

# Depth of Interval

Input file: standard input  
Output file: standard output  
Time limit: 2 seconds  
Memory limit: 1024 megabytes

You are given a positive integer  $N$  and a permutation  $P = (P_1, P_2, \dots, P_N)$  of  $(1, 2, \dots, N)$ .

For an integer pair  $(L, R)$ , we define the value  $f(L, R)$  recursively as follows.

- If  $1 \leq L < R \leq N$ : Let integers  $a$  and  $b$  be such that, among  $P_L, P_{L+1}, \dots, P_R$ , the smallest element and the second smallest element are  $P_a$  and  $P_b$ , respectively. Then we define

$$f(L, R) = f(\min(a, b) + 1, \max(a, b) - 1) + 1.$$

- Otherwise, we define  $f(L, R) = 0$ .

For each  $k = 1, 2, \dots, N$ , find the number of integer pairs  $(L, R)$  such that  $f(L, R) = k$ .

## Input

The input is given in the following format:

$N$
$P_1 \ P_2 \ \dots \ P_N$

- All input values are integers.
- $2 \leq N \leq 3 \times 10^5$
- $(P_1, P_2, \dots, P_N)$  is a permutation of  $(1, 2, \dots, N)$

## Output

Print  $N$  lines. For each  $k = 1, 2, \dots, N$ , print the number of integer pairs  $(L, R)$  satisfying  $f(L, R) = k$  on the  $k$ -th line.

## Examples

standard input	standard output
7 2 6 5 1 4 7 3	14 7 0 0 0 0 0
5 1 2 3 4 5	10 0 0 0 0
9 8 6 2 4 9 7 3 5 1	25 8 3 0 0 0 0 0

## Note

In the first example, the value  $f(1, 7)$  is computed as follows. Among  $P_1, P_2, \dots, P_7$ , the smallest element and the second smallest element are  $P_4$  and  $P_1$ , respectively. Thus,  $f(1, 7) = f(2, 3) + 1$ .

Next, among  $P_2, P_3$ , the smallest element and the second smallest element are  $P_3$  and  $P_2$ , respectively, so  $f(2, 3) = f(3, 2) + 1$ .

Since  $f(3, 2) = 0$ , we have  $f(2, 3) = 1$ , and therefore  $f(1, 7) = 2$ .