

**The LNM Institute of Information Technology, Jaipur**  
**Department of Electronics and Communication Engineering**  
**Modeling and Simulation of MOS Transistor (ECE4181)**  
**Mid Term**

**Time:** 90 Minutes**Date:** 25/09/2019**Maximum Marks:** 30

**Instructions:** There are total 5 Questions. All the Questions are Compulsory.

**Q.1:** (a) In a MOS capacitor with an oxide layer thickness of 10 nm, the maximum depletion layer thickness is 100 nm. The permittivities of the semiconductor and the oxide layer are  $\epsilon_s$  and  $\epsilon_{ox}$  respectively. Assuming  $\epsilon_s / \epsilon_{ox} = 3$ , Find the ratio of the maximum capacitance of the minimum capacitance of this MOS capacitor. [4]

(b) What is Fermi Potential? Explain Fermi potential of P type Silicon and N type silicon. [2]

**Q.2:** (a) A voltage  $V_G$  is applied across the MOS capacitor with metal Gate and p – type silicon substrate at  $T = 300 K$ . The inversion carrier density (in number of units per unit area) for  $V_G = 0.8V$  is  $2 \times 10^{11} cm^{-2}$  and for  $V_G = 1.3V$ , the inversion carrier density is  $4 \times 10^{11} cm^{-2}$ .  
 What is value of inversion carrier density of  $V_G = 1.8V$ . [4]

(b) Explain the effect of gate-body voltage on surface conditions of a MOS Capacitor [2]

**Q.3:** (a) Calculate the flatband voltage for a p-type body with  $N_a = 3 \times 10^{18} cm^{-3}$ . A  $SiO_2$  insulator with a thickness = 2 nm, and an n-type polysilicon gate with  $N_d = 10^{20} cm^{-3}$ . The interface charge  $Q'$  is  $10^{-8} C/cm^2$ . Estimate the threshold voltage  $V_{T0}$  assuming at the onset of strong inversion, Surface potential  $\Psi_s = 2\phi_F$ . [4]



(Given:  $\phi_{ms} = -1.036 V$ , Temperature=300K, Body coefficient  $\gamma = 0.337$ , Intrinsic carrier concentration  $n_i = 10^{10} cm^{-3}$ )

(b) Derive the expression for carrier concentration at the surface of a MOS capacitor [2]

**Q.4:** (a) Briefly explain small signal capacitance in the two terminal MOS structure. [4]  
 Draw suitable diagrams and explain the capacitance value in each region of operation  
 (b) Draw and explain (i) and (ii) for all regions of operation when Flat band voltage is zero.  
 i. Surface potential vs Gate voltage  
 ii. Channel charge vs Gate voltage [2]

- Q.5:** (a) Neatly draw and explain the energy band diagram for the following in a MOS [4]  
Capacitor (Assume  $\phi_{ms} = 0$  and oxide interface charge=0)  
i. Flat Band condition  
ii. Accumulation  
iii. Depletion  
iv. Inversion
- (b) Write the summary of what you learnt in this Course and how it is useful for [2]  
your future perspective.

d) i: Ans: Maximum capacitance  $C_{max} = C_{ox}$  = Oxide capacitance

$$\text{Minimum Capacitance } C_{min} = \frac{C_{ox} \cdot C_{depletion}}{C_{ox} + C_{depletion}}$$

→ 1 mark  
→ 1 mark

$C_{ox}$  and  $C_{depletion}$  are capacitance per unit area.

$$\frac{C_{max}}{C_{min}} = \frac{\frac{C_{ox}}{C_{ox} \cdot C_{dep}}}{\frac{C_{ox} + C_{dep}}{C_{dep}}} = \frac{C_{ox} + C_{dep}}{C_{dep}}$$

$$= 1 + \frac{C_{ox}}{C_{dep}} = 1 + \frac{\epsilon_{ox}/t_{ox}}{\epsilon_s/d}$$

$$= 1 + \frac{\epsilon_{ox}}{\epsilon_s} \cdot \frac{d}{t_{ox}} = 1 + \frac{1}{3} \times \frac{100}{10} = 4.33 \quad \text{--- (2 marks)}$$

(ii) i: b: Refer class Note definition [1 mark]

P type & N type [0.5 + 0.5]

Q) 2: a) Ans:

For  $V_G = 0.8V$ , inversion carrier density  
 $= 2 \times 10^{11} \text{ cm}^{-2}$ .

For  $V_G = 1.3V$ , Inversion layer carrier density  $= 4 \times 10^{11} \text{ cm}^{-2}$ .

For MOS capacitor

$$\begin{aligned} \text{Change } Q &\propto (V_G - V_T) \\ Q_i &= k(V_G - V_T). \end{aligned} \quad \left. \right\} \text{Ans.} \quad (1)$$

$Q_i = Q_A \times \text{inversion carrier density}$ .

$$\frac{2 \times 10^{11} \cdot 2A}{4 \times 10^{11} \cdot 2A} = \frac{0.8 - V_T}{1.3 - V_T} \quad \text{--- 1 mark}$$

$$V_T = 0.3 \text{ V}$$

For  $V_G = 1.8 \text{ V}$

$$\frac{\varphi_i - 2 \cdot A}{2 \times 10^{11} q \cdot A} = \frac{1.8 - 0.3}{0.8 - 0.3}$$

$$\varphi_i = 6 \times 10^{11} / \text{cm}^2 . \quad [2 \text{ marks}]$$

Q) 2: b: For details refer class Note.

Flat Band

Accumulation

Depletion

Inversion

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Eq's

Diagrams

Explanations

[2 marks]

Q) 3: a:  $\Phi_F = \frac{kT}{q} \ln \left( \frac{N_A}{n_i} \right) = 0.508 \quad [1 \text{ mark}]$

$$2\Phi_F = 1.02 \text{ V}$$

$$\Phi_{ms} = -1.036 \text{ V}$$

$$V_{FB} = -1.036 - \frac{\Phi_0'}{Cox}$$

$$= -1.036 - 0.006 \text{ V} = -1.042 \text{ V} \quad [1 \text{ mark}]$$

$$V_{To} = -1.042 \text{ V} + 1.02 + 0.337 \sqrt{1.02 \text{ V}}$$

$$= 0.318 \text{ V}$$

[2 marks].

$$\frac{n_{\text{surface}}}{n_0} = e^{4s/\Phi_t} \quad \text{--- [2 marks]}$$

$$\Phi_F = \Phi_t \ln \frac{N_A}{n_i}$$

$$n_{\text{surface}} = N_A e^{(4s - 2\Phi_F)/\Phi_t}$$

For details, verify class note.

1) a : Diagram

Expression

{ 2 marks

Explanation for all region — 2 marks.

(b) : Diagram and explanation — 1 mark

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" → 1 mark,

[mark]

5) a : Diagram and explanation for each region - 1 mark

b : Discussed in class.

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