

## Continuous Test Space

### DPG Form

$$b(u_h, v) = l(v)$$

### Optimal Test Functions

For each  $u \in U_h$ , find  
 $v_u \in V : (v_u, w)_V = b(u, w) \forall w \in V$

## Discrete Test Space

### DPG Form

$$b(u_h, v_h) = l(v_h)$$

### Optimal Test Functions

For each  $u \in U_h$ , find  
 $v_u \in V_{p+\Delta p} : (v_u, w)_V = b(u, w)$   
 $\forall w \in V_{p+\Delta p}$

### Stiffness Matrix

$$K_{ij} = b(e_i, v_{e_j}) = (v_{e_i}, v_{e_j})_V = (v_{e_j}, v_{e_i})_V = b(e_j, v_{e_i}) = K_{ji}$$

### Error (for adaptivity)

$$\begin{aligned} & \|u - u_h\|_E \\ &= \|R_V^{-1}(Bu_h - l)\|_V \end{aligned}$$

### Error (for adaptivity)

$$\begin{aligned} & \|u - u_h\|_E \\ &\approx \left\| R_{V_{p+\Delta p}}^{-1}(Bu_h - l) \right\|_{V_{p+\Delta p}} \end{aligned}$$