



# Database Systems

## L12: Revisions

## Parameterized Query

### Issue #1

SQL query contains **no variable**.

```
SELECT password  
FROM   Users  
WHERE  username = 'Alice';
```

Username = ''; DROP TABLE Users;  
SELECT '';

### Issue #2

Dynamic creation of SQL query is vulnerable to **SQL injection attack**.

```
query = "SELECT password "  
      + "FROM   Users "  
      + "WHERE  username = $1 + username + $2";
```

## Cursors

### Issue

Some problems are easier to solve in **imperative** way.

- i.e., describe how rather than what.
- e.g., finding the difference in mark between current student and next highest student (*in some order*) which may include duplicate values.

Functions/procedures with control flow is Turing complete.

- Anything that can be computed can be computed using functions/procedures.



## Function

### Declaration

```
CREATE OR REPLACE FUNCTION <name>
(<param_name> <param_type>,
 <param_name> <param_type>, ...)
RETURNS <return_type> AS $$
```

<code>

```
$$ LANGUAGE <language>;
```

### Note

- Returns a value.
- Invoke using **SELECT**.

## Procedure

### Declaration

```
CREATE OR REPLACE PROCEDURE <name>
(<param_name> <param_type>,
 <param_name> <param_type>, ...)
RETURNS <return_type> AS $$
```

<code>

```
$$ LANGUAGE <language>;
```

### Note

- Does not return any value.
- Invoke using **CALL**.

# Variables

## Declaration

```
DECLARE  
[<var_name> <data_type>];  
[<var_name> <data_type>];  
[<var_name> <data_type>];  
:  
:
```

## Assignment

```
<var_name> := <expression>
```

## Note

- <var\_name> is a variable name
- <data\_type> is a data type
- <expression> is an expression
  - Expression returns a value

INT DATE TIME

MONEY NUMERIC

TEXT

## Selection

## IF-THEN-ELSE

```
IF <condition> THEN  
  <statement>  
[ELSIF <condition> THEN  
  <statement>]  
[ELSIF <condition> THEN  
  <statement>]  
:  
[ELSE  
  <statement>]  
END IF
```

## Note

- ELSE IF
- You can have 0 or more ELSIF
    - Can also be spelled ELSEIF ↑
  - You can have 0 or 1 ELSE
    - Must be after all the ELSIF
  - <condition> is a conditional expression
    - Returns a boolean value ←
    - Condition is satisfied if it evaluates to → TRUE
  - <statement> is a statement
    - Code evaluated for its effect and not return value

## Repetition

## Loop

```
LOOP  
  EXIT <label> WHEN <condition>;  
  <statement>  
END LOOP;
```

→ CURSOR

## While-Loop

```
WHILE <condition>  
LOOP  
  <statement>  
END LOOP;
```

#

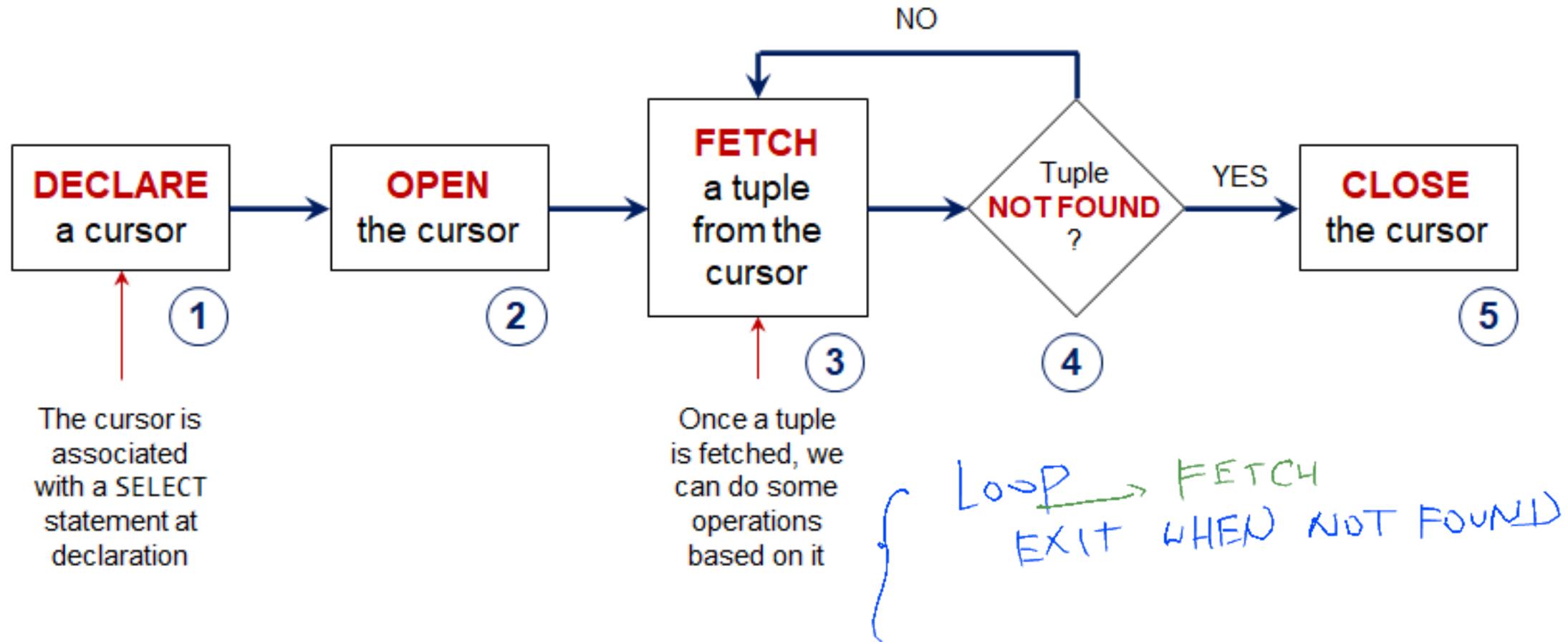
## Note

This is an infinite loop with a break condition.

## For-Loop

```
FOR <var_name> IN <lower> .. <upper>  
LOOP  
  <statement>  
END LOOP;
```

## Cursor

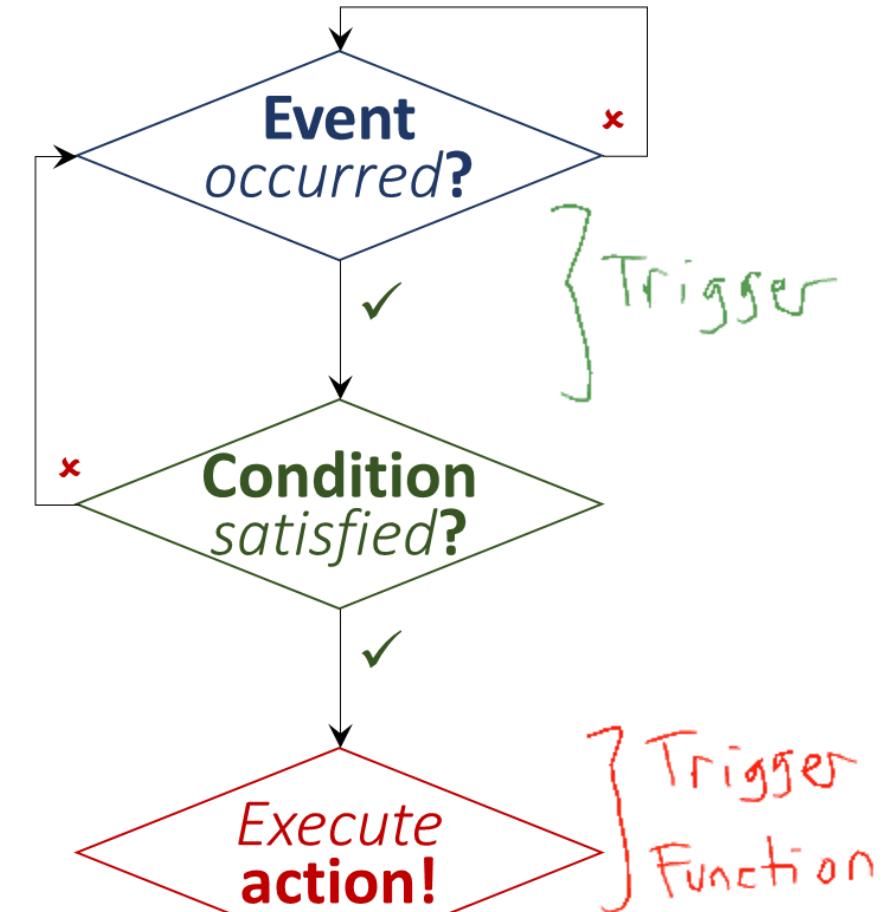
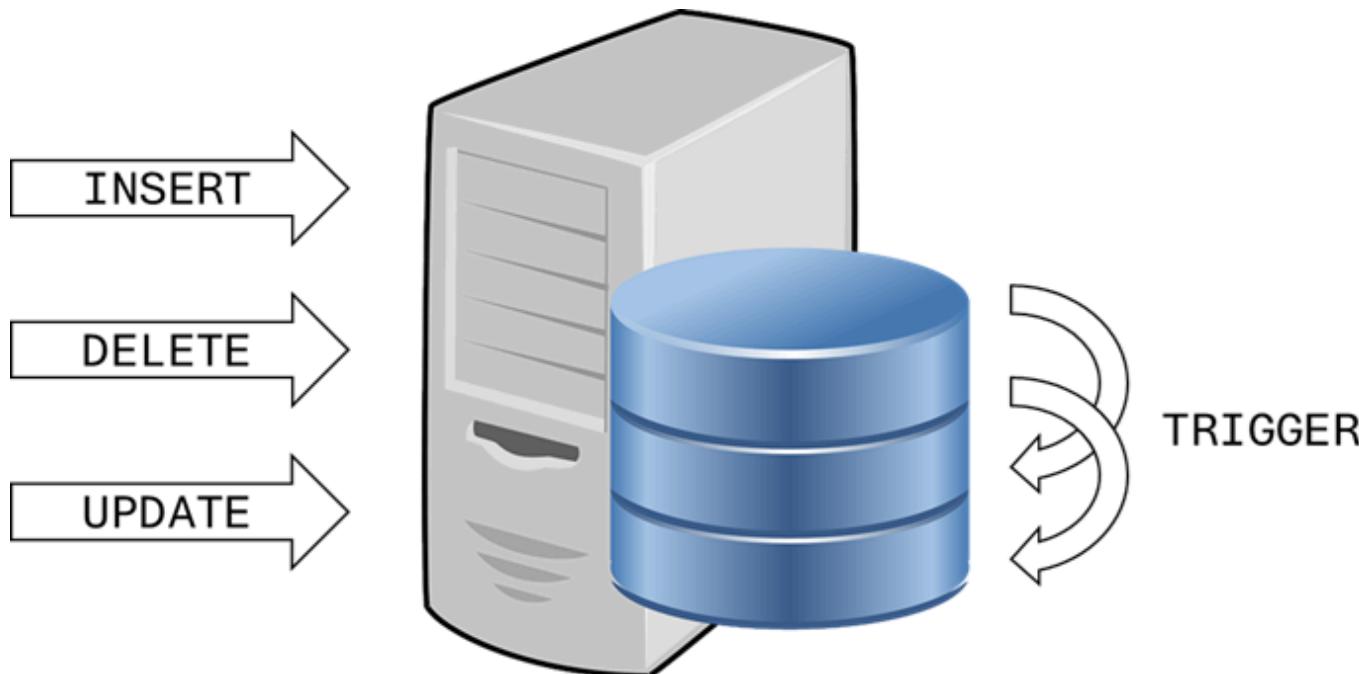


END Loop;

## Event-Condition-Action

### Event-Condition-Action

A **trigger** is a procedure or function executed when a database **event** occurs on a table.



## Trigger Function

### Syntax

```
CREATE OR REPLACE FUNCTION <func>()
RETURNS TRIGGER AS $$  
BEGIN
    <code>
END;
$$ LANGUAGE plpgsql;
```

## Trigger

### Syntax

```
CREATE TRIGGER <name>
<trigger_timing> <trigger_event>
    ON <table> ①
    FOR EACH <trigger_granularity>③
        [WHEN <condition>] ④
    EXECUTE FUNCTION <func>();
```

Same name

## Timings

## Keywords

BEFORE, AFTER, INSTEAD OF (*only for VIEW*)

- BEFORE trigger is executed **before the event**.
  - May modify/cancel the event by using return value.
- AFTER trigger is executed **after the event**
  - The event already occurred, cancellation done using EXCEPTION.

BEFORE

<event>

AFTER

## Example

```
CREATE TRIGGER log_all
AFTER <-->
    INSERT OR DELETE OR UPDATE ON Table
FOR EACH ROW
WHEN (condition)
EXECUTE FUNCTION log_function();
```

## Events

## Keywords

INSERT, DELETE, UPDATE

- May check for multiple events using **OR** keyword.
- The triggering operation is captured in the special variable called **TG\_OP** (*in uppercase*). 

## Example

```
CREATE TRIGGER log_all
AFTER
    INSERT OR DELETE OR UPDATE ON Table
FOR EACH ROW
WHEN (condition)
EXECUTE FUNCTION log_function();
```

## Granularity

**Keywords**

*row-level*      *statement-level*

**FOR EACH ROW, FOR EACH STATEMENT**

- Some checks may only need to be done once regardless of how many rows are affected.
  - e.g., checking all groups have more than one person.
- Return value has no effect on the subsequent operations.
  - Cancellation has to be done using **EXCEPTION** for statement-level.

**Example**

```
CREATE TRIGGER log_all
AFTER
    INSERT OR DELETE OR UPDATE ON Table
FOR EACH ROW
WHEN (condition)
EXECUTE FUNCTION log_function();
```

## Condition

## Keywords

## WHEN

- NO SELECT in WHEN()
- NO OLD in WHEN() for INSERT
- NO NEW in WHEN() for DELETE
- NO WHEN() for INSTEAD OF

## Example

```
CREATE TRIGGER log_all
AFTER
    INSERT OR DELETE OR UPDATE ON Table
FOR EACH ROW
WHEN (condition)
EXECUTE FUNCTION log_function();
```

## Variables

**Transition Variables**

- Every row-granularity operation on database can be abstracted into a modification of a row
  - **INSERT:** → new value (**NEW**)
  - **UPDATE:** old value (**OLD**) → new value (**NEW**)
  - **DELETE:** old value (**OLD**) →
- **OLD** and **NEW** signals our "***intention***"
- **NEW** is known even *before* the EVENT is executed
- **OLD** is known even *after* the EVENT finished executing
- The *intention* can be modified before the EVENT is executed
  - This is where the return value is important
  - Whatever we return is the new intention

**Non-NULL Value**

Events	OLD	NEW
INSERT	✗	✓
UPDATE	✓	✓
DELETE	✓	✗

Not all values are available for all operations. If the value is not available, the value is **NULL**.

- **OLD** is **NULL** value on **INSERT**.
- **NEW** is **NULL** value on **DELETE**.

## Return Values

**Non-NULL Value**

Events + Timings	NULL Tuple	Non-NULL Tuple $t$
BEFORE INSERT BEFORE UPDATE BEFORE DELETE	No insertion No update No deletion	Tuple $t$ will be inserted Tuple $t$ will be the <i>updated</i> tuple Deletion proceeds as normal ( $t$ is ignored)
AFTER INSERT AFTER UPDATE AFTER DELETE	<b>NO EFFECT</b>	<b>NO EFFECT</b>

## Deferrable Trigger

### Keywords

**CONSTRAINT, DEFERRABLE, INITIALLY DEFERRED, INITIALLY IMMEDIATE**

- Checked only at the **end of the transaction**.
- Require the **CONSTRAINT** keyword.
- Can only be **AFTER** trigger.
- Can only be **FOR EACH ROW** trigger.

```
CREATE CONSTRAINT TRIGGER <trigger_name>
<trigger_timing> <trigger_event> ON <trigger_table>
[ DEFERRABLE INITIALLY [ DEFERRED | IMMEDIATE ] ]
FOR EACH <trigger_granularity>
[ WHEN <trigger_condition> ]
EXECUTE FUNCTION <trigger_function_name>();
```

## Deferrable Trigger

### Activation Order

For the **same event** on the **same table**:

1. BEFORE statement-level triggers
2. BEFORE row-level triggers
3. EVENT for the given ROW
4. AFTER row-level triggers
5. AFTER statement-level triggers

Within the **same category**: alphabetical order.

a      => n v l  
b

### Note

IF (2) returns **NULL**, then (3) and (4) are cancelled.

# Break

---



Back by 12:39

## Quiz #1

### Question

Consider the attribute mapping on the right. Given the following requirement, which functional dependency captures this requirement?

Each shop can sell at most one product

$$\begin{cases} S_1, P_1 \\ S_1, P_2 \end{cases}$$

Attribute	Letter
User	U
Product	P
Shop	S
Cost	C
Date	D

### Choice

### Comment

A	$\{P, D\} \rightarrow \{S\}$	NO	<span style="color: red;">✗</span>
B	$\{P\} \rightarrow \{U\}$	NO	<span style="color: red;">✗</span>
C	$\{U, P, S, D\} \rightarrow \{C\}$	NO	<span style="color: red;">✗</span>
D	$(\{S\} \rightarrow \{P\})$	YES	<span style="color: green;">✓</span>
E	$\{P\} \rightarrow \{S\}$ <span style="color: red;">✗</span>	NO	<span style="color: red;">✗</span>

## Quiz #2

### Question

Consider the attribute mapping on the right. Given the following requirement, which functional dependency captures this requirement?

**No two different users can buy the same product**

Attribute	Letter
User	U
Product	P
Shop	S
Cost	C
Date	D

### Choice

### Comment

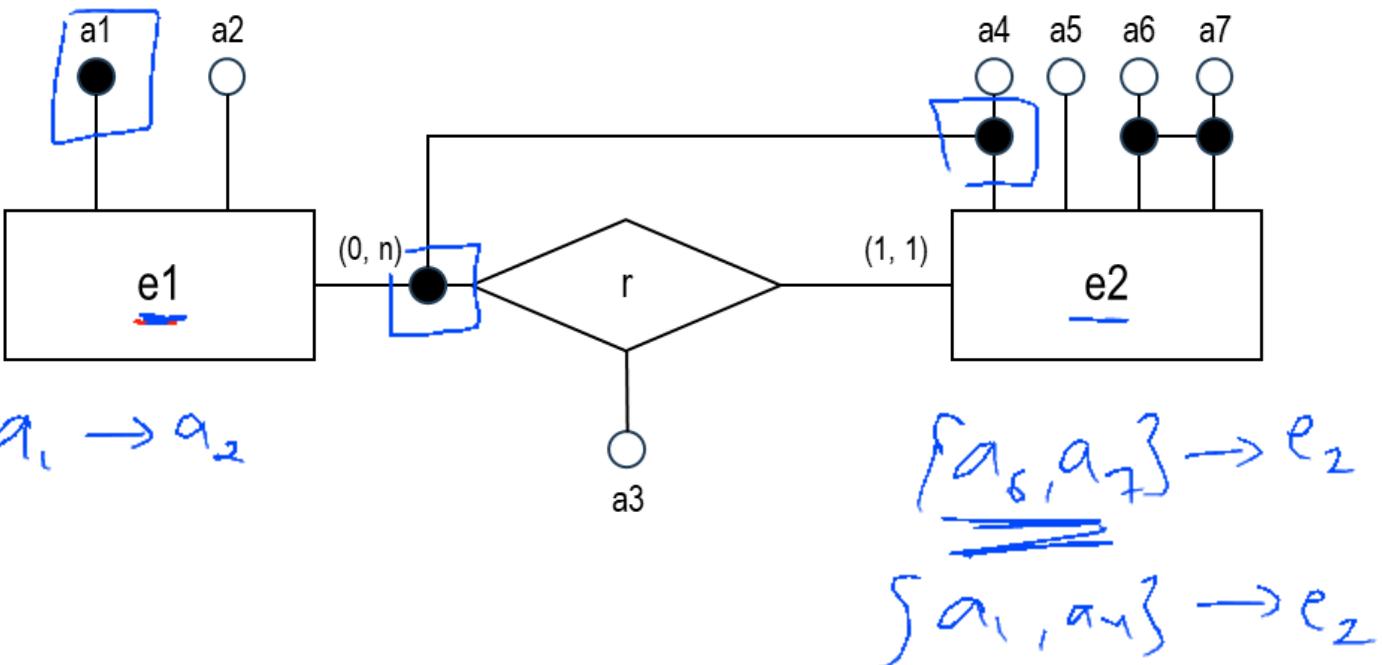
A	$\{P, D\} \rightarrow \{S\}$	NO	<span style="color: red;">✗</span>
B	$\{P\} \rightarrow \{U\}$	YES	<span style="color: green;">✓</span>
C	$\{U, P, S, D\} \rightarrow \{C\}$	NO	<span style="color: red;">✗</span>
D	$\{S\} \rightarrow \{P\}$	NO	<span style="color: red;">✗</span>
E	$\{P\} \rightarrow \{S\}$	NO	<span style="color: red;">✗</span>

$e_2(a_1, a_4, a_5, a_6, a_7)$

## Quiz #3

### Question

Consider the entity-relationship diagram on the right. Which functional dependency holds?



### Choice

### Comment

A	$\{a_1\} \rightarrow \{a_4\}$	NO: this is key of $e_1$	<input checked="" type="checkbox"/>
B	$\{a_4\} \rightarrow \{a_1\}$	NO: this is partial key	<input checked="" type="checkbox"/>
C	$\{a_4\} \rightarrow \{a_5, a_6, a_7\}$	NO: this is partial key	<input checked="" type="checkbox"/>
D	$\{a_6, a_7\} \rightarrow \{a_1\}$	YES: this is not partial key	<input checked="" type="checkbox"/>
E	None of the above	NO	<input checked="" type="checkbox"/>

## Quiz #4

### Question

Consider the functional dependency below. Which table on the right is a valid table with respect to the functional dependency below?

$$\{A, C\} \rightarrow \{B\}$$

T1

A	B	C
1	1	1
1	2	1
2	2	1

T2

A	B	C
1	1	1
1	1	1
2	2	2

T3

A	B	C
2	2	2
1	1	1
1	2	1

T4

A	B	C
1	1	1
2	1	2
1	2	1

### Choice

### Comment

A	T1	NO: see row 1 and 2	<input checked="" type="checkbox"/>
B	T2	YES: not proper because of duplicate but valid	<input checked="" type="checkbox"/>
C	T3	NO: see row 2 and 3	<input checked="" type="checkbox"/>
D	T4	NO: see row 1 and 3	<input checked="" type="checkbox"/>

## Example

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

### 1. Compute Candidate Key

Reduce complexity in checking

- Superkeys
- Candidate keys
- Prime attributes
- BCNF violation
- 3NF violation

### 2. Compute Minimal Cover

Reduce complexity in computing

- Attribute closure
- Projection
- Lossless-join
- Dependency preserving
- 3NF synthesis

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \underline{\{C\}} \rightarrow \underline{\{E\}}, \{B\} \rightarrow \underline{\{E\}}, \{B\} \rightarrow \underline{\{A\}}, \underline{\{C,E\}} \rightarrow \underline{\{D\}}, \{B,E\} \rightarrow \underline{\{C\}}, \underline{\{A,D\}} \rightarrow \underline{\{B\}}, \{A,D\} \rightarrow \underline{\{C\}} \}$$

## 1. Compute Candidate Key

$$A^+ = A$$

$$B^+ = ABCDE = R$$

$$C^+$$

$$D^+$$

$$E^+$$

$$\boxed{AC^+ \\ AD^+}$$

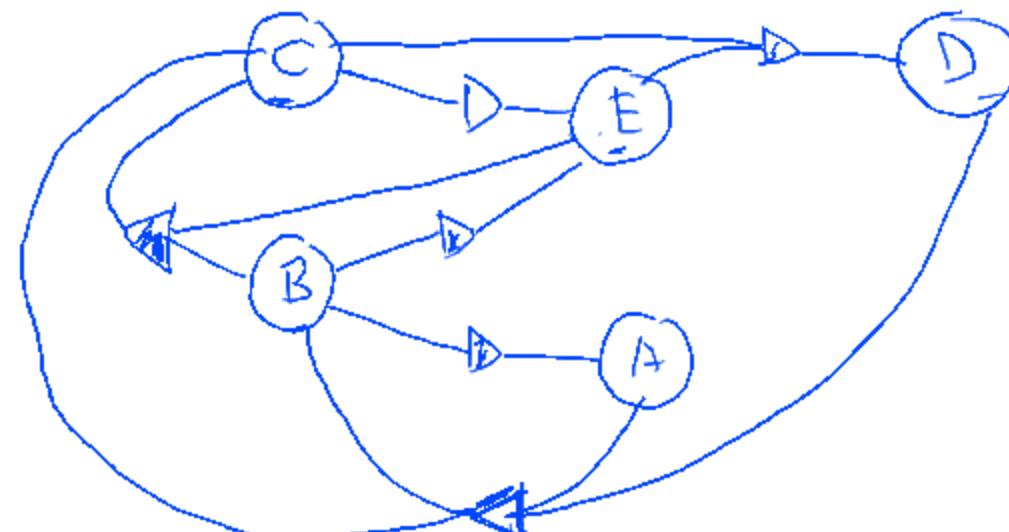
$$AE$$

$$CD^+$$

$$CE$$

$$DE$$

## 2. Compute Minimal Cover



## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

## Singleton

$$\{A\}^+$$

$$\{B\}^+$$

$$\{C\}^+$$

$$\{D\}^+$$

$$\{E\}^+$$

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

## Singleton

$$\{A\}^+ = \{A\}$$

$$\{B\}^+ = \{A,B,C,D,E\}$$

$$\{C\}^+ = \{C,D,E\}$$

$$\{D\}^+ = \{D\}$$

$$\{E\}^+ = \{E\}$$

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

## Singleton

$$\{A\}^+ = \{A\}$$

$$\{B\}^+ = \{A,B,C,D,E\}$$
 ✓

$$\{C\}^+ = \{C,D,E\}$$

$$\{D\}^+ = \{D\}$$

$$\{E\}^+ = \{E\}$$

## 2. Compute Minimal Cover

## Computation #1

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

Pair

{B}

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Pair

{B}

$$\{A,C\}^+$$

$$\{A,D\}^+$$

$$\{A,E\}^+$$

$$\{C,D\}^+$$

$$\{C,E\}^+$$

$$\{D,E\}^+$$

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Pair

{B}

$$\{A,C\}^+ = \{A,B,C,D,E\}$$

$$\{A,D\}^+ = \{A,B,C,D,E\}$$

$$\{A,E\}^+ = \{A,E\}$$

$$\{C,D\}^+ = \{C,D,E\}$$

$$\{C,E\}^+ = \{C,D,E\}$$

$$\{D,E\}^+ = \{D,E\}$$

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Pair

{B}

$$\{A,C\}^+ = \{A,B,C,D,E\} \quad \checkmark$$

$$\{A,D\}^+ = \{A,B,C,D,E\} \quad \checkmark$$

$$\{A,E\}^+ = \{A,E\}$$

$$\{C,D\}^+ = \{C,D,E\}$$

$$\{C,E\}^+ = \{C,D,E\}$$

$$\{D,E\}^+ = \{D,E\}$$

## 2. Compute Minimal Cover

## Computation #1

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

**Triple**

{A,D} {A,C} {B}

## 2. Compute Minimal Cover

## Computation #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Triple**

{A,D} {A,C} {B}

$$\{C,D,E\}^+ = \{C,D,E\}$$

## 2. Compute Minimal Cover

## Computation #1

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

**Ans:**

{A,D} {A,C} {B}

## 2. Compute Minimal Cover

## Computation #2

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C,E\} \rightarrow \{D\}$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Ans: {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C,E\} \rightarrow \{D\}$

Can we remove C?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Ans: {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C,E\} \rightarrow \{D\}$

Can we remove C?

$$\{E\}^+ = \{E\} \not\supseteq \{D\}$$

$\Rightarrow$  cannot remove C

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C,E\} \rightarrow \{D\}$

Can we remove E?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

Ans: {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C,E\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C,E\} \rightarrow \{D\}$

Can we remove E?

$$\{C\}^+ = \{C,D,E\} \supseteq \{D\}$$

$\Rightarrow$  can remove E

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider

$$\{B, \cancel{E}\} \rightarrow \{C\} \Rightarrow B \rightarrow C$$

$$\{A,D\} \rightarrow \{B\}$$

$$\{A,D\} \rightarrow \{C\}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B,E\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider

$$\begin{array}{ll} \{B,E\} \rightarrow \{C\} & \{B\} \rightarrow \{C\} \\ \{A,D\} \rightarrow \{B\} & \{A,D\} \rightarrow \{B\} \\ \{A,D\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \end{array}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{C\} \rightarrow \{E\}$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{C\} \rightarrow \{E\}$

$$\{C\}^+ = \{C,D\} \not\supseteq \{E\}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{C\} \rightarrow \{E\}$

$$\{C\}^+ = \{C,D\} \not\supseteq \{E\}$$

$\Rightarrow$  cannot remove  $\{C\} \rightarrow \{E\}$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{B\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{B\} \rightarrow \{E\}$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{l} \{C\} \rightarrow \{E\} \\ \underline{\{B\}} \rightarrow \underline{\{E\}} \\ \{B\} \rightarrow \{A\} \end{array}$$

$$\begin{array}{l} \{C\} \rightarrow \{D\} \\ \{B\} \rightarrow \{C\} \\ \underline{\{B\}} \rightarrow \underline{\{A\}} \end{array}$$

$$\begin{array}{l} \{A,D\} \rightarrow \{B\} \\ \{A,D\} \rightarrow \{C\} \end{array}$$

Consider  $\{B\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{B\} \rightarrow \{E\}$

$$\{B\}^+ = \{A,B,C,D,E\} \supseteq \{E\}$$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ \{B\} \rightarrow \{E\} & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{B\} \rightarrow \{E\}$ , can we remove this?

First assume no  $\{B\} \rightarrow \{E\}$

$$\{B\}^+ = \{A,B,C,D,E\} \supseteq \{E\}$$

$\Rightarrow$  can remove  $\{B\} \rightarrow \{E\}$

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{B\} \rightarrow \{A\}$ , can we remove this?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{C\} \rightarrow \{D\}$ , can we remove this?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{B\} \rightarrow \{C\}$ , can we remove this?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\begin{array}{lll} \{C\} \rightarrow \{E\} & \{C\} \rightarrow \{D\} & \{A,D\} \rightarrow \{B\} \\ & \{B\} \rightarrow \{C\} & \{A,D\} \rightarrow \{C\} \\ \{B\} \rightarrow \{A\} & & \end{array}$$

Consider  $\{A,D\} \rightarrow \{B\}$ , can we remove this?

## Computation #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

$$\{C\} \rightarrow \{E\}$$

$$\begin{array}{l} \{C\} \rightarrow \{D\} \\ \{B\} \rightarrow \boxed{C} \end{array}$$

$$\{B\} \rightarrow \{A\}$$

$$\begin{array}{l} \{A,D\} \rightarrow \{B\} \\ \{A,D\} \rightarrow \{C\} \end{array}$$

Consider  $\{A,D\} \rightarrow \{C\}$ , can we remove this?

## Computation #2

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

 $\{C\} \rightarrow \{E\}$        $\{C\} \rightarrow \{D\}$        $\{A,D\} \rightarrow \{B\}$   
 $\{B\} \rightarrow \{A\}$        $\{B\} \rightarrow \{C\}$

## Computation #3

 $R = \{A, B, C, D, E\}$  $\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$ 

## 1. Compute Candidate Key

**Ans:** {A,D} {A,C} {B}

## 2. Compute Minimal Cover

 $\{C\} \rightarrow \{E\}$        $\{C\} \rightarrow \{D\}$        $\{A,D\} \rightarrow \{B\}$   
 $\{B\} \rightarrow \{A\}$        $\{B\} \rightarrow \{C\}$ 

## 3. Compute Canonical Cover

 $\{C\} \rightarrow \{D,E\}$        $\{B\} \rightarrow \{A,C\}$        $\{A,D\} \rightarrow \{B\}$

## Quiz #1

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## Question

Which of the following is **NOT** a **superkey** of  $R$  with  $\Sigma$ ?

**Key:**  $\{B\}, \{A,C\}, \{A,D\}$

**Min Cover:**  $\{\{C\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C\} \rightarrow \{D\}, \{B\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}\}$

## Choice

## Comment

A	$\{B,E\}$	<i>NO: <math>\{B,E\} \supseteq \{B\}</math></i>	
B	$\{A,C,D\}$	<i>NO: <math>\{A,C,D\} \supseteq \{A,C\}</math></i>	
C	$\{C,D,E\}$	<i>YES: not superset of any key</i>	
D	$\{B\}$	<i>NO: <math>\{B\} \supseteq \{B\}</math></i>	

## Quiz #2

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## Question

Which of the following is a **key** of  $R$  with  $\Sigma$ ?

**Key:**  $\{B\}, \{A,C\}, \{A,D\}$



**Min Cover:**  $\{\{C\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C\} \rightarrow \{D\}, \{B\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}\}$

## Choice

## Comment

A	$\{B,E\}$	NO: $\{B\}$ is superkey	
B	$\{A,C,D\}$	NO: $\{A,C\}/\{A,D\}$ are superkey	
C	$\{C,D,E\}$	NO: not even superkey	
D	$\{B\}$	YES: minimal	

## Quiz #3

$$R = \{A, B, C, D, E\}$$

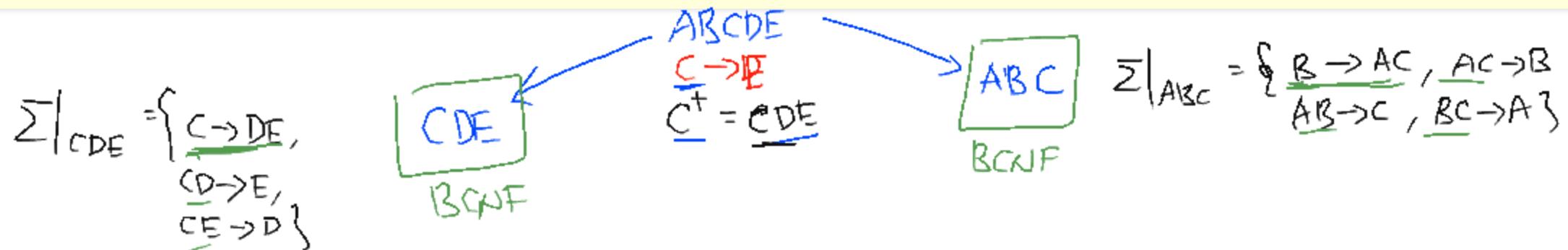
$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \underline{\{B\}} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## Question

Find one lossless-join decomposition of  $R$  with  $\Sigma$  in BCNF. Is it dependency preserving?

**Key:**  $\{B\}, \{A,C\}, \{A,D\}$

**Min Cover:**  $\{\underline{\{C\}} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \underline{\{C\}} \rightarrow \{D\}, \underline{\{B\}} \rightarrow \{C\}, \boxed{\{A,D\} \rightarrow \{B\}}\}$



## Quiz #4

$$R = \{A, B, C, D, E\}$$

$$\Sigma = \{ \{C\} \rightarrow \{E\}, \{B\} \rightarrow \{E\}, \{B\} \rightarrow \{A\}, \{C,E\} \rightarrow \{D\}, \{B,E\} \rightarrow \{C\}, \{A,D\} \rightarrow \{B\}, \{A,D\} \rightarrow \{C\} \}$$

## Question

Find one lossless-join dependency preserving decomposition of  $R$  with  $\Sigma$  in **3NF**.

**Key:** {B}, {A,C}, {A,D}

**Min Cover:** {C} → {E}, B → A, C → D, B → C, A,D → B

$$C \rightarrow DE$$

$$B \rightarrow AC$$

$$AD \rightarrow B$$

$$\{C, D, E\}$$

$$\{A, B, C\}$$

$$\{A, B, D\}$$

## Quiz #5

## Question

Consider an arbitrary  $R = \{A, B, C, D, E, F\}$  with an unknown  $\Sigma$ . Suppose that  $R$  is not in 3NF with respect to  $\Sigma$ . What is the maximum number of keys of  $R$  with  $\Sigma$ ?

Choice	Comment	
A 1	NO	✗
B 5	NO	✗
C 10	YES	✓
D 15	NO	✗
E 20	NO	✗
F 25	NO	✗
G 30	NO	✗
H 32	NO	✗

## Quiz #7

## Question

Consider an arbitrary relation  $R$ . Suppose there are two different sets of functional dependencies  $\Sigma_1$  and  $\Sigma_2$  such that the key of  $R$  with  $\Sigma_1$  is equal to the key of  $R$  with  $\Sigma_2$ .

Does it imply that  $\Sigma_1 \equiv \Sigma_2$ ?

$$\left. \begin{array}{l} \{A, B, C\} \\ \Sigma_1 = \{A \rightarrow B, A \rightarrow C\} \\ \Sigma_2 = \{A \rightarrow B, B \rightarrow C\} \end{array} \right| \begin{array}{l} \{AB \rightarrow C\} \\ \{A \rightarrow C\} \end{array}$$

## Choice

## Comment

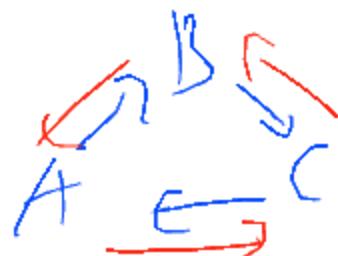
A	Yes	NO	<input checked="" type="checkbox"/>
B	No	YES: $R = \{A, B, C\}$ , $\Sigma_1 = \{A \rightarrow B\}$ , $\Sigma_2 = \{C \rightarrow B\}$	<input checked="" type="checkbox"/>

## Quiz #7

## Question

Consider an arbitrary set of functional dependencies  $\Sigma$ . Further consider **any** two *minimal cover* of  $\Sigma$  named  $\Sigma_1$  and  $\Sigma_2$ .

Does it imply that  $\Sigma_1 \cap \Sigma_2 \neq \emptyset$  (i.e., they share at least one common functional dependency)?



$$\Sigma_1 = A \rightarrow B \quad B \rightarrow C \quad C \rightarrow A$$

$$\Sigma_2 = A \rightarrow C \quad C \rightarrow B \quad B \rightarrow A$$

## Choice

## Comment

A	Yes	NO	<input checked="" type="checkbox"/>
B	No	YES: $\Sigma_1 = \{A \rightarrow B, B \rightarrow C, C \rightarrow A\}$ , $\Sigma_2 = \{A \rightarrow C, C \rightarrow B, B \rightarrow A\}$	<input checked="" type="checkbox"/>

```
postgres=# exit
```

Press any key to continue . . .

