

# Problem H

## Merge Sort

The 3rd Universal Cup, Stage 40: Potyczki. Limits: 1024 MB, 3 s.

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*Merge sort* is one of the most well-known sorting algorithms. In this task, we use an implementation described by the following pseudocode:

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**Algorithm:** Implementation of the merge sort algorithm.

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1: function MERGESORT( $p, n$ )           ▷ Returns a sorted version of the list  $p = [p[0], p[1], \dots, p[n-1]]$ .
2:   if  $n = 1$  then
3:     return  $p$ 
4:    $\text{left} \leftarrow \text{MERGESORT}([p[0], \dots, p[\lceil n/2 \rceil - 1]], \lceil n/2 \rceil)$ 
5:    $\text{right} \leftarrow \text{MERGESORT}([p[\lceil n/2 \rceil], \dots, p[n-1]], \lceil n/2 \rceil)$ 
6:    $(i, j) \leftarrow (0, 0)$ 
7:    $\text{result} \leftarrow []$                                      ▷  $[]$  denotes an empty list.
8:   while  $i < |\text{left}|$  and  $j < |\text{right}|$  do             ▷  $|\text{left}|, |\text{right}|$  are lengths of lists  $\text{left}, \text{right}$ .
9:     if  $\text{left}[i] < \text{right}[j]$  then
10:      Append the value  $\text{left}[i]$  to the end of list  $\text{result}$ .
11:       $i \leftarrow i + 1$ 
12:     else
13:      Append the value  $\text{right}[j]$  to the end of list  $\text{result}$ .
14:       $j \leftarrow j + 1$ 
15:   Append the values  $\text{left}[i], \dots, \text{left}[|\text{left}| - 1]$  to the end of list  $\text{result}$ .
16:   Append the values  $\text{right}[j], \dots, \text{right}[|\text{right}| - 1]$  to the end of list  $\text{result}$ .
17:   return  $\text{result}$ 

```

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You are given numbers  $n$ ,  $a$ , and  $b$ . Your task is to count such permutations of numbers from 1 to  $n$  that sorting the permutation using the MERGESORT procedure performs a comparison of  $a$  and  $b$  at least once in line 9. Output the remainder of the division of the number of such permutations by 1 000 000 007 ( $10^9 + 7$ ).

Note that a permutation should be counted if numbers  $a$  and  $b$  are compared in any recursive call of the MERGESORT procedure, not necessarily in the shallowest call. Also note that we allow comparison of numbers  $a$  and  $b$  in any order. In other words, checking only one condition  $a < b$  or  $b < a$  is enough to count the permutation.

Additionally, you need to solve multiple test cases.

## Input

The first line of the input contains an integer  $t$  ( $1 \leq t \leq 10\,000$ ), representing the number of test cases.

The next  $t$  lines contain descriptions of consecutive test cases. The  $i$ -th line contains three integers  $n$ ,  $a$ , and  $b$  ( $2 \leq n \leq 1\,000\,000$ ;  $1 \leq a, b \leq n$ ;  $a \neq b$ ), as described in the task.

## Output

The output should consist of  $t$  lines. The  $i$ -th line should contain a single integer – the remainder of the division by  $10^9 + 7$  of the number of sought permutations in the  $i$ -th test case.

## Example

For the input data:

```

3
4 2 3
5 4 1
3 1 3

```

the correct result is:

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24
52
4

```

**Explanation:** In the first test case, the numbers 2 and 3 would be compared during the sorting of all permutations of length 4.

In the third test case, we will compare the numbers 1 and 3 during the sorting of permutations  $[1, 2, 3]$ ,  $[1, 3, 2]$ ,  $[2, 1, 3]$  and  $[3, 1, 2]$ .