

# Maximum Segment Sum

Input file: *standard input*  
Output file: *standard output*  
Time limit: 1.5 seconds  
Memory limit: 1024 mebibytes

Calculate the number of sequences of  $-1$  and  $1$  of length  $n$  with maximum subsegment sum  $k$ . Solve this task for all  $k$  from  $0$  to  $n$ , and print the answers modulo  $998\,244\,353$ . The empty subsegment is considered too.

## Input

The input contains a single integer  $n$  ( $1 \leq n \leq 5 \cdot 10^5$ ).

## Output

Print  $n + 1$  integers modulo  $998\,244\,353$ : the answers for  $k = 0, 1, \dots, n$ .

## Examples

<i>standard input</i>	<i>standard output</i>
1	1 1
2	1 2 1
3	1 4 2 1
7	1 33 41 28 14 8 2 1

## Note

In the third example where  $n = 3$ , the maximum subsegment sum:

- of  $(-1, -1, -1)$  is  $0$ ;
- of  $(1, -1, -1)$ ,  $(-1, 1, -1)$ ,  $(-1, -1, 1)$ , and  $(1, -1, 1)$  is  $1$ ;
- of  $(1, 1, -1)$  and  $(-1, 1, 1)$  is  $2$ ;
- of  $(1, 1, 1)$  is  $3$ .