# Standardized low resolution brain electromagnetic tomography (sLORETA): technical details

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Running title: sLORETA

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#### **Abstract**

Scalp electric potentials (EEG) and extracranial magnetic fields (MEG) are due to the primary (impressed) current density distribution that arises from neuronal post-synaptic processes. A solution to the inverse problem, i.e. the computation of images of electric neuronal activity based on extracranial measurements, would provide important information on the time course and localization of brain function. In general, there is no unique solution to this problem. In particular, an instantaneous, distributed, discrete, linear solution capable of exact localization of point sources is of great interest, since the principles of linearity and superposition would guarantee its trustworthiness as a functional imaging method, given that brain activity occurs in the form of a finite number of distributed "hot spots". Despite all previous efforts, linear solutions at best produced images with systematic non-zero localization errors. A solution is reported here, which yields images of standardized current density with zero localization error. The purpose of this paper is to present the technical details of the method, allowing researchers to test, check, reproduce, and validate the new method (sLORETA).

#### Introduction

This study is strictly limited to EEG/MEG inverse solutions of the type: instantaneous, distributed, discrete, and linear. The generic form of the inverse problem follows. There are  $N_{\scriptscriptstyle E}$  instantaneous extracranial measurements. There are  $N_{\scriptscriptstyle V}$  voxels in the brain. Typically, the voxels are determined by subdividing

uniformly the solution space, which is usually taken as the cortical grey matter volume or surface. At each voxel there is a point source, which may be a vector with three unknown components (i.e., the three dipole moments), or a scalar (unknown dipole amplitude, known orientation). The cases considered here correspond to  $N_V \gg N_E$ .

In 1984, Hämäläinen and Ilmoniemi (1) were the first to report an instantaneous, distributed, discrete, linear solution to the EEG/MEG inverse problem: the well known minimum norm solution. However, the minimum norm solution is notorious for totally misplacing actual deep sources onto the outermost cortex, as demonstrated in (3), (2), and (8).

The problem of excessively large errors of localization remained unsolved until the introduction of the method known as LORETA (low resolution brain electromagnetic tomography) in 1994 (18). LORETA has fairly good accuracy in localizing test sources even when they are deep. The overall average localization error is smaller than one grid unit (see e.g. (3), (2), and (8)).

A series of papers published in 1998 and 1999 (see (19)-(23)) introduced for the first time the method of high time resolution statistical parametric mapping for tomographic images of electric neuronal activity. The idea was to adopt the methods of statistical inference for the localization of brain function as used in PET and fMRI studies. This methodology was applied to high time resolution, time varying LORETA images.

In the present study a new tomographic method for electric neuronal activity is introduced, where localization inference is based on images of standardized current density. The method is denoted as standardized low resolution brain electromagnetic tomography (sLORETA). Unlike the method recently introduced by Dale et al. (6), which has systematic non-zero localization error, sLORETA has zero localization error.

#### Method

### Case 1: EEG with unknown current density vector

The equation of interest takes the form:

$$\mathbf{F} = \mathbf{KJ} + c\mathbf{1}$$

In Eq. 1,  $F \in \mathbb{R}^{N_E \times 1}$  is a vector containing scalp electric potentials measured at  $N_E$  cephalic electrodes, with respect to a common, arbitrary reference electrode located anywhere on the body.

The primary (impressed) current density  $\mathbf{J} \in \mathbb{R}^{(3N_V) \times 1}$  is defined as:  $\mathbf{J} = \left(\mathbf{J}_1^T, \mathbf{J}_2^T, \mathbf{J}_3^T, ..., \mathbf{J}_{N_V}^T\right)^T$  Eq. 2

where  $\mathbf{J}_l \in \mathbb{R}^{3\times 1}$  for  $l = 1...N_V$ . At the  $l^{\text{th}}$  voxel,  $\mathbf{J}_l^T = \left(J_l^x, J_l^y, J_l^z\right)$  contains the three unknown dipole moments.

The superscript "T" denotes transpose.

The lead field  $\mathbf{K} \in \mathbb{R}^{N_E \times (3N_V)}$  has the following structure:

$$\mathbf{K} = \begin{pmatrix} \mathbf{k}_{1,1} & \mathbf{k}_{1,2} & \dots & \mathbf{k}_{1,N_V} \\ \mathbf{k}_{2,1} & \mathbf{k}_{2,2} & \dots & \mathbf{k}_{2,N_V} \\ \dots & \dots & \dots & \dots \\ \mathbf{k}_{N_E,1} & \mathbf{k}_{N_E,2} & \dots & \mathbf{k}_{N_E,N_V} \end{pmatrix}$$
 Eq. 3

with  $\mathbf{k}_{i,l} \in \mathbb{R}^{1 \times 3}$ , for  $i = 1...N_E$ , and for  $l = 1...N_V$ . Note that  $\mathbf{k}_{i,l} = \left(k_{i,l}^x, k_{i,l}^y, k_{i,l}^z\right)$ , where  $k_{i,l}^x$  is the scalp electric potential at the  $i^{\text{th}}$  electrode, due to a unit strength X-oriented dipole at the  $l^{\text{th}}$  voxel;  $k_{i,l}^y$  is the scalp electric potential at the  $i^{\text{th}}$  electrode, due to a unit strength Y- oriented dipole at the  $l^{\text{th}}$  voxel; and  $k_{i,l}^z$  is the scalp electric potential at the  $i^{\text{th}}$  electrode, due to a unit strength Z- oriented dipole at the  $l^{\text{th}}$  voxel.

In Eq. 1, c is an arbitrary constant which embodies the fact that the electric potential is determined up to an arbitrary constant; and  $\mathbf{1} \in \mathbb{R}^{N_E \times 1}$  is a vector of ones. The parameter c allows the use of any reference for the lead field and the measurements.

Hämäläinen, M.S., and Ilmoniemi (1) were the first to publish a particular solution to the instantaneous, distributed, discrete, linear EEG/MEG inverse problem. Their solution is known as the minimum norm inverse solution. However, the minimum norm solution is notorious for totally misplacing actual deep sources onto the outermost cortex (2).

Dale et al. (6) proposed a method in which localization inference is based on a standardization of the current density estimates. In particular, they employed the current density estimate given by the minimum norm solution, and they standardized it by using its expected standard deviation, which is hypothesized to be originated exclusively by measurement noise. The method of Dale et al. (6) produces systematic non-zero localization errors (8), even in the presence of negligible noise. This fact was not evaluated nor admitted in their original paper.

sLORETA is similar to the Dale et al. (6) method: it employs the current density estimate given by the minimum norm solution, and localization inference is based on standardized values of the current density estimates. However, standardization in sLORETA takes a completely different route (explained below). The consequence is that, unlike the Dale et al. (6) method, sLORETA is capable of exact (zero-error) localization.

The minimum norm inverse solution is harmonic (2), which means that the Laplacian of the current density is zero, i.e.,  $\nabla^2 \mathbf{J}(\mathbf{r}) \equiv \mathbf{0}$ , where  $\mathbf{r}$  denotes volume coordinates in the brain. Therefore, the minimum norm inverse solution is very smooth. The concept of smoothness employed here is discussed in greater detail in

(8), with special emphasis on its electrophysiological interpretation. However, as previously mentioned, the minimum norm inverse solution is notorious for its incapability of correct localization of deep point sources (2).

This problem is solved by standardization of the minimum norm inverse solution, and basing localization inference on these standardized estimates.

The functional of interest here is:

$$F = \|\mathbf{F} - \mathbf{K}\mathbf{J} - c\mathbf{1}\|^2 + \mathbf{a}\|\mathbf{J}\|^2$$
 Eq. 4

where  $a \ge 0$  is a regularization parameter. This functional is to be minimized with respect to **J** and c, for given **K**, F, and **a**. The explicit solution to this minimization problem is (see e.g. (3)):

$$\hat{\mathbf{J}} = \mathbf{T}\mathbf{F}$$

where:

$$\mathbf{T} = \mathbf{K}^T \mathbf{H} \left[ \mathbf{H} \mathbf{K} \mathbf{K}^T \mathbf{H} + \mathbf{a} \mathbf{H} \right]^+$$
 Eq. 6

$$\mathbf{H} = \mathbf{I} - \mathbf{1}\mathbf{1}^T/\mathbf{1}^T\mathbf{1}$$
 Eq. 7

with  $\mathbf{H} \in \mathbb{R}^{N_E \times N_E}$  denoting the centering matrix;  $\mathbf{I} \in \mathbb{R}^{N_E \times N_E}$  the identity matrix; and  $\mathbf{1} \in \mathbb{R}^{N_E \times 1}$  is a vector of ones.

For any matrix  $\mathbf{M}$ ,  $\mathbf{M}^+$  denotes its Moore-Penrose pseudoinverse (see e.g. (9)).

The centering matrix **H** in Eq. 7 is the average reference operator.

In what follows, for all EEG cases, the symbols F and K will denote the average reference transforms of the EEG measurements and the lead field, respectively. This simplifies the notation. But most important of all, the correct solution to EEG problems is based on these average reference transforms.

Therefore, when using average reference transforms of F and  $\boldsymbol{K},$  Eq. 1 becomes:

$$F = KJ$$

and the functional in Eq. 4 becomes:

$$F = \|\mathbf{F} - \mathbf{K}\mathbf{J}\|^2 + \mathbf{a}\|\mathbf{J}\|^2$$
 Eq. 9

with minimum:

$$\hat{\mathbf{J}} = \mathbf{T}\mathbf{F}$$

where:

$$\mathbf{T} = \mathbf{K}^T \left[ \mathbf{K} \mathbf{K}^T + \mathbf{a} \mathbf{H} \right]^+$$
 Eq. 11

Standardization of the estimate  $\hat{\mathbf{J}}$  requires an estimate of its variance.

Note that Eq. 9 can be derived from a Bayesian formulation of the inverse problem (see e.g. (5), Eq. 1.88 therein). In this view, the *actual* source variance (*prior*)  $\mathbf{S_J} \in \mathbb{R}^{(3N_V) \times (3N_V)}$  is equal to the identity matrix, i.e.:

$$\mathbf{S_J} = \mathbf{I} , \mathbf{I} \in \mathbb{R}^{(3N_V) \times (3N_V)}$$
 Eq. 12

In addition, from the Bayesian point of view, the electric potential variance is due to noisy measurements:

$$\mathbf{S}_{\mathrm{F}}^{noise} = \mathbf{a}\mathbf{H}$$

Note that in Eq. 13, the average reference operator **H** plays the role of the identity matrix in the subspace spanned by the measurement space.

It is usually assumed that activity of the actual sources and the noise in the measurements are uncorrelated.

Based on the linear relation in Eq. 8, making use of Eqs. 12 and 13, and taking into account the independence of actual source activity and measurement noise, the electric potential variance  $\mathbf{S}_{\mathrm{F}} \in \mathbb{R}^{N_E \times N_E}$  then is:

$$\mathbf{S}_{\mathrm{F}} = \mathbf{K}\mathbf{S}_{\mathbf{J}}\mathbf{K}^{T} + \mathbf{S}_{\mathrm{F}}^{noise} = \mathbf{K}\mathbf{K}^{T} + \mathbf{a}\mathbf{H}$$
 Eq. 14

See e.g. (10), Eqs. 1.5.1-1.5.6 therein.

Due to the linear relation in Eq. 10, and making use of Eq. 14, the variance of the estimated current density is:

$$\mathbf{S}_{\hat{\mathbf{J}}} = \mathbf{T}\mathbf{S}_{\mathbf{F}}\mathbf{T}^{T} = \mathbf{T}(\mathbf{K}\mathbf{K}^{T} + a\mathbf{H})\mathbf{T}^{T} = \mathbf{K}^{T}[\mathbf{K}\mathbf{K}^{T} + a\mathbf{H}]^{+}\mathbf{K}$$
 Eq. 15

See e.g. (10), Eqs. 1.5.1-1.5.6 therein, and (9).

Note that the variance of the *estimated* current density is equivalent to the Backus and Gilbert (4) resolution matrix, which is obtained by plugging Eqs. 8 and 11 into 10:

$$\hat{\mathbf{J}} = \mathbf{T}\mathbf{K}\mathbf{J} = \mathbf{K}^T \left[ \mathbf{K}\mathbf{K}^T + \mathbf{a}\mathbf{H} \right]^{+} \mathbf{K}\mathbf{J} = \mathbf{R}\mathbf{J} = \mathbf{S}_{\hat{\mathbf{J}}}\mathbf{J}$$
 Eq. 16

with:

$$\mathbf{S}_{\hat{\mathbf{J}}} = \mathbf{R} = \mathbf{K}^T \left[ \mathbf{K} \mathbf{K}^T + \mathbf{a} \mathbf{H} \right]^{+} \mathbf{K}$$
 Eq. 17

where  $\mathbf{R}$  is the resolution matrix.

Note that the variance of the *estimated* current density in Eqs. 15 and 17 is <u>not</u> the posterior variance in the Bayesian formulation (see e.g. (5), Eq. 1.94).

In contrast, according to Dale et al. (6), the variance of the *estimated* current density is based on the assumption that the only source of variation is measurement noise. This means that Eq. 14 now is:

$$\mathbf{S}_{\mathrm{F}}^{Dale} = \mathbf{S}_{\mathrm{F}}^{noise}$$

and Eq. 15 now is:  

$$\mathbf{S}_{\hat{\mathbf{j}}}^{Dale} = \mathbf{T}\mathbf{S}_{F}^{Dale}\mathbf{T}^{T} = \mathbf{T}\mathbf{S}_{F}^{noise}\mathbf{T}^{T}$$
Eq. 19

Note that unlike the approach of Dale et al. (6), sLORETA takes into account two sources of variation: mainly the variation of the actual sources, and then finally, if any, the variation due to noisy measurements.

Finally, sLORETA corresponds to the following estimates of standardized current density power:

$$\hat{\mathbf{J}}_{l}^{T}\left\{ \left[\mathbf{S}_{\hat{\mathbf{J}}}^{}\right]_{ll}^{}\right\} ^{-1}\hat{\mathbf{J}}_{l}$$
 Eq. 20

where  $\hat{\mathbf{J}}_l \in \mathbb{R}^{3\times l}$  is the current density estimate at the  $l^{\text{th}}$  voxel given by Eqs. 10 and 11 (for average reference transforms); and  $\left[\mathbf{S}_{\hat{\mathbf{J}}}\right]_{ll} \in \mathbb{R}^{3\times 3}$  is the  $l^{\text{th}}$  diagonal block of matrix  $\mathbf{S}_{\hat{\mathbf{J}}}$  in Eqs. 15 or 17.

Note that the pseudo-statistic in Eq. 20 has the form of an "F" statistic.

Note that Eq. 20 is different in form from the Dale et al. (6) standardization (see (6), Eq. 7 therein). The Dale et al. (6) standardized estimates are:

$$\hat{\mathbf{J}}_{l}^{T} \left[ Diag \left( \left[ \mathbf{S}_{\hat{\mathbf{J}}}^{Dale} \right]_{ll} \right) \right]^{-1} \hat{\mathbf{J}}_{l}$$
 Eq. 21

where  $\left[\mathbf{S}_{\hat{\mathbf{J}}}^{Dale}\right]_{ll} \in \mathbb{R}^{3\times3}$  is the  $l^{\text{th}}$  diagonal block of matrix  $\mathbf{S}_{\hat{\mathbf{J}}}^{Dale}$  in Eq. 19; and for any symmetric matrix  $\mathbf{M}$ ,  $Diag(\mathbf{M})$  is the diagonal matrix formed by the diagonal elements of  $\mathbf{M}$ .

# Case 2: EEG with known current density vector orientation, unknown amplitude

This case usually corresponds to the inverse problem when the cortical surface is completely known. Voxels are now distributed along the cortical surface, and the dipoles at each voxel have known orientation (perpendicular to the cortical surface). The unknowns correspond to the amplitudes, which may take positive, zero, or negative values. The dipole orientations (defined as unit length vectors with three components) can be incorporated into the lead field **K** in Eq. 8. Details can be found in (3).

In this case Eq. 8 has the same form, but now  $\mathbf{J} \in \mathbb{R}^{N_V \times 1}$  since it only contains one unknown scalar per voxel, and  $\mathbf{K} \in \mathbb{R}^{N_E \times N_V}$  since it includes the dipole orientation at each voxel. Details can be found in (3). All the derivations employed in Eqs. 8-17 remain formally identical.

However, *s*LORETA now corresponds to the following estimates of standardized current density power:

$$\frac{\left(\hat{J}_{l}\right)^{2}}{\left[\mathbf{S}_{\hat{\mathbf{J}}}\right]_{n}}$$
 Eq. 22

where the scalar  $\hat{J}_l$  is the current density amplitude estimate at the  $l^{\text{th}}$  voxel; and the scalar  $\left[\mathbf{S}_{\hat{\mathbf{J}}}\right]_{ll}$  is the  $l^{\text{th}}$  diagonal element of matrix  $\mathbf{S}_{\hat{\mathbf{J}}} \in \mathbb{R}^{N_V \times N_V}$ .

Note that the pseudo-statistic in Eq. 22 has the form of an "F" statistic.

#### Case 3: MEG

The equations for the MEG case have identical form to Eqs. 8-17, 20, and 22, depending on the case of unknown dipole moments, or only unknown amplitudes.

Note that the average reference does not apply to MEG.

The only change corresponds to the equations for the MEG lead field, which are different to those for the EEG.

#### **Head models**

Simulations were carried out in a three-shell spherical head model registered to the Talairach human brain atlas (11), available as a digitized MRI from the Brain Imaging Centre, Montreal Neurological Institute. Registration between spherical and realistic head geometry used EEG electrode coordinates reported by Towle et al. (12).

In one set of practical, realistic, simulations, the solution space was restricted to cortical gray matter and hippocampus, as determined by the corresponding digitized Probability Atlas also available from the Brain Imaging Centre, Montreal Neurological Institute. A voxel was labeled as gray matter if it met the following three conditions: its probability of being gray matter was higher than that of being white matter, its probability of being gray matter was higher than that of being cerebrospinal fluid, and its probability of being gray matter was higher than 33%. Only gray matter voxels that belonged to cortical and hippocampal regions were used for the analysis. A total of 6430 voxels at 5mm spatial resolution were produced under these neuroanatomical constraints. At each voxel, three unknown values (the three dipole moments) were estimated, making a total of 6430x3=19290 unknowns. 25 electrodes (in EEG experiments), or 25 magnetometer sensors (in MEG experiments) were used. In both cases, sensors and electrodes were placed in the same locations.

In the second set of practical, realistic, simulations, the solution space was restricted to the cortical surface, represented as 12980 triangles (voxels) (13). This case corresponded to unknown current density amplitude (but with known orientation), making a total of 12980 unknowns. 101 electrodes (in EEG experiments), or 101 magnetometer sensors (in MEG experiments) were used. In both cases, sensors and electrodes were placed in the same locations.

### Comparison of imaging methods

The minimum norm solution, the method of Dale et al. (6), and sLORETA were compared in terms of localization errors and spatial spread. The methods were tested with point sources located at the voxels. For the case corresponding to 3 unknowns per voxel, an arbitrary (random) orientation of the test source was employed. The test

sources were used to generate the measurements (forward equation (Eq. 8)), which were then given to the imaging methods. Simulations included "noise free" and "noisy" measurements.

In the minimum norm solution case, the imaging method is based on Eqs. 20 and 22, but without standardization, which is achieved by setting the variance to the identity matrix, i.e.,  $\mathbf{S}_{\hat{i}} \equiv \mathbf{I}$ .

In the minimum norm solution and in sLORETA, the regularization parameter  $\boldsymbol{a}$  in the previous equations was estimated by cross-validation. Exact details and equations for a practical implementation of the cross-validation method can be found in (14).

In the Dale et al. (6) method, the parameter  $\boldsymbol{a}$  is interpreted as the variance of the noise in the measurements, and this value was determined by the simulation design. In the "noise free" case, a very small value of  $\boldsymbol{a}$  was used, typically in the order of  $10^{-10}$  times the power of the scalp field produced by the test source with lowest scalp field power.

Localization error was defined as the distance between the actual test source and the location of the maximum in the imaging method. The spatial spread was defined identically as in (3), which corresponds to a measure of spatial standard deviation of the imaging method centered at the actual test source, and not at the imaging method's own maximum, since this would unjustifiably favor the method's performance.

#### Results

Figures 1a-1h summarize localization error, spatial spread, and estimated activity values for the three imaging methods (minimum norm, Dale, and sLORETA).

Note that the estimated activity values at test source locations cannot be compared among the different imaging methods, since these values are in different units for the different imaging methods. However, this feature is very informative for comparing the quality of the different methods. For example, from Fig 1a, the ratios of estimated source activity (maximum to minimum) were 850, 103, and, 30, for minimum norm, Dale, and sLORETA, respectively. This means that with sLORETA, some sources (especially deep ones) will be underestimated. However, sLORETA outperforms tremendously the minimum norm and the Dale methods in this aspect.

In all noise free simulations, only *s*LORETA has exact, zero error localization. In all noisy simulations, *s*LORETA has by far the lowest localization errors. In most cases, the spatial spread (i.e. "blurring") of *s*LORETA is smaller than that of the Dale method.

Figure 1a	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
Variable						Quartile	Quartile	
MNE	6430	37.83832	32.78719	0.00000	140.3567	21.79449	48.21825	22.17381
MNSSD	6430	52.19853	49.57677	29.37124	96.0995	43.22689	59.34685	11.85655
MNMaxAtPoint	6430	0.00132	0.00072	0.00002	0.0170	0.00034	0.00180	0.00150
DaleE	6430	33.49835	30.82207	0.00000	104.0432	21.79449	43.01163	15.89892
DaleSSD	6430	55.25780	54.72793	37.51842	86,7242	49.27447	60.61464	7.97651
DMaxAtPoint	6430	0.73773	0.64132	0.04674	4.7933	0.42049	0.93426	0.46353
LORE	6430	0.00000	0.00000	0.00000	0.0000	0.00000	0.00000	0.00000
LORSSD	6430	55.91575	55.66131	37.46555	79.1693		59.50099	5.50024
LORMaxAtPoint	6430	0.00109	0.00092	0.00015	0.0045	0.00063	0.00145	0.00060
Figure 1b								
. iguiro in	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
Variable						Quartile	Quartile	
MNE	6430	39.88576		0.00000	144.6548	22.36068	50.49752	
MNSSD	6430	54.08980	51.30133	30.05812	100.7998	44.34347	61.70680	12.82109
MNMaxAtPoint	6430	0.00124	0.00068	0.00002	0.0117	0.00033	0.00171	0.00135
DaleE	6430	33.58242	30.82207	0.00000	104.0432	21.79449	43.01163	16.05038
DaleSSD	6430	55.78534	55.27424		88.7353	49.70205	61.29503	8.08541
DMaxAtPoint	6430	24.60999	21.34088	1.34483	158.8102	14.14819	31.15955	15.45903
LORE	6430	4.58698	0.00000	0.00000	50.2494	0.00000	7.07107	6.29806
LORSSD	6430	56.84441	56.65639	36.48186	78.5615			5.70991
LORMaxAtPoint	6430	0.00104	0.00087	0.00010	0.0027	0.00058	0.00140	i n nonzel
LOMINAXALE OITIL	0430	0.00104	0.00007	0.00010	0.0037	0.00000	0.00140	0.00058
	0430	0.00104	0.00007	0.00010	0.0037	0.00030	0.00140	0.00036
Figure 1c	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
<b>Figure 1c</b> Variable	Valid N	Mean	Median	Minimum	Maximum	Lower Quartile	Upper Quartile	Std.Dev.
Figure 1c Variable MNE	Valid N 6430	Mean 39.04392	Median 32.40370	Minimum 0.00000	Maximum 118.3216	Lower Quartile 18.70829	Upper Quartile 54.08327	Std.Dev. 24.91432
Figure 1c Variable MNE MNSSD	Valid N 6430 6430	Mean 39.04392 51.74000	Median 32.40370 51.28205	Minimum 0.00000 22.53735	Maximum 118.3216 93.9798	Lower Quartile 18.70829 40.37547	Upper Quartile 54.08327 60.93124	Std.Dev. 24.91432 13.88708
Figure 1c Variable MNE MNSSD MNMaxAtPoint	Valid N 6430 6430 6430	Mean 39.04392 51.74000 0.00161	Median 32.40370 51.28205 0.00059	Minimum 0.00000 22.53735 0.00000	Maximum 118.3216 93.9798 0.0312	Lower Quartile 18.70829 40.37547 0.00021	Upper Quartile 54.08327 60.93124 0.00188	Std.Dev. 24.91432 13.88708 0.00260
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE	Valid N 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096	Median 32.40370 51.28205 0.00059 26.92582	Minimum  0.00000  22.53735  0.00000  0.00000	Maximum 118.3216 93.9798 0.0312 105.1189	Lower Quartile 18.70829 40.37547 0.00021 16.58312	Upper Quartile 54.08327 60.93124 0.00188 44.15880	Std. Dev. 24.91432 13.88708 0.00260 19.78573
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD	Valid N 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331	Median 32.40370 51.28205 0.00059 26.92582 56.32226	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE	Valid N 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE	Valid N 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298 0.0063	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080
Figure 1c Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137	Std.Dev. 24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732
Figure 1c  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Variable	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102 Mean	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076 Median	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298 0.0063	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.
Figure 1c  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE	Valid N 6430 6430 6430 6430 6430 6430 6430 Valid N	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102 Mean 44.27823	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076 Median 35.35534	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000	Maximum  118.3216  93.9798  0.0312  105.1189  90.9237  14.9132  0.0000  85.2298  0.0063  Maximum  166.2077	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528
Figure 1c  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD	Valid N 6430 6430 6430 6430 6430 6430 6430 Valid N 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102 Mean 44.27823 60.91795	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672	Maximum  118.3216  93.9798  0.0312  105.1189  90.9237  14.9132  0.0000  85.2298  0.0063  Maximum  166.2077  121.0887	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118
Figure 1c  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD  MNMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430 6430 Valid N 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean 44.27823 60.91795 0.00133	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000	Maximum  118.3216  93.9798  0.0312  105.1189  90.9237  14.9132  0.0000  85.2298  0.0063  Maximum  166.2077  121.0887  0.0313	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233
Figure 1c  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE	Valid N 6430 6430 6430 6430 6430 6430 6430 Valid N 6430 6430 6430 6430 6430	Mean 39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean 44.27823 60.91795 0.00133 33.24084	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040 27.38613	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000 0.00000	Maximum 118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298 0.0063  Maximum 166.2077 121.0887 0.0313 148.1553	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012 16.58312	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152 45.27693	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233 21.59598
Figure 1c  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean  39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean  44.27823 60.91795 0.00133 33.24084 59.52341	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040 27.38613 59.46867	Minimum  0.00000 22.53735 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000 28.68398	Maximum  118.3216  93.9798  0.0312  105.1189  90.9237  14.9132  0.0000  85.2298  0.0063  Maximum  166.2077  121.0887  0.0313  148.1553  107.2327	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012 16.58312 47.85251	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152 45.27693 70.34295	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233 21.59598 13.95973
Figure 1c  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean  39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean  44.27823 60.91795 0.00133 33.24084 59.52341 17.20670	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040 27.38613 59.46867 9.43516	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000 28.68398 0.16072	Maximum  118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298 0.0063  Maximum  166.2077 121.0887 0.0313 148.1553 107.2327 299.3523	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012 16.58312 47.85251 3.98560	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152 45.27693 70.34295 21.80584	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233 21.59598 13.95973 22.43950
Figure 1c  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORE  LORE  LORE  LORE  LORE  MNE  MNE  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean  39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean  44.27823 60.91795 0.00133 33.24084 59.52341 17.20670 14.24706	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040 27.38613 59.46867 9.43516 7.07107	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000 0.00000 28.68398 0.16072 0.00000	Maximum  118.3216  93.9798  0.0312  105.1189  90.9237  14.9132  0.0000  85.2298  0.0063  Maximum  166.2077  121.0887  0.0313  148.1553  107.2327  299.3523  147.3092	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012 16.58312 47.85251 3.98560 0.00000	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152 45.27693 70.34295 21.80584 18.70829	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233 21.59598 13.95973 22.43950 20.14731
Figure 1c  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1d  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint	Valid N 6430 6430 6430 6430 6430 6430 6430 6430	Mean  39.04392 51.74000 0.00161 32.01096 56.59331 0.85813 0.00000 55.07968 0.00102  Mean  44.27823 60.91795 0.00133 33.24084 59.52341 17.20670 14.24706	Median 32.40370 51.28205 0.00059 26.92582 56.32226 0.47528 0.00000 54.83463 0.00076  Median 35.35534 58.75015 0.00040 27.38613 59.46867 9.43516	Minimum  0.00000 22.53735 0.00000 0.00000 28.19129 0.00115 0.00000 32.32223 0.00000  Minimum  0.00000 23.72672 0.00000 28.68398 0.16072	Maximum  118.3216 93.9798 0.0312 105.1189 90.9237 14.9132 0.0000 85.2298 0.0063  Maximum  166.2077 121.0887 0.0313 148.1553 107.2327 299.3523	Lower Quartile 18.70829 40.37547 0.00021 16.58312 45.52004 0.19275 0.00000 51.05409 0.00044 Lower Quartile 20.61553 45.67004 0.00012 16.58312 47.85251 3.98560	Upper Quartile 54.08327 60.93124 0.00188 44.15880 66.56503 1.08481 0.00000 58.79261 0.00137 Upper Quartile 63.44289 73.79142 0.00152 45.27693 70.34295 21.80584 18.70829	Std.Dev.  24.91432 13.88708 0.00260 19.78573 13.19172 1.12301 0.00000 6.57732 0.00080  Std.Dev.  30.57528 18.58118 0.00233 21.59598 13.95973 22.43950

Firmer 4 a								
Figure 1e	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
Variable					THE AMERICAN	Quartile	Quartile	010.00
MNE	100	28.98679	25.36807	0.00000	91.1744	14.34387	39.08800	19.36050
MNSSD	100	53.90649	48.95036	23.76909	100.3630	41.37335	65.95370	18.61981
MNMaxAtPoint	100	0.00742	0.00317	0.00037	0.0666	0.00124	0.00961	0.01051
DaleE	100	42.29466	33.04389	0.00000	166.5460	19.13596	49.98529	35.84860
DaleSSD	100	71.99582	71.43313		110.9749	57.10882	84.82082	18.75077
DMaxAtPoint	100	0.20637	0.15743	0.01566	0.6211	0.09072	0.32076	0.14919
LORE	100	0.00000	0.00000	0.00000	0.0000	0.00000	0.00000	0.00000
LORSSD	100	62.80766	62.93061	27.10507	95.0718			16.19637
LORMaxAtPoint	100	0.00628	0.00494	0.00169	0.0227	0.00310	0.00861	0.00423
LORIVIAXALFUITI	100	0.00020	0.00434	0.00103	0.0227	0.00310	0.00001	0.00423
Figure 1f								
riguic ii	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
Variable						Quartile	Quartile	
MNE	100	35.9899	31.8368		167.1248	20.6669	43.8966	25.68608
MNSSD	100	69.1564	67.4566		142.7591	57.5730	77.9292	16.18904
MNMaxAtPoint	100	0.0048	0.0020	0.00036	0.0606	0.0009	0.0048	0.00816
DaleE	100	70.0574	51.9784	2.44020	167.3185	24.4963	120.5450	51.44283
DaleSSD	100	110.5303	112.2489	70.58756	130.1740	104.4996	118.6246	11.71376
DMaxAtPoint	100	2.0920	1.7073	-1.13414	7.0096	0.5953	3.4344	1.91975
LORE	100	5.9143	0.0000	0.00000	167.1248	0.0000	4.5863	18.62143
LORSSD	100	71.6598	71.5749	42.62740	138.2016	62.4085	80.4276	13.43835
LORMaxAtPoint	100	0.0037	0.0026	0.00079	0.0000	0.0045	0.0042	0.00254
CONTRACTOR OFFI	100	0.0037	0.0020	0.00073	0.0226	0.0015	0.0043	0.00354
	100	0.0037	0.0026	0.00079	0.0226	0.0015	0.0043	0.00354
Figure 1g								
Figure 1g	Valid N	Mean	Median	Minimum	Maximum	Lower	Upper	Std.Dev.
<b>Figure 1g</b> Variable	Valid N	Mean	Median	Minimum	Maximum	Lower Quartile	Upper Quartile	Std.Dev.
Figure 1g Variable MNE	Valid N	Mean 24.14936	Median 18.00278	Minimum 0.00000	Maximum 74.9658	Lower Quartile 8.30879	Upper Quartile 38.12478	Std.Dev. 20.31740
Figure 1g Variable MNE MNSSD	Valid N 100 100	Mean 24.14936 51.29687	Median 18.00278 48.30866	Minimum 0.00000 17.19826	Maximum 74.9658 111.1994	Lower Quartile 8.30879 36.99803	Upper Quartile 38.12478 62.50606	Std.Dev. 20.31740 19.73759
Figure 1g Variable MNE MNSSD MNMaxAtPoint	Valid N 100 100 100	Mean 24.14936 51.29687 0.00816	Median 18.00278 48.30866 0.00442	Minimum 0.00000 17.19826 0.00011	Maximum 74.9658 111.1994 0.0744	Lower Quartile 8.30879 36.99803 0.00102	Upper Quartile 38.12478 62.50606 0.01176	Std.Dev. 20.31740 19.73759 0.01065
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE	Valid N 100 100 100 100	Mean  24.14936 51.29687 0.00816 24.72421	Median 18.00278 48.30866 0.00442 18.61624	Minimum  0.00000  17.19826  0.00011  0.00000	Maximum 74.9658 111.1994 0.0744 121.7062	Lower Quartile 8.30879 36.99803 0.00102 8.83806	Upper Quartile 38.12478 62.50606 0.01176 31.34624	Std.Dev. 20.31740 19.73759 0.01065 23.32379
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD	Valid N 100 100 100 100 100	Mean 24.14936 51.29687 0.00816 24.72421 63.19210	Median 18.00278 48.30866 0.00442 18.61624 57.17276	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453	74.9658 111.1994 0.0744 121.7062 116.9826	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint	Valid N 100 100 100 100 100 100	Mean 24.14936 51.29687 0.00816 24.72421 63.19210 1.01759	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE	Valid N 100 100 100 100 100 100 100	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD	Valid N 100 100 100 100 100 100 100 100	Mean 24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE	Valid N 100 100 100 100 100 100 100	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000
Figure 1g Variable MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint	Valid N 100 100 100 100 100 100 100 100 100	Mean 24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint	Valid N 100 100 100 100 100 100 100 100	Mean 24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620	Median 18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058	74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint Variable	Valid N 100 100 100 100 100 100 100 100 Valid N	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean	Median  18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586  Median	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum	Maximum 74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint Figure 1h Variable MNE	Valid N 100 100 100 100 100 100 100 Valid N	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986	Median  18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586  Median  18.66037	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint Figure 1h Variable MNE MNSSD	Valid N  100 100 100 100 100 100 100 100 Valid N	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619	Median  18.00278  48.30866  0.00442  18.61624  57.17276  0.84079  0.00000  61.28746  0.00586  Median  18.66037  47.54100	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305 113.7560	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint  Figure 1h Variable MNE MNSSD MNMaxAtPoint	Valid N 100 100 100 100 100 100 100 100 100 10	Mean 24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean 24.45986 51.35619 0.00643	Median  18.00278  48.30866  0.00442  18.61624  57.17276  0.84079  0.00000  61.28746  0.00586  Median  18.66037  47.54100  0.00365	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305 113.7560 0.0361	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095	Std.Dev. 20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev. 21.15045 19.03778 0.00759
Figure 1g Variable MNE MNSSD MNMaxAtPoint DaleE DaleSSD DMaxAtPoint LORE LORSSD LORMaxAtPoint Variable MNE MNSSD MNMaxAtPoint DaleE	Valid N  100 100 100 100 100 100 100 100 100 1	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619 0.00643 26.01610	Median  18.00278  48.30866  0.00442  18.61624  57.17276  0.84079  0.00000  61.28746  0.00586  Median  18.66037  47.54100  0.00365  16.77787	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004 0.00000	Maximum 74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum 112.0305 113.7560 0.0361 140.5733	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088 7.61179	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095 28.2769	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778 0.00759 27.68495
Figure 1g  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1h  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD	Valid N  100 100 100 100 100 100 100 100 100 1	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619 0.00643 26.01610 63.01346	Median  18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586  Median  18.66037 47.54100 0.00365 16.77787 56.41088	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004 0.00000 27.18239	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305 113.7560 0.0361 140.5733 118.5519	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088 7.61179 45.99483	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095 28.2769 79.7158	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778 0.00759 27.68495 22.79567
Figure 1g  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1h  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DaleSSD  DaleSSD  DMaxAtPoint	Valid N  100 100 100 100 100 100 100 100 100 1	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619 0.00643 26.01610 63.01346 95.85396	Median  18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586  Median  18.66037 47.54100 0.00365 16.77787 56.41088 77.37389	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004 0.00000 27.18239 3.74402	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305 113.7560 0.0361 140.5733 118.5519 399.8879	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088 7.61179 45.99483 27.72483	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095 28.2769 79.7158 148.8874	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778 0.00759 27.68495 22.79567 88.56923
Figure 1g  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1h  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE	Valid N  100 100 100 100 100 100 100 100 100 1	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619 0.00643 26.01610 63.01346 95.85396 0.86365	Median  18.00278  48.30866  0.00442  18.61624  57.17276  0.84079  0.00000  61.28746  0.00586  Median  18.66037  47.54100  0.00365  16.77787  56.41088  77.37389  0.00000	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004 0.00000 27.18239 3.74402 0.00000	Maximum 74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum 112.0305 113.7560 0.0361 140.5733 118.5519 399.8879 24.3981	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088 7.61179 45.99483 27.72483 0.00000	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095 28.2769 79.7158 148.8874 0.0000	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778 0.00759 27.68495 22.79567 88.56923 3.73665
Figure 1g  Variable  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DMaxAtPoint  LORE  LORSSD  LORMaxAtPoint  Figure 1h  Variable  MNE  MNSSD  MNMaxAtPoint  DaleE  DaleSSD  DaleSSD  DaleSSD  DMaxAtPoint	Valid N  100 100 100 100 100 100 100 100 100 1	Mean  24.14936 51.29687 0.00816 24.72421 63.19210 1.01759 0.00000 59.88620 0.00666  Mean  24.45986 51.35619 0.00643 26.01610 63.01346 95.85396 0.86365	Median  18.00278 48.30866 0.00442 18.61624 57.17276 0.84079 0.00000 61.28746 0.00586  Median  18.66037 47.54100 0.00365 16.77787 56.41088 77.37389	Minimum  0.00000 17.19826 0.00011 0.00000 20.47453 0.05285 0.00000 23.63058 0.00092  Minimum  2.27264 21.34614 0.00004 0.00000 27.18239 3.74402	Maximum  74.9658 111.1994 0.0744 121.7062 116.9826 3.7928 0.0000 101.2460 0.0241  Maximum  112.0305 113.7560 0.0361 140.5733 118.5519 399.8879	Lower Quartile 8.30879 36.99803 0.00102 8.83806 48.07145 0.29971 0.00000 49.22148 0.00281 Lower Quartile 7.42037 37.58425 0.00088 7.61179 45.99483 27.72483	Upper Quartile 38.12478 62.50606 0.01176 31.34624 76.21105 1.54114 0.00000 69.53170 0.00957 Upper Quartile 33.5709 63.7877 0.0095 28.2769 79.7158 148.8874	Std.Dev.  20.31740 19.73759 0.01065 23.32379 21.03505 0.83204 0.00000 16.08875 0.00440  Std.Dev.  21.15045 19.03778 0.00759 27.68495 22.79567 88.56923

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Figure 1: "a-h" summarize in tabular form localization error, spatial spread, and estimated activity values for the three imaging methods (minimum norm, Dale, and sLORETA). (a) EEG, 6430 voxels, 3 unknowns per voxel, 25 electrodes, 6430 test sources with random orientation, no noise. (b) Same as (a), but with additive random noise (noise scalp field standard deviation equal to 0.12 times the test source with lowest scalp field standard deviation). (c) MEG, 6430 voxels, 3 unknowns per voxel, 25 sensors, 6430 test sources with random orientation, no noise. (d) Same as (c), but with additive random noise (noise scalp field standard deviation equal to 7.21 times the test source with lowest scalp field standard deviation). (e) EEG, 12980 voxels, 1 unknown per voxel, 101 electrodes, 100 randomly selected test sources, no noise. (f) Same as (e), but with additive random noise (noise scalp field standard deviation equal to 0.082 times the test source with lowest scalp field standard deviation). (g) MEG, 12980 voxels, 1 unknown per voxel, 101 sensors, 100 randomly selected test sources, no noise. (h) Same as (g), but with additive random noise (noise scalp field standard deviation equal to 8.49 times the test source with lowest scalp field standard deviation). MNE: minimum norm localization error (mm); MNSSD: minimum norm spatial standard deviation (mm); MNMaxAbs: estimated minimum norm activity value at test source location (arbitrary units); DaleE: Dale localization error (mm); DaleSSD: Dale spatial standard deviation (mm); DMaxAbs: estimated Dale activity value at test source location (arbitrary units); LORE: sLORETA localization error (mm); LORSSD: sLORETA spatial standard deviation (mm); LORMaxAbs: estimated sLORETA activity value at test source location (arbitrary units). Note that the estimated activity values at test source locations cannot be compared among the different imaging methods (see text for explanation).

#### **Discussion**

# Properties of sLORETA for EEG and MEG with unknown current density vector

The main properties of sLORETA, for both EEG and MEG, based on estimates of activity given by Eq. 20 are:

- 1. Exact, zero error, localization for test dipoles located at voxel positions, in the absence of noisy measurements.
- 2. Exact, zero error, localization of test dipoles *with arbitrary orientation*, located at voxel positions, in the absence of noisy measurements.
- 3. Exact, zero error, localization of test dipoles with arbitrary orientation, located at voxel positions, in the absence of noisy measurements, even under regularization (a > 0).
- 4. Exact, zero error, localization even for dipoles corresponding to a non-connected grid. For example, *cortical and non-connected subcortical grey matter can now be modeled as the solution space*. The error remains zero.

# Properties of sLORETA for EEG and MEG with known current density vector orientation, unknown amplitude

The main properties of sLORETA based on estimates of activity given by Eq. 22 are:

- 1. Exact, zero error, localization of test dipoles located at voxel positions, in the absence of noisy measurements.
- 3. Exact, zero error, localization of test dipoles located at voxel positions, in the absence of noisy measurements, even under regularization (a > 0).
- 4. Exact, zero error, localization even for dipoles corresponding to non-connected grids. For example, *cortical and non-connected subcortical grey matter can now be modeled as the solution space*. The error remains zero.
- 5. These results mean that the distribution of voxels can be quite arbitrary. For example, voxels do not have to be uniformly distributed from the geometrical point of view, although they should be uniformly distributed from the "grey matter density" point of view. Furthermore, different types of voxels may exist, some with unknown current density vector, and some with known current density orientation but unknown amplitude.

#### A Generalization

Suppose there exist reasons to *believe* that the *actual* (*prior*) current density variance is the diagonal, positive definite matrix **W**. This situation arises for example, in some approaches that force fMRI hot spot locations onto the EEG/MEG inverse solution (see for example (6)). In this case, Eq. 8 can be rewritten as:

$$\mathbf{F} = (\mathbf{K}\mathbf{W}^{1/2})(\mathbf{W}^{-1/2}\mathbf{J})$$
 Eq. 23

where the new unknown variable  $(\mathbf{W}^{-1/2}\mathbf{J})$  has been "pre-standardized" to have the identity matrix as its variance. This transformed variable plays the role of  $\mathbf{J}$  in all equations above, and  $(\mathbf{K}\mathbf{W}^{1/2})$  plays the role of the lead field in all equations above. All else proceeds identically with these new formal substitutions.

Note that the final sLORETA image corresponds to standardized estimates of activity (Eqs. 20 or 22) for the pre-standardized current density ( $\mathbf{W}^{-1/2}\mathbf{J}$ ).

Note that this approach can be applied to any actual (prior) current density variance W, as long as it is positive definite, and there exists a meaningful decomposition:

$$\mathbf{W} = \left(\mathbf{W}^{1/2}\right)^T \left(\mathbf{W}^{1/2}\right)$$
 Eq. 24

for the square root matrix  $\mathbf{W}^{1/2}$ . For example, this is the case of the classical LORETA method (2), where  $\mathbf{W}^{-1/2}$  embodies a discrete spatial Laplacian operator that achieves smoothness between neighboring voxels.

### Estimating the regularization parameter a

The regularization parameter *a* cannot be estimated from the functional in Eq. 8. However, it can be estimated via the cross-validation functional. This has been published in (14), in a reply to comments made to the paper in (2), which includes the detailed derivation of the method, and a set of equations that can be used efficiently in practice.

# sLORETA in experimental designs (statistical analysis of tomographic images)

Although *s*LORETA calculations produce pseudo-statistics, it is highly recommended to *not* use these values as actual statistics in testing of hypotheses in experimental designs.

Unlike the approach of Dale et al. (6), which makes use of their statistics for hypothesis testing, it is recommended to use *s*LORETA pseudo-statistic values as *estimates of activity*, and to apply standard techniques such as in statistical non-parametric mapping (SnPM) (7) for the analysis of experimental designs.

## sLORETA in testing for absolute activation

Note that tests for absolute activation with sLORETA can be performed by using the modified pseudo-statistics:

$$\left\{ \left[\mathbf{S}_{\hat{\mathbf{J}}}
ight]_{ll}^{-1/2}\hat{\mathbf{J}}_{l}$$
 Eq.  $25$ 

R.D. Pascual-Marqui. sLORETA. In press at: Methods & Findings in Experimental & Clinical Pharmacology (http://www.prous.com/journals/advpubmf.html) (SCI=0.644) (in Medline, etc.) 2002-November. Author's version.

$$\frac{\hat{J}_l}{\sqrt{\left[\mathbf{S}_{\hat{\mathbf{j}}}\right]_n}}$$
 Eq. 26

which correspond to Eqs. 20 and 22, respectively.

These pseudo-statistics should be used in an experimental design where there are N independent sLORETA images. For example, in a visual event related potential study with N=10 subjects, consider the 10 sLORETA images at the P100 latency.

In Eq. 25,  $\{[\mathbf{S_j}]_{ll}\}^{-1/2}$  denotes the unique symmetric inverse square root matrix of  $[\mathbf{S_j}]_{ll}$ . The pseudo-statistic in Eq. 26 has the form of a univariate Student's t-statistic, and the pseudo-statistic in Eq. 25 has the form of a Mahalanobis transform (10).

In the case of unknown amplitudes only, significant absolute activation is based on testing for zero mean of the pseudo-statistic in Eq. 26. SnPM can be used to correct for multiple comparisons and to bypass assumptions of Gaussianity.

In the case of unknown current density vector, significant absolute activation is based on testing for zero mean of the "*max-statistic*" of the pseudo-statistic in Eq. 25. This corresponds to the maximum of the absolute value among the three components. The "*max-statistic*" reduces three numbers per voxel to a single number per voxel. This is then used in SnPM to correct for multiple comparisons and to bypass assumptions of Gaussianity.

#### **Conclusions**

- 1. Localization error can not be improved beyond the present result. It is zero. Up to the present, no other instantaneous, distributed, discrete, imaging method for EEG/MEG has been published (to the best of the author's knowledge) that achieved perfect localization. All other previously published methods at best produced systematic non-zero localization errors (see (2), (6), (15), (16), (17)).
- 2. If the aim is localization, this new method, denoted as *s*LORETA, at least has perfect first order localization.
- 3. A distributed imaging method capable of exact localization of point sources is of great interest, since the principles of linearity and superposition would guarantee its trustworthiness as a functional imaging method, given that brain activity occurs in the form of a finite number of distributed "hot spots".
- 4. The detailed information provided here allows the reader to reproduce, check, test, and validate the previous claims.

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