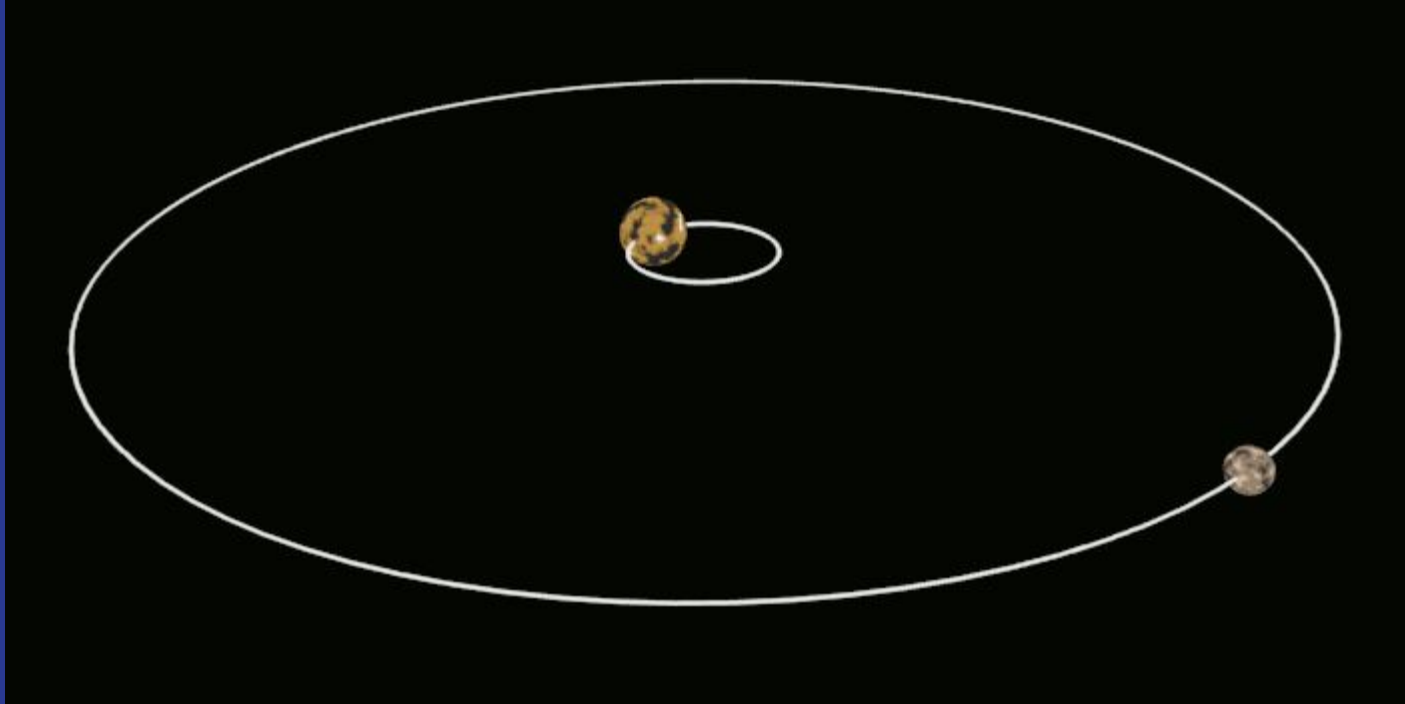
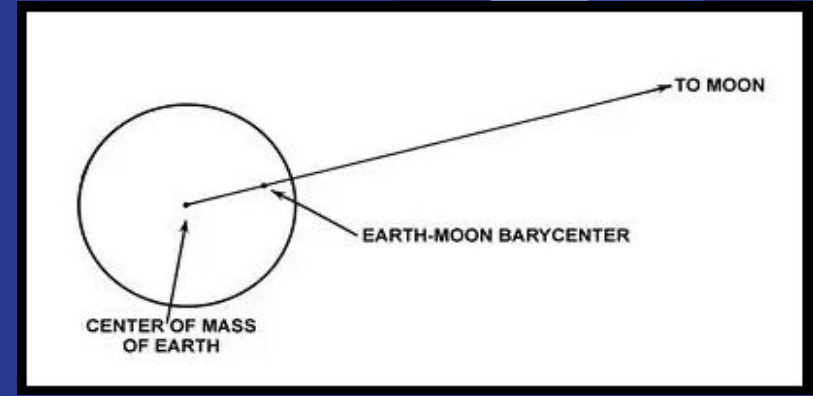
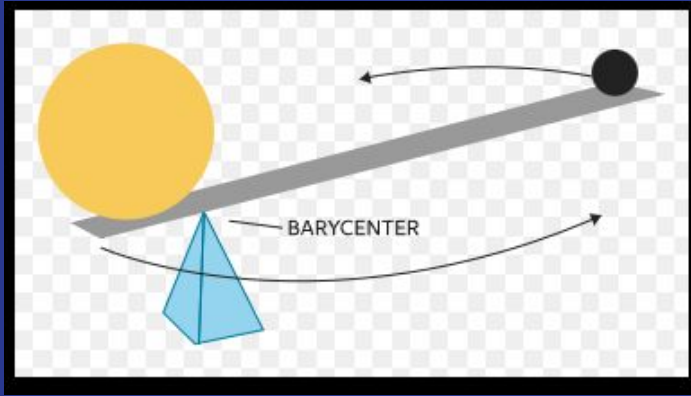


Pluto-Charon System

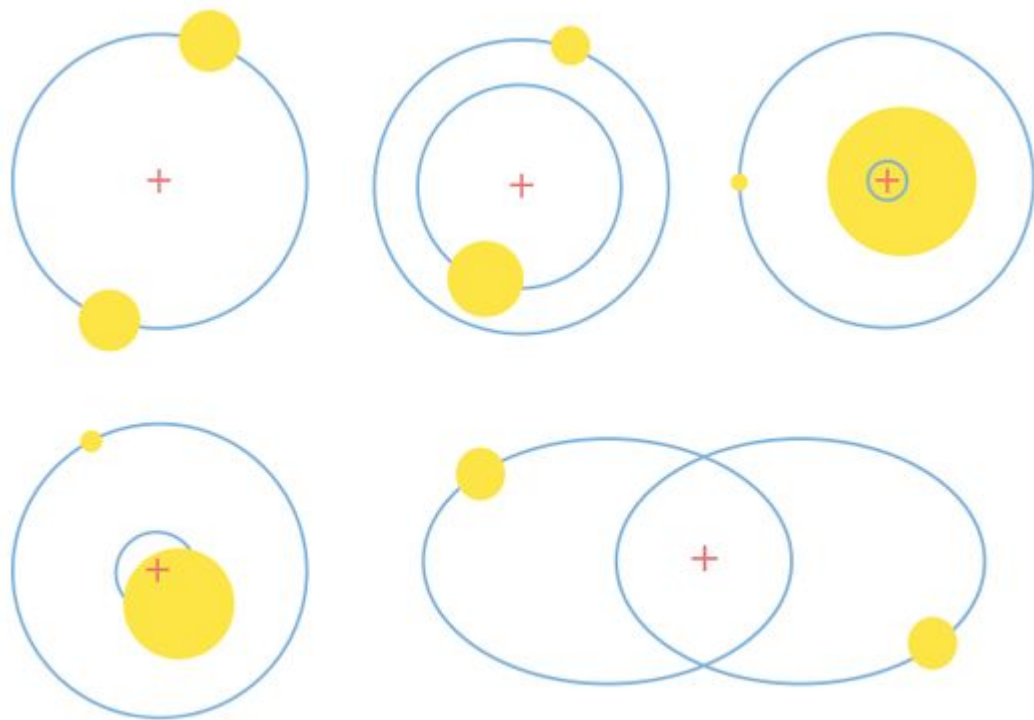


Elliptical Orbits (Why Planets and Satellites revolve in elliptical Orbits ??)

Barycentre:



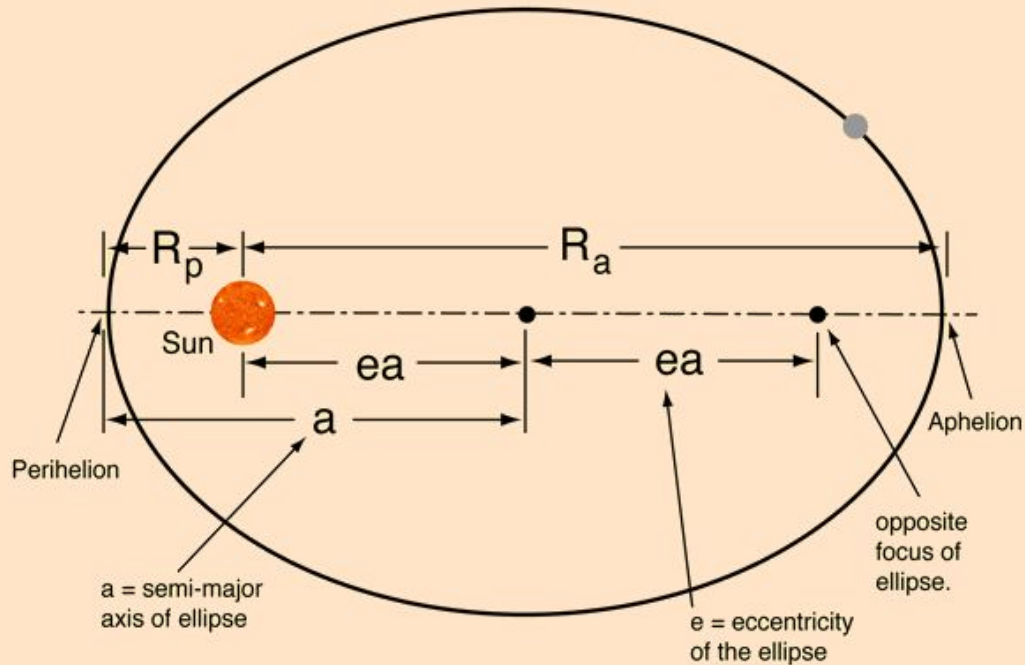
- In the two body system, when the objects moving under the gravitational influence of each other, then the objects revolve around a common centre which is known as Barycenter.
- Barycenter is the point lies between the centre of both the objects otherwise known as centre of the mass.
- Centre of mass of both the objects will be a point lying closer towards the heavier mass, but further away from the lighter mass. Lighter mass is revolving around the BC not around centre of heavier mass
- In Earth Moon System , In reality, the moon is revolving around the point, which lies inside the earth, around 4671 km (75 % of Earth Radius)



Different two-body systems with indicated orbits (blue) and barycenters (red).

The Law of Orbits

All planets move in elliptical orbits, with the sun at one focus.



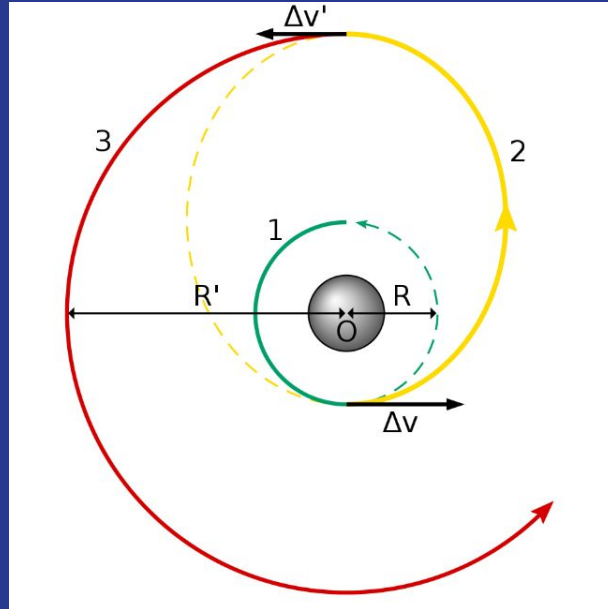
$$R_a = a(1+e) \quad R_p = a(1-e)$$

Orbit Transfers

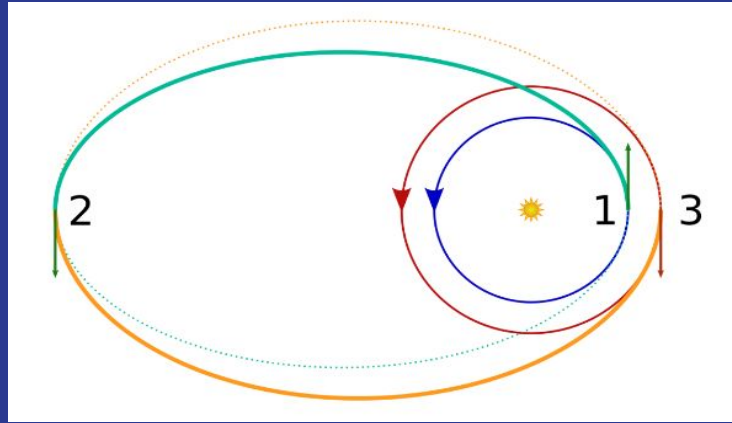
- **Gravity Assist:** A gravitational slingshot, gravity assist maneuver, or swing-by is the use of the relative movement and gravity of a planet or other celestial body to alter the path and speed of a spacecraft, typically in order to save propellant, time, and expense.

Gravity assistance can be used to accelerate, decelerate and/or redirect the path of a spacecraft. The "assist" is provided by the motion (orbital angular momentum) of the gravitating body as it pulls on the spacecraft

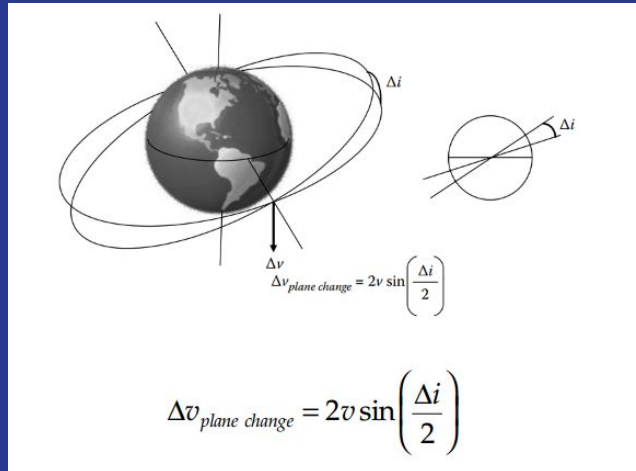
- **Hohmann transfer orbit** is an elliptical orbit used to transfer between two circular orbits of different altitudes, in the same plane.



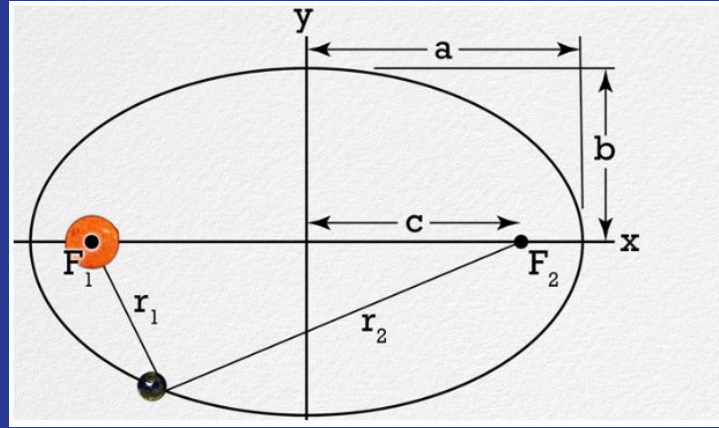
Bi-elliptic transfer is an orbital maneuver that moves a spacecraft from one orbit to another and may, in certain situations, require less delta-v than a Hohmann transfer maneuver.



Orbit plane inclination change



Orbital Energy invariance Law (Vis-Via Equation)



- **Energy of an object in an orbit is the sum of kinetic energy and Potential Energy.** And Energy and Momentum remained **conservative** throughout the orbit. **Angular Momentum at Periapsis is equivalent to Angular momentum at apoapsis.**
- Total Energy = $0.5 mV^2 - (GMm/r)$
- Specific Energy of mass(m) = $0.5 V^2 - (GM/r)$
- Angular Momentum of mass (m) moving around Mass (M) = $m * V * r$
- Specific Angular Momentum = $V*r$

M = Mass of larger Object

m = Mass of smaller object

r = Distance of that smaller mass from the centre of the larger mass.

V = Velocity of smaller mass

(-) indicates gravitational potential energy is a negative term.

$$G = 6.673 \times 10^{-11} \text{ Nm}^2 \text{ kg}^{-2}$$

Significance of Vis Via Eqn

WKT, **Angular Momentum at Periapsis is equivalent to Angular momentum at apoapsis.** Equating Angular Momentum at Periapsis and Apoapsis finally give Orbital Energy Invariance Law

$$0.5 V^2 = GM \left[\frac{1}{r} - \frac{1}{2a} \right]$$

Where, GM = Standard Gravitational Parameter (μ)

Significance of Vis Via Eqn,

- This Equation connects the object going from circular orbit to elliptical orbit.
- For a Circular Orbit, Semi major axis is radius of a circle. So Orbital Velocity of an object for an orbit of radius 'r'.

$$V = [GM/r]^{0.5}$$

- Escaping from circular orbit to space. Elliptical orbit of semi major axis is infinity.

$$V = [2GM/r]^{0.5}$$

This is escape speed and not much related to direction

Flight to Orbit

