

# Fast Bogosort

Input file:            **standard input**  
Output file:          **standard output**  
Time limit:           3 seconds  
Memory limit:        1024 megabytes

Have you heard of Bogosort? Bogosort is a very interesting random sorting algorithm, which can sort an array of  $n$  elements in the best-case time complexity of  $O(n)$ . The algorithm can be described as follows:

- Uniformly shuffle the entire array.
- Check if the array is sorted.

Yes, after reading the algorithm above, you will realize that the expected time complexity of Bogosort is actually  $O(n \cdot n!)$ !

Bogosort is so fascinating, but it runs so slowly, which is quite unfortunate. Therefore, let's help improve it by optimizing it using the following algorithm, Fast Bogosort, to sort a permutation of numbers from 1 to  $n$ :

- If the array is already sorted, stop.
- Otherwise, divide the array into as many segments as possible, such that each segment corresponds to the interval  $[l_i, r_i]$  and contains exactly the permutation of numbers  $[l_i, r_i]$ . Note that the segments must not overlap and their union must be the entire range  $[1, n]$ .
- For each segment  $[l, r]$  that has been divided, if  $l < r$ , call `shuffle(l, r)` to uniformly shuffle the numbers within that segment.

If we only care about the number of calls to `shuffle(l, r)`, it is clear that the original Bogosort has an expected number of calls of  $n!$ . Now, given a permutation of numbers from 1 to  $n$ , please calculate the expected number of times Fast Bogosort will call `shuffle(l, r)`.

## Input

The first line of the input contains one integer  $n$  ( $1 \leq n \leq 10^5$ ), indicating the length of the array.

The second line contains  $n$  integers  $a_1, a_2, \dots, a_n$ , indicating the content of the array. It is guaranteed that  $a_1, a_2, \dots, a_n$  form a permutation of  $1 \sim n$ .

## Output

Output the expected number of times Fast Bogosort will call `shuffle(l, r)`. It can be proved that the expected number is always a rational number. Additionally, under the constraints of this problem, it can also be proved that when that value is represented as an irreducible fraction  $\frac{P}{Q}$ , we have  $Q \not\equiv 0 \pmod{998244353}$ . Thus, there is a unique integer  $R$  such that  $R \times Q \equiv P \pmod{998244353}$ ,  $0 \leq R < 998244353$ . Report this  $R$ .

## Examples

standard input	standard output
5 2 1 5 3 4	332748123
10 4 2 3 1 6 5 9 7 10 8	453747445