

# Problem N

## Frequency Function

The 3rd Universal Cup, Stage 40: Potyczki. Limits: 1024 MB, 2 s.

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Let's define a function  $f(a)$  which takes as an argument a sequence of  $n$  integers  $a_1, a_2, \dots, a_n$  in the range  $[0, n]$  and returns a sequence  $b_1, b_2, \dots, b_n$  such that  $b_i$  is the number of occurrences of the number  $i$  in the sequence  $a_1, a_2, \dots, a_n$ .

Additionally, let's define its  $k$ -fold composition:

$$f^k(a) = \begin{cases} a & \text{for } k = 0, \\ f(f^{k-1}(a)) & \text{for } k > 0. \end{cases}$$

You are given a sequence  $a_1, a_2, \dots, a_n$ . Your task is to handle two types of queries:

- 1  $v$   $x$  – Change the value of  $a_v$  to  $x$ .
- 2  $k$   $v$  – Print the  $v$ -th element of the sequence  $f^k(a)$ .

## Input

The first line of the input contains two integers  $n$  and  $q$  ( $1 \leq n \leq 300\,000$ ;  $1 \leq q \leq 500\,000$ ), representing the length of the input sequence and the number of queries, respectively.

The second line of the input contains a sequence of  $n$  integers  $a_1, a_2, \dots, a_n$  ( $0 \leq a_i \leq n$ ).

The next  $q$  lines contain descriptions of the queries in the format specified in the problem statement. It holds that  $1 \leq v \leq n$ ,  $0 \leq x \leq n$  and  $0 \leq k \leq 300\,000$ .

It is guaranteed that there will be at least one query of the second type.

## Output

The output should contain as many lines as there are queries of the second type. The  $i$ -th line should contain a single integer – the answer to the  $i$ -th query of the second type.

## Example

For the input data:

```
6 6
2 1 2 3 0 3
2 3 2
1 5 2
2 0 2
1 2 3
2 0 2
2 2 3
```

the correct result is:

```
1
1
3
2
```

**Explanation:** Let's analyze the last query. We have:

- $f^0(a) = [2, 3, 2, 3, 2, 3]$ ,
- $f^1(a) = [0, 3, 3, 0, 0, 0]$ ,
- $f^2(a) = [0, 0, 2, 0, 0, 0]$ .

The answer to this query is 2.