

$$\sum_0^n (5i+2)^2 = \sum_0^n (25i^2 + 20i + 4) = \sum_0^n 25i^2 + \sum_0^n 20i + \sum_0^n 4 = 25 \sum_0^n i^2 + 20 \sum_0^n i + 4 \sum_0^n 1$$

$$25 \cdot \left(\frac{n(n+1)(2n+1)}{6} \right) + 20 \cdot \left(\frac{n^2+n}{2} \right) + 4 \cdot (n+1) = 25 \left(\frac{2n^3+3n^2+n}{6} \right) + 20 \left(\frac{n^2+n}{2} \right) + 4n+4$$

$$\frac{50n^3 + 75n^2 + 25n + 60n^2 + 60n + 24n + 24}{6} = \boxed{\frac{50n^3 + 135n^2 + 109n + 24}{6}} //$$

Indução:

$$1) \text{ Base Ind: } \frac{50 \cdot 0^3 + 135 \cdot 0^2 + 109 \cdot 0 + 24}{6} = \textcircled{4} \checkmark$$

2) Indução propriamente dita:

$$S_n = S_{n-1} + a_n \rightarrow S_n = \frac{50(n-1)^3 + 135(n-1)^2 + 109(n-1) + 24}{6} + (5n+2)^2$$

$$S_n = \frac{50(n^3 - 3n^2 + 3n - 1) + 135(n^2 - 2n + 1) + 109n - 109 + 24}{6} + 25n^2 + 20n + 4$$

$$S_n = \frac{50n^3 - 150n^2 + 150n - 50 + 135n^2 - 270n + 135 + 109n - 85 + 150n^2 + 120n + 24}{6}$$

$$\boxed{S_n = \frac{50n^3 + 135n^2 + 109n + 24}{6}} \checkmark //$$