$	PD
$B \rightarrow C$	PC
$D \rightarrow C$	DC

$$\begin{aligned}
 \text{CK} \quad (AB)^+ &= \{ A, B, C, D, E \} \\
 (D)^+ &= \{ D, E \} \\
 (A)^+ &= \{ C, A \} \\
 (B)^+ &= \{ B, D \}
 \end{aligned}$$

decompose
into
3 NF

S1): find cause. (either min/cur).



AC BD DE AB

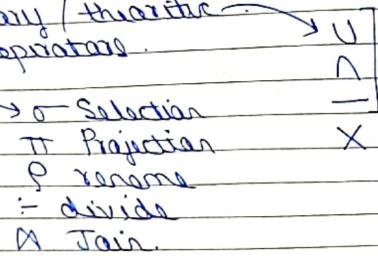
dependency preserving

add CK.

* RELATIONAL ALGEBRA

- Collection of methods that are applied for retrieving data as per user requirement is called relational Algebra.
- The methods we apply are the operators of relational Algebra.
- Such operators are divided into 2 types:

- (i) Set theory / algebraic
- (ii) Native operators.



* Degree

- Total no. of attributes present in a relation or total no. of columns present in a Table is called degree of the relation.
- degree of relation R is represented as $d(R)$.

* Cardinality

- Total no. of rows present in a table or the tuples present in a relation is

Date _____
Page 40

Date _____
Page 41

called cardinality of the relation.

$$|R| \leftarrow \text{cardinality}$$

* Domain

Total range of accepted values for an attribute of the relation is called domain of the attribute.

e.g. create table T

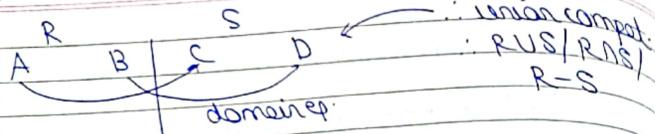
{
 | a char
 | b int
 | }
range of accepted values.

* Union compatibility

Two relations R and S are said to be union compatible with each other if and only if:

- they have the same degree.
 - The domain of the respective attributes is same in both the relations.
- In order to apply union, intersection & minu operators among the relations, they must be union compatible with each other.

Set Theory



$$\begin{aligned} \cdot d(RUS) &= d(R) = d(S) \Rightarrow 2 \\ \cdot d(R-S) &= d(R) - d(S) \end{aligned}$$

present in R, not present in S.

$$1) \cdot d(RUS) = d(R) = d(S)$$

$$\max(|R|, |S|) \leq |RUS| \leq |R| + |S|$$

$$2) \cdot d(RNS) = d(R) = d(S)$$

$$0 \leq |RNS| \leq \min(|R|, |S|)$$

$$3) \cdot d(R-S) = d(R) - d(S)$$

$$0 \leq |R-S| \leq |R|$$

RHS

- Subtraction

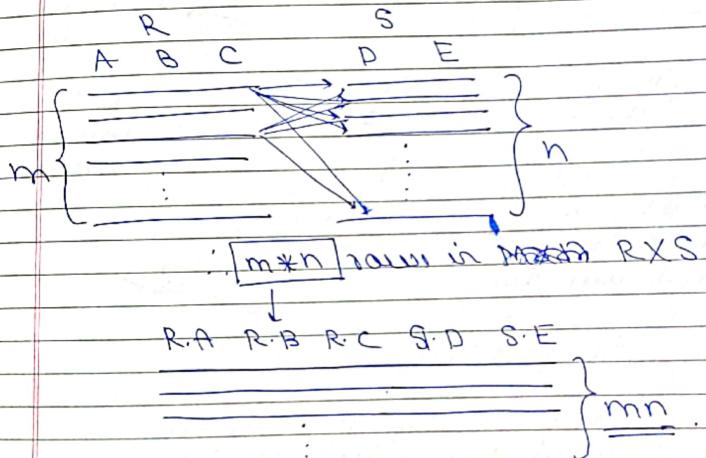
* CROSS PRODUCT (CARTESIAN)

$$d(RXS) = d(R) + d(S)$$

$$|RXS| = |R| * |S|$$

- Relations need not be union compatible for CP.

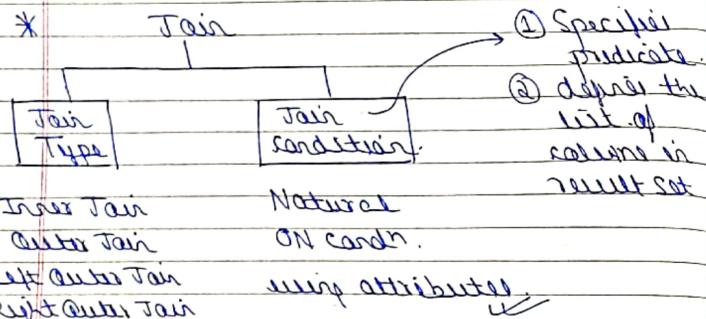
- If in case, the application/user query requires the type of data which can't be extracted from any of the tables directly.
- The data extraction requires the association of columns of relation R with the columns of relation S.
- In order to apply Cartesian Product on any 2 relations, they need not be union compatible with each other.
- Cartesian Product Produces all the possible associations among the values of the given relations in the result set.



* JOIN

- Result of the Join operator is the subset of the result of the Cartesian Product
Hence, operator 'Join' is considered as the subset of the operator 'Cartesian Product'
- Join operator has 2 Sections:

- 1) Join condition
- 2) Join Type



* Join Condition

It is primarily responsible for :

- (i) Specifying the predicate used for Join.
- (ii) Defining the list of attributes that would be the part of the result set.

→ There exists 3 Join Conditions :

(i) Natural Condition

- (1) In order to apply this condition on any 2 relations, there must have atleast one common column.
- (2) This generates the predicate on the common column with equal to comparison operator only.
Hence, also called "EQU JOIN".
- (3) This join condition eliminates the duplicates of the common column in the result set.

(ii) ON Condition

- (1) we can apply this join condition on any of the two relations irrespective of they have common column / not.
- (2) within the join Predicate, we could make use of any of the comparison operators [THETA JOIN]
- (3) This join condition will not eliminate any of the columns in the result set.

(iii) USING Attributes Join

- (1) This is the special case of Natural Join in which ~~one~~ / some/all the common columns can be used in the join predicate.
- (2) The duplicates of the columns that are used in the predicate gets eliminated in the result set.
- (3) If all the common columns are used, then result of this Join condition will exactly be same as the result of Natural Join.

* JOIN TYPE

This component of Join primarily responsible for:

- (1) Finding whether the rows are matched or not as per join condition.
- (2) Decision on including/excluding the unmatched rows in the result set.

(i) INNER JOIN

This Join type will allow only the matched rows in the result set.

(ii) LEFT OUTER JOIN

This Join Type allows the following:-

- (1) The Matched rows.
- (2) The Unmatched rows of Left Side relation along with Null Value for the columns

- (3) of right side relation.
- (3) Left Outer Join rep deficiency as the right side relation.

(iii) RIGHT OUTER JOIN

This Join type will allow:

- (1) The Matched rows.
- (2) UnMatched rows of right Side relation along with Null Value for the columns of left Side relation.
- (3) ROT represents deficiency on the Left Side relation.

(iv) FULL OUTER / OUTER JOIN

This Join type will allow the matched rows, unmatched rows of both left & right side relations along with Null Value for the respective positions in the result set.

$$\text{Left Outer Join} \cup \text{Right Outer Join} = \text{Outer Join}$$

R			S		
A	B	C	A	B	E
1	b ₁	c ₁	1	b ₁	e ₁
2	b ₂	c ₂	3	b ₂	e ₂
3	b ₃	c ₃	4	b ₃	e ₃

$$\left. \begin{array}{l} R.A = S.A \\ \& \\ R.B = S.B \end{array} \right\} \text{Natural condition}$$

Type of Join.

A			B	C	F
1	b ₁	c ₁	c ₁		↙ Inner J.
2	b ₂	c ₂	NULL		↙ Left Outer J.
3	b ₃	c ₃	NULL		
4	b ₃	NULL	c ₃		

Full Outer Join.

- NOTE:
- Join operators consider a row as qualified if it gets matched at least once.
[Like 1 b₁ c₁]
 - To represent all "at least once" scenarios, join operator should be applied.

Date _____
Page _____ 48

classmate
Date _____
Page _____

* DIVIDE

- In order to apply $R : S$, the pre-requisite is the list of attributes of the right side relation should always be the subset of the list of attributes of left side relation.
- We would get the values of attributes of left side relation in the result that get associated with all the values of right side relation.

Note: Divide considers a row as qualified if & only if, it gets matched with all the required values.

$R : S$

$S \subseteq R$

R		S	
Sno	Pno	Pno	
S ₁	P ₁	P ₁	
S ₂	P ₁	P ₂	
S ₁	P ₂		
S ₂	P ₂		
✗ S ₃	P ₁		
✗ S ₄	P ₂		
✗ S ₅	P ₁		
✗ S ₆	P ₂		

Sno
S1
S2

* Selection [in Relational Algebra]

- This operator of relational Algebra would produce the logical, horizontal subset of rows that are specified by the predicate.
- The result of the Selection operator in RA would be same as the result of where clause in SQL.

$$d(\sigma_{\text{result}}) = d(\text{original})$$

$$|\sigma_{\text{result}}| \leq |\text{original}|$$

e.g.: $\sigma_{\text{deptno}=10}$

* Projection

- This operator of RA would produce the logical, vertical subset of rows by eliminating the duplicate values in the result set.
- This operator is equivalent to "Select with distinct" clause of SQL.

$$d(\pi_{\text{result}}) \leq d(\text{original})$$

$$d(\pi_{\text{result}}) \leq |\text{original}|$$

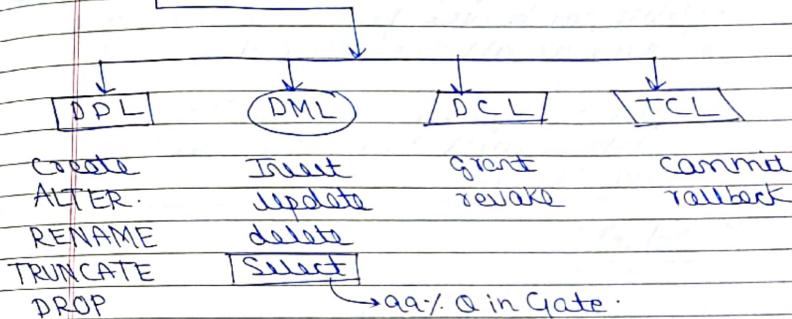
∴ gets rid of duplicate values

Date _____
Page 50

* Rename

- This operator of RA would neither change the degree nor the cardinality.

* SQL ANSII Standard SQL



- 1] All the DDL commands would exhibit the auto-commit Property.
- 2] When any of the DDL commands get executed, the metadata gets updated automatically.
- 3] Every relational data object would consist of 2 sections of information:
 - (i) Metadata of the object.
 - (ii) Mordata of the object.
- 4] When truncate command is issued, only new data gets parsed, & mordata remains as it is.

Date _____
Page 51

5) Whereas drop commands execution will purge not only the user data but also metadata.

* Truncate v/s delete

- Truncate command is used for purging all the values of the table at a time.
- Delete can be used for purging either one or some or all the values of the table.

Truncate requires only one step.
Delete requires two steps for the execution. \checkmark

* Select

M | ⑥ Select.

M | ① From <Source of data>

rows	② where <predicate>
X	③ Group by.
group	④ Having <expression>
O	⑤ Order by

-classmate
Date _____
Page 52

Q on Where
 \downarrow

-classmate
Date _____
Page _____

q1

Select *
from emp
where deptha=10
or
deptha=20
and
Sal > 5000

exp2

q2

Select *
from emp
where (deptha=10)
or
deptha=20
and
Sal > 5000

Exp1
Exp2

OR
AND
NOT

$q_2 \subseteq q_1$

* where deptha=10
or
deptha=20
or
deptha=30

= where
deptha IN
(10, 20, 30)

Note: If all the list of values of comparison are provided, we could make use of a special operator or 'IN' within the predicate. \checkmark

* Select *
 from emp
 where sal < 5000
 and
 sal > 2500
) equal
 Select *
 from emp
 where sal BETWEEN 2500
 and 5000

Date
Page 54.

in Between part
lower limit first

- ① If the range of values of comparison is provided, then we could use between operator in the predicate.
- ② While between gets used, the following points must be valid:
 - (i) Always the limits of comparison should be included in the predicate.
 - (ii) Between exp should consist of lower limit first followed by the higher limit.

* LIKE PREDICATE

- Like Predicate gets used for performing the String matching in SQL.
- There exists 2 Special char that are used within the like bracket: _ & %.
- 'Underscore' can be used while matching one char at a time.
- '%' can be used for matching 0/more char at a time.

where Ename like '_ _ _ like '%/.' ← 4 char name.

* Select *
 from emp
 where job like 'SA##_ /'
 starts with SA-
 : escape '#'

classmate
Date _____
Page _____

Job
 Salesman
 Salesclerk
 SA Rep
 SA Bay
 SA - girl

* FUNCTIONS IN SQL

at least 1 value must be returned to calling

→ Unlike the normal Prog. language functions, in SQL, each & every function must & should return atleast 1 Value to the calling environment.

→ In SQL, functions divided into 2 Types:

1. Single Row
function

2. Multiple row / Group /
Set / Aggregate functions

- These functions could be applied on 1 row at a time to get one result per row.
- eg: case translation functions
Upper / Lower / Initcap

② Character functions.

eg: Concat, Strlen, Instr, Substring

③ Number functions

eg: Sceil / Floor etc.



④ Date functions.

eg: MONTHS BETWEEN, GETDATE() etc.

⑤ Conversion functions

- These functions can be applied for converting char to date data type / vice-versa.

* ⑥ Multiple Row Functions



- These funcs can be applied on multiple rows of the table at a time to get 1 result.

- MR could either be :

- all the rows of the table
- the rows of the table Splitted into groups using group by clause.

eg: max(), min(), sum(), avg(), count()

//

where → are raw at a time.

Q) Select empno, deptno, Sal

from emp

where sal = max(Sal).

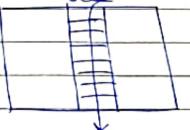
not compatible

- only Single row functions are compatible
to be used in the where clause.

- Group functions are not compatible
to be used in the where clause.

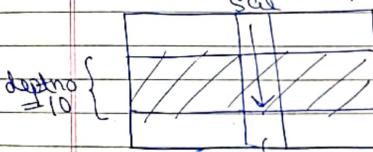
* Group By

1) Select max(Sal) from emp



highest sal.

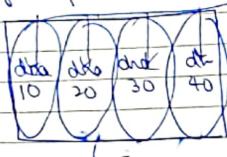
2) Select max(Sal) from emp
where deptno = 10



highest sal of
deptno 10.

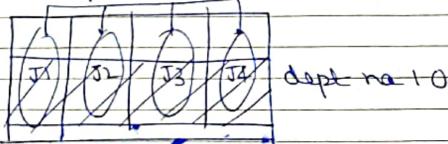
Q)

3) Select max (Sal)
from emp
group by deptno.

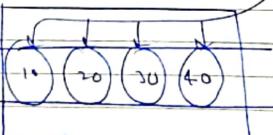


return 4 values (max sal of each department).

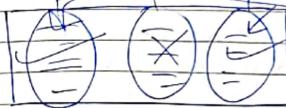
4) Select max (Sal)
from emp
where deptno = 10
group by job



5) Select count (empno), deptno
from emp
where sal > 11
group by deptno



6) Select sum (Sal), deptno
from emp
group by deptno
Having count (empno) > 4



7) Select max (Sal),
from emp
group by deptno

5000
8000
6000

deptno
can be P/A.

8) Select max (Sal), deptno
from emp
group by deptno

non-group attribute present.

NOTE: All the non-group expression that exists in the Select clause along with group expression must & should be present in the group by clause. Else, the query returns an error.
• It is not vice-versa.

* Order By

- By default, SQL displays the result set in the same order as the data got inserted.
- In case if we want to override that behaviour, we can make use of order by clause.
- If multiple expressions are used within the order by clause, then Sorting takes place based on exp 1 first. On top of its result, exp 2 gets applied and so on.

eg: `Select deptno, sal`

`from emp`

`order by deptno, sal desc`

10	5K
10	4K
10	3K
20	8K
20	7K
20	6K
30	9K
30	10K

`Select deptno, sal`
`from emp`
`order by`
①, ② desc

same output.

→ We could also specify the column name in the order by expression based on the Select query.

* SubQuery

- If in case, the Predicate based on which the query has to be computed is not ready for the execution then we would end up writing 1 query inside another query.
- The inner query is also called SubQuery & the outer query is also called Main Query.
- Always, the SubQuery will complete the execution first. After the completion, it could return either 1 value/ many values to the main query.
- If the SubQuery returns only 1 value, it is called Single row SubQuery.
- If the SQ returns multiple values, it is called multiple row SQ.

→ In case of MR SubQ : we should make use of multiple row operators for making the comparison compatible.

eg:
`Select *`
`from emp`
`where sal = (` 1 value - single row
`Select max(sal)`
`from emp)`

Q) * Select max(sal)
 from emp
 $\text{where sal} < (\text{Select max(sal)}$
 from Emp ↗ 15000
 where
 $\text{sal} < (\text{Select max(sal)}$
 $\text{from emp})$

Sal
 10K
 5K
 8K
 12K
 15 K
 9K

(3rd highest salary.
 [10K] ✓

* Multi Row SQ

Select emp_no, Ename, deptno, Sal
~~from emp~~
~~where deptno IN~~ ↗ return multi row
~~(Select deptno~~
~~from dept~~
~~where location =~~
~~'Pune')~~
 if '='
 and
 $\text{sal} > 50000$
 and
 $\therefore \text{IN}$.

Q) Select E.empno, E.ename,
 $\text{from Emp F, Dept D}$
 $\text{where E.deptno} = \text{D.deptno}$
 and
 $\text{D.location} = \text{'Pune'}$
 and
 $\text{E.sal} > 50,000$.
 same off as 2001.

JOIN

Q) Select *
 from Emp
 $\text{where sal} > \text{All} (\text{Select sal}$
 from Emp
 $\text{where job} = \text{'CLERK'})$

=

Where $\text{sal} > (\text{Select max(sal)}$
 from emp
 $\text{where job} = \text{'CLERK'})$

details of the employees whose salary
 is greater than the max salary of clerk

- In General, the normal Subquery gets executed only once irrespective of no. of rows we have in the Table.

* CORRELATED SUBQUERIES

- There are the Special type of Subqueries which gets executed no. of times equal to the no. of rows we have in the table.
- We could identify the correlated subquery by making use of the column belongs to the outer query, inside the inner query.

* Execution Procedure

- Step 1: Main Query will identify the row for processing after that as candidate row.
- Step 2: Main Query will pass the candidate row values to the subquery.
- Step 3: Subquery will complete the execution once based on the candidate row values it receive & return the result to the main query.
- Step 4: Main Query takes the decision of either including/excluding that row in the result set before it finds the next candidate row value.
- Step 5: The above procedure gets repeated for all the candidate row values.

eg: from Emp A

 | Select A.Sal

 | from Emp A

 | where 4 = (Select count(distinct(B.Sal))

 | | at rank. (q-1)

 | | from emp B

 | | n to rank. (n-1)

 | | where B.Sal > A.Sal)

alias of emp
relation

A	B
emp	emp
Sal	Sal
→ 12K	12K
→ 36K	36K
→ 10K	10K
8K	8K
15K	15K
18K	18K
12K	12K

6th
point

* In SQL, we can use Set operators for combining the results of 1 or more Select queries.

- When Set operator is used, the query collectively is called Compound Query.
- The individual Select Statements are referred as component queries.
- The component queries must be union compatible with each other.

$\{J_1, J_2, J_3\} \cup \{J_2, J_4, J_6\}$
 $\{J_1, J_2, J_3, J_4, J_6\}$

~~*~~ Select Job
 from Emp
 where deptno = 10.
 UNION

Select Job
 from Emp
 where deptno = 20
 will eliminate
 duplicates.

Select Job
 from emp
 where deptno = 10
 and
 deptno = 20

want
 eliminate
 duplicate.
 [add select
 diff. job]

~~*~~ Select Job $\{J_1, J_2\}$
 from Emp
 where deptno = 10
 INTERSECT.

Select Job
 from Emp
 where deptno = 20
 Jobs where
 dept no is 10 and
 20 both.

Select Job
 from emp
 where deptno = 10
 and
 deptno = 20

result.
 :: when mapp
 many row.
 :: [not possible].

- H/W
 1) diff b/w commit & checkPoint.
 2) What is NP complete Problem.
 3) Describe Shadow Paging.
 4) What is WAL Protocol
 5)

12/16/19
Saturday

Date _____
Page 68

Lecture 3

→ min 1M a.

* TRANSACTION MANAGEMENT

consistent state = data must be correct

⇒ A sequence of instruction which could convert the database from 1 consistent state to another consistent state is called transaction.

⇒ A group of DML instructions which could convert the database to a consistent state by executing all the instructions atomically is called transaction.

⇒ Each & every such transaction in RDBMS must satisfy the following properties:

- (i) Atomicity
 - (ii) Consistency
 - (iii) Isolation
 - (iv) Durability
- } ACID ✓

1) Atomicity

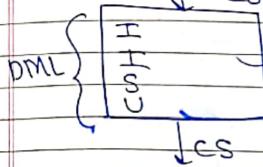
- According to this property of transaction, either all instruction of transaction should get executed or none of the instruction of transaction should get executed.
In every RDBMS, the intent of the transaction

gets embedded between:

begin tran & end-tran commands
Among them, Specifying begin tran is optional and end-tran is mandatory.

NOTE: End of 1 transaction indicates the begin for the next transaction.

beginning ↓ 1cs



2) Consistency

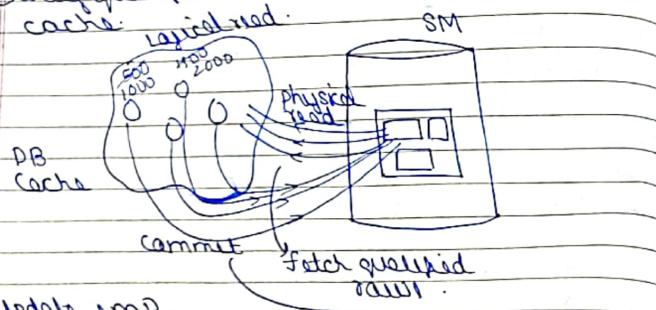
- According to this property of transaction, data in the database must remain consistent not only before the transaction but also after the transaction, impact of the transaction gets committed/no. - RDBMS will make use of the concept called Shadow Paging for guaranteeing the consistency property.

* Shadow Paging

According to this Property, RDBMS keep track of the following detail:

- 1) Copy of the data item before the transaction.
- 2) Copy of the DT after the transaction
- 3) Details of the transaction that performed the modification.

- Only specified rows are stored into PB cache.



> Update imp
Set sal = sal + 500
where deptno = 20
> Commit

RDBMS
processes after
transact with
back to disk.

Rollback (abort) : the
modification are ignored
and must get replaced
with the before
transaction values.

* End of the transaction could either be commit / rollback.

In case of COMMIT:

all the modifications performed by the specific transaction are allowed to be transferred from the volatile cache to the non-volatile disk.

In case of ROLLBACK:

The abort operation takes place. Abort operation has the following steps:

- (i) Ignore all the modifications performed by the transaction.
- (ii) Replace such values with the values of the data items before the transaction which could either be previously committed or consistent values etc.

3) ISOLATION [Vimp]

According to this property of transactions isolation must be guaranteed across the execution of transactions in the database.

- i.e. any transaction will not be able to affect any other transaction during the execution.
- i.e. all the transactions are guaranteed to be executed in an isolated environment.

* SCHEDULE

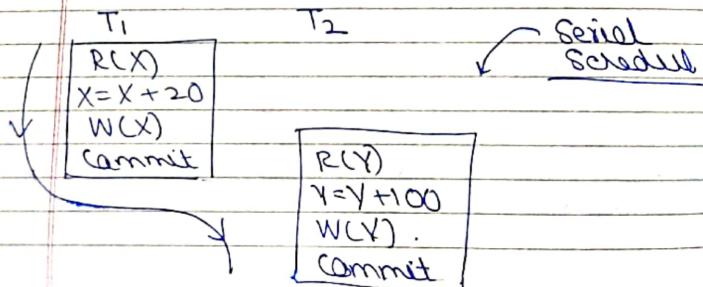
- Schedule is the representation of execution of the individual instructions of transaction.
- Schedules are of two types:
 - (i) Serial Schedule
 - (ii) Concurrent Schedule.

(i) Serial Schedule

A Schedule is said to be Serial if & only if all the instructions of all the transactions gets executed non-preemptively.

NOTE: If there exists n no. of transactions, then the total no. of possible Serial Schedules are $n!$.

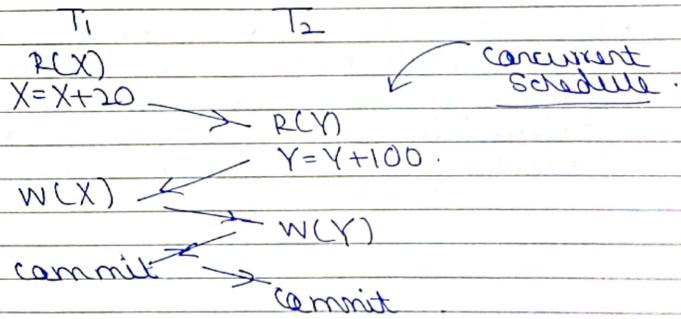
e.g. if there exists 3 trans : $T_1 T_2 T_3$.
Total no. of possible Serial schedules are : $3! \Rightarrow 3 \times 2 \times 1$



- Each & every possible Serial Schedule is guaranteed to produce data consistency always.
- Serial Schedule could get affected with:
 - (1) Possible high avg. wait time.
 - (2) Not acceptable response time.
 - (3) Low throughput.

(ii) Concurrent Schedule

- A Schedule is said to be concurrent if the instructions of the transactions are getting executed preemptively.
- Concurrent Schedule guarantees:
 - (i) Reduced Avg. wait time.
 - (ii) Acceptable response time.
 - (iii) Optimal throughput.
- However, they can't guarantee data consistency due to the possible conflicting operations.



* Conflicting Operations

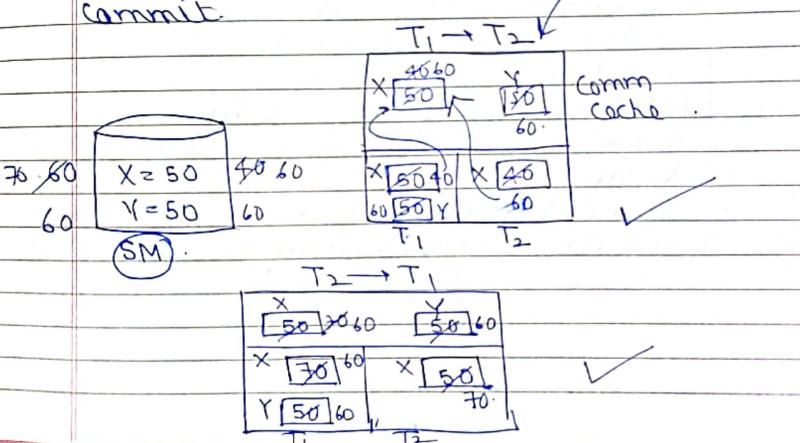
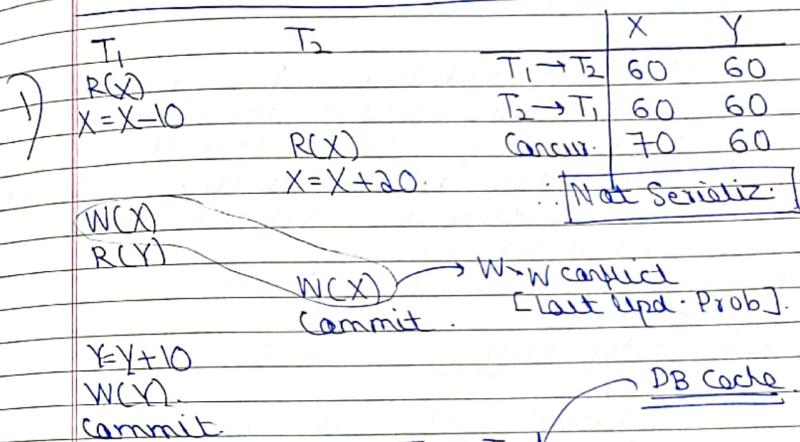
- A pair of operations are said to be conflicting with each other iff :
- they belong to two different transactions.
 - Both the operations are accessing the same data item.
 - At least one of those operations is a "Write" operation.

T_i	T_j	
1) $W(X)$	$R(X)$	$W \downarrow W \rightarrow$ conflict \rightarrow last update problem
2) $W(X)$	$R(Y)$	$W \downarrow R \rightarrow$ conflict \rightarrow dirty read problem
3) $R(X)$	$W(X)$	$R \downarrow W \rightarrow$ conflict \rightarrow unrepeatable read prob.

- * RDBMS implemented the concept called concurrency control for guaranteeing data consistency always.
- concurrency control mechanism ensures resulting serializable schedules always.

* Serializable Schedules

A Given concurrent Schedule is said to be Serializable if and only if it produces the result same as atleast 1 of the possible Serial Schedules always.



Bless
You

concurrent

X [50]	Y [50]
50 70	60
X [50] 40	X [50] 70
Y [50] 60	

✓

NOTE

1. The Given Schedule is not Serializable.
2. In the above Schedule, the update performed by T_1 on the data item X was getting lost as the update performed by T_2 . Hence, the problem is called "Last Update Problem".

* Dirty Buffer

- The data item which got modified only in the cache and not yet modified in the disk is referred as dirty buffer.
- All the updates performed by any ongoing transaction ideally be the dirty buffer.
- If any transaction does perform read operation on such dirty buffer, then it is referred as dirty read.

classmate
Date 76
Page

	X
$T_1 \rightarrow T_2$	110 ✓
$T_2 \rightarrow T_2$	110 ✓
concurrent	100

classmate
Date 77
Page

50	60
----	----

	T_1	T_2
*	50 R(X)	
40	$X = X - 10$	
40.	W(X)	

$$\begin{aligned} & R(X) \quad 40 \\ & X = X + 60 \quad 100 \\ & W(X) \quad 100 \\ & \text{Commit} \end{aligned}$$

Rollback

- The above Schedule is not Serializable.
- In the above Schedule, T_2 had been performing the read on the data item that got modified by another ongoing transaction T_1 .

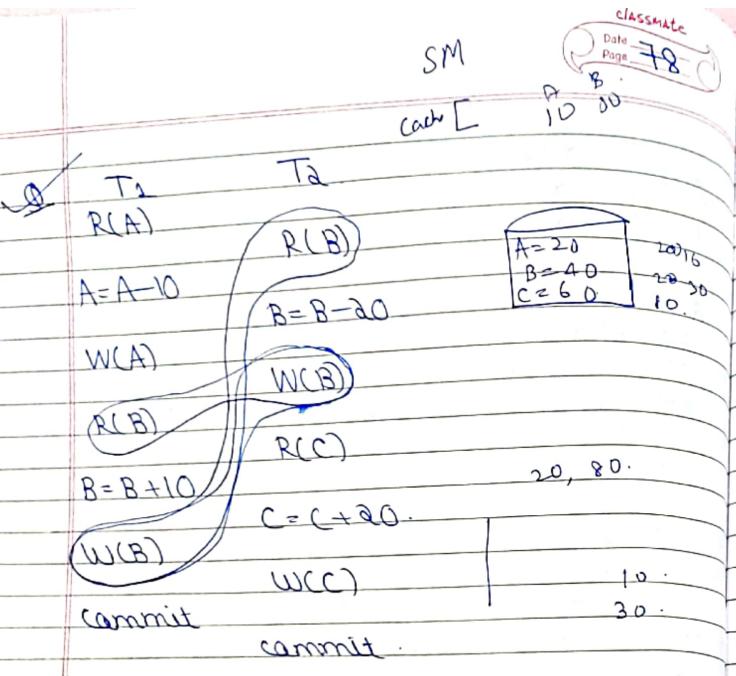
Here, that is referred as dirty read.

	T_1	T_2
2)	50 R(X)	
	R(X)	
	$X = X + 50$	

$$\begin{aligned} & R(X) \\ & X = X + 50 \\ & W(X) \end{aligned}$$

R, W conflict
Unrepeatable
read Prob.

[Not Serializable]



- (i) Identify all possible conflicts.
 (ii) Is schedule serializable / not.

- ✓ 1) $W(B) \rightarrow R(B)$ [Dirty].
 ✓ 2) $W(B) \rightarrow W(B)$
 ✓ 3) $R(B) \rightarrow W(B)$

(iii)

	A	B	C	30.	80.
$T_1 \rightarrow T_2$	10	30	80		
$T_2 \rightarrow T_1$	10	30	80		
Concurrent	10.	30	80		

\checkmark \checkmark \checkmark

\checkmark **Serializable Schedule**

NOTE :

1) The given schedule has all the possible conflicting operations. Despite of that, it is producing the result same as the possible Serial Schedule. Hence, the given schedule is declared as Serializable Schedule.

2) The above example proves that if there exists conflicting operations in a schedule, it only means there could be possible data inconsistency.

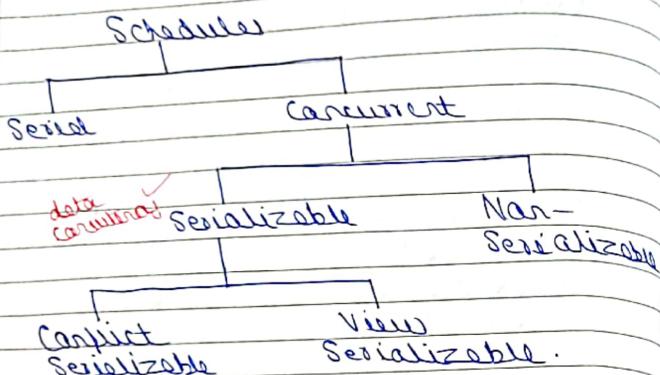
NOTE : If a given concurrent schedule becomes equivalent to one of the Serial Schedule, then it is referred as Serializable Schedule.

- If the given concurrent Schedule is conflict equivalent to one of the possible Serial schedules then it is referred as conflict Serializable Schedule.

- If the given concurrent Schedule is view equivalent to one of the possible Serial schedules, then the given schedule is declared as View Serializable.

\rightarrow If the schedule is either conflict / view or / both, we declare that Schedule as conflict Serializable.

→ If it is neither of them, then it is deadlock or not Serializable.



* Conflict Equivalence

2 schedules S_1 and S_2 are said to be conflict equivalent to each other if & only if the order of conflicting operations is same in both the schedules.

* Precedence Graph Algorithm

We could apply the algo for finding whether the given schedule is conflict serializable or not.

Step 1: Create the no. of nodes in the Graph that are equivalent to the no. of transaction in the Schedule.

Step 2:

Starting from each & every node i.e. each & every transaction, identify all the existing conflicting operations & represent them in the Graph in the form of edges following the direction of conflicting operations.

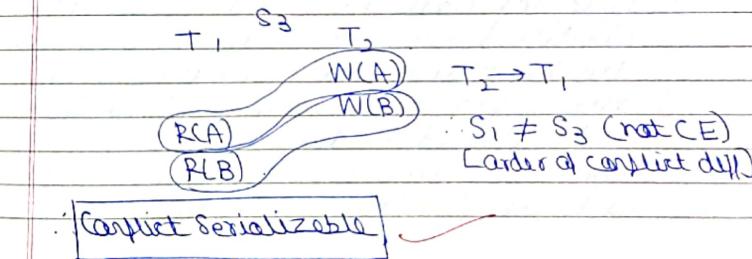
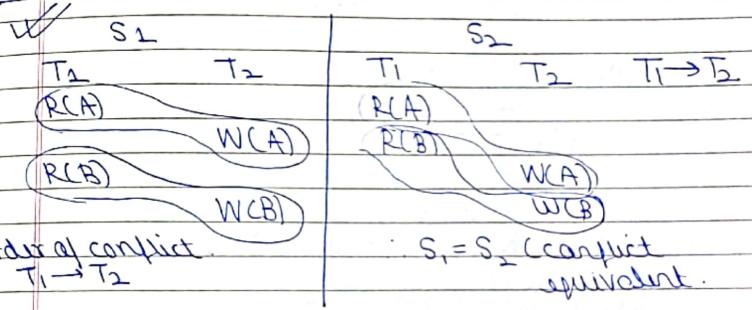
Step 3:

Check if the precedence graph has any cycle/loop.

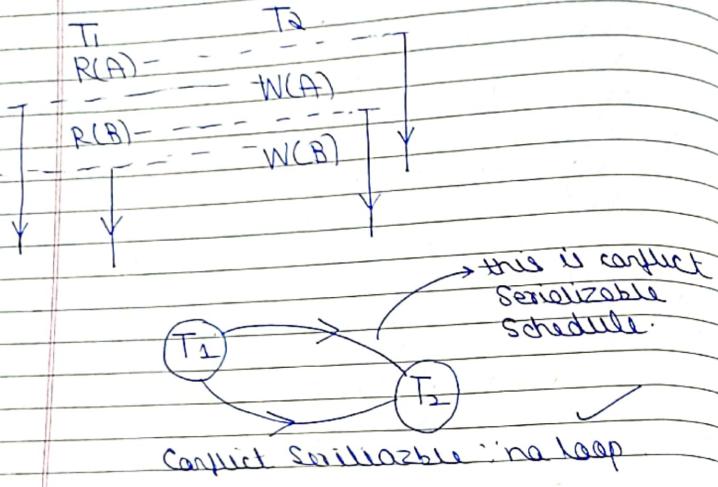
- If the cycle/loop doesn't exist; then the given schedule is conflict serializable.

Step 4:

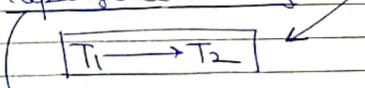
If the schedule is conflict serializable, then apply the topological ordering on the Graph for finding the equivalent serial schedule.



* Prec Graph Algo



* Topological ordering :



The process of identifying the node with indegree 0 always, is called Topological ordering.

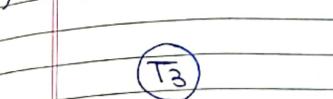
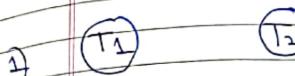
After the node with Indegree 0 gets identified, we must ignore that node further & also we must ignore all the edges that were emerging from that selected node.

From the remaining graph, we must continue identifying the next node.

with indegree 0.

→ The above process will continue until all the nodes of the Graph gets selected.

* Take these precedence Graphs :



all are ID = 0.

$T_1 \rightarrow T_3 \rightarrow T_2$

$T_1 \dots$

choose any

: 3! ways.

$T_1 \rightarrow T_2 \rightarrow T_3 \rightarrow T_4 \rightarrow T_5$

$T_1 \rightarrow T_2 \rightarrow T_4 \rightarrow T_3 \rightarrow T_5$

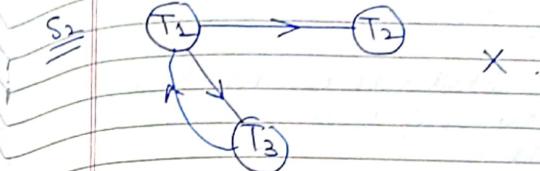
* If there exists more than 1 node with indegree 0 in the Graph, then we should consider all the possibilities with respect to the equivalent Serial Schedule.

it

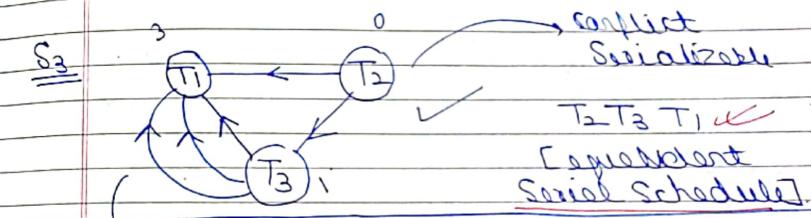
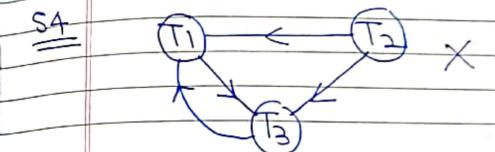
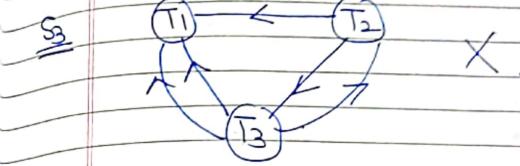
GATE 2015

There exist Schedules as given below,
Find whether there are conflict
Serializable.

	S1			S2		
	T1	T2	T3	T1	T2	T3
R(X)				R(X)		
R(X)				R(X)		
W(X)				W(X)		
W(X)				W(X)		
				R(X)		

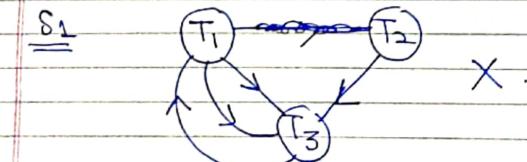


	S3			S4		
	T1	T2	T3	T1	T2	T3
R(X)				R(X)		
R(X)				R(X)		
W(X)				W(X)		
W(X)				W(X)		
				R(X)		



∴ this is conflict serializable,
hence its also Serializable.

conflict
Serializable
T2 T3 T1 ✗
[equivalent
Serial Schedule].



GATE 2007

There exist schedules as given below.
Find out which of them are conflict
Serializable.

S1) $R_1(X), R_1(Y), R_2(Y), R_2(X), W_2(Y), W_1(X)$

S2) $R_1(X), R_1(Y), R_2(Y), R_2(X), W_2(Y), W_1(X)$

T_1
 $R(X)$
 $R(Y)$



$R(Y)$
 $R(X)$
 $W(Y)$

X [not conflict
Serializable]

T_2, T_1 [equiv.
Serial
scheduling]

T_2

T_1
 $R(X)$



$R(X)$
 $R(Y)$
 $W(Y)$

$R(Y)$
 $W(X)$

✓
Conflict
Serializable -

* View Equivalence

→ NP complete
Problem.

2. Schedules S_1 and S_2 are said to be view equivalent to each other if and only if all the following points are valid for all the data items:

Step1: The transactions that are performing the initial reads on the data item in Schedule 1 are expected to perform the initial reads on those respective data items in Schedule 2 as well.

Step2: If there exists [Write-Read] conflict on any data item in S_1 , then the same conflict must exist on the same data item in S_2 as well.

Step3: The transactions that are performing the first write operations on the data items in S_1 are expected to perform the first write operations on those respective data items in S_2 as well.

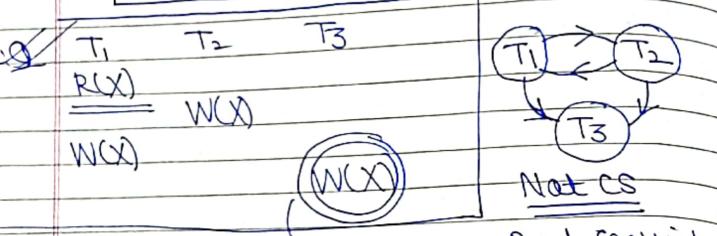
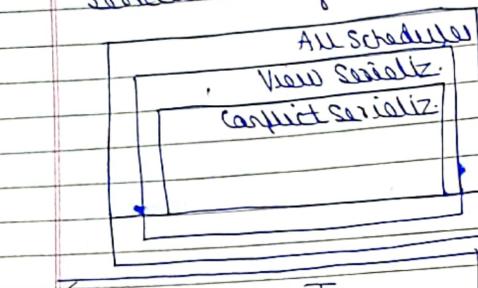
NOTE :

1. Finding whether the given schedule is view Serializable or not is NP complete problem.
2. If a schedule is conflict Serializable, always it must be View Serializable as well.
But is not vice-versa.

(C)^v

classmate
Date _____
Page 88

* Hierarchy of Schedules based on Serializability:



Check for VS \rightarrow No write-read conflict

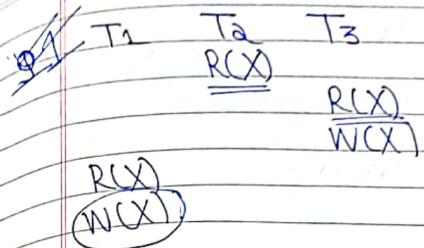
view equiv:	$T_1 \rightarrow T_2 \rightarrow T_3$	✓
	$T_1 \rightarrow T_3 \rightarrow T_2$	✗
	$T_2 \rightarrow T_1 \rightarrow T_3$	✗
	$T_2 \rightarrow T_3 \rightarrow T_1$	✗
	$T_3 \rightarrow T_1 \rightarrow T_2$	✗
	$T_3 \rightarrow T_2 \rightarrow T_1$	✗

} All serial equivalents

VS ✓

initial Read = T_2, T_3] \times var.
final write = T_1 .

classmate
Date _____
Page 89



unit val = $T_2 T_3$.
unit = T_1

* check for VS

$T_1 \rightarrow T_2 \rightarrow T_3$ ✗

$T_1 \rightarrow T_3 \rightarrow T_2$ ✗

$T_2 \rightarrow T_1 \rightarrow T_3$ ✗

$T_2 \rightarrow T_3 \rightarrow T_1$ ✓

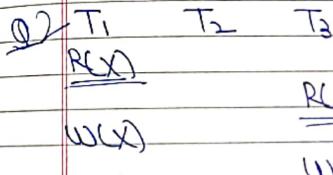
$T_3 \rightarrow T_1 \rightarrow T_2$ ✗

$T_3 \rightarrow T_2 \rightarrow T_1$ ✗

$T_2 T_3 T_1$

R(X)

view serializable
and conflict
serializable.



$T_2 \rightarrow T_1 \rightarrow T_3$

$T_2 \rightarrow T_3 \rightarrow T_1$

$T_2 T_1 T_3$

R(X)

W(X)

R(X)

W(X)

initial read
final write = T_3 .

Date _____
Page 90

T_1	T_2	T_3	
<u>R(X)</u>		<u>R(X)</u>	→ 2 initial reads $[T_1, T_3]$
<u>WC(X)</u>		<u>WC(X)</u>	
		<u>R(X)</u>	

if we start with T_1 , T_3 won't satisfy initial read.

No Serializability ✗

Note: If there exists more than 1 transaction performing the initial read on the data item and atleast 2 of these transactions are performing the write on the same data item, then the scheduled will never be view Serializable.

I

T_1	T_2	T_3
<u>R(X)</u>		<u>R(X)</u>
<u>WC(X)</u>		<u>WC(X)</u>

$\{T_1, T_2, T_3\}$ will get initial read.

Not VS

⇒ Not Serializable.

✗

✓

4) DURABILITY

According to this Property of transaction, all the modifications performed by any committed transaction are ensured to be present in the Non-Volatile Storage of database.

* Write Ahead Log Protocol

According to this protocol, all the modifications performed by each & every committed transaction, must & should be written to a special file called [redo log file] before they gets written to the actual data file.

* Redo log file → used by only RDBMS.

- It is the special file used ^{by} only RDBMS during the recovery of the database.
- This file consists of collection of Redo log buffer.
- Each & every redo log buffer consists of the following information:
 - (1) copy of the data items before the transaction.
 - (2) copy of the data items after the transaction.

✓

✓

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[Shadow copy by Redo Log buffer].

Date _____
Page 92

- (3) Details of the transaction that perform the modification.

* RECOVERY

According to ARIES database Recovery Procedure, RDBMS gets into database recovery in 3 phases.

These are:

- (1) Analysis Phase
- (2) Redo / Roll Forward Phase
- (3) Undo / Roll Back Phase.

1) ANALYSIS PHASE

- During this Phase of recovery, RDBMS will calculate the total no. of transactions that still get received.
- In each & every RDBMS, these exists as unique no associated with each & every committed transaction.

e.g.: In Oracle, that is System Change no. SCN #.

In MSS, that is Log Sequence no. LSN #.

2) Redo / Roll FORWARD PHASE

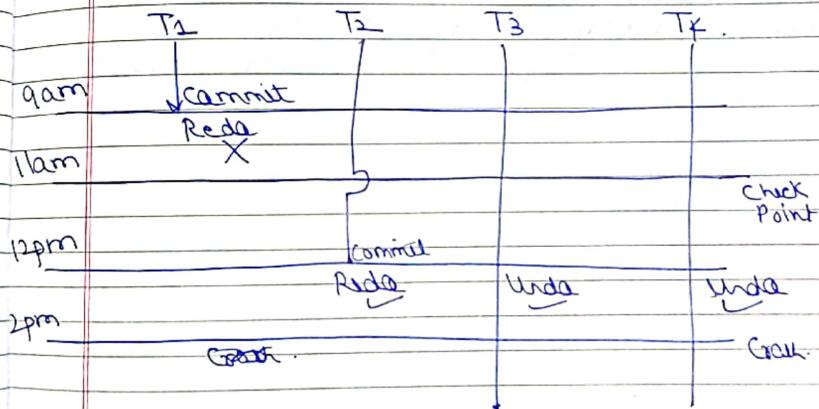
During this Phase of recovery, RDBMS will start reapplying/reading all the entries of redo log file irrespective of the entry belongs to a committed Transaction or Not.

- all transactions in day, must be present in redo log file.

3) Undo / Roll Back Phase

- During this Phase of recovery, RDBMS will perform abort operation on the entries belongs to uncommitted/ open transactions.

Diff b/w com



[Shadow Pages Viewed by Redo Log Buffer].

CLASSMATE
Date _____
Page 92

CLASSMATE
Date _____
Page 92

- (3) Details of the transaction that perform the modification.

* RECOVERY

According to ARIES DataBase Recovery Procedure, RDBMS gets into DataBase recovery in 3 phases.

These are:

- (1) Analysis Phase
- (2) Redo / Roll Forward Phase
- (3) Undo / Roll Back Phase.

1) ANALYSIS PHASE

- During this Phase of recovery, RDBMS will calculate the total no. of transactions that shall get recovered.
- In each & every RDBMS, there exists an unique no associated with each & every committed transaction.
eg: In Oracle, that is System Change no. SCN #.

In MSS, that is Log Sequence no. LSN #.



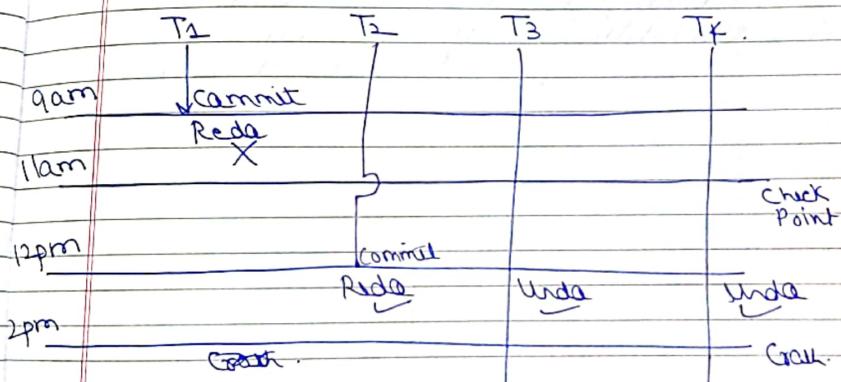
2) Redo / ROLL FORWARD PHASE

During this Phase of recovery, RDBMS will start reapplying / reading all the entries of redo log file irrespective of the entry belongs to a committed transaction or Not.
all transactions in day, must be present in redo log file.

3) Undo / Roll Back Phase

- During this Phase of recovery, RDBMS will perform abort operation on the entries belong to uncommitted/ open transactions.

Diff b/w com



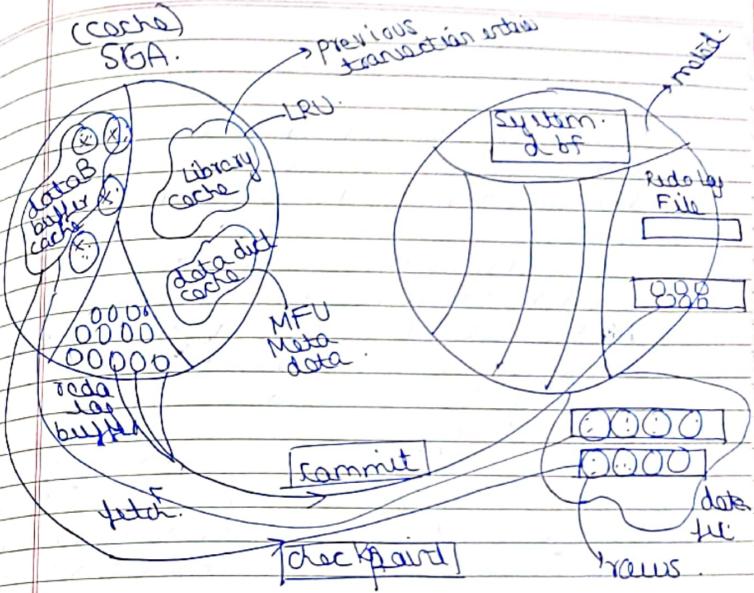
Commit

- (i) This is a transaction specific command. This is a never used operation.
- (ii) When commit is issued, all the writes belong to that transaction are guaranteed to be transferred to the Redolog File.
- (iii) If a transaction gets committed before the check point, we need not apply Redo operation on such transaction.
- (iv) This command is issued for guaranteeing the durability Property.

Check Point

This command is issued for reducing the time of database recovery.

(cache)
SGA.



update emp
set sal = sal + 500
where deptno = 20
commit

* SCHEDULES BASED ON Recoverability

- Based on recoverability, Schedules are divided into 3 types:
- (i) Recoverable Schedule
- (ii) Cascaded Schedule
- (iii) Strict Schedule.

(i) Recoverable Schedule

A Schedule is said to be recoverable if and only if, for each & every pair of transactions (T_i, T_j) is such a way that:

T_i performs the modification on the data item followed by T_j .
needs that; then always completion of the transaction should be in the order of T_i followed by T_j .

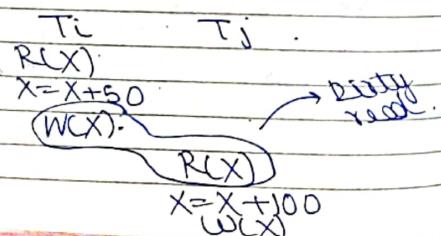
↳ Parent ↳ child
[Master] [dependent]

→ Recoverable Scheduler gets affected by the problem of cascading Roll Back.

* Cascading Roll Backs

In case if Parent / Master transaction gets roll back, then to maintain data consistency all the subsequent child / dependent transactions also should get rolled back.

→ This problem would cause lots of idle Activity.



(ii) Cascadable Schedule

A Schedule is said to be cascadable iff each & every transaction is allowed to perform read operation on the data items updated by only the completed transactions.

- dirty read never allowed.

NOTE :

- (i) All the cascadable schedules are recoverable but not vice-versa.
- (ii) Cascaded Schedules will restrict the possible dirty Read Problem but, it cannot restrict the Potential write-write conflict (lost Update Prob).
- (iii) Cascadable Schedules could have possible data inconsistency.

(iii) Strict Schedule

A Schedule is said to be strict iff every transaction is either allowed to perform read nor to perform update on the modification done by other transaction until other transaction gets completed.

ie/

- Note:
1. All the strict schedules are always cascaded & recoverable but not vice-versa.
 2. SS would control the concurrency of execution.
 - 3.

* Hierarchy of Schedules based on recoverability



* Procedure for finding Highest Recoverable Option for Given Schedule

Step 1: Find out all data items present in the schedule.

Step 2: For each data item, perform following steps:

S-3: Identify the time stamp of modification performed on data item and completion of transaction that performed modification.

time stamp of write
open on data item

no read
no write
performed
by other
trans. on
that data
item

strict

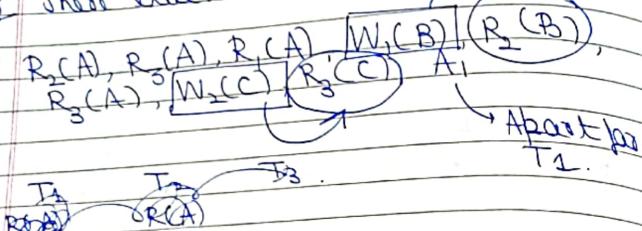
no read
performed by
other trans.
on that
data item
⇒ cascaded

if read on
that data
item by
other trans
are found
 (i) identify
master / ,
child trans
 (ii) validate
completion
of trans
are in order
 a)
master → child
 ⇒ Recoverable

time stamp of completion
of trans. performed
modification

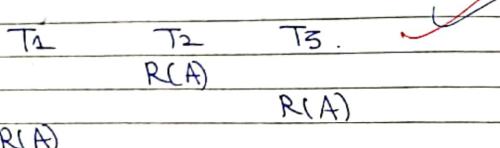
S-4: Highest common recoverable for data items
⇒ Highest recoverability for Schedule.

Q) There exists schedule or represented:



- If T1 gets aborted, which of the other transactions also will get rolled back?

- only T2
- only T3
- both T2, T3
- Neither T2, T3



both T2, T3 would rollback
dependent.
[corroborating RB] ✓

Q) Find the highest recoverable option for the following Schedule.

S1) $R_1(X), R_2(Z), R_1(Z), R_3(X), R_3(Y),$
 $W_1(X), C_1, W_3(Y), C_3, R_2(Y), W_2(Z),$
 $W_2(Y), C_2$

S2) $R_1(X), R_2(Z), R_1(Z), R_3(X), R_3(Y),$
 $W_1(X), W_3(Y), R_2(Y), W_2(Z),$
 $W_2(Y), C_1, C_2, C_3$

S3) $R_1(X), R_2(Z), R_3(X), R_1(Z), R_2(Y),$
 $R_3(Y), W_1(X), C_1, W_2(Z), W_3(Y),$
 $W_2(Y), C_3, C_2$

CL. ✓

S1) $X \rightarrow \text{strict}$
 $Y \rightarrow S$
 $Z \rightarrow S$

} strict ✓

S3) $X \rightarrow S$
 $Y \rightarrow C$
 $Z \rightarrow S$

} corrodable

Not Recov

S2) $X \rightarrow S$
 $Y \rightarrow RNR$
 $Z \rightarrow$

$T_3 \rightarrow T_2$

T_3 complete first.
But in Q: T_2

13/10/19
Sunday

3*

classmate
Date _____
Page 102

Lecture 4

* CONCURRENCY CONTROL

- RDBMS has concurrency control implemented through locking mechanism for ensuring data consistency always.
- RDBMS has a sub-prog called lock manager which is responsible for either accepting/rejecting the log request of different transactions.
- Log writers to lock requests.
- Lock Manager internally makes use of the lock compatibility matrix while taking all the decisions (existing state of item & my state).
- Initially there exist only 2 modes for the data items. Those are:

- (i) locked mode
- (ii) unlocked mode

As noticed, the degree of utilization getting reduced they introduced a different mode of locked states. Those are:

- (i) Shared mode
- (ii) Exclusive mode

- If in case the transaction wants to perform only the read operation, then they could

acquire Shared mode of lock on the data item.

→ In case if the transaction wants to perform both read & write opns, then they should acquire an exclusive mode of lock.

→ The concurrency control mechanism developed in RDBMS would aim for producing the strict serializable schedule always.

↳ Transaction prod. lock req.

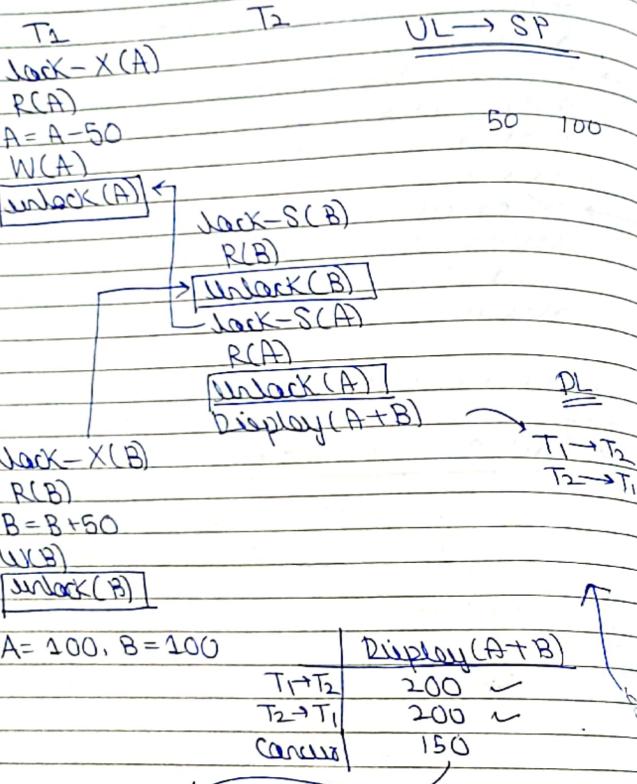
* Lock compatibility Matrix

		Current Mode		
		UnLock	S-Mode	X-Mode
Request Mode	UnLock	-	Yes	Yes
	S-Mode	Yes	Yes	No
	X-Mode	Yes	No	No

↳ T_i is write to read.
T_i is writing.
∴ T_i needs to wait in queue

↳ S not comp. with X.

✓



Transitivity is still Present, \therefore Locking is random.

- In the above example, locking & unlocking had been applied randomly due to which data consistency wasnt guaranteed.
- As per RDBMS always locking & unlocking

should be performed as per a protocol called 'Locking Protocol'.

→ One such widely used 'Locking Protocol' is 2 Phase Locking Protocol.

* 2 PHASE LOCKING PROTOCOL

According to this Protocol, the transaction process will be done in 2 phases. These are:

- (i) Growing Phase
- (ii) Shrinking phase.

→ During the Growing Phase all the transactions are allowed to acquire all the locks required for its processing.

→ Transactions cannot afford to release any of the locks acquired in this Phase.

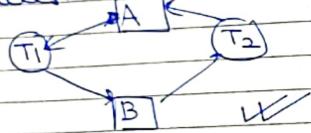
During this Phase of transaction process, the transactions are allowed to release all the acquired locks & they cant afford to acquire any new lock for them.

NOTE: 2 Phase LP gets affected by:

1. The deadlock Problem.
 2. Cascading rollback Problem.
- Deadlocks would be addressed by detection & recovery technique.
- if P rolls back,
all child
rollbacks.

→ RDBMS makes use of Resource Allocation Graph (RAG) for detecting the DL.
As part of Recovery:

- one of the transactions can be selected as victim & kill the transaction.
- 2 Phase LP always ensures the serializable schedules.



* Strict 2 Phase Locking Protocol

- This is hyper variant of 2P LP in which Growing & Shrinking Phase concepts are still valid.
- In addition to them, a new rule of "not releasing all the acquired ~~locks~~ exclusive locks of the transaction gets added".
 - can release till Ti commits.
- This protocol also gets affected by the Deadlock Problem.
- This protocol always produces the strict serializable schedules.

TIMESTAMP BASED PROTOCOL

- The most unique concurrency control technique that doesn't have the concept of lock & deadlock is time stamp based protocol.
- As per this protocol, an unique TS will be assigned for each & every transaction.

For each data item, 2 TS gets assigned. These are:

- (i) read TS
- (ii) write TS.

- The TS of the transaction that performed the most recent read on a data item becomes the read TS of the data item.
- The TS of the transaction that performed the most recent write operation on a data item becomes the write TS of the data item.
- TS based protocol is not implemented in the SQL Database practically yet.

* ER DIAGRAMS

* Phase of DataBase Design

1. Requirement Analysis:

During this phase of DB design, user will gather all the requirements for creating the database.

2. Conceptual Design

During this phase of DB design, ER diagram would get prepared. Preparing the ER diagram is independent of the RDBMS structure, OS platform selection, Geography etc.

3. Logical Design

During this phase of DB design, we would decide all the different tables would be part of the DB & the list of columns that would be part of each table along with list of integrity constraints.

4. Physical design

During this phase of DB design, user would execute : create DB, create table commands

* Referential Integrity constraints

This is the process of validating the correctness of data with a reference.

Foreign Key constraints would eventually validate the referential integrity of data.

* Foreign Key

The Primary Key of Master / Parent Table which would exist in the child / dependent tables is referred as Foreign Key in the child Table.

While defining the foreign key, there exists 2 options :

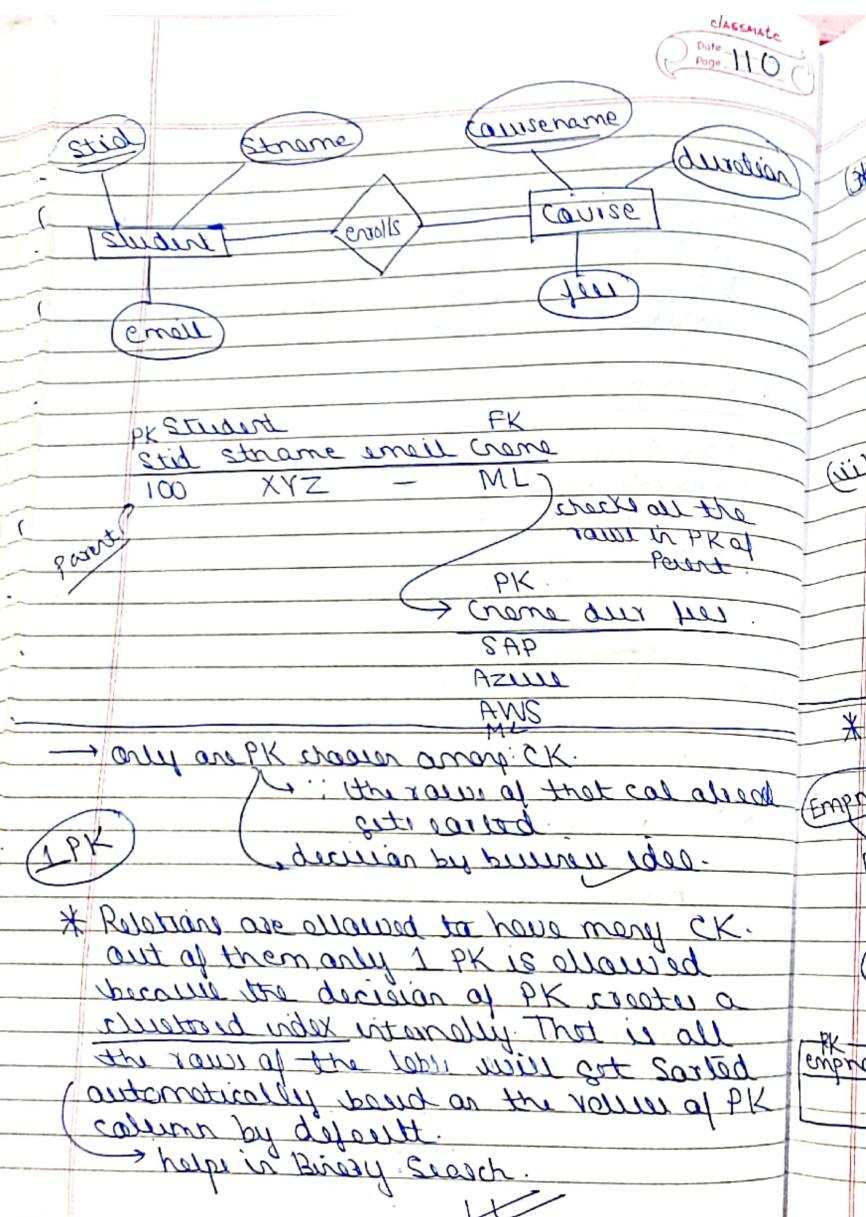
- (i) On delete cascade.
- (ii) On delete No Action.

→ must be PK of other relation.

→ FK always guarantees the parent-child relationship.

According to referential integrity / parent-child relationship, a value is allowed in the foreign key column of the child Table only if it has a reference to one of the values of the Primary Key column of the Parent Table.

• It is not vice-versa.



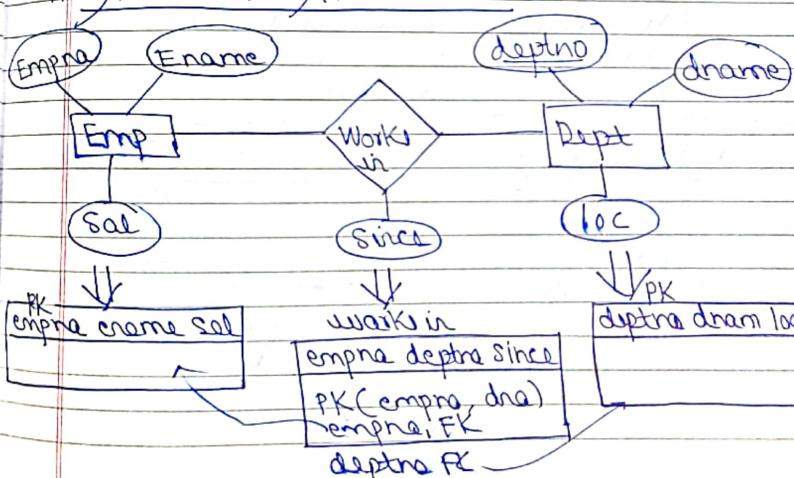
(ii) On Delete Cascade

If the FK is defined with this option, then in case if the PK value gets deleted then By default all the referencing FK values of the child table also are allowed to be deleted for validating the referential integrity.

(iii) On Delete No Action

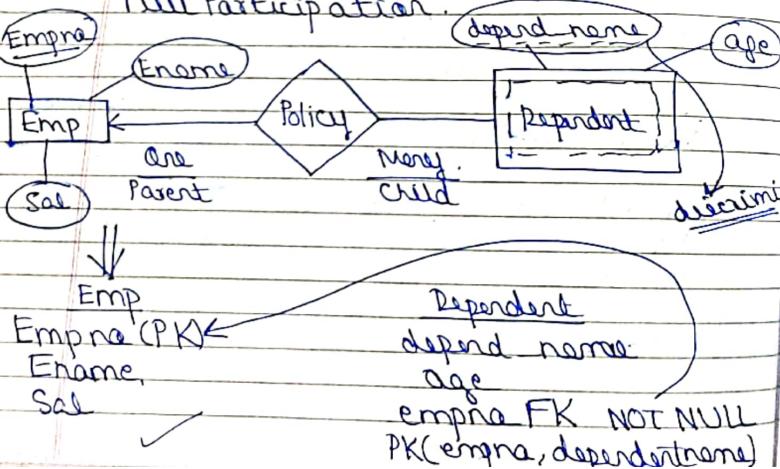
If the FK is defined with this option, then user has to manually perform update operation on the FK's value & ensure there are no references to the PK value that is going to get deleted.

* BASIC ER DIAGRAMS



* Weak Entities

- The entities which doesn't have any PK is called weak entity.
- weak entities always involves in a relationship with other strong entities for identifying the rows inside weak entity.
- The column / list of columns of weak entity that gets combined with primary key of the strong entity for the identification of rows is called discriminator.
- Discriminators are represented with underlying attributes with a dashed line.
- weak entities could only involve in the relationship with other strong entities in Full Participation.



classmate
Date _____
Page 114

GATE Q.S

GATE 2006.

These exists relation R, with A & C attributes.

$A \rightarrow PK$

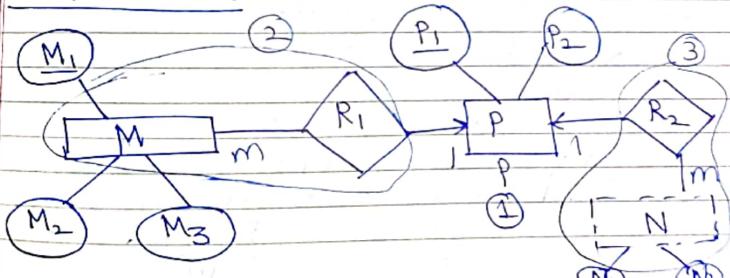
$C \rightarrow FK$ that references A with an delete cascade property.

If tuple (2, 4) gets deleted, which other tuples should also get deleted as per referential integrity.

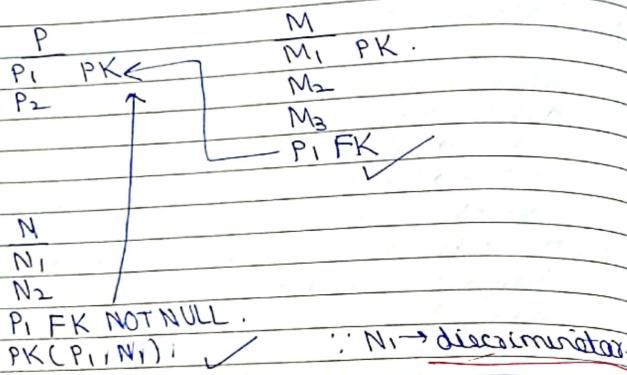
PK A	C	FK
2	4	or delete cascade
3	4	
4	3	
5	2	
6	4	
7	2	
9	5	

(d) $\{(5, 2), (7, 2), (9, 5)\}$ also gets deleted.

GATE - 2008

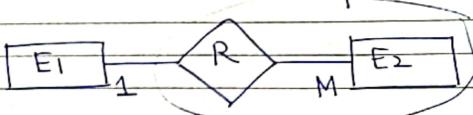


⇒ 3 Tables minimum.



✓ Gate 2004

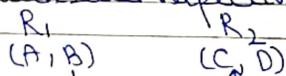
There exists ER diag given below along with cardinalities represented.



∴ 2 min tables ✓

✓ R₁(A, B); R₂(C, D) Gate 2012

There exists relations R₁ & R₂ with (A, B) & (C, D) attributes respectively. Let us



assume A and C are the PK in those relations and B is the FK that references to C in R₂. In case if all the data satisfies the referential integrity concept then which of the following statements always

a) $\Pi_C(R_2) = \Pi_B(R_1)$

b) $\Pi_C(R_2) = \Pi_B(R_1) = \emptyset$

c) $\Pi_B(R_1) - \Pi_C(R_2) = \emptyset$ in R₁, but not in R₂

d) None

B can't have any values which are not there in C. ✓

✓ Gate 2012

There exists a table T with (X, Y) attrib. A row got inserted into the table with the values (X=1, Y=1).

Let MX, MY denote the highest value of X & Y at any given point in time.

New rows are inserted into the table with the values:

$$X = MX + 1$$

$$Y = MY + 1$$

Then find out the result of the query?

$X \times Y$
 (1, 1)
 (2, 3)
 (3, 7)
 (4, 15)
 (5, 31)
 (6, 63)
 (7, 127)

$$2^{n-1}$$

$$Y = 2^X - 1$$

\checkmark There exists train reservation system as
 follows: [Gate 2010]

Passenger			Reservation		
Pid	Name	Age	Pid	Class	Tid
0	Sachin	65	0	AC	8200
1	Rahul	66	-1	AC	8201
2	Saurav	67	X2	SC	8203
3	Anil	69	3	AC	8204
			5	AC	8206
			X1	SC	8202

\checkmark Select R.Pid
 from Reservation
 where class='AC'
 and

\checkmark exits (Select *
 from Passenger P.
 where Age > 65
 and
 P.pid = R.pid).

(d) (1, 3)

Gate 2005

There exists a relation Book with (Title, Price) tuple.

Let us assume the relation has info of atleast 6 books.

The title & price in the table are supposed to be unique.
 what will be the c/p of query?

Select B.Title

from Book as B

where (Select count(*)

from Book as T

where T.price > B.price) < 5.

Soln:

B		T	
Book		Book	
Title	Price	Title	Price
A	500	A	500
B	450	B	450
C	400	C	400
D	150	D	150
E	100	E	100
F	200	F	200
G	250	G	250
H	300	H	300

\Rightarrow 5 Most expensive BOOKS ✓

Ques Date-2011

Loan-Records table Given below:

Borrower	Bank-Mgr	Loan-Amount
Ramesh	Sunder	10,000
Suresh	Ramgopal	5000
Mahesh	Sunder	7000

Select Count (*)

From ((Select Borrower, Bank Mgr
from Loan Records) AS S

NATURAL JOIN

(Select Bank Mgr, Loan_Amt
from Loan Records) AS T.

S	T
R	Sunder
S	Ramgopal
Mahesh	Sunder

S	T
Ram	Sunder
Suresh	Ramgopal
Mahesh	Sunder

\Rightarrow 5 Rows ✓

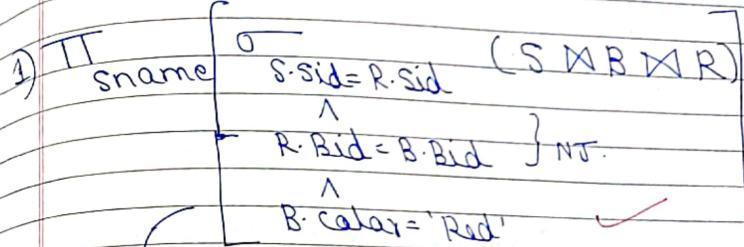
CLASSEmate
Date _____
Page 120

CLASSEmate
Date _____
Page 121

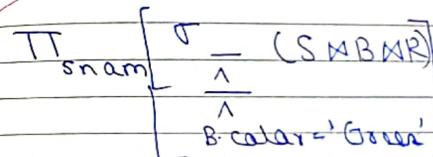
(S) Sailors (Sid, Sname, age, Grade)

(B) Boats (Bid, Bname, color)

(R) Reserves (Sid, Bid, day)



distinct Sailor Names who reserved at least one red color boat,



ij: (i) when : distinct Sailor names who reserved at least one red boat or atleast one green

(ii) Intersection: at least one red & atleast one Green ✓

(iii) difference: atleast one red colour but didn't receive atleast one green.

$$\exists \{ \Pi_{\text{sid}, \text{Bid}} (\text{R}) = \Pi_{\text{Bid}} (\text{Ecolor} = \text{'Red'}) \}$$

$\text{Bid} \subseteq (\text{sid}, \text{Bid})$

$$\Pi_{\text{sid}} [\sigma_{\text{temp}} (\text{s} \bowtie \text{temp})]$$

$\text{s.sid} = \text{temp.sid}$

→ distinct seller, name who have received all red colour
Books. ✓

GATE 2003

These exists relations as given below in the DataBase

S - Students (rollno, name, do_b)
 C - Courses (course, coursename, Instructor)
 G - Grades (rollno, courseno, Grade)

From S, C, G

Date _____
 Page 122

select distinct s.name
from S, C, G

Date _____
 Page 123

where S.rollno = G.rollno
and
G.courseno = C.courseno
and
C.Instructor = 'Karth'
and
G.grade = 'A' .

→ District Student name who get grade A in atleast one of the courses instructed by Karth . ✓

RA

$$\Pi_{\text{s.name}} [\sigma_{\text{(S} \bowtie \text{C} \bowtie \text{G)}} (\text{s.rollno} = \text{G.rollno})]$$

$\text{G.courseno} = \text{C.courseno}$

$\text{C.Instructor} = \text{'Karth'}$

$\text{G.grade} = \text{'A'}$ ✓

TC

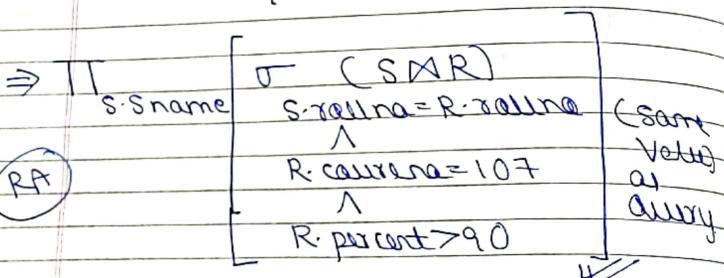
$$\{ t \mid \exists \text{S} \in \text{Students} \wedge \exists \text{C} \in \text{Courses} \wedge \exists \text{G} \in \text{Grades} .$$

eliminate
dups
values

$$(\sigma_{\text{s.rollno} = \text{G.rollno}} \wedge \sigma_{\text{G.courseno} = \text{C.courseno}} \wedge \sigma_{\text{C.instructor} = \text{'Karth'}} \wedge \sigma_{\text{G.grade} = \text{'A'}} \wedge \sigma_{\text{t.name} = \text{s.name}})$$

Gate 2013

S Students (rollno, Sname)
 C courses (CourseNo, Cname)
 R Registration (rollno, CourseNo, percent)
 Select S where distinct
 from S, R
 where S.rollno = R.rollno
 and
 R.CourseNo = 107
 and
 R.percent > 90



RA

TC

$\{ t \mid \exists S \in \text{Students}$
 $\exists R \in \text{Registration}$
 $S.rollno = R.rollno$
 $R.courseNo = 107$
 $R.percent > 90$
 $\} \quad t.sname = S.sname \leftarrow$

classmate
Date _____
Page 124

Gate 2001

$R(A, B, C, D, E)$

$\{$
 $A \rightarrow B$
 $BC \rightarrow E$ OCD.
 $ED \rightarrow A$ P.D.

}

$A^+ = \{A, B\}$

$BC^+ = \{B, C, E\}$

$ED^+ = \{E, D, A, B\}$

$\exists [EDC, BCD, ECD]$

NF

3

✓

$R(L, M, N, O, P)$

$M \rightarrow O$ OCD.

$NO \rightarrow P$ FD.

$P \rightarrow L$ FD.

$L \rightarrow MN$ FD

}

$M^+ = \{M, O\}$

$NO^+ = \{N, O, P, LM, MN\}$

$(P)^+ = \{P, L, M, N\}$

$(L)^+ = \{L, M, N, O, P\}$

$[NO] \rightarrow CK$

$\text{CK } \{L, P\}$

$\text{NF } \{L, P\}$

NO

\uparrow
NM

$\leftarrow L \leftarrow P$

$3NF$

Gate 2003

$R(A, B)$

$\overline{\text{BCNF}}$
 $\{ A \rightarrow B \text{ FD}$

$\} \quad \{ B \rightarrow A \text{ FD}$

$\overline{\text{BCNF}}$

$R(A, B)$

$\overline{\text{BCNF}}$
 $\{ A \rightarrow B \text{ FD}$

$\overline{\text{BCNF}}$

$\{A, B\}$

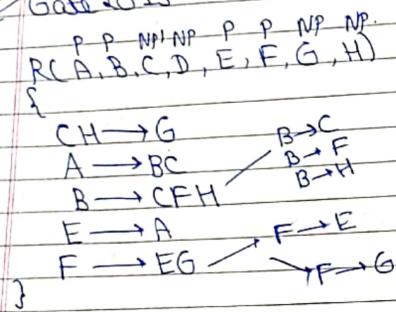
$\{A, B\}$

$\overline{\text{BCNF}}$

</

NOTE: Binary Relations would always exist in BCNF.

Gate 2013



$$(CH)^+ = \{C, H, G\}$$

$$(A)^+ = \{A, B, C, F, H, E, G\}$$

$$(B)^+ = \{B, C, F, H, E, G, A\}$$

$\{A, B, E, F,$

$\{AD, BD, ED, FD\} \rightarrow CKS.$

1NF

$R(N, R, C, T, Z)$

$\{$
 $N \rightarrow RCT$ FD.
 $RCT \rightarrow Z$ TD.
 $Z \rightarrow CT$ TD

$$RCT^+ = \{R, C, T, Z\}$$

$$\begin{aligned} N^+ &= \{N, R, C, T, Z\} \\ Z^+ &= \{Z, C, T\} \end{aligned}$$

$(N) \rightarrow CK.$

$\boxed{2NF}$

$R(V, W, X, Y, Z)$

$\{$
 $VY \rightarrow W$
 $WX \rightarrow Z$
 $ZY \rightarrow V$

$$\begin{aligned} VY^+ &= \{V, Y, W\} \\ WX^+ &= \{W, X, Z\} \\ ZY^+ &= \{V, Z, Y\} \end{aligned}$$

$\{WXY \rightarrow W, X \rightarrow V, W, X, Y, Z, V\}$

$\{WZY \rightarrow X, XZY, WXY, VYX\}$

$\{VYX = \{V, Y, X, W, Z\}\}$

$\boxed{3NF}$

~~$R(A, B, C, D, E, F, G)$~~

$\{$
 $A \rightarrow B$
 $BC \rightarrow DE$
 $AEF \rightarrow G$

$A^+ = \{A, B\}$
 $BC^+ = \{B, C, D, E\}$
 $AEF^+ = \{A, E, F, G, B\}$
 $AEFC^+ = \{A, E, F, G, B, C, D, G\}$

1) Candidate Key for relation R is: (ACF)

$$(ACF)^+ = \{A, C, F, B, D, E, G\}$$

$\Rightarrow ACF.$

\checkmark
 $AEFC$
 $ABCF$

2) a) INF.

~~R(A,B,C,D)~~

$AB \rightarrow CD$

$B \rightarrow A$

$C \rightarrow B$

$C \rightarrow D$

INF

BCNF

{AB, B}

TD

CK

{B, C}

~~R(A,B,C,D,E,F)~~

$AB \rightarrow CDEF$ FD.

$C \rightarrow B$

$D \rightarrow C$

$E \rightarrow D$

$F \rightarrow E$

} OCF.

$C^+ = \{C, B\}$.

$D^+ = \{D, C, B\}$

$\Rightarrow \{AB, AC, AD, AE, AF\}$.

3NF

19.

14.

CLASSMATE
Date _____
Page 128

R(A,B,CD)

$AB \rightarrow CD$

$C \rightarrow A$

$D \rightarrow B$

$AB \}$
 $CB \}$
 $CD \}$
 $AD \}$
CK.

$\Rightarrow 3NF = \text{Highest NF}$

* B+ TREES

We use B+ tree for organizing the data in the DataBase because:

1. B+ trees are balanced.
2. They exhibit Binary Search tree property.
3. In B+ Trees, data of the indexed column would be organized at the non-leaf level and the actual rows of the table would be organized at the leaf level.
4. The above feature makes B+tree as the best fit for the range based query execution and also the optimal resource utilization.

* ORDER / DEGREE OF B+ TREE

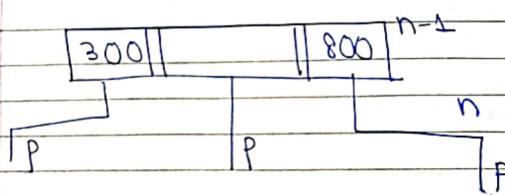
NOTE: The total no. of index/ tree pointers that could be available for a B+ tree node.

→ If we assume 'n' is the order/degree of B+ tree then each B+ tree node is expected to have:
 $(n-1)$ no. of index Key Values

→ Let us assume:
Each index / tree pointer consume p
no. of bytes and the index key value
consumes K bytes then the following
expression should be valid:

$$n * p + (n-1) * k \leq B$$

Block Size of the File



classmate
Date _____
Page 130

SQL GATE Qs

① Gate 98 - Cell

FREQUENTS A
SERVES B
LIKES C.

Write the story

Q. Gate 99

- a) SQL query cont autom. eliminate duplicates.
 - b)
 - index is maintained at physical level.
 - index used in query optimizn, not SQL.
 - SQL → logical level.
 - c) 2 attributes with same name not allowed in SQL.

Q3 Select ^{district} w,x from r,s.

r		s		Carte Product			
w	x	y	z	w	x	y	z
a	b			a	b	1	2
c	d	3	4	a	b	3	4
				c	d	1	2

$\begin{matrix} & \downarrow \\ a & b \\ c & d \end{matrix}$

but if, $w \neq$
 $a \neq b$ → result remains different
 $c \neq d$
 $a \neq b$

If S is empty, CP no C/P.

↳ same R not possible.

→ σ has no duplicates & S is non-empty

Gate 2003

equivalent RA expression.
 → CP of all the tables.

a) $\prod_{a_1, a_2, \dots, a_n} \sigma_p (r_1, r_2, \dots, r_m)$.

b) Join condition is used.

Gate 2011 → 5 tuples (Repeated Q)

Gate 2012

Needed query → Not correlated query.

execute internal query
 once, place it & execute
 the outside query.

→ check row by row in outside table.

CLASSmate
 Date _____
 Page _____

CLASSmate
 Date 133
 Page _____

Nothing will be returned. . . 3 ✓

Gate 2014

employees
 departments

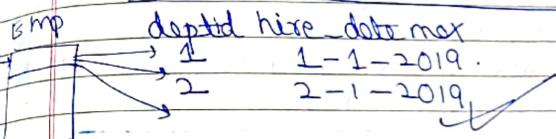
only for some departments

[IN → pairwise comparison allowed]

→ execute inner query first (non-correlated).

emp_id + name ... sal deptid dname ... lid

(1)	(2)	(3)	(4)	0
1700	1700					



Gate 2014

→ tuple attribute.
 Select * from R where a IN (Select s.a
 from s)

duplicate allowed.

	R	S	S1
X → 1	a	2	a 2
X → 1		2	5
✓ → 2		5	9
✓ → 2		5	4
X → 3		9	2
✓ → 4		4	2

(2, 5, 9, 4)

d/p	RS
2	2 2
2	2 2
4	2 2
{2, 2, 2, 4}	2 2
b) {2, 4}	2 2
c) {2, 2, 4}	2 2
d) X	4 4

Select R.* from R, S, where R.a = S.a and
 vii where R.X.
 "where is used while creating table/
 in select query" ✓

Gate 2005

Nested correlated query

→ Take eg always terms SQL query
 ↴ 6 books ✓

Back (B)		T	P
a	1	a	1
b	2	b	2
c	3	c	3
d	4	d	4
e	5	e	5
f	6	f	6

classmate
 Date _____
 Page _____
 135

all rows are
 copied with
 the current
 row ✓

(d) five most expensive books. ✓

Gate 2003

CP in a meaningful way.

(c) atleast one of the courses taught by
 Keerti & sat A' grade ✓

Gate 2004

group by department.

display only names, whose average salary

Not correlated query

avg of all salary in company
 ↴ 100

having → filter out groups

(d) The avg salary of male employees is more than
 avg salary in company. ✓

Q4) Gate 2006

(Student, course) \rightarrow PK in Enrolled
Student. PK in Paid

(Q4) For every row in 'Paid', we need to execute
the inner query once

Consider Duplicates

Correlated Sub
Query.

Enrolled		Paid	
Student	Course	Student	Amount
a	1	\rightarrow a	10
a	2	b	11
b	1	c	12
b	2		
c	1		
c	2		

(Q1) {a, a, b, b, c, c} \because non-correlated query.

(Q2) {a, b, c} \because inner query = aabbcc.

(Q3) {a, a, b, b, c, c}

x/s

(Q4) Correlated inner query

a

(a, 10) \rightarrow

b

for (b, 11), \rightarrow entire query is
executed

c

b	1
b	2

classmate
Date _____
Page 136

exists: there exist atleast one raw / not.

(C, 12) \rightarrow

\rightarrow All compute intersection b/w 2 sets.

a) identical raw sets. ~~✓~~ (no duplicates)

b) X

c) X [Q3 \rightarrow more rows than Q2].

d) X no FK, no integrity violation ~~✓~~

Q5) Gate 2007

Salary greater than all employees in dep 5

e	empid	name	dep	sal	s.
e	1	x	-	5	105
	2	x	-	2	206
	3	x	-	5	300
	4	v	-	2	400
	5	v	-	2	500

NOT exists \rightarrow when inner query returns nothing
e. empid will be printed.

1) O/P = {4, 5}

2)

e	S				
empid	Sal	dept	empid	Sal	dept
→ 1	100	5X	1	100	5.
→ 2	200	2	2	200	2
3	300	5	3	300	5.
4	400	2	4	400	2
5	500	2	5	500	2

Q1 ✓

Q2 {2, 3, 4, 5} X [Replace inner query with 100, 300].
Non-correlated Subquery ✓

Select operation in SQL.

Projection oper in RA except that SQL retains duplicates. ✓

Gate 2014

employee (empid, ename, dept). 1

customer

every seller.empid must be empid.

correlated Subquery

employee			customer			
cid	ename	dept	cust_id	Name	sal	dept
→ 1	a	X	4	1	good	(2)
2			5	2	bad	
3			6	3	avg	
			7	4	so so	
			8	5	awful	

(1)

(d) all customers having a good Rating ✓

Gate 2016 Q6.

Add of theater with max capacity

venue P1

Add capacity	
a	100
b	200
c	300
d	400

P2

Addr.	Capacity
a	100
b	200
c	300
d	400

(a) d

⇒ Non-correlated query

(b)

{100, 200, 300, 400}

(c)

x a) 300 i.e. d
x b) {b, c, d}

c) > 400 ⇒ No tuple

d) > 400 ⇒ No tuple

Gate 2016

Imp Q

'with' → naming SQL

tatel

name	capacity
Ajmer	20
Bikaner	40
Churu	30
Dungarpur	10

total - avg

capacity
25

{Bikaner, Churu}

* Gate 2012

P. Having clause should be applied only with Group-by clause.
↳ need to filter groups.

→ All attributes must appear in Select clause
↳ if in Group-by, we put in Aggregate functn ✓

* RELATIONAL ALGEBRA GATE Qs

Gate 98 Q

assume LHS is right

$$\checkmark a) \sigma_{C_1}(\sigma_{C_2}(R_1)) \rightarrow \sigma_{C_2}(\sigma_{C_1}(R_1))$$

Selection is commutative.

$$\checkmark b) \sigma_{C_1}(\Pi_{A_1}(R_1)) \rightarrow \Pi_{A_1}(\sigma_{C_1}(R_1))$$

$$\checkmark c) \sigma_{C_1}(R_1 \cup R_2) \rightarrow$$

	R ₁	R ₂	R ₁ ∪ R ₂
A	A ₁ A ₂	A ₁ A ₂	A ₁ A ₂
	✓	✓	✓
			✓

x d)

$$\Pi_{A_1}(\sigma_{C_1}(R_1)) \rightarrow \sigma_{C_1}(\Pi_{A_1}(R_1))$$

R₁

	A ₁	A ₂	A ₃
✓			

	A ₁	A ₂	A ₃
✓			

↳ Selection is applied.

Assumption: LHS is true. ✓

R ⋈ S.

↳ join condition [CP + selection].

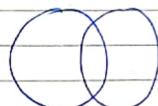
$$\checkmark \{ t \mid t[A] \wedge t[B] = 20 \} \quad \text{Gate 99}$$

A	B
10	20

x a) {10, 20}

x b) $\sigma_{(A=10)}(t) \cup \sigma_{(B=20)}(t)$

$$\checkmark c) \sigma_{(A=10)}(t) \wedge \sigma_{(B=20)}(t)$$



Gate 2000
using RA operations.

- a) ✓
 - b) apply join again ✓
 - c) Sum of all
- Agg function can be done using RA

Gate 2002

RA has same power as SQL

using join need to infinite loop in RC.

Gate 2004

Student (name, sex, marks)

[P → revenue]

(Imp)

(≤m)

Student

<u>name</u>	sex	marks	<u>non</u>	x	m
a	M	10	a	M	10
b	M	20	b	M	20
c	M	30	c	M	30
d	f	25	d	f	25
e	f	15	e	f	15
f	f	40	f	f	40

2nd half query:

name	sex	marks	n	x	m
d			25	C	M
e			15	b	M
c			15	C	M

$$(def) - (d, e) = f$$

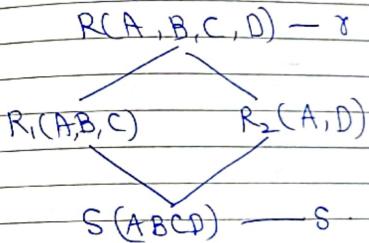
[a, b, c] ✓

name of girls with marks lesser than atleast 1 male

[Train]

Gate 2005

II question:



A	B	C	D
1	b ₁	c ₁	a ₁
1	b ₂	c ₂	a ₂
2	b ₃	c ₃	a ₃
2	b ₄	c ₄	a ₄

A	B	C
1	b ₁	c ₁
1	b ₂	c ₂
2	b ₃	c ₃
2	b ₄	c ₄

A	D
1	d ₁
1	d ₂
2	d ₃
2	d ₄

A B C D
 1 b₁ c₁ d₁
 1 b₁ c₁ d₂
 1 b₂ c₂ d₁
 1 b₂ c₂ d₂

If common attribute 'a' is not a PK,
 we get Spurious tuples.

r CS → more tuples. ✗

Gate IT 2006

r₁ → 2000T. (P, Q, R)

r₂ → 2500T. (R, S, T)

The max size of natural join.

[not FK]

r ₁			r ₂		
P	Q	R	R	S	T
1			1		
2			2		
2			3		
3			4		
3			5		
4					

unique.

✗

every tuple will match with
 r₂ R atmost 1.

max = 2000

minValue = 0 (if none matches).



Gate 2007

studentinfo (studid, name, sex).

(All female id paired with all course id.)

eg

studid	sex
1	M
2	M
3	F
4	F
5	F

era	sid	cid
3	C ₁	{C ₁ , G, G ₁ }
4	C ₁	
5	C ₁	
3	C ₂	
4	C ₃	
1	C ₁	
1	C ₂	
1	C ₃	

✓

3

4

5

C₁

C₂

C₃

Final

{3 not taken}

sid cid

3 C₁

3 C₂

3 C₃

4 C₁

4 C₂

4 C₃

5 C₁

5 C₂

5 C₃

if a girl
has taken

[C₂, C₃] ↗

[if atleast one girl has
not registered].

Gate 2008

* → NT

R(P, Q, R₁, R₂, R₃)
S(P, Q, S₁, S₂)

eg

R			S		
P	Q	R ₁ R ₂ R ₃	P	Q	S ₁ S ₂
1	2	- - -	1	2	- -
2	3	- - -	2	1	- -

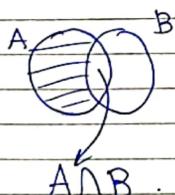
a) $\{1, 2\} * \{1, 2\} \rightarrow \{1\}$

b) $\{1, 2\} * \{1, 2\} \rightarrow \{1\}$

c) $P Q \rightarrow \{1\}$

d) $A - (A - B)$

III & IV are same.



Gate 2012 on RA

(A ∪ B) ~~Ans~~ C
A.id > 40 V c.id < 15

A ∪ B

ID Name Age

12	Arun	60
15	Shreya	24
99	Rohit	11
25	Hari	40
98	Rohit	20

C ID Phne

10	2200
99	2100

7 tuples

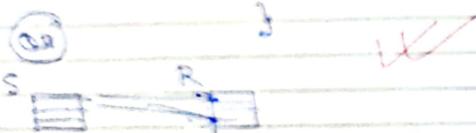
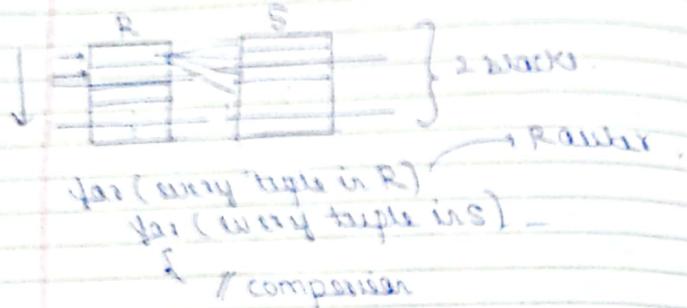
Take up or else you will get 9.

Aid cid

12	10
15	10
99	10
25	10
98	10
12	99
15	99
99	99
25	99
98	99

Gate 2014

R & S using nested loop method.



for every t in S)
 for every t in R),

).

R S disk blocks might vary,

* R S Blocks in S = 100.
Blocks in R = 20 T = 1000.
R = 200. E:

→ No of records in block = 100

for each tuple in R, move all blocks of S
200 * 100.

[20 + 200 * 100] - Total disk mov.
New worse:
→ 2020



100 + (1000 * 20) = 20100.
for each tuple in S

[for every record, 1 block has to be moved]

∴ $\tau(R)$ should be in outer loop for better performance.

Join Selection factor - o/p tuples out of original tuples

✓

Scanned with CamScanner

Q) Gate 2014

(eg)

dependent			emp		
deptId	depName	empId	empName	age	
10	1	1		20	
15	1	2		30	
20	2	3		40	
40	2	4		50	
45	3				
46	3				
50	4				
51	4				

Join all employees with his dependent
where age of dept is less than him

empId

2 20 1 20.
3 20 1 15.

40 2 2 30
45 3

of
(b)

∴ O/p = 1 [Age greater than all its
dependents] ✗

IT
empId (employee ⋈ dependent)
(empId = e.id) ∧ (empAge <
deptAge). a
empId whose age is less than
at least one of its dependents. ✓

Q) Full Natural Join = NJ + FOJ

R1.

A	B
1	5
3	7

R2

A	C
1	7
4	9

A	B	C
1	5	7
3	7	N
4	N	9

(c). e,f,g but
not a,b.

Q) Gate 2007

{e.name | employee(e)}

Λ

(+n ...)

e / n [using
employee
table]

Vn(p → q)

(employee(n) Λ n.supervisorN = e.name)
→ n.sex = 'm' ✓

e

name	sex	supervN
a	m	a
a	f	b
b	f	a

name	sex	Sup.Na
a	m	a
a	m	b
a	m	a
b	X F	a

∴ p is false.

All the names of employees who have more subordinates. ✓

Q Gate 2006 ✓

Q Gate 2008

$$\forall t \in r(p(t))$$

✓ 1. X

X 2.

✓ 3. $\forall t \in r(p(t))$ ✓

4. $\exists t \in r(p(t))$

✓ 2. $\exists t \in r(\neg p(t))$ X ✓

* Unsafe Relational Calculus

a) $\exists t$ ✓ safe.

then doesn't exist.

c) $\{t \mid \neg(t \in R)\}$ ✓

classmate
Date _____
Page _____

classmate
Date _____
Page 153

* Safe & Unsafe Query

$\{s \mid s \notin S\}$ → unsafe query. ✓

* Domain of Query:

→ All tables used in query.

∴ Domain = $S \cup R_1 \cup R_2$. ✓

2. $\{t \mid \exists s \in S \text{ such that } \exists r \in R \text{ such that } t[sid] = s.sid \wedge t[rid] = r.bid \wedge t[pid] = s.pid \wedge t[pid] = r.bid \wedge t[pid] = s.pid \wedge t[pid] = r.bid\}$ 007
 ∵ R.sid = s.sid \wedge R.bid = s.pid \wedge T.name = s.name.

∴ Domain = S, R. ✓

O/p ⊂ Domain of tables ✓ ∴ Safe. ✓

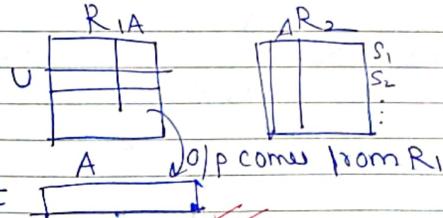
3. $\{t \mid \exists u \in R_1(t[A] = u[A]) \wedge$

$\exists s \in R_2(t[A] = s[A])\}$

↓
 (there exist no s belong to R₂
 such that t[A] = s[A])

$\{t \mid \exists u \in R_1(t[A] = u[A]) \wedge$

$\forall s \notin R_2(t[A] \neq s[A])\}$



- Q $\forall t \exists x (P(t))$ ✓
1. $\forall t \exists c x (P(t))$. X
↳ No student pass physics exam.
2. $\exists t \forall x (P(t))$.
↳ There is a person not a student, but passed phy. ✗
- ✓ 3. $\forall t \exists c x (\neg P(t))$.
↳ There is no student who failed phy exam. ✗ ✗

* TRANSACTION MANAGEMENT

Gate 2012

- concurrent execution
 - ↳ intended only in conflict
- | | |
|--------------------------------------|--------------------------------------|
| T_1 | T_2 |
| read(p) | read(q) |
| read(q) | read(p) |
| $\text{if } p=0 \text{ then } q=0+1$ | $\text{if } q=0 \text{ then } p=p+1$ |
| write(q) | write(p) |

Any non-serial interleaving of T_1 & T_2 has concurrent access leads to $\therefore T_1 \rightarrow T_2 / T_2 \rightarrow T_1$ (not possible).



T_1 : read(p)
 T_2 : read(q)
 T_2 : write(p)
 T_1 : write(q)

T_1 : read(p)
 T_2 : read(q)
 T_1 : write(q)
 T_2 : write(p)

T_2 : read(q)
 T_1 : read(p)
 T_1 : write(q)
 T_2 : write(p)

T_2 : read(q)
 T_1 : read(p)
 T_2 : write(p)
 T_1 : write(q)

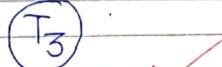
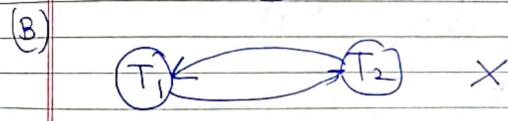
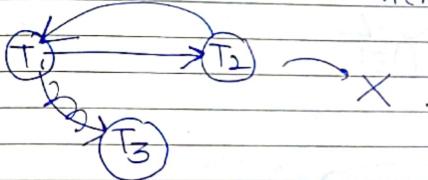
T_1 : read(p)
 T_2 : read(q)
 T_1 : write(q)
 T_2 : write(p)

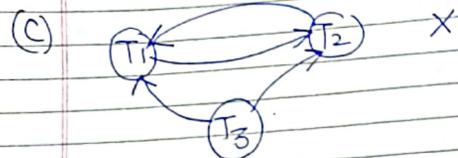
T_2 : read(q)
 T_1 : read(p)
 T_2 : write(p)
 T_1 : write(q)

Nothing is conflict serializable. (B) ✗

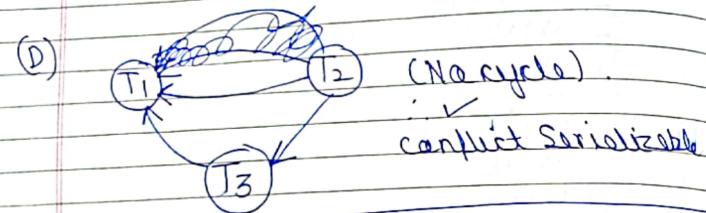
Gate 2014

$r_i(x), w_i(x)$

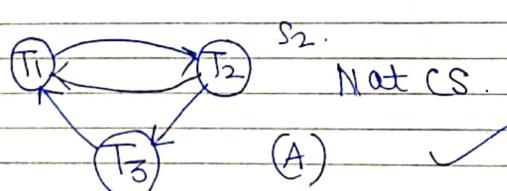
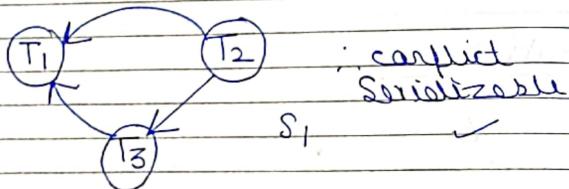




classmate
Date _____
Page _____



Q Gate 14 Q.



Q Gate 2014 Q

classmate
Date 157
Page _____

recoverable:
see the reds.

T1 T2 T3 T4
 $r(x)$

$w(x)_{T_4}$
commit

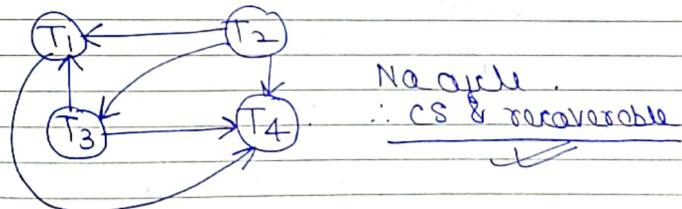
$w(y)_{T_4}$
commit

$w(y)_{T_4}$
 $r(z)$
commit

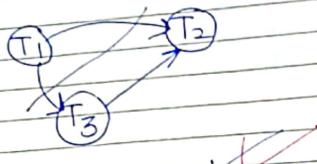
$r(x)$
 $r(y)$

→ after write, we immediately
commit, ∵ consider the
[no dirty read].

$w(x)_{T_1}$ → $r(x)_{T_2}$
(commits b4. T_1).



Q) Gate A on CS Schedule



(A) T₁ T₃ T₂

Q) Gate 2016

$a_i \rightarrow$ abort by T_i .

↳ if due to some problem, user of resources, rollback all changes.

[don't commit] ~~✓~~

T ₁	T ₂
$r(x)$	$r(y)$
$w(x)$	$r(y) \rightarrow$ need directly from DB.
$r(y)$	
Abort	$w(y)$

abort:

• recoverable \rightarrow write/read.

[No dirty read here] ~~✓~~

recoverable & consistent

S does not have a cascading chart.

strict ~~✓~~

T₂ writes data b4 + 1 commits.

Q) Gate 2015

T₁

read (x)

$$x = x - 50$$

write (x)

\therefore (B) consistency.

T₂

$r(y)$

$$y = y + 50$$

$w(y)$

Q) Strict 2 Phase Lock

a) not strict

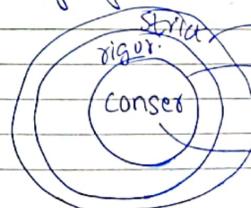
b) strict

c) strict

↳ unlocking before commit

↳ exclusive locks are unlocked after commit. ~~✓~~

- Every rigorous is strict.



↳ release only exclusive locks after commit.

↳ release SL after commit

↳ release all locks after commit

FILE STRUCTURES - Prev Years.

- Refer 6.16 from database Prev 6 ip.
- B+ Tree is preferred to BST, since data transfer from disk is in BLOCKS. [& B+ tree can hold large count of keys in a block/node].
- B Tree Q. \rightarrow 6.5
- B+ Tree Insertion \rightarrow 6.12, 6.13.
- 6.15 Secondary index

* View Serializability

A Serial Schedule 'S' & non-serial schedule 'S' need to be serial, view equivalent if:

- same trans. performing initial read in both. (for every data variable)

e.g.: $T_1 \ T_2 \ T_3$.

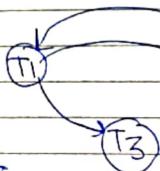
$R(A)$

$W(A)$

$W(A)$.

View serializable?

CS



: T1st VS

e.g.: $T_1 \ T_2$

$R(A)$

$W(A)$

T_2

(Not CS).

∴ 1 blind write.
(1st for VS).



: Nat VS ∵ cycle.

e.g.: $T_1 \ T_2$

$R(A)$

$W(A)$

T_2

CS ✓

∴ obviously VS

$R(B)$

$W(B)$

$R(B)$

$W(B)$.

Date _____
Page _____ 160

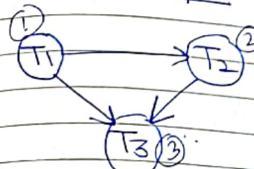
classmate
Date _____
Page _____

$W_2(A)$

Blind write: writing before reading.
[If no Blind write, & not CS,
it's VS].

Here, we can't comment.

Draw Polygraph:



initial read: T_1
blind write: T_3 .

∴ VS ✓ [T_1, T_2, T_3]
(due to the
cycle of WR dep?).

T_1

T_2

T_3

3

2

1

4

5

6

7

8

9

10

11

12

13

14

15

16

17

18

19

20

21

22

23

24

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240

* Polygraph Example:

$$S = T_1(A) W_2(A) T_3(A) W_1(A) W_3(A)$$

$T_1 \quad T_2 \quad T_3$

$\gamma(A)$ $(W(A))$ $\gamma(A)$

$W(A)$

Init read: T_1 ,
Init write: T_3

$T_1 \quad T_2 \quad T_3$

serial
schedule.
[view 4:
1st thru].

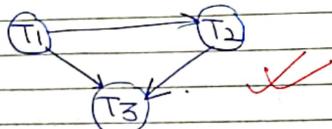
$T_1 \rightarrow T_2 \rightarrow X$

(T_3)

∴ Blind write. (Not check 1st)

CS

VS



$$\text{eg1 } S = T_1: \gamma(X), T_2 = W(Y), T_3 = W(X)$$

~~Temp.~~

$T_1 \quad T_2$

$R(X)$
 $W(X)$

commit

→ blind write.

abort → abort.

[no cascading
abort].

→ delete T_1 .

∴ [If 1 transaction → CS & VS both]

T_1	T_2	T_3
$R(X)$		
$W(X)$	$R(Y)$	
	$R(Y)$	
	$W(Y)$	
		$R(Y)$

~~init read: T_1~~
~~init write: T_1~~

~~①~~

init read: T_2

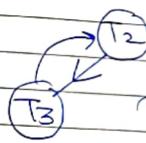
~~②~~

WR conflict
 $T_3 \rightarrow T_2$

Not CS (loop b/w T_3 & T_2)

→ Blind repeating write: $W_3(Y)$; check for VS.

(T_1)



~~init read: T_1~~

~~③~~

Not VS

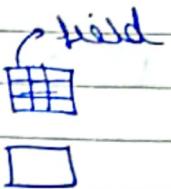
T_3 after T_2 definitely.

(T_1 can be anywhere, doesn't matter)

can set only serial
Schedule which is VE
to given Schedule.

FILE ORGANIZATION

DB: collection of data (colln of files)

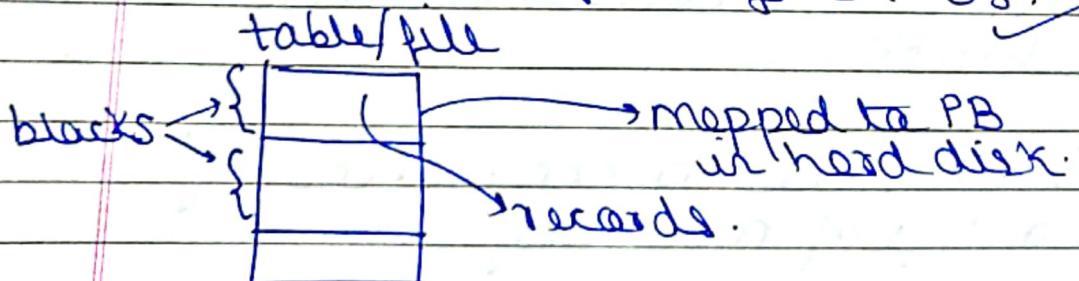


file
|
record
|
field

→ in OS: we want to access file from begin to end.

in dbms: we need 1 particular record.

∴ File org of dbms is diff from file system - OS.



Avg no. of records per block = Blocking Factor.

1024 B

4 B

→ record size.

- Strategies for storing file of records into blocks.

1) Spanned Strategy

R₄ → not stored completely.
B₁ fully utilized.

To access R₄ → 2 blocks accessed.
[B₁ & B₂].

- If VarSize records, use this.

eg: pure content → varsize.

but employee table: unspaced

2) Unspanned Strategy

No record can be stored in more than 1 block.

- No. of block access to acc. a record.

- But, wastage of memory.

Suitable for fixed length record.

* Organization of records in file

for storing data in HD, order must.

1) Ordered file organization

emp

SSN
1
2
3
⋮
7

records are ordered based on a field (SSN)
if Emp T → 100B.

100X10

records.

B-1	B-2	B-3	⋮	B-100
1-10	11-20	21-30	⋮	991-1000

Record no 25. → apply BS (Bin Search)

- if search based on key on which ordering is done → efficient.

Insertion is expensive

if 22 record put up, lot of move

2) unordered

All records in file are inserted wherever the place is available at the end of file.
Search: LS. (Search every Block).
Search is inefficient.

* Intra-Indexing

- Size of each record big.
- BS → $\log_2 1000 \rightarrow 10$ searches / block access
 ↴ To access a record.
 ∵ ordered based on Key

Maintain index

index file small.
[Key, Block Pointer]

Value divided in blocks (8).

$$\therefore \log_2 8 = 3 \text{ block access}$$

$$\therefore \log_2 8 + 1 \Rightarrow 4$$

If file is unordered, index file can be ordered.
But if sorted,
(1 index record per a block)

* Structure of index files

[Key | Block Pointer]

{ Block Add where
Key is available.

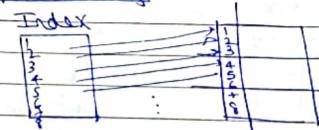
1100 | 200

Block 1
200 1111

- Index = ordered file.
- Searching: BS.
- To access a record using index
avg no. of block access
 $\log_2 Bi + 1$
↳ data block access.
- Index block access.
- Index can be created on any field of relation; ordered / unordered file.
[PK, nonkey, CK].

* Classification of Indexing

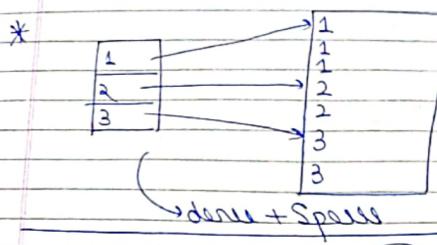
1) Dense index:



For every search key value: index entry.

2) Sparse index:

index entry created only for some records.



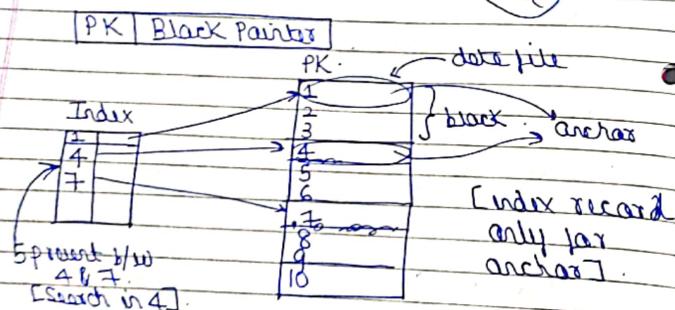
* Type of indexing → Cell

If 1 index file : Single level index.
Indexing on index file: multi level

* Primary Index (Primary Key + ordered)

DF ordered based on PK.

(Cell)



→ No index record for 2 & 3.
Sparse indexing

- No. of index entries = No. of data blocks
- Avg no. of block Access

→ B_i blocks in index.

$$\therefore \lceil \log_2 B_i + 1 \rceil$$

↳ after finding ref block in index.

7

* Example on Primary index

→ Cell.

Unspaced

records are fixed.

Find no. of block Access with/without index.



Block Size = 1024B.

Records = 100B.

$$\text{Records/block} = \frac{1024}{100} \Rightarrow 10.24 \rightarrow \text{cont put 11 records.}$$

: 10 ✓

: unspaced.
⇒ 0.24 width

8

$$\text{No. of data blocks} = \frac{30,000}{10} = 3000 \text{ blocks}$$

needed to hold all records.

i) We have ordered file (based on PK)

Search based on PK, then how many blocks occur → [say, 3000]

1) Without index → 11
→ 12

ii) With Primary index

index → 15B.

4B	6B
----	----

index record = 15B.

$$\text{index record/black} = \frac{1024}{15} = \underline{\underline{68}} \rightarrow \underline{\underline{68}}$$

$$\text{No. of index records} = 3000.$$

$$\text{No. of blocks required in index} = \frac{3000}{68} = \underline{\underline{44}} \rightarrow \underline{\underline{45}}$$

$$[\log_2 45 + 1] \rightarrow \underline{\underline{6}}, 6 + 1 = \underline{\underline{7}}$$

9

* Clustering index → (all) → entry in file first occurrence at key.

ordered or non-key field [repeated]

[for every distinct key value → 1 index record]

Spent less both ↗

$$\text{No. of block Access} \geq \log_2 B_i + 1$$

No. of blocks in index file.

* Secondary index

i) Primary index → Empno, & SAL query based on era → OK.

But if we get query extreme, not used.

Maintain separate index.

index → ordered.

but on unsorted data file.

∴ BS on index file.

→ index created for every record in file [Point] (Not Spread).

→ [No. of index entries = no. of records].

* Example of Secondary Index

30,000 records in a file.

Block Size = 1024 B.

Record size = 100 B.

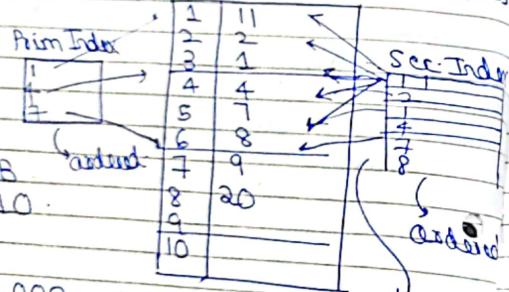
→ ordered file based on PK.

Primary index already exists.

Secondary index on Key (no repeat).

↳ An ordered file.
From SI.

PK K → Candidate key (non-repeat)



Block Size = 1024

Record size = 100 B

Records / block = 10.

No of blocks

$$\text{Required by file} \Rightarrow \frac{30,000}{10} = 3000 \text{ blocks}$$

↳ unsorted based on key

→ 3000 B blocks

$$\Rightarrow \frac{(1+3000)}{2} = 1500 \text{ Block Access}$$

Without index

Key → data points
Size of index record = 9 + 6 = 15 B.
No. of index records = 30,000.
in Secondary index

$$\text{No. of index records / block} = \frac{30,000}{15} \Rightarrow 68.$$

$$\therefore \text{No. of blocks} = \frac{30,000}{68} \Rightarrow \frac{442}{[441]}.$$

reqd by the index file

$$\therefore [log_2 442 + 1] \Rightarrow 9 + 1 \Rightarrow 10.$$

8.-

Q) Gates on 13.08

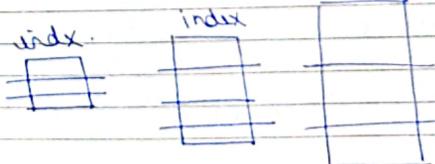
An index is clustered if:

data records of file are organized in the same order as the data entries of index.

↳ clustering → non-key & ordering

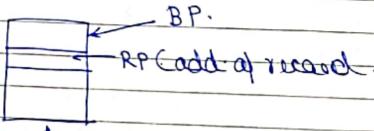
* B-Trees 1

↳ Multilevel indexing method (Generalized)



* B & B+ dynamic → size var/dec.
(general of multi level indexing).

- (i) node Painter/black Painter [add of block]
- (ii) record Painter
[points to the record we are searching for]



BP = 6B (identify which block)
if 1024 records in block = 10B

16B

* Key + data Painter → block/record



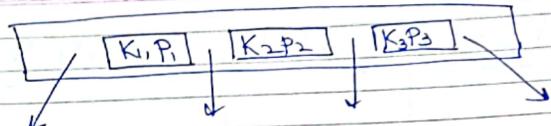
Key = value on which we search.

Root can have children b/w 2 & p.
order

* B-tree 2

Internal nodes can have children b/w $\lceil \frac{p}{2} \rceil$ and p.
- can have keys b/w $\lceil \frac{p}{2} \rceil - 1$ and p-1

13



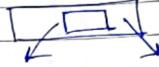
children = KP + 1

* Leaf Nodes

Keys b/w $\lceil \frac{p}{2} \rceil - 1$ and p-1

dist. from root to any leaf is same.

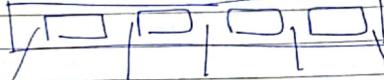
p → order → how to get p?



eg min children = 2.

at root

max children = 5.



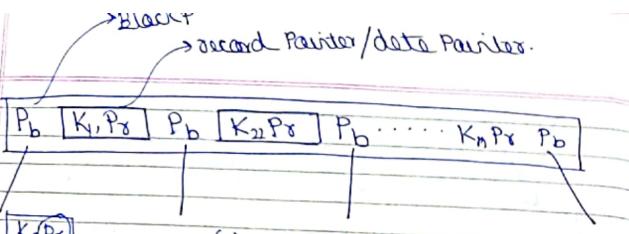
* Example 1 on B-Trees

Key Size = 10B.

Block Size = 512B.

data Painter = 8B.

Block Painter = 5B.



If order = n (Assume)

$$nP_b + (n-1)(K + P_r) \leq \frac{\text{Block Size}}{512}$$

Size of Key

\downarrow no. of Block

$$\therefore n5 + (n-1)[10+8] \leq 512$$

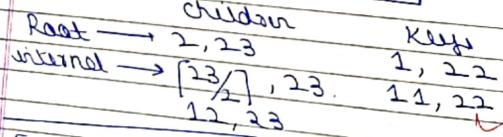
$$\Rightarrow 28n \leq 512$$

$$\Rightarrow 5n + 18n - 18 \leq 512$$

$$\Rightarrow 23n \leq 530$$

$$\Rightarrow n \leq \frac{530}{23} \approx 23 \therefore = \underline{23}$$

Max children = 23 (p) ✓



* Example on B-Trees

IS

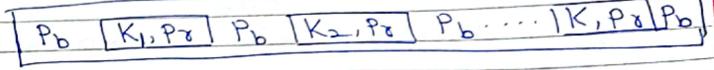
if searching anything less than K_1 ,
go to P_b (add. of node in next
level).

Key = 9B

$P_r = 7B$

$P_b = 6B$

Block Size = 512



Let order be n.

$$n * P_b + (n-1)[K + P_r] \leq \frac{\text{Block Size}}{512}$$

$$\Rightarrow 6n + (n-1)(16) \leq 512$$

$$6n + 16n - 16 \leq 512$$

$$22n \leq 528$$

$$n \leq \frac{528}{22} = 24$$

∴ 24. [Max no. of children]

child ht of tree will be less.

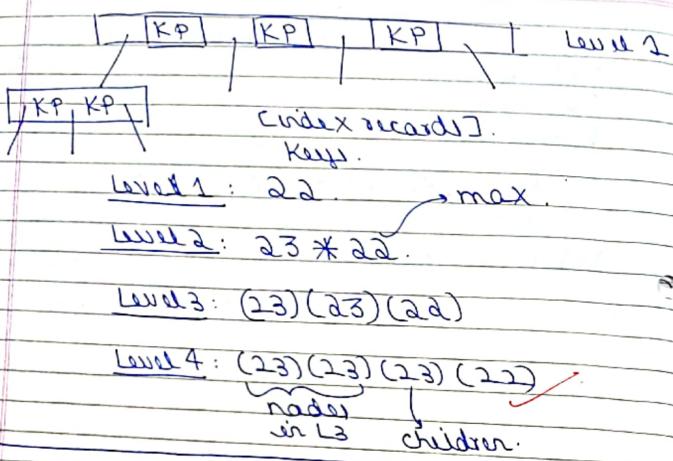
root : 2, 24

internal : 12, 24 ✓

* Example 3 on B-Trees

Order of B-tree = 23.
4-level.

16



* Underflow and overflow in B-Trees

if order = p → max no. of children.
keys exceed $p-1$ [max]
(root/internal/leaf).
overflow.

eg: insert 9. (b/w 8 8 10).
but already max keys [$p-1$].
Overflow

17

* Underflow → delete a node
(merging 2f).

Root: min keys = 1
internal: min keys = $\lceil \frac{p}{2} \rceil - 1$

if [no. of search < $\lceil \frac{p}{2} \rceil - 1$] (Underflow)
Key value

node has what it is actually required.

if $p=5$ → 2 (min).

|| 9 || 10 || 11 || 12 || delete 10.

because $1 < 2$. [Underflow].

* B-Trie Search

- Search index record in B-Trie

→ We have p choices to make at each node [p way search]

eg: Search record with key value 17.

- (first get into root)
- i) match: stop at root
- Adv: need not go till last node.

$17 < 25$.

(go left.)

[Keep hierarchy in Linear fashion].

(till 18, go left.)

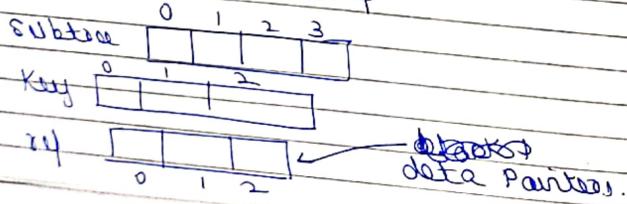
(we find 17 at Level 3.)

All index records are distributed over B-tree.
(No of comparison very less).

* B-tree Searching Algorithm

- Search the node, till we find a key greater than the key we are searching for. & go left.
if equal its: return it.

Step i): find exact key,
till end & Stop.



$t_K \rightarrow$ Target Key.

$t_K < \text{node.Key}[S]$;
break.

Also \rightarrow Cell.

as, Order \uparrow , Time \downarrow

Time complexity: $\log p^n$

Node

depth
of tree

$p \rightarrow$ order of B-tree

$n \rightarrow$ no. of Search Key

* Intuition \rightarrow Steps Cell

first search the position.

- Split if no Space.

* Eg 1 on B-tree Insertion

order of tree = 4

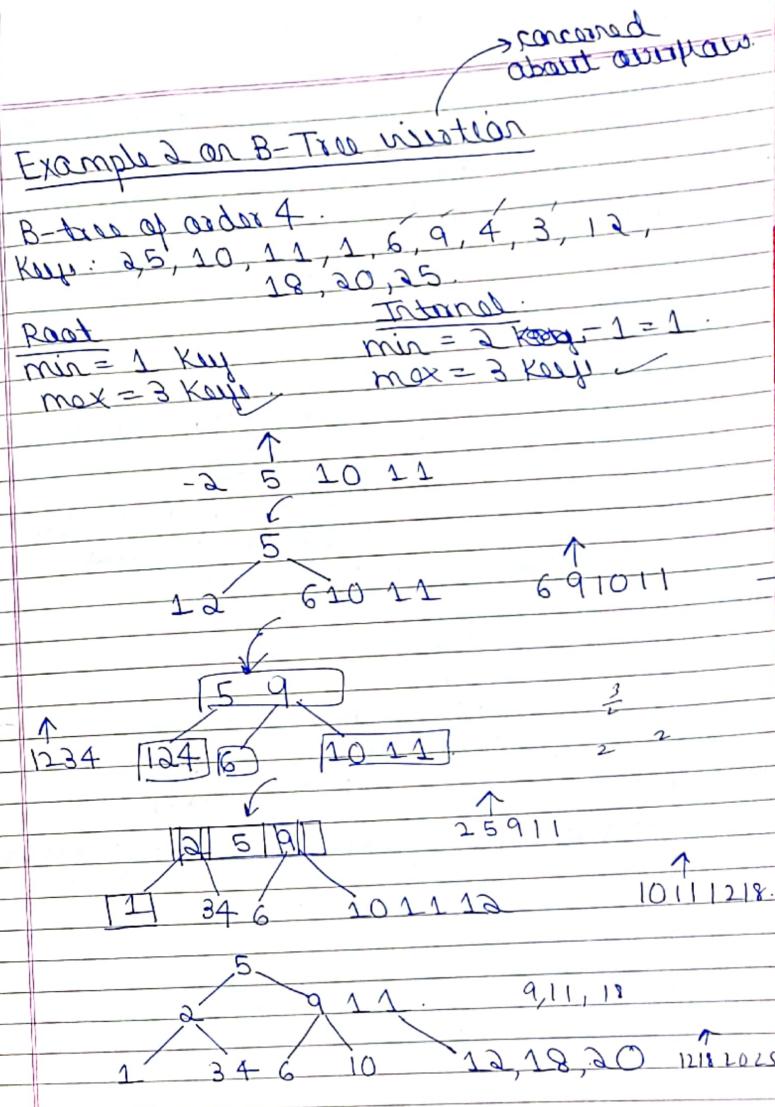
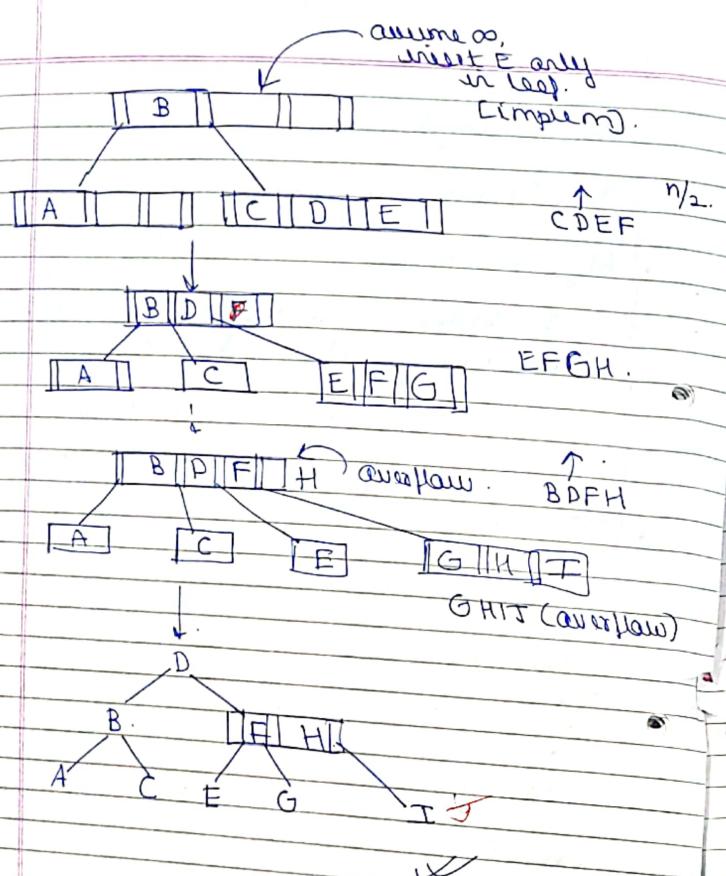
unit A, B, C, D, E, F, G, H, I, J.

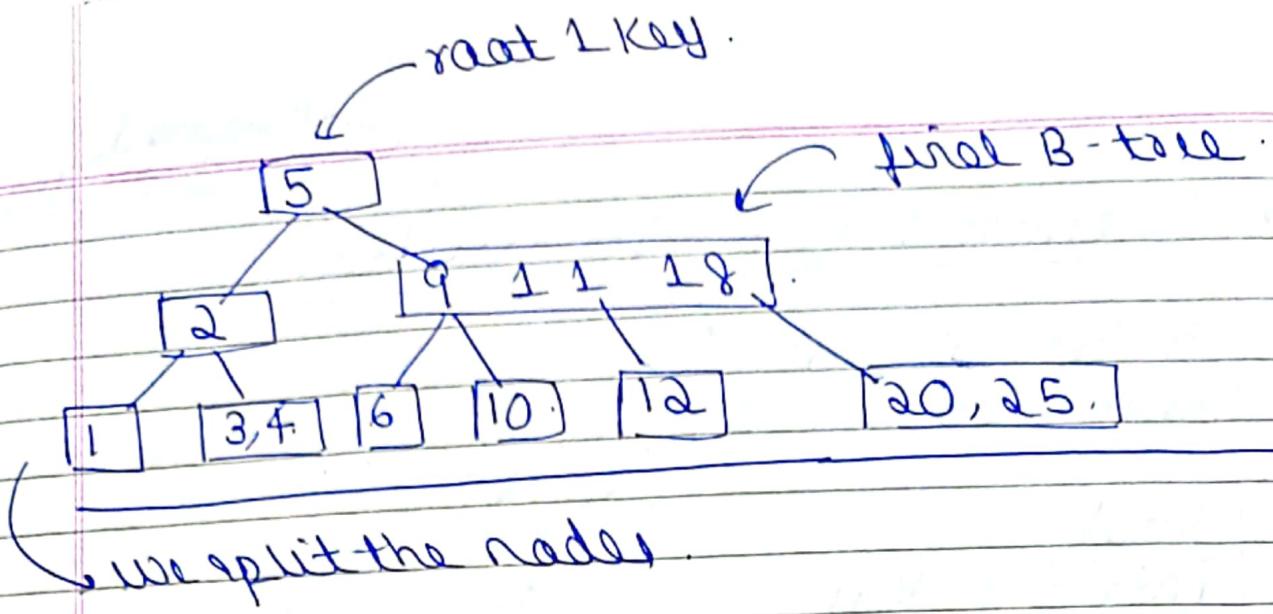
|| A || B || C ||

↑
ABCD.

$\rightarrow \max = p - 1$

$\rightarrow \min = \lceil \frac{p}{2} \rceil - 1$





if Order = "p".
 $\max = p+1 + 1 = p \text{ Keys (overflow)}.$

\downarrow
 median is promoted up.
 [p-1 keys distributed over

$$\begin{array}{c|c} p-\text{add} & p=\text{over 2 nodes}. \\ \frac{p-1}{2} & \frac{p-1}{2} \quad \left\lfloor \frac{p-1}{2} \right\rfloor \quad \left\lceil \frac{p-1}{2} \right\rceil + 1. \end{array}$$

All satisfy min criteria.

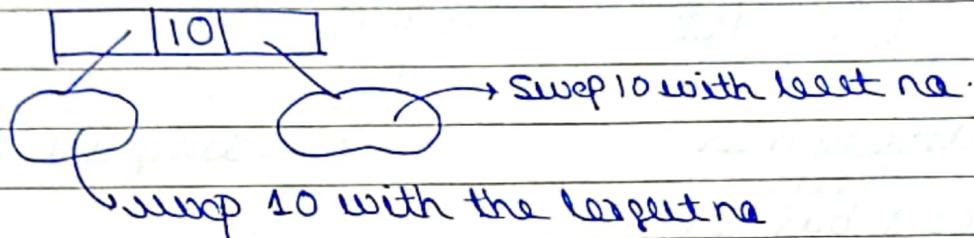
\therefore Dont worry abt underflow.
 [in insertion].

2) When inserting item, how many Splits?

→ screen abt underflow

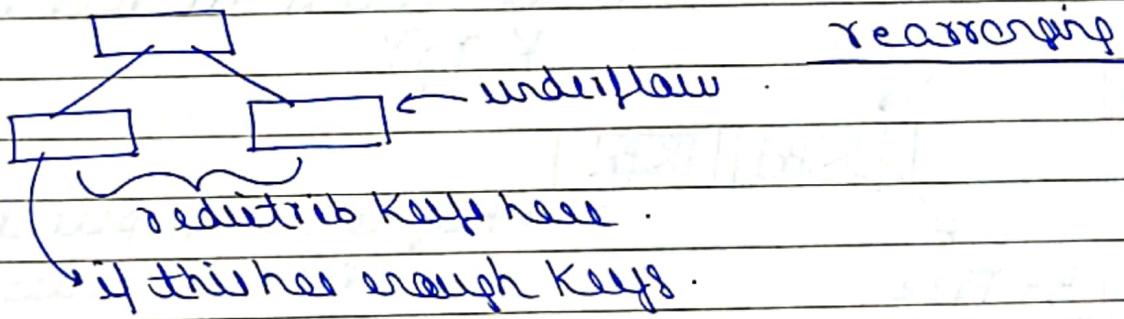
* Deletion from a B-Tree 1

- deletion std



- $\lceil \frac{P}{2} \rceil - 1 \rightarrow$ min keys any leaf can have.

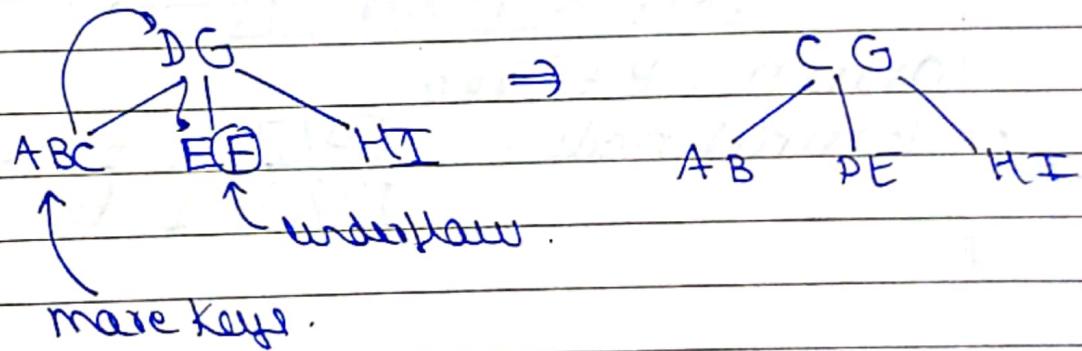
- II underflow: consider 2 immediate siblings.

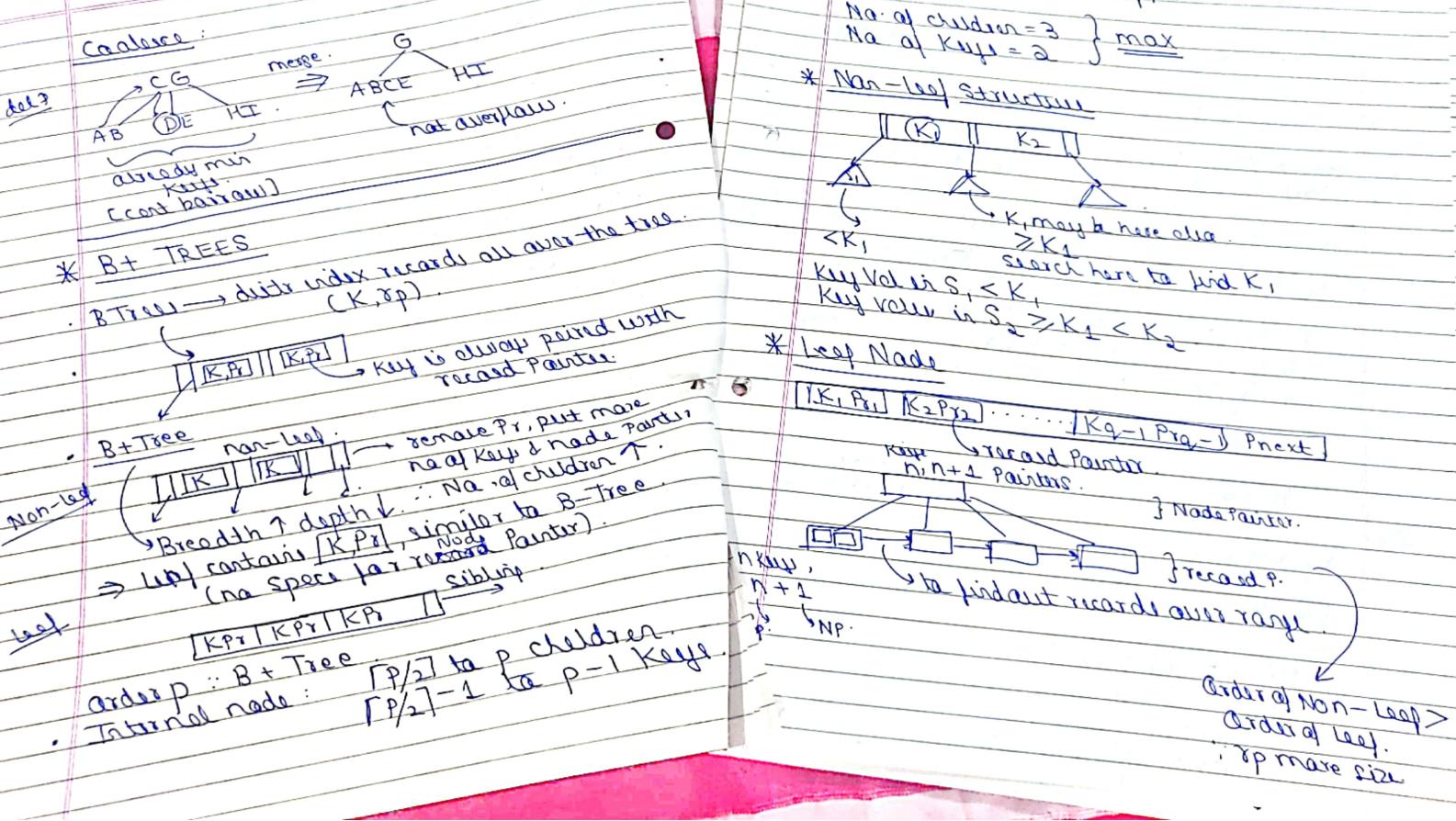


- II both immediate Sib. have exactly min no of keys, then merge. colliding
- II parent Key \rightarrow underflow: prop. upwards

* del: from B-tree 2

Borrow: 5 order tree $\rightarrow \lceil \frac{5}{2} \rceil - 1 = 2$





RP 1-1

- 1-2025. 35

27

Order of non-leaf : max no of children it can have
Order of leaf : max no of K-V pairs present
if both are same, some order.

* Example 1 on B+ Trees

Search Key = 9 B.
Block P = 6 B.
Record P = 7 B.

internal node (root / nonleaf)

$$\begin{aligned} & [P_b, K_1, P_b, K_2, P_b, K_3, \dots, K_{n-1}, P_n] \\ & n(P_b) + (n-1)K \leq 512B. \\ & n + (n-1)9 \leq 512. \\ & \Rightarrow 15n \leq 512. \\ & \therefore n \leq \frac{512}{15} \leq 34.5. \end{aligned}$$

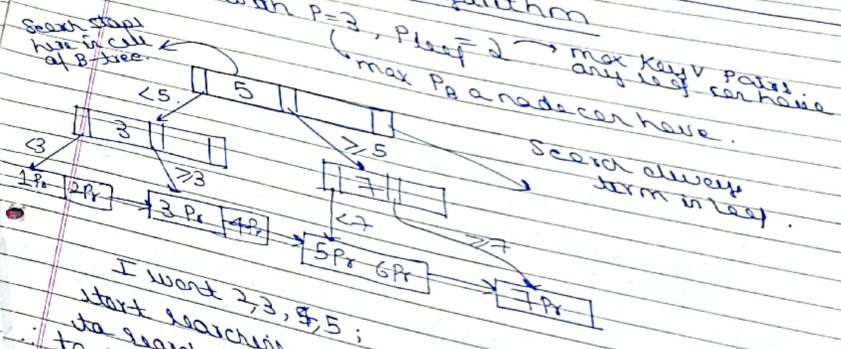
$\therefore n=34$ ← Order of Non-leaf.
[No. of Black P. is 34].

Leaf Node

$$\begin{aligned} & [K_1 P_r_1, K_2 P_r_2, K_3 P_r_3, \dots, K_m P_r_m, P_b] \\ & m[K + P_r] + P_b \leq 512. \\ & m[9 + 7] + 6 \leq 512. \\ & 16m \leq 506. \\ & m \leq \frac{506}{16} = 31. \end{aligned}$$

* Order of Leaf = 31. (max KV pairs it has).
if only block pointers in Leaf, Order will be 1 less as some.
Searching B+ Tree Algorithm

B+ Tree with $P=3$, $P_{leaf}=2$ → max keys per page
(max P as a node can have).



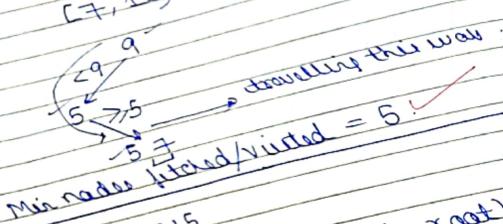
I went 2, 3, 4, 5;
start searching with 2, to find 3, no need
to search from root.
Breadth ↑; Search time ↓: depth ↓.
time complexity. As. $O(1) = O(N) = \text{same}$
order, value, $\log n$. much higher than

Q Gate 2015 (B+ Tree)

≤ 7 and < 15

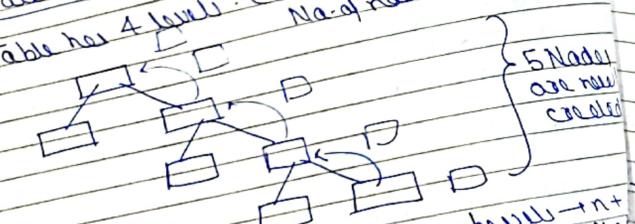
records pointers there, but not shown.
Here, doubly linked list.

[7, 15)



Gate 1T-2015

Table has 4 levels. (including root)
No. of nodes newly created



Assume all
nodes are full
(p-1) Keys.

RP 1-1. 1 - 2 - 2 - 5 35

2A

Q Gate 2015 Q [B+]

Key = 128.

Block Size = 1024B

PR = 10B

Block pointer = 8

Non-leaf.

$P_1 K_1 P_2 K_2 \dots K_3 P_{n+1}$

$$n \times K + (n+1)P_B \leq 1024 \\ \Rightarrow 12n + (n+1)8 \leq 1024$$

$$\Rightarrow 12n + 8n + 8 \leq 1024 \\ \Rightarrow 20n + 8 \leq 1024$$

$$20n \leq 1016$$

$$n \leq \frac{1016}{20}$$

$\therefore n=50$ (Max Keys).

* Gate 2003
2-3-4. (2 or 3 or 4) [children].

min \uparrow max.
 $K_{\text{lf}} = 1$ $K_{\text{rf}} = 3$

Lexicographical order used

$\lceil \frac{p}{2} \rceil - 1$ - 1/12/2025. 35

31

* B & B+ Tree are perfectly balanced.

* Gate 2010 on B+ Trees

Q) $\max \text{Key}_p = 5$

$$n-1=5, n=6$$

$$\textcircled{2} \quad \lceil \frac{6}{2} \rceil - 1 = 2$$

if order = p, $\max \text{Key}_p = p-1 \therefore p=6$
 $\min \text{Key}_p = \lceil \frac{p}{2} \rceil - 1 = 3 - 1 = 2$ (b).

(in non-root Node - root = 1)

* Gate 2007

$O(\log p) = \max \text{no. of K-V pairs}$

(Record Pairs)

P_r: 7 B.

Key: 9 B.

P_b: 16.

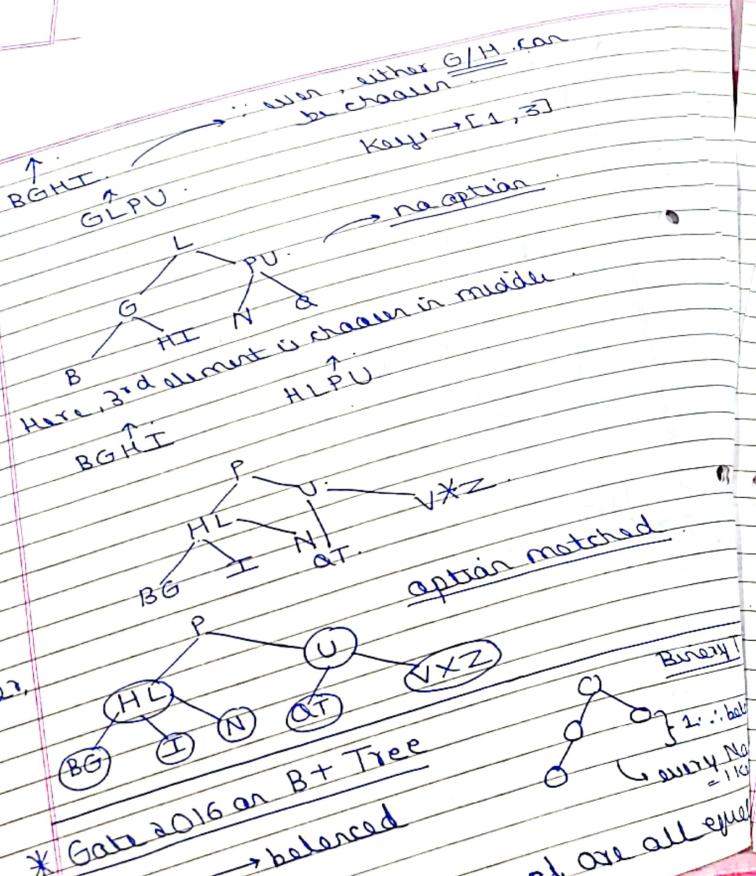
$$m(7+9) + 16 \leq 1024.$$

$$16m$$

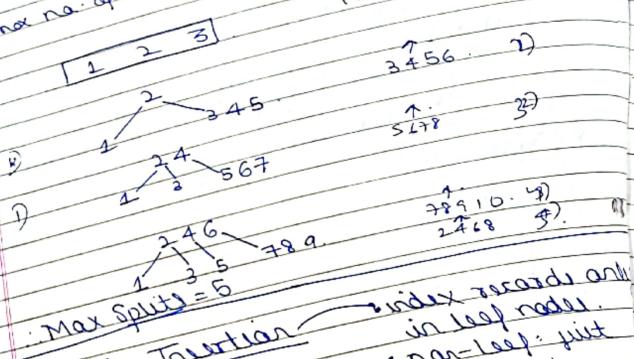
$$16m \leq 1024 - 16 = 1008.$$

$$m \leq \frac{1008}{16} \Rightarrow m = 63.$$

$$\therefore m = 63$$



* Gate 2008 on B-Tree
Order=4; 10 successive insertions
(max=3 of node splitting).



Max Split = 5

* B+ Tree Insertion
- insertion starts from leaf.
(key, record pointer).

index records and
in leaf nodes.
• non-leaf: first
insert key.

RP 1-1. 1. - - - 35

33

Order 5 [B+Tree]

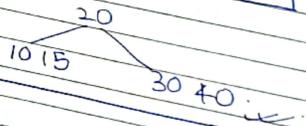
max Keys at any node = 4.
ever after splitting, 9 should still be present
copy the smallest key value of and node in Parent.

Overflow: when no. of search key values exceed ' $p-1$ '
order is same for leaf & non-leaf = practical.

e.g. order=5.

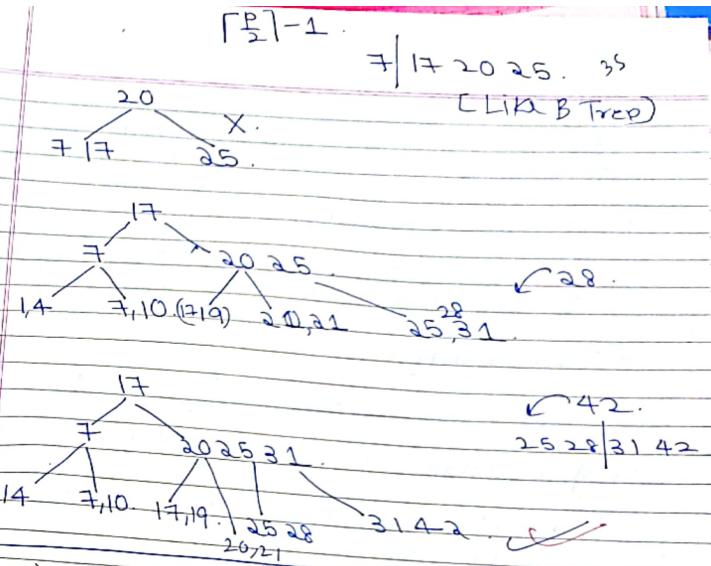
Overflow in Parent:

10 20 30 40 ← non-leaf.



10 15 20 30 40

$\frac{n-1}{2}$



- * D/H b/w B/B+Trees & BST.
 - ↳ grow in the breadth.
 - less height comp to BST.
 - Search time ↓
 - ↳ ht of B > ht of B+-tree.
 - [Key-Pg.] [Early Key: internal node]
 - : more children.

BT tree: Range based Queries easily implemented.

Binary Tree → not preferred in DBMS.

* B+ Tree Deletion (cell)

- entry in the leaves, & key in non-leaf idea
B-tree: key will appear only in 1 node.

→ check underflow.

if L contains at least $\lceil \frac{P}{2} \rceil - 1$, done!

if underflow, $L = \lceil \frac{P}{2} \rceil - 2$ entries.
if any of siblings have keys greater than min.

you can borrow.
if redict full, merge ✓.

If merge ✓, corresponding entry must
be deleted
replaces with inorder successor.

* EXAMPLE 1 on B+ Tree Deletion

$$5 \rightarrow \left\lceil \frac{5}{2} \right\rceil - 1 = \frac{2}{2} \text{ (min)} \\ \text{root} \rightarrow 1$$

DELETE 19, 20

[delete 19]

DELETE 19, 2

Search 22.

delete 22 → underflow.

(cell)

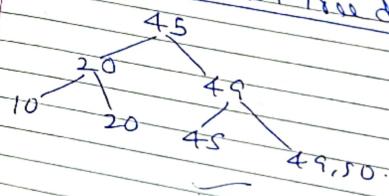
replace with
smallest
in PFT
24, 30
17
24, 27, 29.

17, 24, 27, 29.

27, 30.

30, 34, 38, 39.

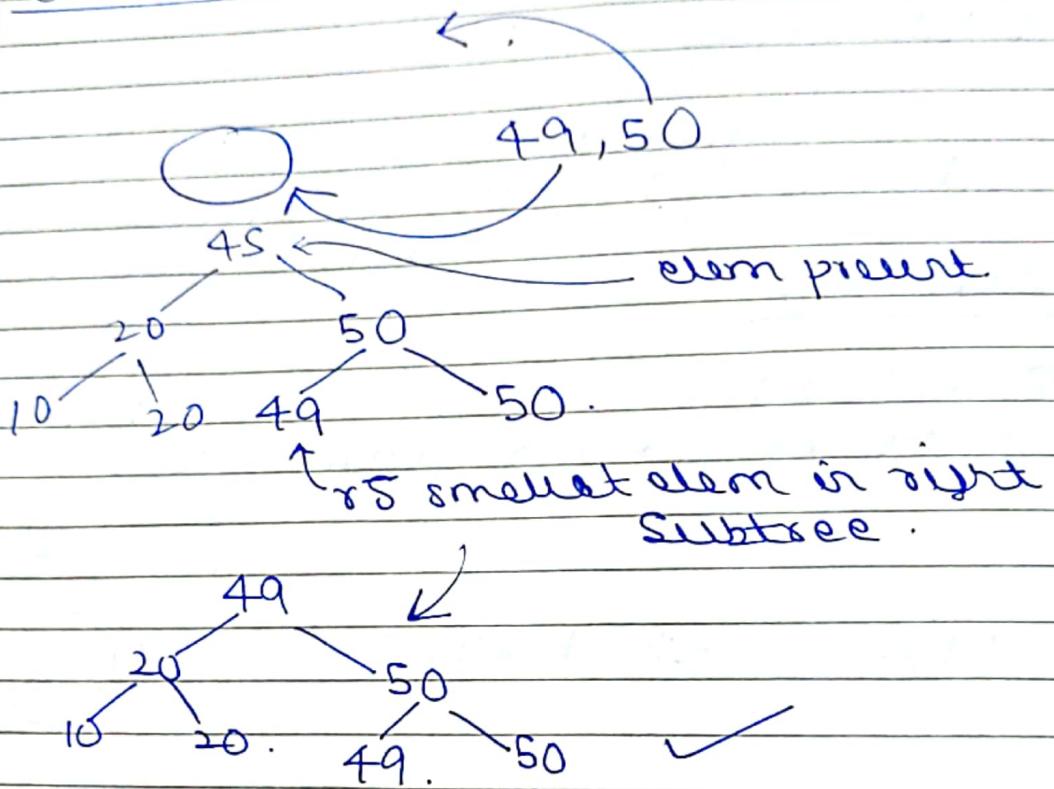
(* Example 2 on B+ Tree deletion



$$\left\lceil \frac{3}{2} \right\rceil - 1$$

① atleast
1 key.

delete 45



* Example 3 on B+ Tree Deletion

