## **Product Matrix**

Input file: standard input
Output file: standard output

Time limit: 3 seconds Memory limit: 1024 megabytes

### The time limit for this problem might be tight.

You are given an  $N \times N$  square matrix P(x), where each element is a polynomials of degree 1 or less. The (i, j)-th element of P(x) is  $a_{i,j}x + b_{i,j}$ .

Compute each coefficient  $c_0, c_1, \ldots, c_M$  of the (1,1)-element  $f(x) = \sum_{i=0}^M c_i x^i$  of the product  $\prod_{i=0}^{M-1} P(2^i x) = P(x) P(2x) \ldots P(2^{M-1} x)$ , modulo  $(10^9 + 7)$ .

#### Constraints

- $1 \le N \le 6$
- $1 \le M \le 5 \times 10^5$
- $0 \le a_{i,j}, b_{i,j} < 10^9 + 7$

### Input

The input is given in the following format from standard input:

```
N \ M
a_{1,1} \ a_{1,2} \dots \ a_{1,N}
a_{2,1} \ a_{2,2} \dots \ a_{2,N}
\vdots
a_{N,1} \ a_{N,2} \dots \ a_{N,N}
b_{1,1} \ b_{1,2} \dots \ b_{1,N}
b_{2,1} \ b_{2,2} \dots \ b_{2,N}
\vdots
b_{N,1} \ b_{N,2} \dots \ b_{N,N}
```

# Output

Output the coefficients  $c_0, c_1, \ldots, c_M$  modulo  $(10^9 + 7)$ , each on a separate line in this order.

# **Examples**

standard input	standard output
2 2	4
1 2	8
3 4	14
2 0	
1 2	
(download in the attchments)	(download in the attchments)
(download in the attchments)	(download in the attchments)

#### Note

For the first sample case:

Since

$$P(x)P(2x) = \begin{pmatrix} x+2 & 2x \\ 3x+1 & 4x+2 \end{pmatrix} \begin{pmatrix} 2x+2 & 4x \\ 6x+1 & 8x+2 \end{pmatrix} = \begin{pmatrix} 14x^2+8x+4 & 20x^2+12x \\ 30x^2+24x+4 & 44x^2+28x+4 \end{pmatrix},$$

the answer is  $f(x) = 14x^2 + 8x + 4$ .