

Transient Incompressible Navier-Stokes

$$-\nabla p + \mu \Delta \mathbf{u} = \frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u}$$
$$\nabla \cdot \mathbf{u} = 0$$

assume
steady

Steady Incompressible Navier-Stokes

$$-\nabla p + \mu \Delta \mathbf{u} = \mathbf{u} \cdot \nabla \mathbf{u}$$
$$\nabla \cdot \mathbf{u} = 0$$

neglect
convective term

Stokes

$$-\nabla p + \mu \Delta \mathbf{u} = \mathbf{0}$$
$$\nabla \cdot \mathbf{u} = 0$$

linearize
convective term

Oseen

$$-\nabla p + \mu \Delta \mathbf{u} = \mathbf{U} \cdot \nabla \mathbf{u}$$
$$\nabla \cdot \mathbf{u} = 0$$