

## Problem M. Dividing Chains

For a sequence  $z_1, z_2, \dots, z_n$ , consider a set  $S = \{1, n+1\}$ . Little Cyan Fish may perform the following operations **exactly** n-1 times:

- Choose an integer x s.t.  $x \notin S$  and  $1 < x \le n$ .
- Let l be the **predecessor** of x in S, i.e., the largest integer in S such that l < x.
- Let r be the successor of x in S, i.e., the smallest integer in S such that x < r.
- Do nothing **or** apply the following update to the sequence z
  - Reverse the subsegment  $z_l, z_{l+1}, \ldots, z_{r-1}$ , i.e.,  $z_i$  becomes  $z_{r-1-(i-l)}$  for all  $l \leq i \leq r-1$ .
- Update  $S \leftarrow S \cup \{x\}$ .

Obviously, in the end, S will become  $\{1, 2, ..., n, n + 1\}$ . For a given **monotonically non-decreasing** sequence  $a_1, a_2, ..., a_n$ , you need to count the number of sequences  $z_1, z_2, ..., z_n$ , modulo 998 244 353, that satisfy the following condition:

• There exists a way to apply the operations above to convert the sequence  $z_1, z_2, \dots, z_n$  to  $a_1, a_2, \dots, a_n$ .

This problem sounds non-sensical to Little Cyan Fish. Therefore, he asked you to solve this problem.

## Input

The first line of the input contains a single integer n ( $1 \le n \le 500$ ).

The next line of the input contains n integers  $a_1, a_2, \ldots, a_n$   $(1 \le a_1 \le a_2 \le \ldots \le a_n \le n)$ .

## Output

Output a single line containing a single integer, indicating the answer modulo 998 244 353.

## **Examples**

standard input	standard output
3	3
2 3 3	
5	29
1 1 3 3 5	
9	26276
1 2 3 5 5 6 7 8 9	