

Problem B

Collatz Sum

The 3rd Universal Cup, Stage 40: Potyczki. Limits: 1024 MB, 0.5 s.

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We define the function f on natural numbers:

$$f(x) = \begin{cases} x/2, & \text{if } x \text{ is even,} \\ 3x + 1, & \text{if } x \text{ is odd.} \end{cases}$$

Let $g(x)$ be the result of applying f to itself k times:

$$g(x) = \underbrace{f(f(\dots f(x) \dots))}_{k \text{ times}}.$$

Your task is, given N and k , to compute the sum

$$S = \sum_{x=1}^N g(x) \pmod{10^9 + 7}.$$

Input

A single line containing two integers N and k ($1 \leq N \leq 10^{12}$, $0 \leq k \leq 32$).

Output

Output a single number – the value of the sum S modulo $10^9 + 7$.

Example

For the input:

10 2

the correct output is:

73

Whereas for the input:

999888777666 1

the correct output is:

990122835

Explanation of the examples:

In the first example, the values of the function $g(i)$ for consecutive i are: 2, 4, 5, 1, 8, 10, 11, 2, 14, 16. Their sum is 73.

In the second example, $S = 874805371740356549439861$.