

# Grid Problem

Input file:            **standard input**  
Output file:         **standard output**  
Time limit:          3 seconds  
Memory limit:       256 megabytes

Yotsugi was playing with a grid  $A$  of height  $h$  and width  $w$ , which was initially filled with zeroes by applying the following 2 operations in some order:

- Pick values  $i, j$  ( $0 \leq i \leq h-1, 0 \leq j \leq w-1$ ) and sign  $+$  or  $-$ , and change values  $A_{i,j}, A_{i,j+1}, A_{i+1,j}, A_{i+1,j+1}$  to  $A_{i,j} \pm 2, A_{i,j+1} \pm 1, A_{i+1,j} \pm 1, A_{i+1,j+1} \pm 2$  correspondingly, where  $\pm$  is replaced with the chosen sign. Here Yotsugi considers  $A_{h,j}$  to be equivalent to  $A_{0,j}$  and  $A_{i,w}$  to be equivalent to  $A_{i,0}$ . In other words, she treats her grid as a torus.
- Pick values  $i, j$  ( $0 \leq i \leq h-1, 0 \leq j \leq w-1$ ) and sign  $+$  or  $-$ , and change values  $A_{i,j}, A_{i,j+1}, A_{i,j+2}, A_{i+1,j}, A_{i+1,j+1}, A_{i+1,j+2}, A_{i+2,j}, A_{i+2,j+1}, A_{i+2,j+2}$  to  $A_{i,j} \pm 2, A_{i,j+1} \pm 5, A_{i,j+2} \pm 2, A_{i+1,j} \pm 5, A_{i+1,j+1} \pm 5, A_{i+1,j+2} \pm 5, A_{i+2,j} \pm 2, A_{i+2,j+1} \pm 5, A_{i+2,j+2} \pm 2$  correspondingly, where  $\pm$  is replaced with the chosen sign. As in the previous operation, Yotsugi treats the grid as a torus.

For easier understanding of the operations, refer to the notes section.

On the next day, the grid was eaten by the fire-breathing slug, and now Yotsugi wonders how many possible grids she could have if, after she finished applying operations, all values  $A_{i,j}$  lay in  $[0, k]$ . Notice that when Yotsugi was applying operations, values  $A_{i,j}$  could be negative or exceed  $k$ . Since the answer can be large, help her find it modulo  $10^9 + 9$ .

## Input

First line contains 3 integers  $h, w, k$  ( $3 \leq h, w \leq 1000, 1 \leq k \leq 10^9$ ) — size of the grid and maximum possible value in the grid.

## Output

Output the answer to the problem modulo  $10^9 + 9$ .

## Examples

standard input	standard output
3 3 1	2
4 4 52	972950693
7 10 123	93519598

## Note

For example, if we had a  $4 \times 4$  matrix, we could apply the operations in the following manner:

Before					After			
0	0	0	0	→	0	0	-2	-1
0	0	0	0		0	0	-1	-2
0	0	0	0		0	0	0	0
0	0	0	0		0	0	0	0

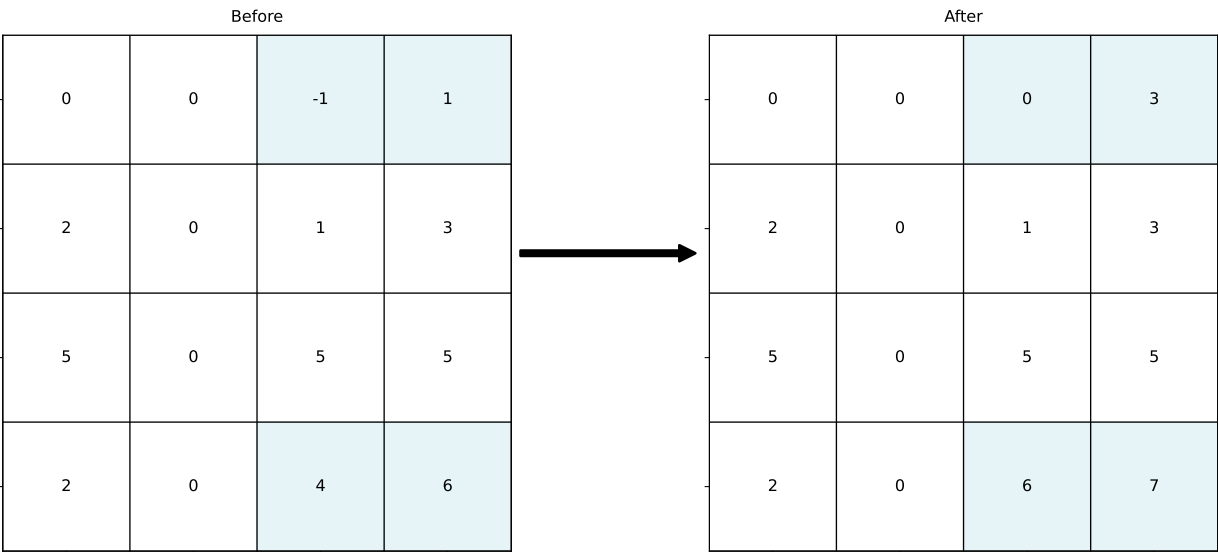
Applying the first operation with sign  $-$ .

Before					After			
0	0	-2	-1	→	0	0	-2	-1
0	0	-1	-2		2	0	1	3
0	0	0	0		5	0	5	5
0	0	0	0		2	0	2	5

Applying the second operation with sign  $+$ .

Before					After			
0	0	-2	-1	→	0	0	-1	1
2	0	1	3		2	0	1	3
5	0	5	5		5	0	5	5
2	0	2	5		2	0	4	6

Applying the first operation with sign +.



Applying the first operation with sign +.

And since all values lie in  $[0, 42]$ , this is one of the matrices you are asked to count in the second sample.