

Hidden Sequence Rotation

Input file: **standard input**
Output file: **standard output**
Time limit: **2 seconds**
Memory limit: **1024 megabytes**

This is an **interactive problem** (a problem where your program interacts with the judge via standard input/output).

You are given an integer N . The judge holds a hidden sequence $A = (A_0, \dots, A_{N-1})$ of length N , where each element is an integer between 1 and 10^5 . Note that throughout the problem, indices are 0-based.

For integers $s = 0, \dots, N-1$ and $l = 1, \dots, N$, define the sequence $A(s, l)$ as follows:

- A sequence of length l whose i -th element is $A_{(s+i) \bmod N}$ for $i = 0, \dots, l-1$.

You can make up to **20 queries** to the judge in the following format:

- You output a list of integer pairs $((s_0, l_0), \dots, (s_{k-1}, l_{k-1}))$ that satisfies the following constraints:
 - $1 \leq k \leq N$
 - $0 \leq s_i \leq N-1$
 - $1 \leq l_i \leq N$
 - $\sum_{i=0}^{k-1} l_i \leq N$
- In response, the judge returns all indices $i = 0, \dots, k-1$ such that $A(s_i, l_i)$ is lexicographically minimal among the sequences. In other words, the judge returns the set $\{i \mid 0 \leq i < k, A(s_i, l_i) = \min_{0 \leq i' < k} A(s_{i'}, l_{i'})\}$.

Using these queries, determine all values of $s = 0, \dots, N-1$ such that $A(s, N)$ is lexicographically minimal. In other words, identify the set $\{s \mid 0 \leq s < N, A(s, N) = \min_{0 \leq s' < N} A(s', N)\}$.

Note that the judge is **not adaptive**, meaning the sequence A is fixed before the interaction for each test case.

Input

The input is given in the following format:

N

- N is an integer in the range $1 \leq N \leq 10^5$.

Output

Once you have determined the answer, output it in the following format:

$! n$
 s_0
 s_1
 \vdots
 s_{n-1}

Here, n is an integer, each s_i is a distinct integer in the range $0 \leq s_i < N$, and it must be satisfied that

$$\{s_0, \dots, s_{n-1}\} = \{s \mid 0 \leq s < N, A(s, N) = \min_{0 \leq s' < N} A(s', N)\}.$$

Interaction Protocol

You may issue queries by outputting them to standard output in the following format:

```
? k
s0 l0
s1 l1
⋮
sk-1 lk-1
```

Ensure that your queries satisfy the conditions described above.

If the query is valid, the judge will respond with:

```
k'
i0
i1
⋮
ik'-1
```

Here, it holds that $k', i_0, i_1, \dots, i_{k'-1}$ are integers, $0 \leq i_0 < i_1 < \dots < i_{k'-1} < k$, and

$$\{i_0, i_1, \dots, i_{k'-1}\} = \{i \mid 0 \leq i < k, A(s_i, l_i) = \min_{0 \leq i' < k} A(s_{i'}, l_{i'})\}.$$

If your query is invalid (for example, if it violates the constraints or exceeds the allowed number of queries), the judge will respond with:

```
-1
```

If -1 is received, terminate your program immediately.

Notes for Interaction

- Be sure to flush the output after every print. Failure to do so may result in a Time Limit Exceeded (TLE) verdict.
- If your program produces invalid output or exits improperly during interaction, the judge's behavior is undefined.
- After printing the final answer or receiving -1, your program must terminate immediately. Failure to do so may result in undefined behavior.
- Avoid unnecessary newlines or spaces in your output, as these may be treated as formatting errors.

Note

The following is an example interaction for $N = 6$, with the hidden sequence $A = (1, 2, 3, 1, 2, 4)$:

Input	Output	Description
6		N is given.
	? 3 0 1 1 1 3 1	Querying sequences (1), (2), and (1).
2 0 2		Sequences at index 0 and 2 are lexicographically smallest.
	? 2 0 3 3 3	Querying sequences (1, 2, 3) and (1, 2, 4).
1 0		Sequence at index 0 is lexicographically smallest.
	! 1 0	Only $s = 0$ lexicographically minimizes the sequence $A(s, N)$, so that is printed as output.