

# Imagined Holly

Input file:            **standard input**  
Output file:           **standard output**  
Time limit:            1 second  
Memory limit:          512 megabytes

Given a non-negative integer matrix  $A$  of size  $n \times n$ . For a tree with  $n$  vertices, numbered from 1 to  $n$ , we call it a *holly tree* if and only if:

- For any pair of vertices  $u$  and  $v$  ( $1 \leq u, v \leq n$ ),  $A_{u,v}$  equals the bitwise XOR sum of the indices of the vertices on the simple path from  $u$  to  $v$  in the tree.

Your task is to construct a holly tree. It is guaranteed that such a holly tree always exists.

## Input

The first line of the input contains an integer  $n$  ( $2 \leq n \leq 2000$ ), which is the size of matrix  $A$ .

The next  $n$  lines of the input describe the matrix  $A$ . The  $i$ -th line contains  $n - i + 1$  integers  $A_{i,i}, A_{i,i+1}, \dots, A_{i,n}$  ( $0 \leq A_{i,j} < 2^{11}$ ). Note that  $A_{i,j} = A_{j,i}$  holds for all  $1 \leq i, j \leq n$ .

It is guaranteed that such a holly tree always exists.

## Output

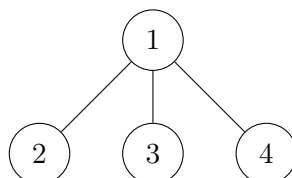
Output  $n - 1$  lines, each containing two integers  $u$  and  $v$  ( $1 \leq u, v \leq n$ ), representing an edge of the holly tree.

## Examples

standard input	standard output
2 1 3 2	1 2
4 1 3 2 5 2 0 7 3 6 4	1 2 1 3 1 4
6 1 7 4 5 2 3 2 1 6 7 0 3 5 4 3 4 3 2 5 5 6	4 1 2 3 6 4 5 2 4 2

## Note

In the second example, the tree in the output is shown in the following figure:



This tree is a holly tree. For example, for the pair of vertices  $(2, 4)$ , the simple path from 1 to 4 includes vertices 2, 1, and 4, with a bitwise XOR sum of  $2 \oplus 1 \oplus 4 = 7$ , which satisfies the constraint  $A_{2,4} = 7$  given in the input.