

# Problem C

## DNA Subsequences



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In this task, we consider sequences of nucleotides in a DNA molecule, which are strings composed of characters 'A', 'C', 'G', and 'T'. For each natural number  $k$ , there are  $4^k$  different  $k$ -letter nucleotide sequences. For a fixed natural number  $k$ , we say that a given nucleotide sequence  $s$  is  $k$ -rich if all  $k$ -letter nucleotide sequences are subsequences of  $s$  (not necessarily contiguous).

You are given an  $n$ -letter nucleotide sequence  $s$ . For each natural number  $k$  in the range  $[1, n]$ , output the minimum number of characters that must be changed in  $s$  to make it a  $k$ -rich sequence. Note that for each  $k$ , the result is calculated independently.

### Input

The first line of the input contains an integer  $n$  ( $1 \leq n \leq 200\,000$ ), representing the length of the string  $s$ .

The second line of the input contains an  $n$ -letter nucleotide sequence  $s$ , consisting only of characters 'A', 'C', 'G', and 'T'.

### Output

The output should consist of  $n$  integers; the  $k$ -th integer should represent the minimum number of characters that must be changed in  $s$  to make  $s$  a  $k$ -rich nucleotide sequence. If it is impossible to change the characters in  $s$  in the described way for a given  $k$ , then the  $k$ -th number should be  $-1$  instead.

### Example

For the input data:

8

AAGTAGAA

the correct result is:

1 3 -1 -1 -1 -1 -1 -1

**Explanation:** For  $k = 1$ , we can change  $s$  with one modification to, for example, AAGTCGAA. The resulting nucleotide sequence then contains all one-letter words as subsequences (in other words, each of the four letters appears at least once), and thus is 1-rich.

For  $k = 2$ , we can change  $s$  with three modifications to, for example, a 2-rich nucleotide sequence CAGTTGAC. Note that we could not change  $s$  to, for example, the sequence CCGTTGAA, as it does not contain the two-letter word AC as a subsequence.

For  $k > 2$ , it is impossible to make the sequence  $s$   $k$ -rich.