

SGupta_HW03Question4

Question 1

(a) Which variables are statistically significant?

```
library(faraway)
data(teengamb)
head(teengamb)
```

	sex	status	income	verbal	gamble
1	1	51	2.00	8	0.0
2	1	28	2.50	8	0.0
3	1	37	2.00	6	0.0
4	1	28	7.00	4	7.3
5	1	65	2.00	8	19.6
6	1	61	3.47	6	0.1

```
# Fit the full model
model <- lm(gamble ~ sex + status + income + verbal, data = teengamb)
summary(model)
```

Call:

```
lm(formula = gamble ~ sex + status + income + verbal, data = teengamb)
```

Residuals:

Min	1Q	Median	3Q	Max
-51.082	-11.320	-1.451	9.452	94.252

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	22.55565	17.19680	1.312	0.1968
sex	-22.11833	8.21111	-2.694	0.0101 *
status	0.05223	0.28111	0.186	0.8535
income	4.96198	1.02539	4.839	1.79e-05 ***
verbal	-2.95949	2.17215	-1.362	0.1803

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 22.69 on 42 degrees of freedom

Multiple R-squared: 0.5267, Adjusted R-squared: 0.4816

F-statistic: 11.69 on 4 and 42 DF, p-value: 1.815e-06

Considering $\alpha = 0.05$, sex is statistically significant as the p value 0.01 is less than 0.05.

Status is insignificant in this model preparation as the p value 0.8 is higher than alpha level.

income is highly significant. its p value is only 0.000017

And verbal is also not significant.

(b) What interpretation should be given to the coefficient for sex?

```
summary(model)$coefficients["sex", c("Estimate", "Std. Error", "t value", "Pr(>|t|)")]
```

Estimate	Std. Error	t value	Pr(> t)
-22.11833009	8.21111453	-2.69370620	0.01011184

A unit increase in sex variable is associated with an average decrease in response variable gamble by about 22.12 units. A female variable tends to gamble less than male by 22.12 units.

(c) Fit a model with just income as a predictor and use an F-test to compare it to the full model.

```
model_income <- lm(gamble ~ income, data = teengamb)
anova(model_income, model)
```

Analysis of Variance Table

Model 1: gamble ~ income

Model 2: gamble ~ sex + status + income + verbal

	Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	45	28009				
2	42	21624	3	6384.8	4.1338	0.01177 *

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

- The F-statistic is about 4.133 with 3 and 42 degrees of freedom.
- The associated p-value is approximately 0.01177
- The RSS difference between the two models is 6,384.8. This is due to the extra variables (variations) by adding the predictors sex, status, and verbal in the full model.
- Since the p-value (0.01177) is less than the significance level (0.05), we reject the null hypothesis that the extra predictors (sex, status, and verbal) contribute no additional significance over the income-only model.