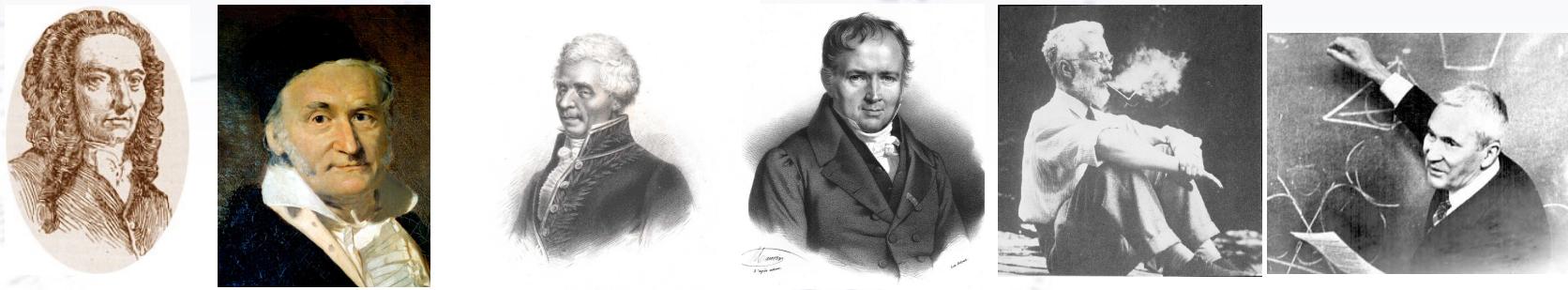
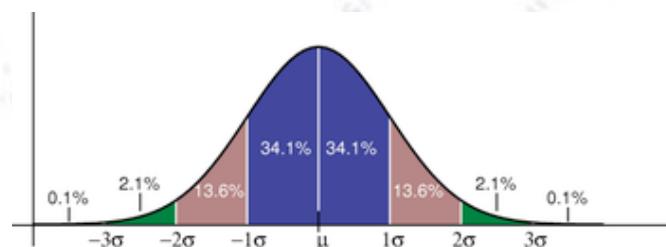


Applied Statistics

Types of data and ways of illustrating it



Troels C. Petersen (NBI)



“Statistics is merely a quantisation of common sense”

Types of data

To first order, data comes in two general types and then “the rest”:

- **Discreet** (typically counting data, i.e. positive integers)
- **Continuous** (at least more or less)
- **The rest**, i.e. text, images - but typically convertible into two first.

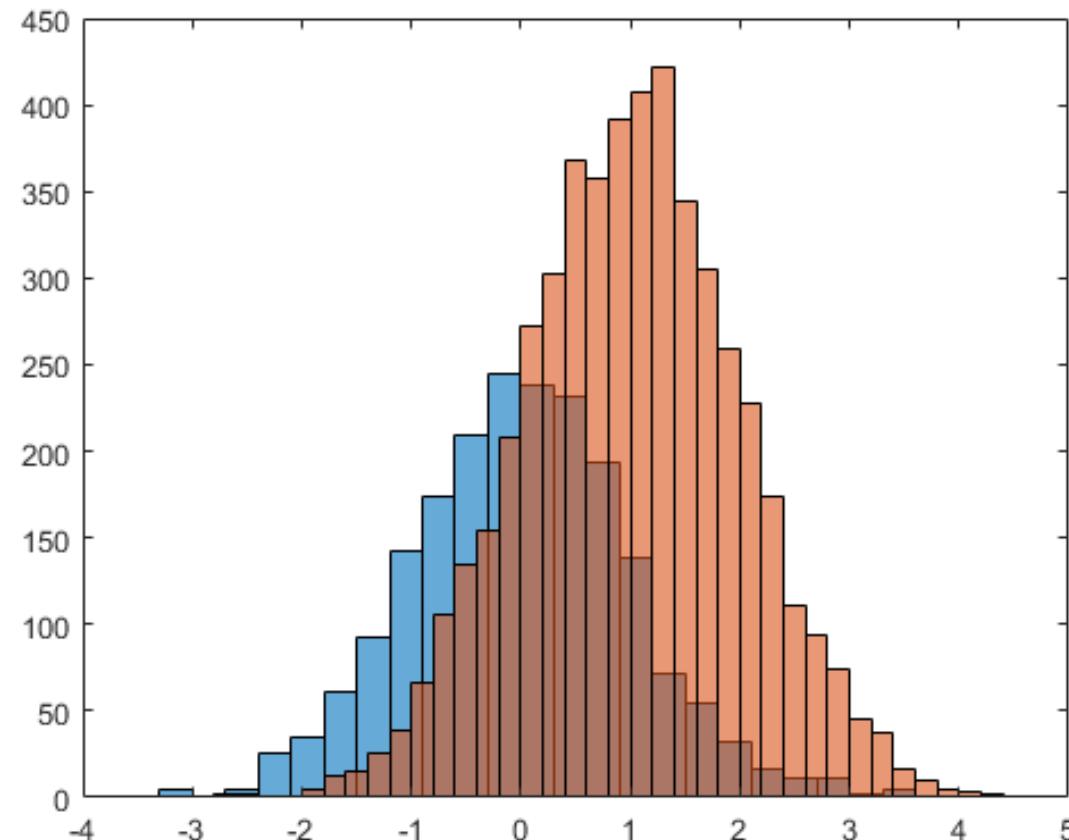
A pitfall is that continuous data is not always continuous, but may seem so!!! The problem arise, if plotting in a histogram with binning comparable (and possibly prime) to steps.

Most basically, one has repeated measurements of things (i.e. 1D distributions). However, often there are several dimensions in the data (possibly 1000s), leading to near-infinite complexity.

Data can be paired in different ways, and / or divisible into groups, experiments, periods, etc. This “meta-data” is important to keep track of.

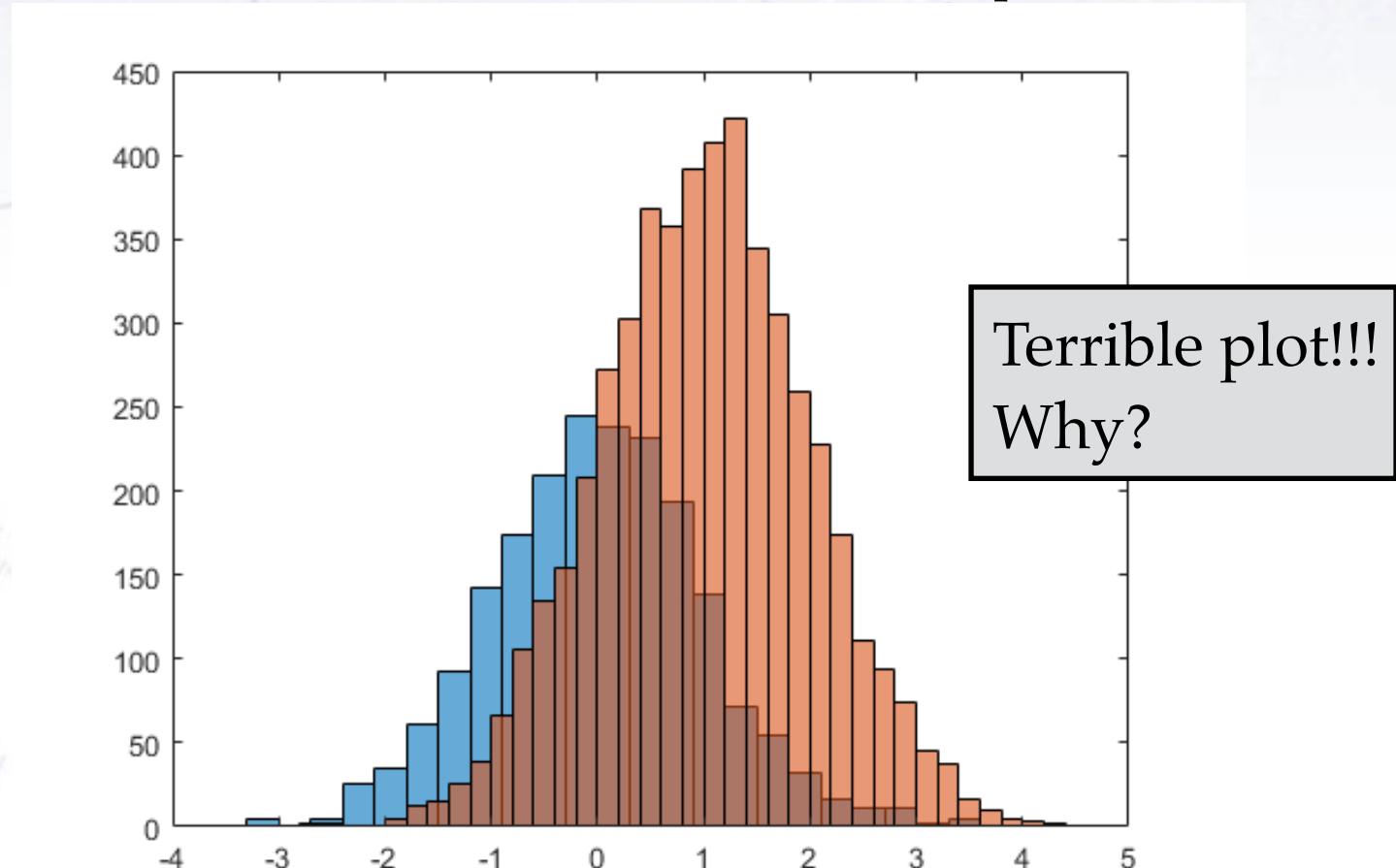
Ways of displaying data

Given repeated measurement of a quantity, the most common way of displaying it, is with a 1D histogram. It is simple and easy to understand, but of course doesn't include more complex information.



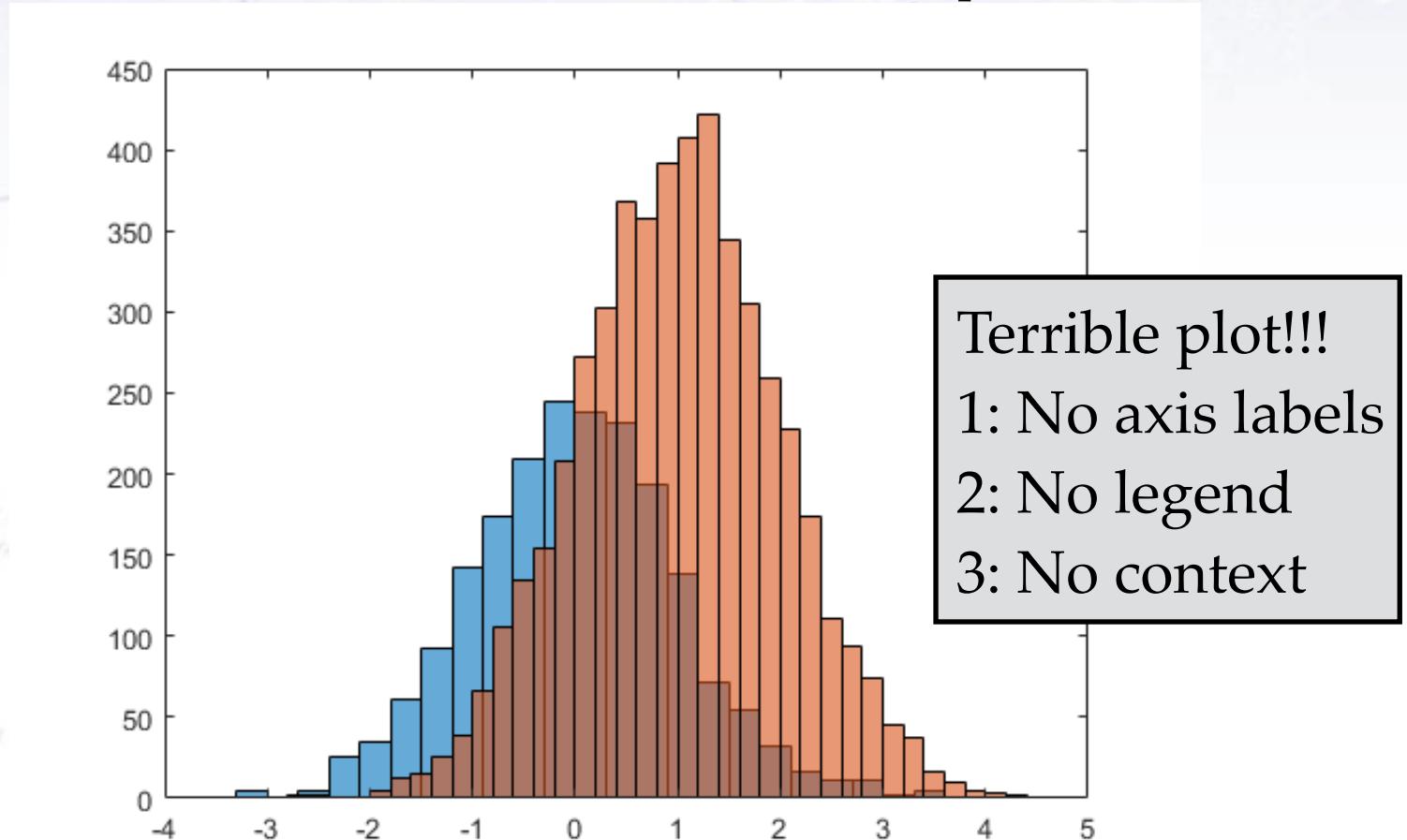
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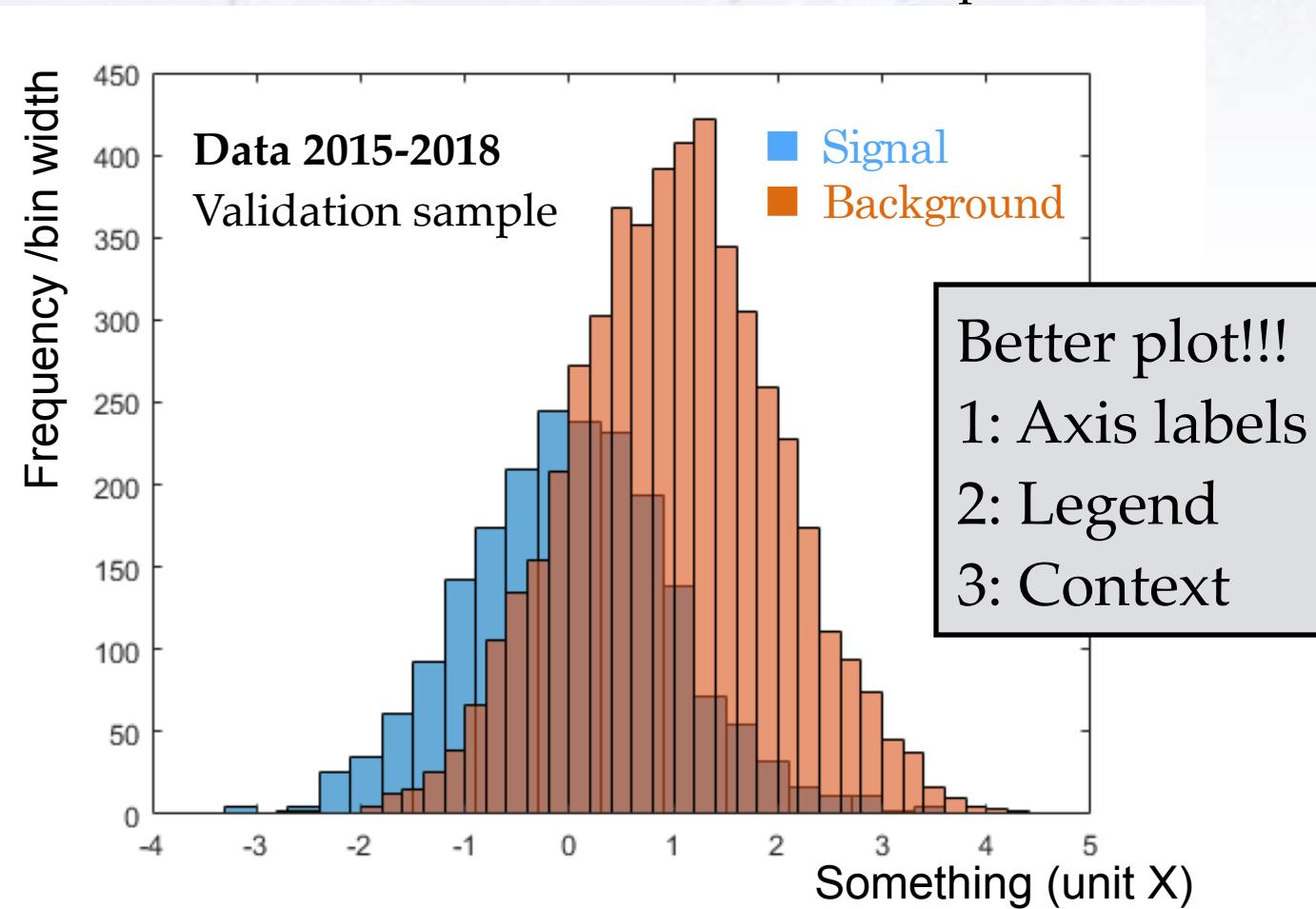
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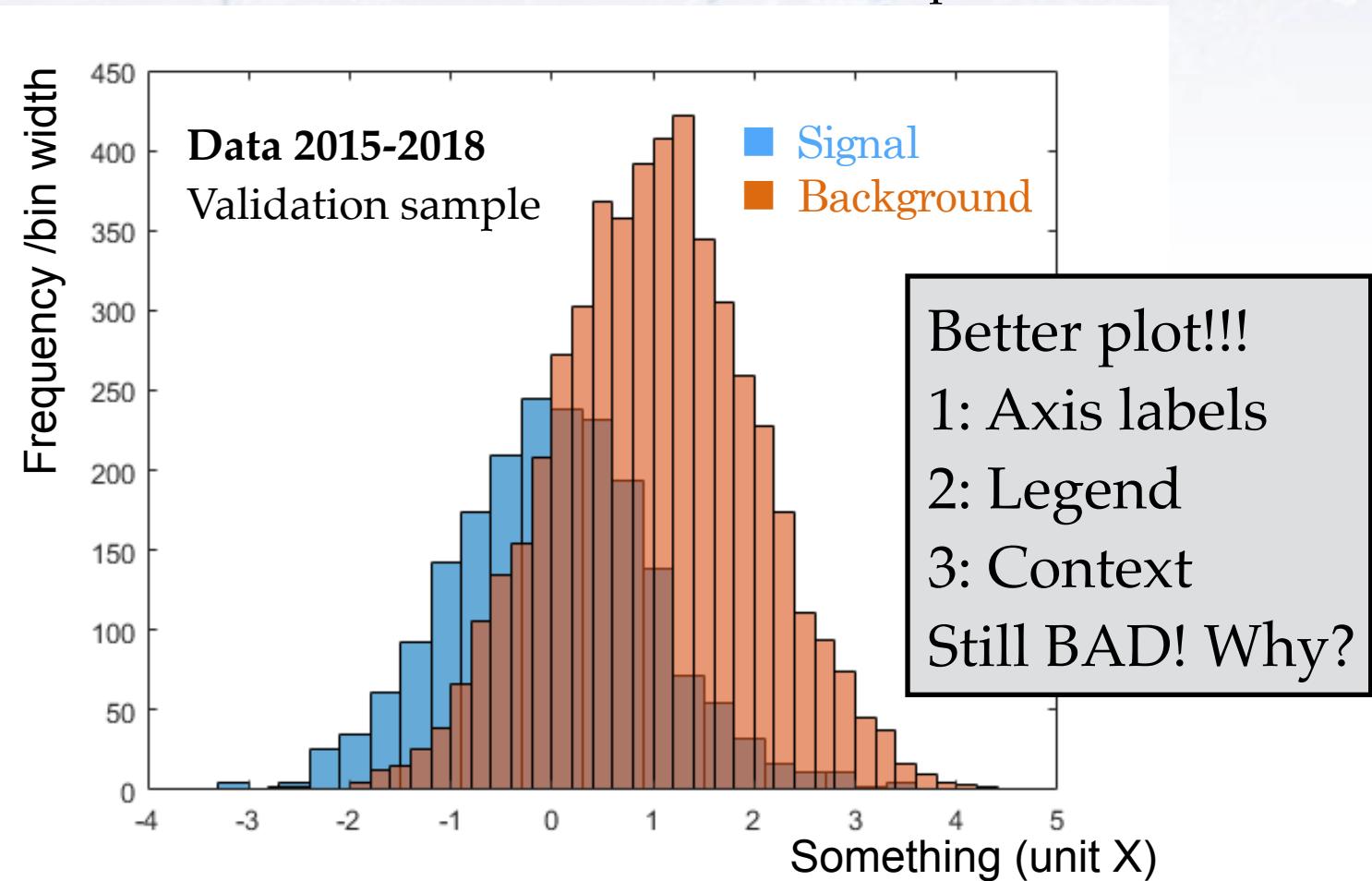
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Ways of displaying data

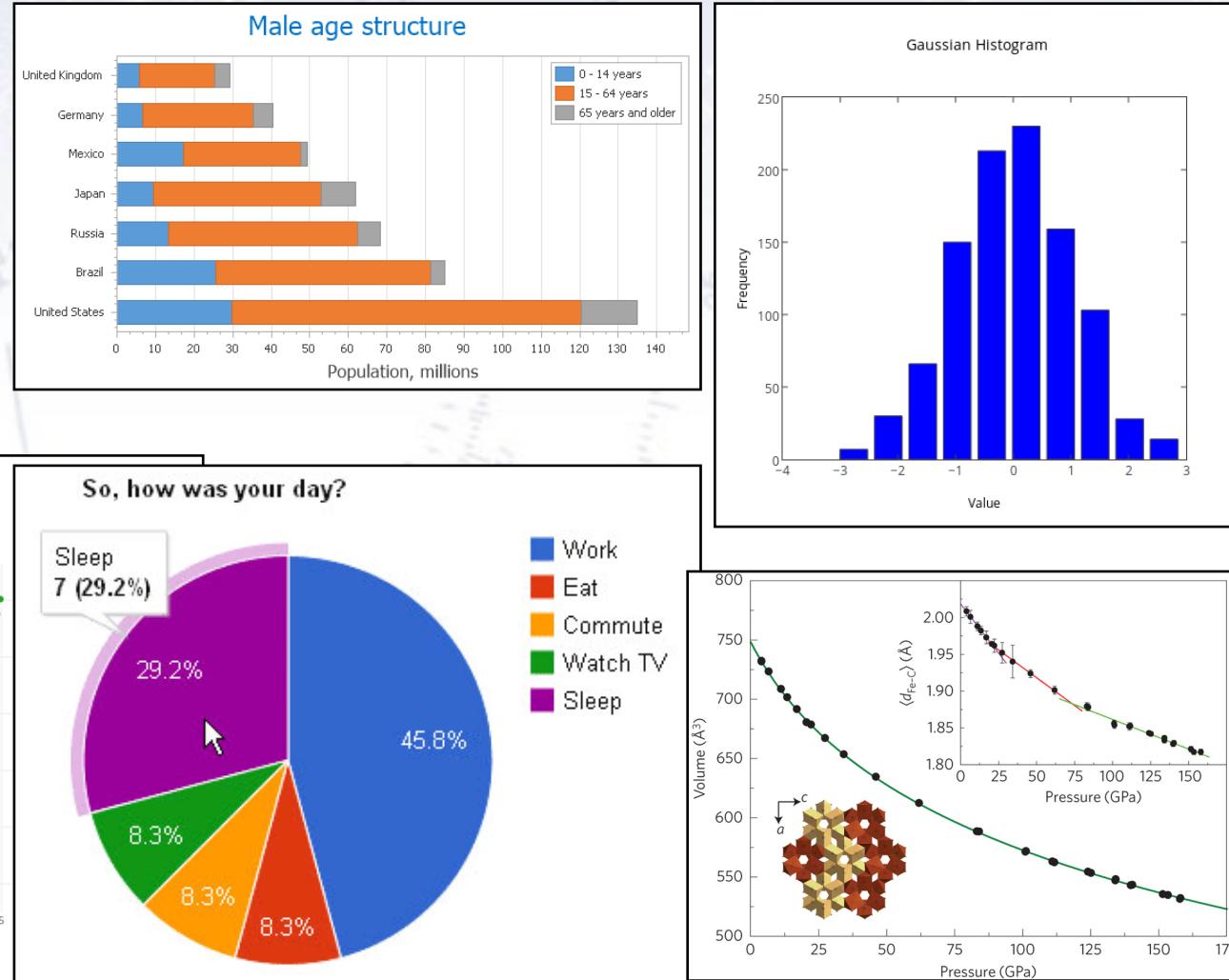
Given repeated measurement of a quantity, the most common way of displaying it, is with a 1D histogram. It is simple and easy to understand, but of course doesn't include more complex information.



Displaying data

There are a multitude of ways to display data, some of which are:

- Bar charts
- Histograms
- Scatter plots
- Pie charts
- Line / fits



A note on plots

Simple plots (for checks):

Most plots you produce is for yourself! Make sure they have labels on the axis, but otherwise don't put too much work into their style.

Time scale to produce: Minutes

Important plots (for showing):

Some plots are for others, and they should be clear cut and illustrative, or the message will be lost. Ask yourself (and then a fellow student), if they understand the plot, and what could be done to improve them.

Time scale to produce: Hours

Central (i.e. money) plots (for public circulation):

A few key plots will be shown elsewhere by others, but ONLY if they are of good quality and illustrate a relevant point well. For these few plots (2-10 in a thesis) you should invest some time in getting them right, as they hold the result of months/ years work.

Time scale to produce: Days

A note on plotting

Always plot your data!!!

You never really know, what goes on in data, until you have SEEN it!

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A Ph.D. student a few months ago comes into my office, asking for help with statistics, as his likelihood fit gave good results, but his Chi2 not!

TP: Have you seen the histograms? **Ph.D.:** No, but they are so simple...

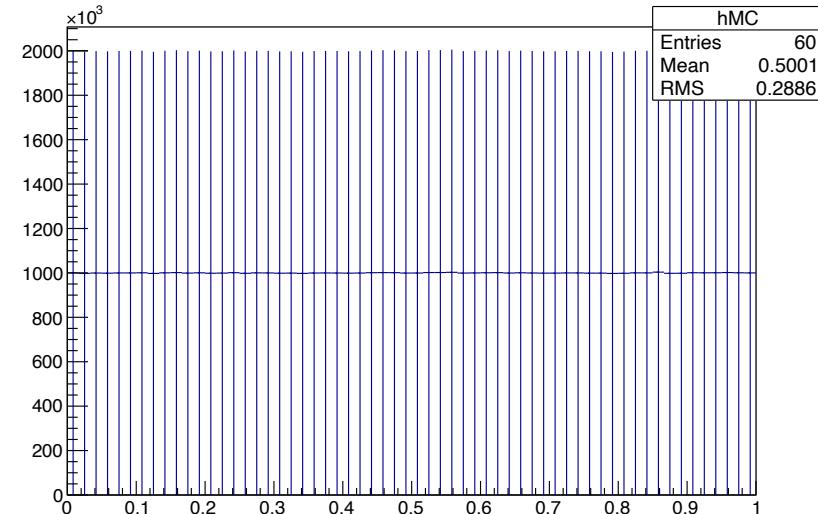
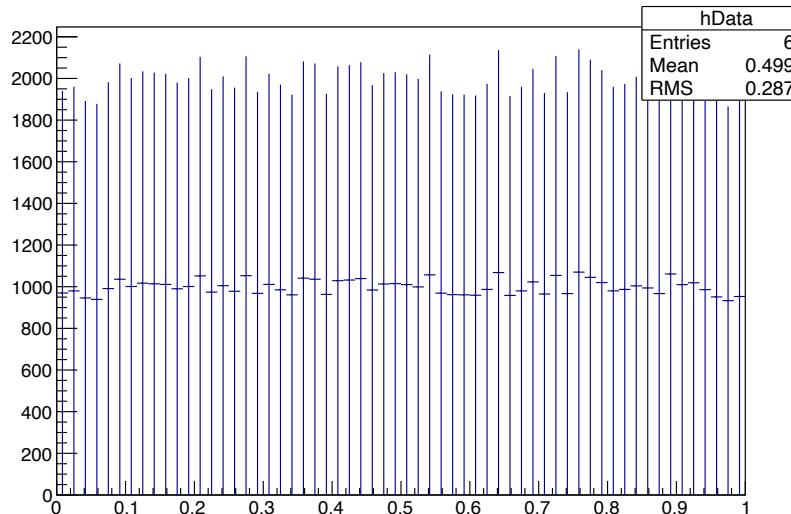
A note on plotting

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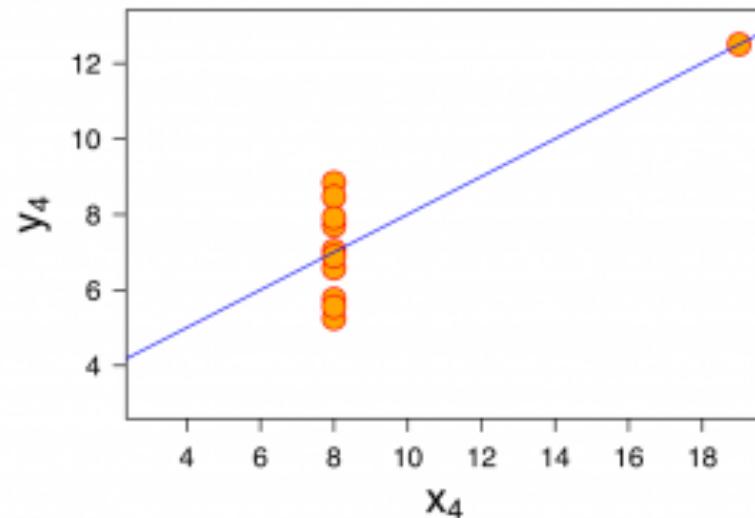
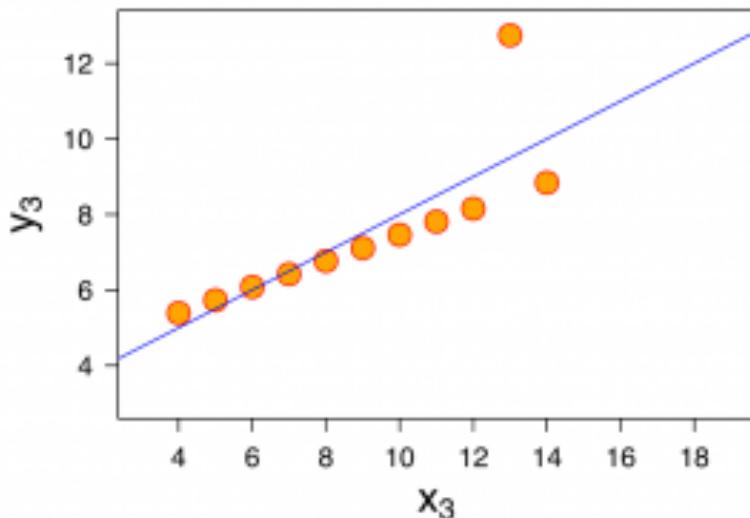
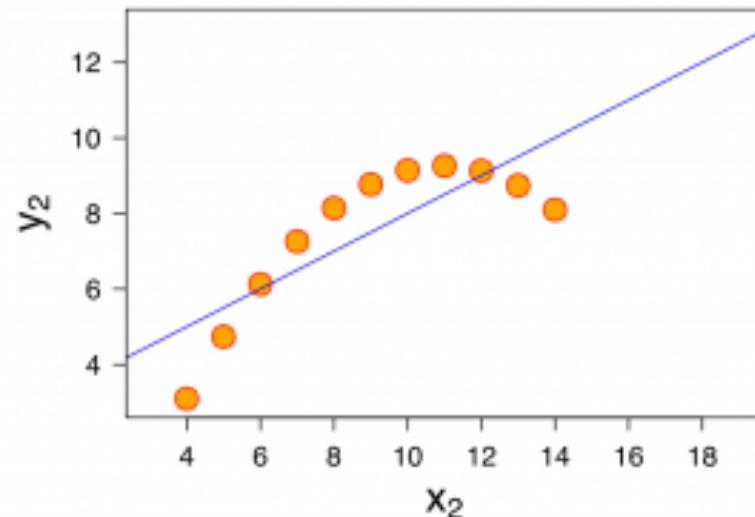
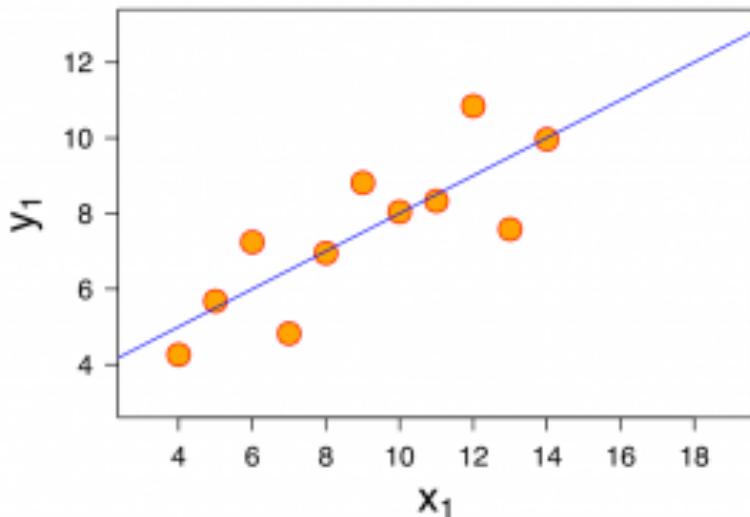
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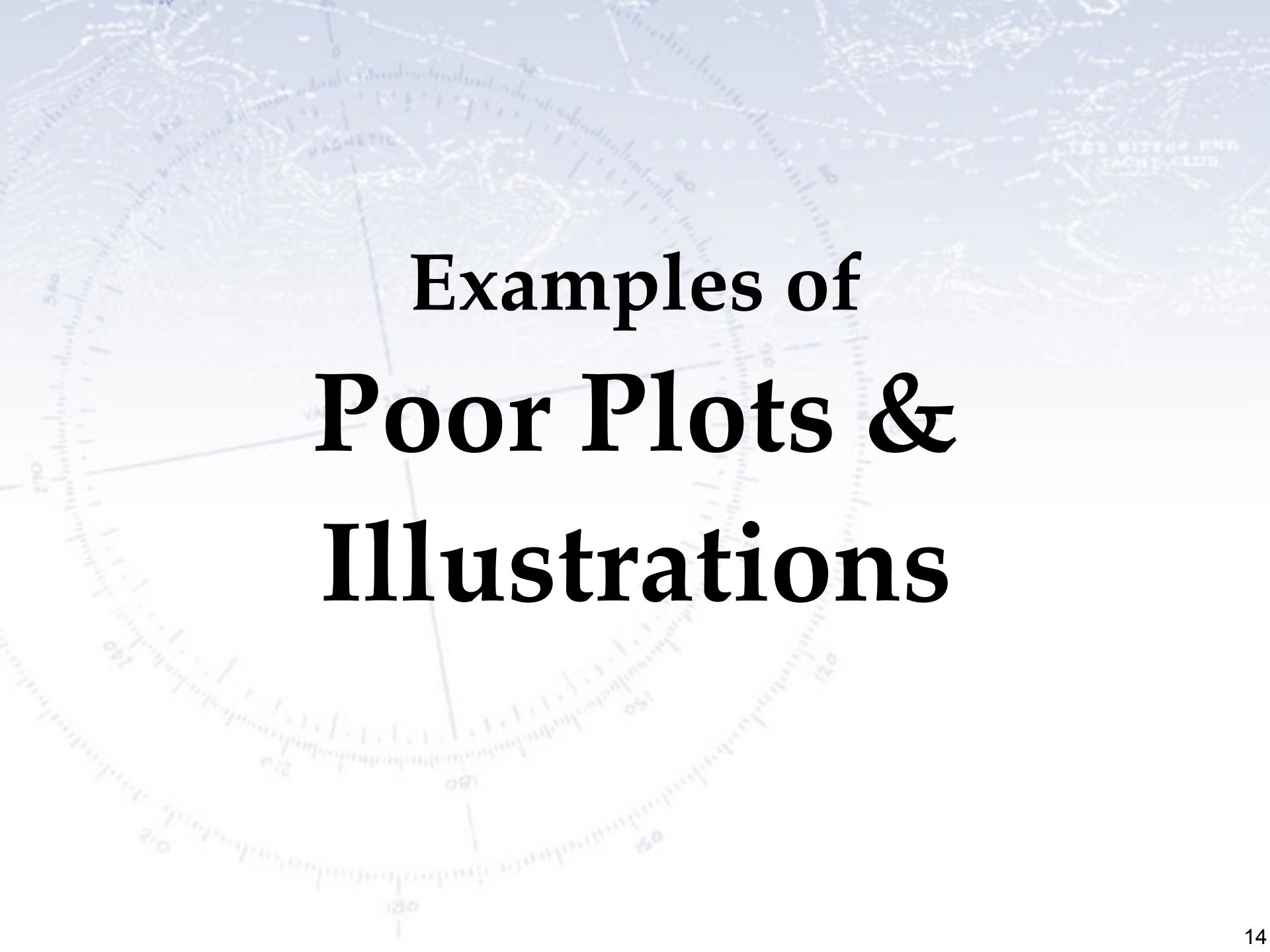
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Anscombe's Quartet





Examples of Poor Plots & Illustrations

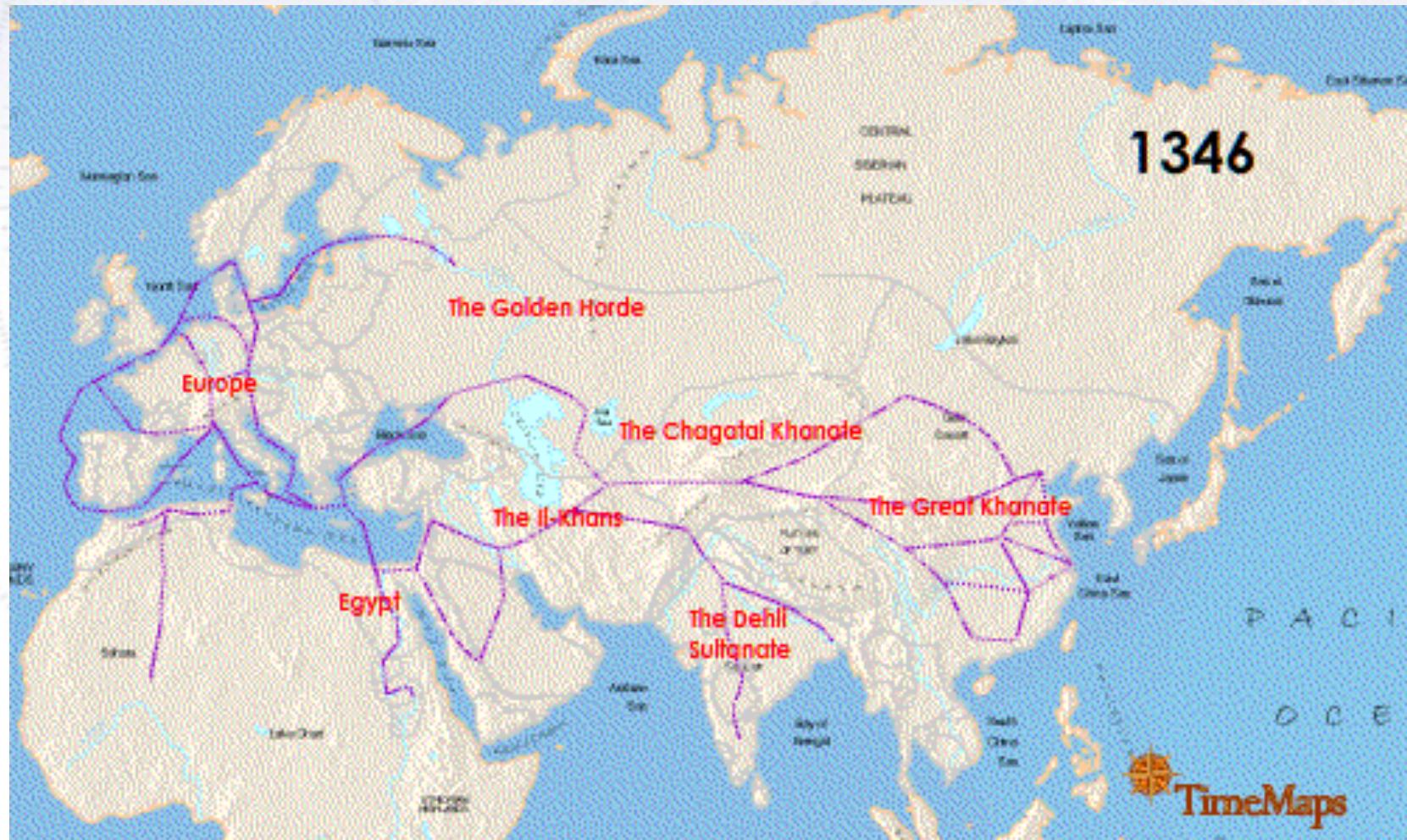
Black Death... and bad plots!

While at first the plot looks very cool, but the use of colors is often misinterpreted. The colors imply differing intensities or mortality rates, but the legend indicates they represent time. The arrows convey all the real information here...



Black Death... and bad plots!

While at first the plot looks very cool, but the use of colors is often misinterpreted. The colors imply differing intensities or mortality rates, but the legend indicates they represent time. The arrows convey all the real information here... but now we can do better!



128% of Americans have tried marijuana?



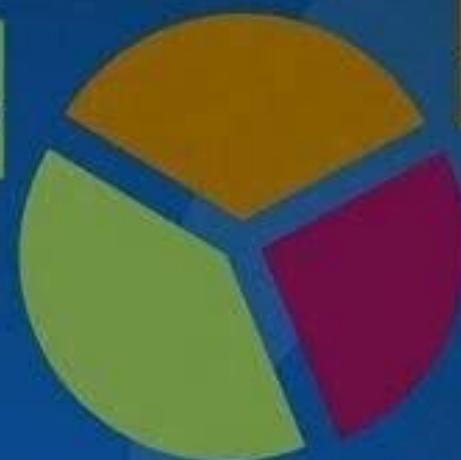
AMERICANS WHO HAVE TRIED MARIJUANA

CBS NEWS POLL

51%
TODAY

43%
LAST YEAR

34%
1997

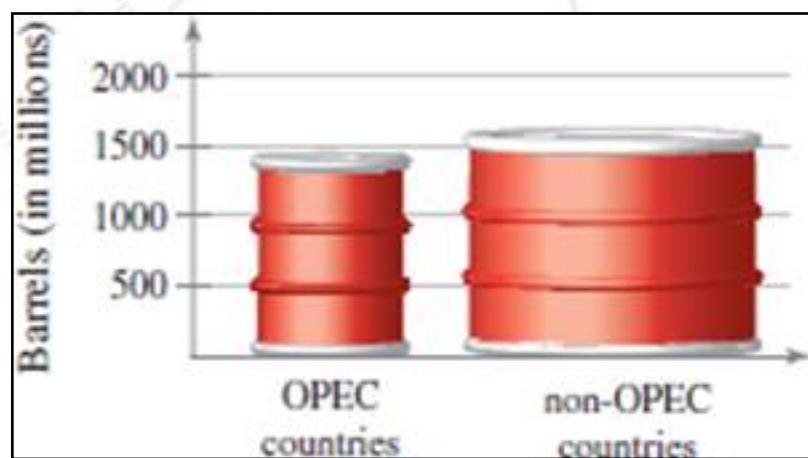
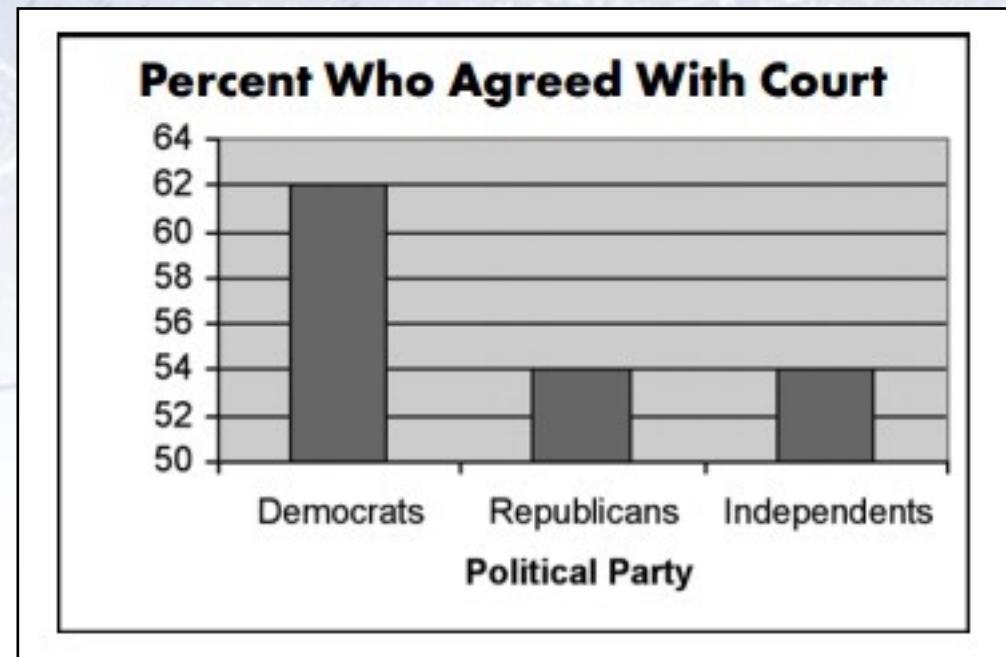


Source: MOE +/- 4%

HIGH SUPPORT FOR LEGALIZING MARIJUANA
MORE THAN HALF OF AMERICANS SAY THEY'VE TRIED POT

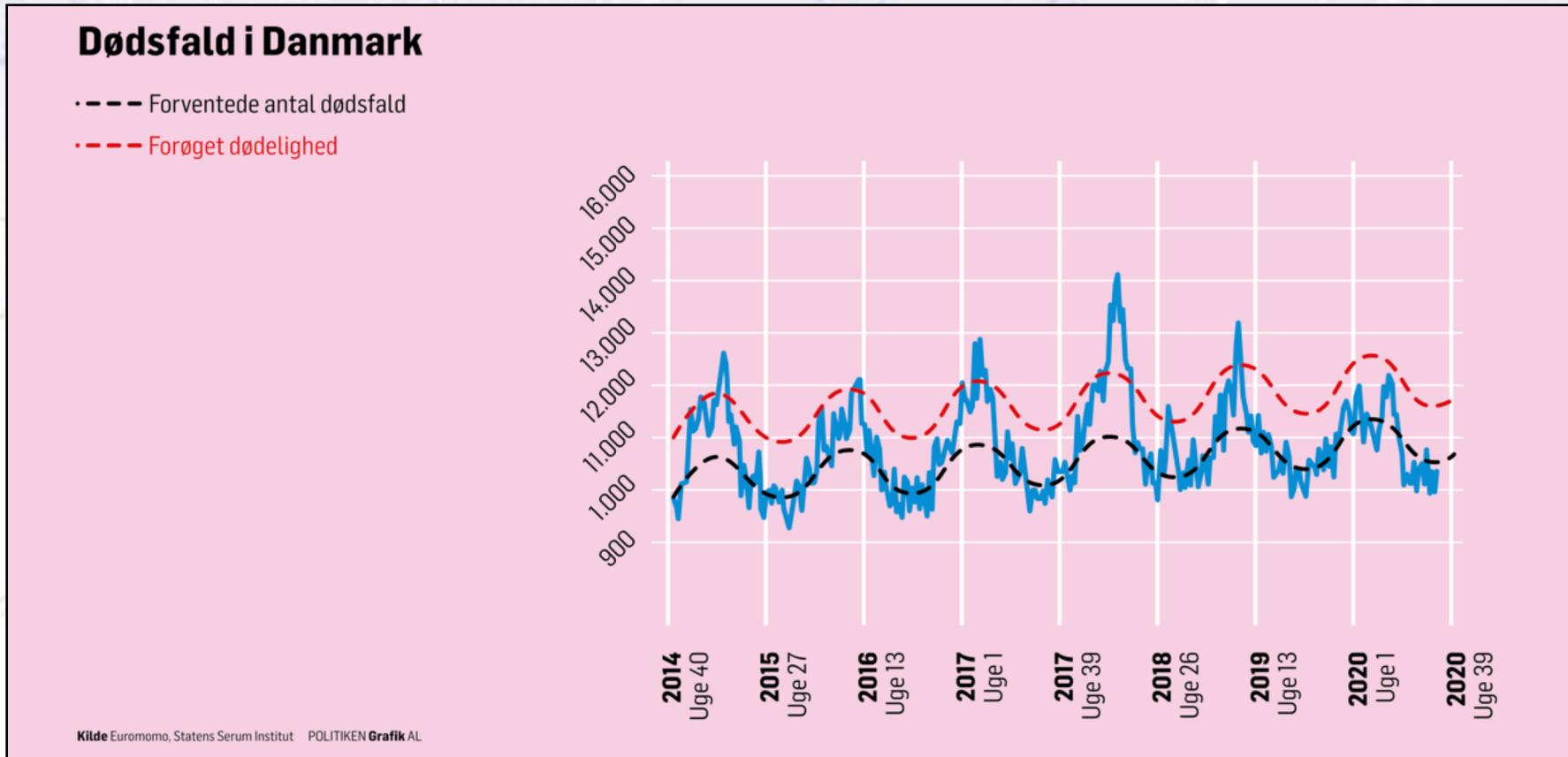
LIVE
 CBSN

A mix of poor plots



A new poor plot

Have a look at this plot (from Politiken, 11th of October 2020, sorry for the Danish), and see if you can see errors and suggest improvements.



A new poor plot

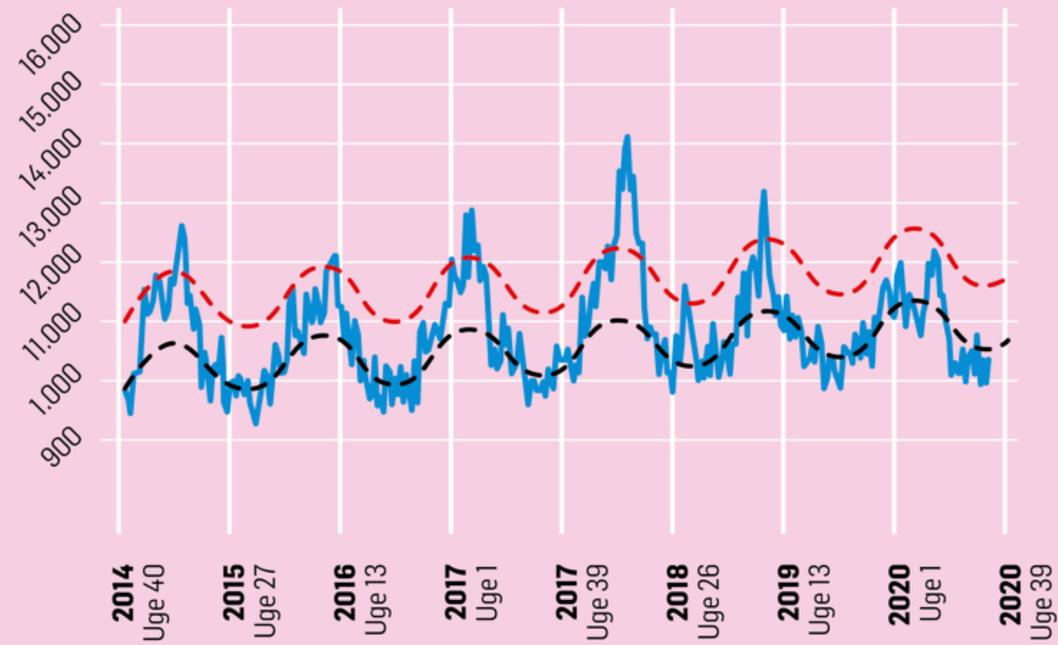
Have a look at this plot (from Politiken, 11th of October 2020, sorry for the Danish), and see if you can see errors and suggest improvements.

Dødsfald i Danmark

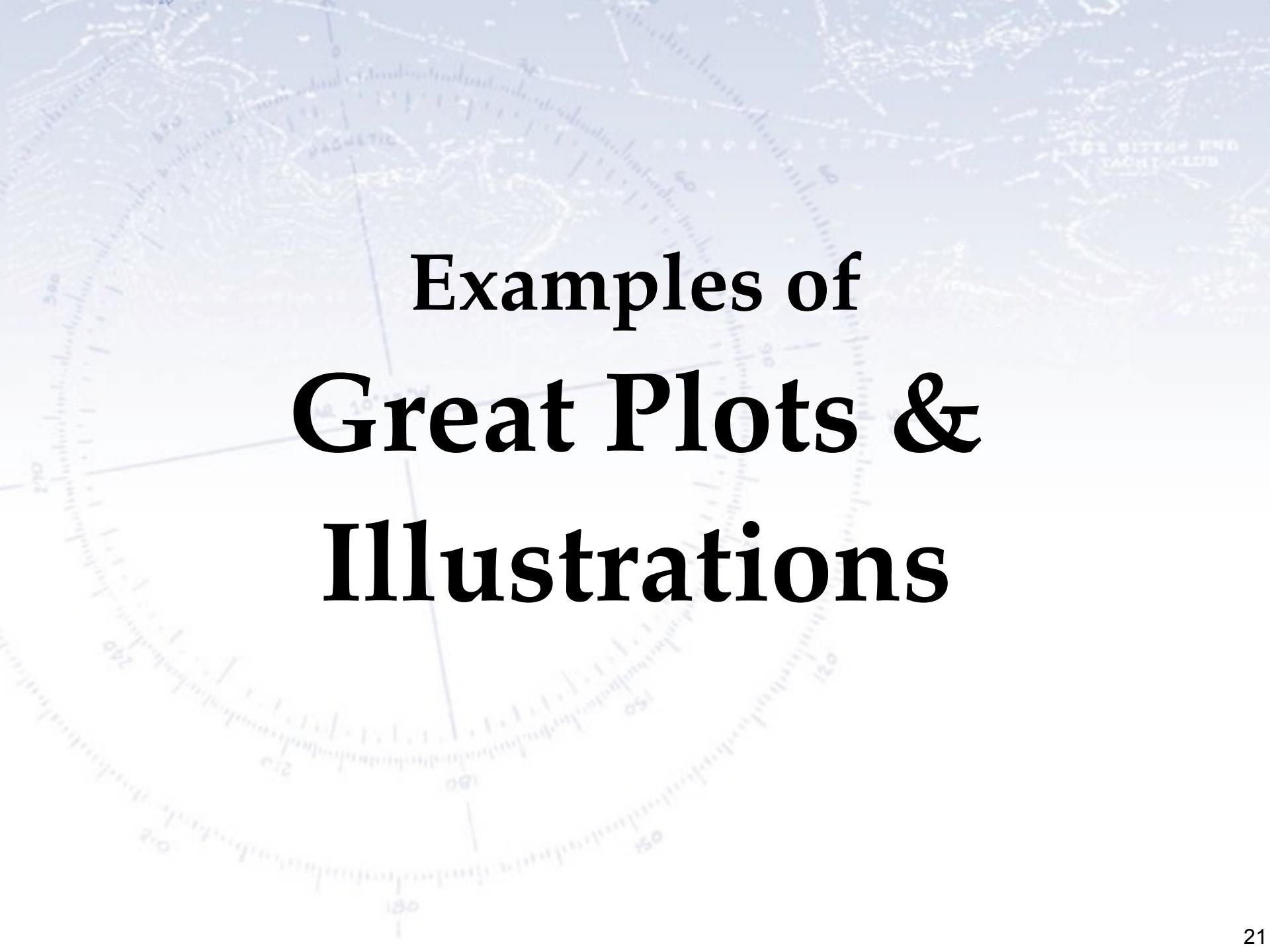
- Forventede antal dødsfald
- Forøget dødelighed

My list:

- 1: Y-axis wrong!
- 2: X-axis very strange.
- 3: No legend for blue curve.
- 4: Models are terrible.



Kilde Euromomo, Statens Serum Institut POLITIKEN Grafik AL



Examples of Great Plots & Illustrations

Napoleon's march on Russia

This has been called by some the "greatest figure ever made". It illustratively tells the story of Napoleon's catastrophic march and retreat in Russia in 1812, losing 400.000 men. The graph contains a massive amount of data, showing landmarks and geographic course the army took, the size of the army over time, and the temperature of the bitter Russian winter. You can study this figure and gain insight as to why Napoleon lost.

*Carte Figurative des pertes successives en hommes de l'Armée Française dans la campagne de Russie 1812 ~ 1813.
Dessinée par M. Minard, Inspecteur Général des Ponts et Chaussées en retraite
Paris, le 20 Novembre 1869.*

Les nombres d'hommes présents sont représentés par les largeurs des zones colorées à raison d'un millimètre pour dix mille hommes; ils sont de plus écrits en travers des zones. Le rouge désigne les hommes qui entrent en Russie; le noir ceux qui en sortent. — Les renseignements qui ont servi à dresser la carte ont été puisés dans les ouvrages de M. M. Thiers, de Léger, de Fezensac, de Chambray et le journal médical de Jacob, pharmacien de l'Armée depuis le 28 Octobre. Pour mieux faire juger à l'œil la diminution de l'armée, j'ai supposé que les corps du Prince Jérôme et du Maréchal Davout, qui avaient été détachés sur Minsk et Mogilow et se rejoignent vers Orscha et Witebsk, avaient toujours marché avec l'armée.

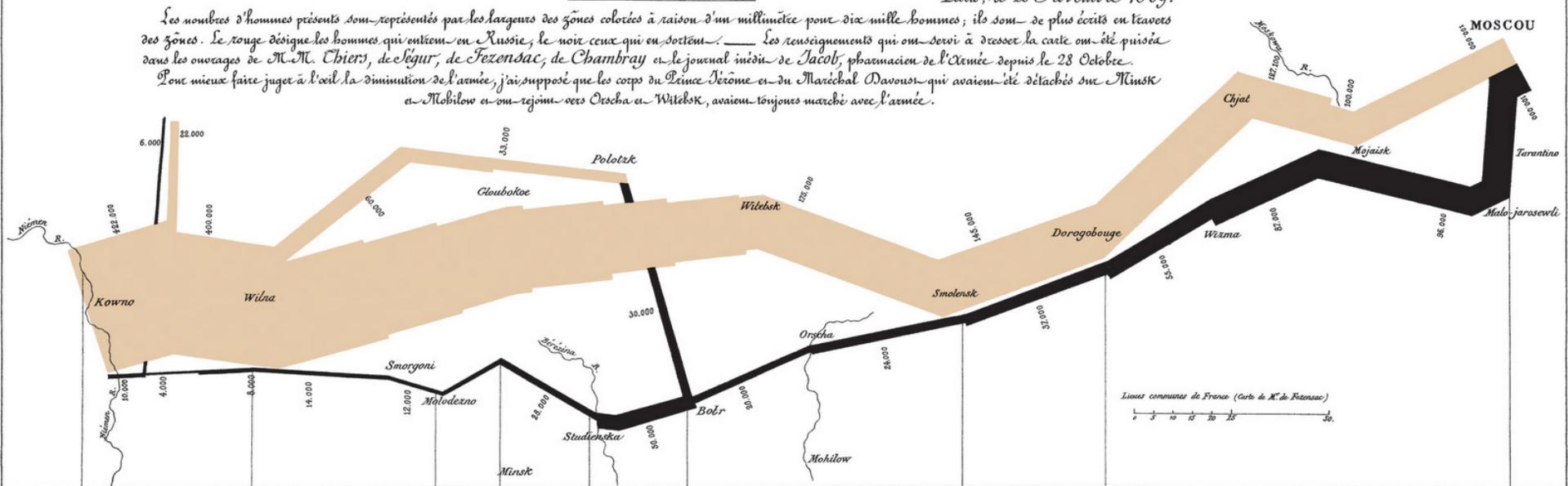
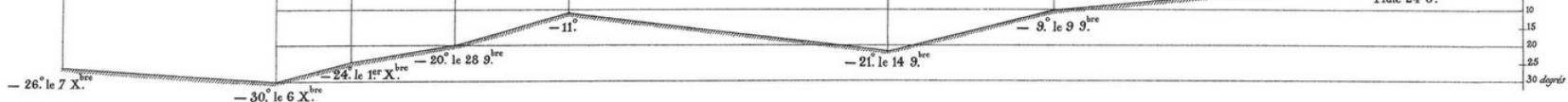


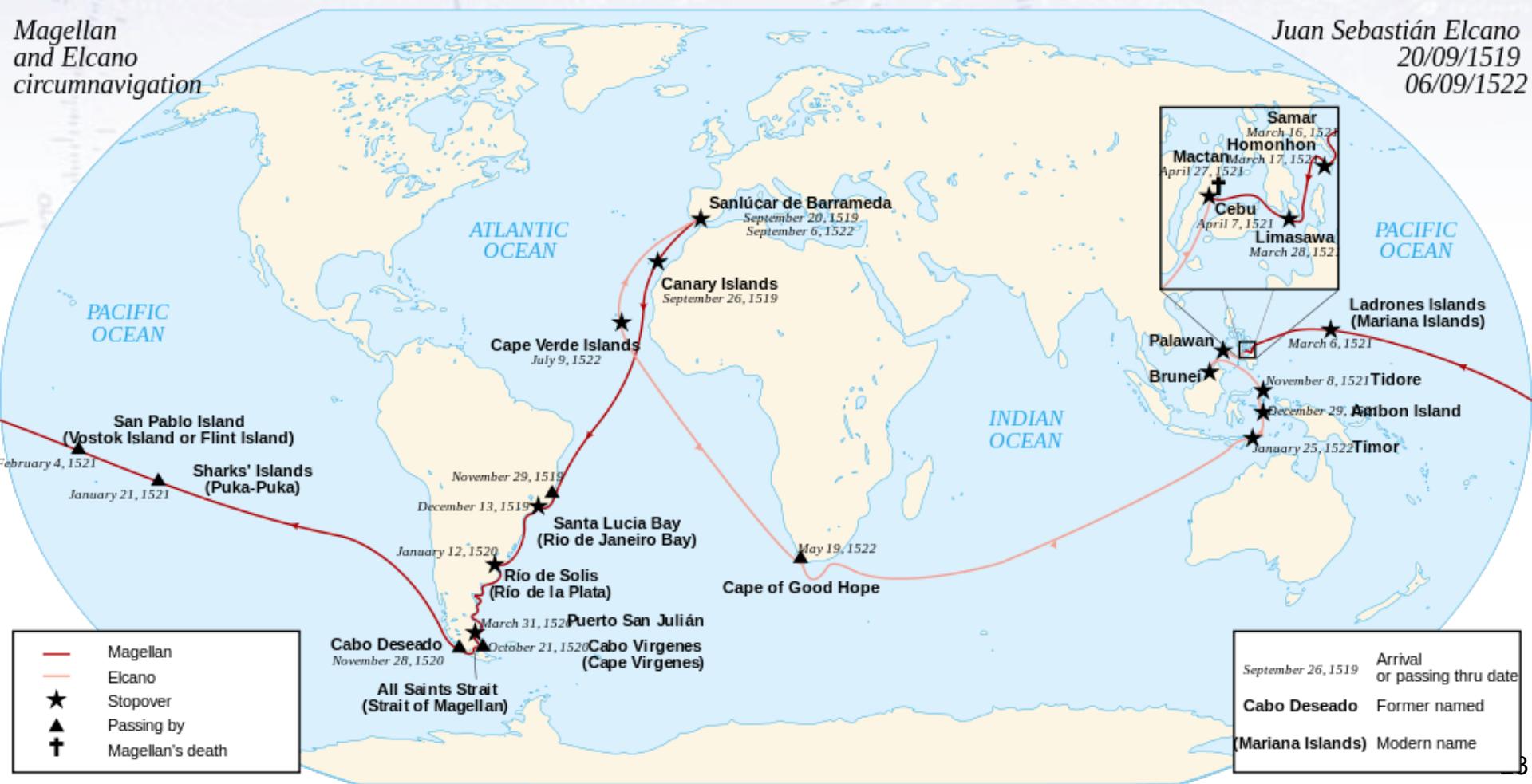
TABLEAU GRAPHIQUE de la température en degrés du thermomètre de Réaumur au dessous de zéro.

Les Cosaques passent au galop
le Niemen gelé.



Magellan's circumnavigation

In addition to starting the globalisation age, the expedition (unwittingly) discovered the need for an **International Date Line**. Despite numerous deaths, an accurate ships log was kept for over 1000 days. When the surviving sailors returned, they realised their log was **off the local calendar by 1 day**. Cool, consider the death, drama, plight, and sheer insanity of the voyage...



Galileo on Jupiter's moons

This is a condensed version of the famous observations Galileo made of the Jovian moons. Jupiter is shown as the O, and the moons as *. Using these simple observations, Galileo deduced that each little * was actually orbiting Jupiter, which gave credence to the controversial Copernican theory that the Earth is not center of the Universe.

What is great about this figure is its simplicity, Tufte would approve the sparse labelling and lack of extemporaneous axes.

When you align each date's observations with Jupiter, as above, the helix pattern the moons trace as they orbit nearly jumps out!





January 7, 1610

* ○ *

January 8

○ * * *

January 9

January 10

* *

January 11

* *

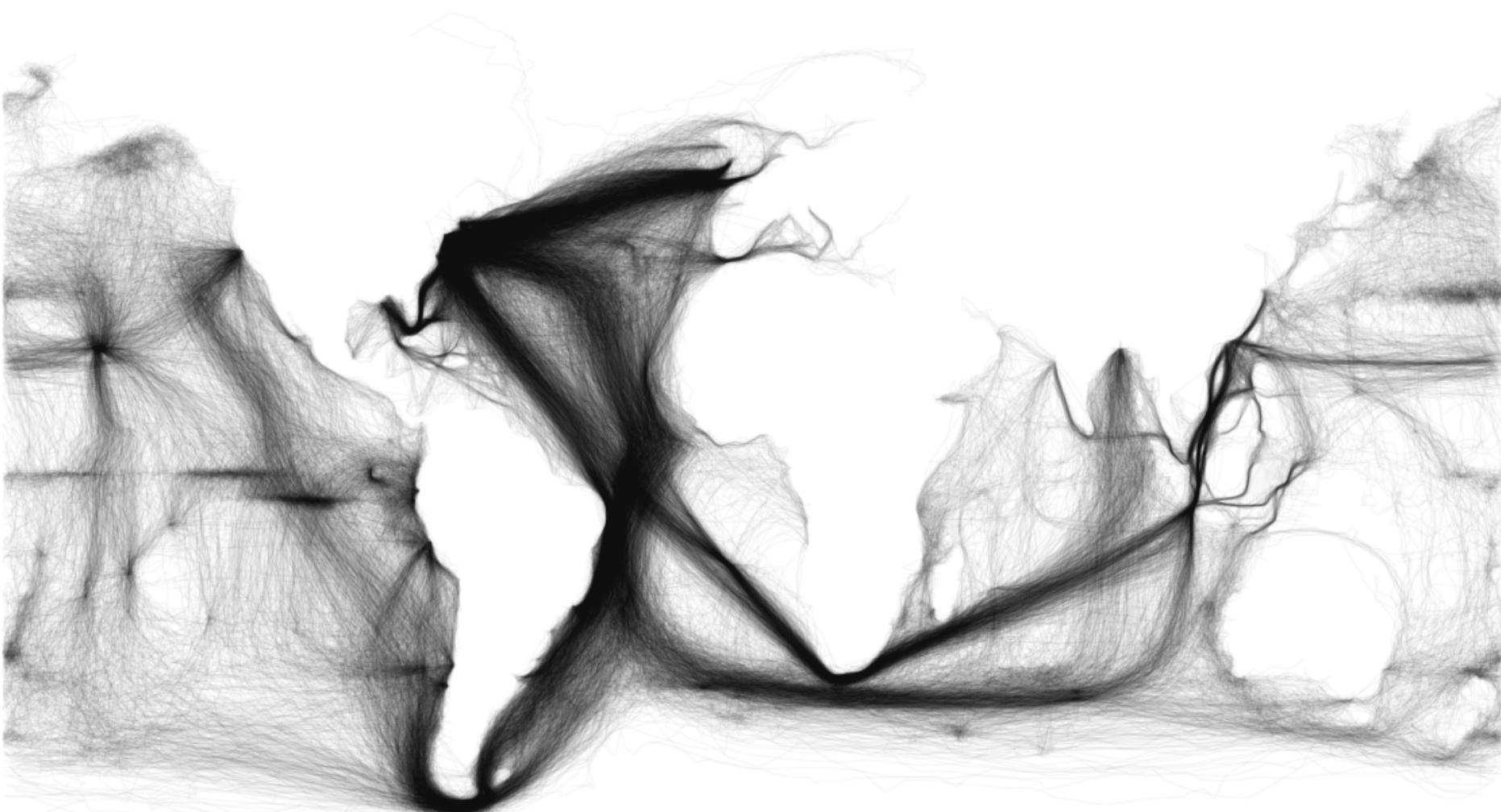
January 12

* ○ * *

January 13

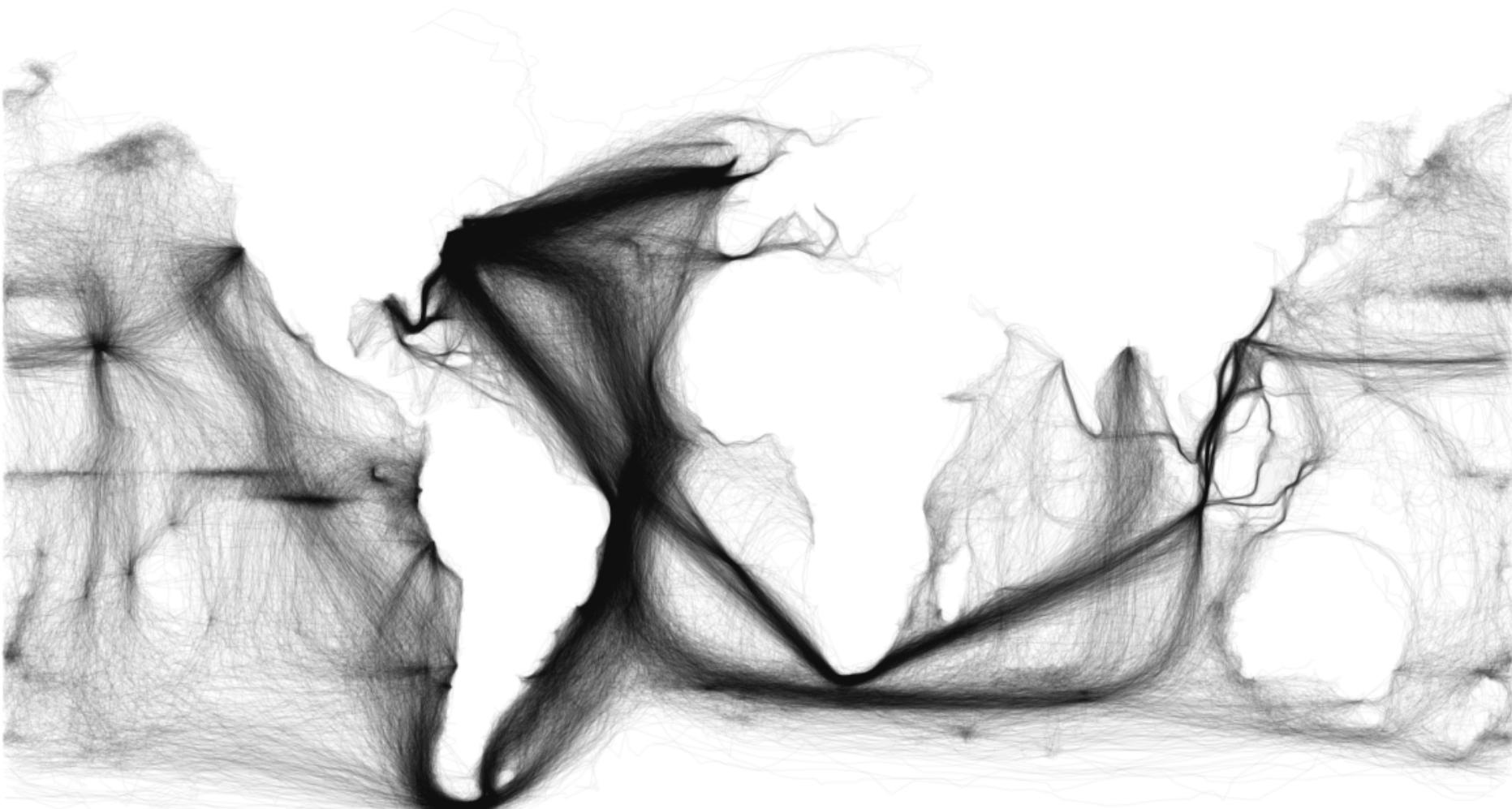
* ○ * *

Guess what this is...

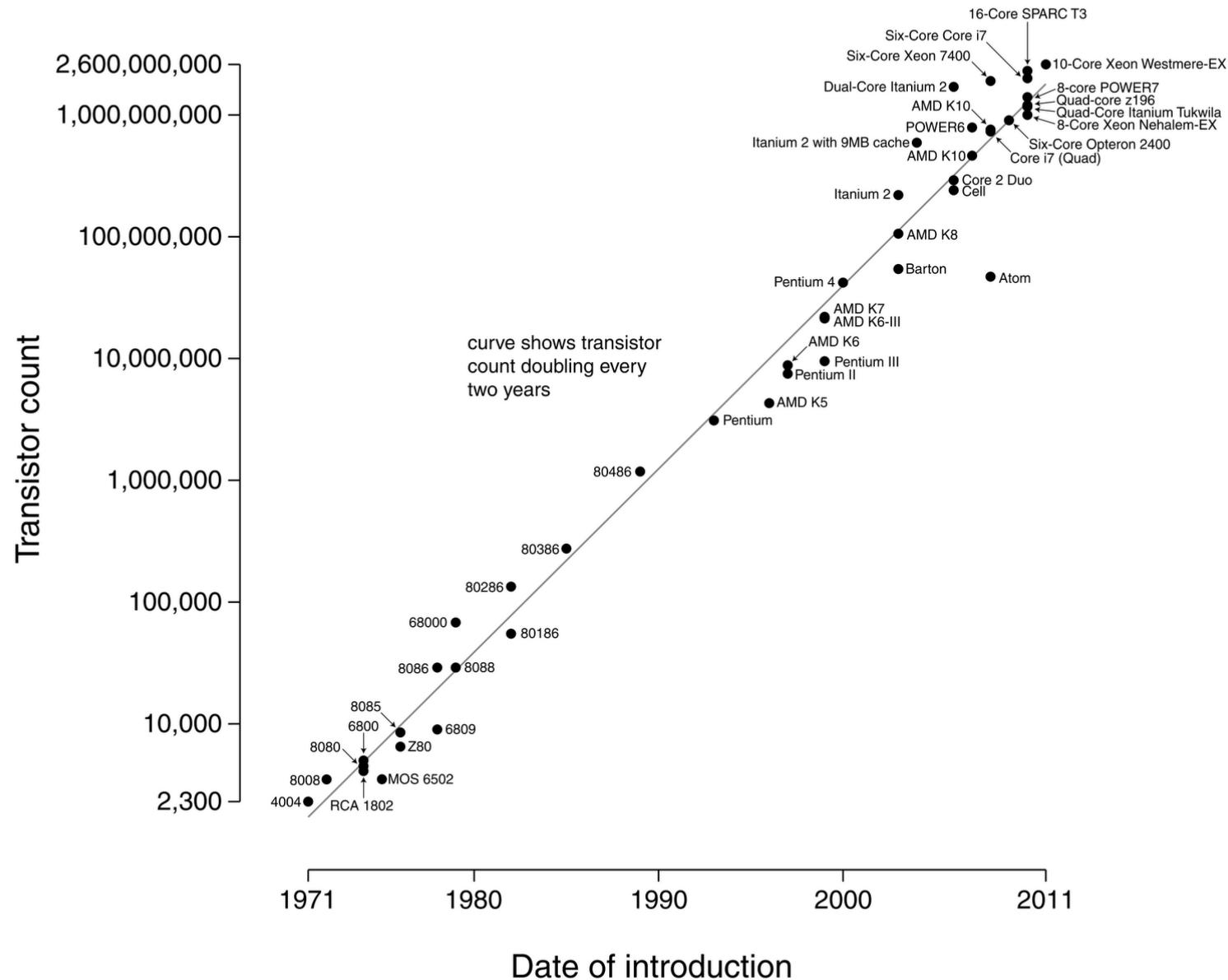


Guess what this is...

Plot millions of journal entries from 18th and 19th century ship logs, and you reveal a picture of ocean trade you've never seen before.



Microprocessor Transistor Counts 1971-2011 & Moore's Law



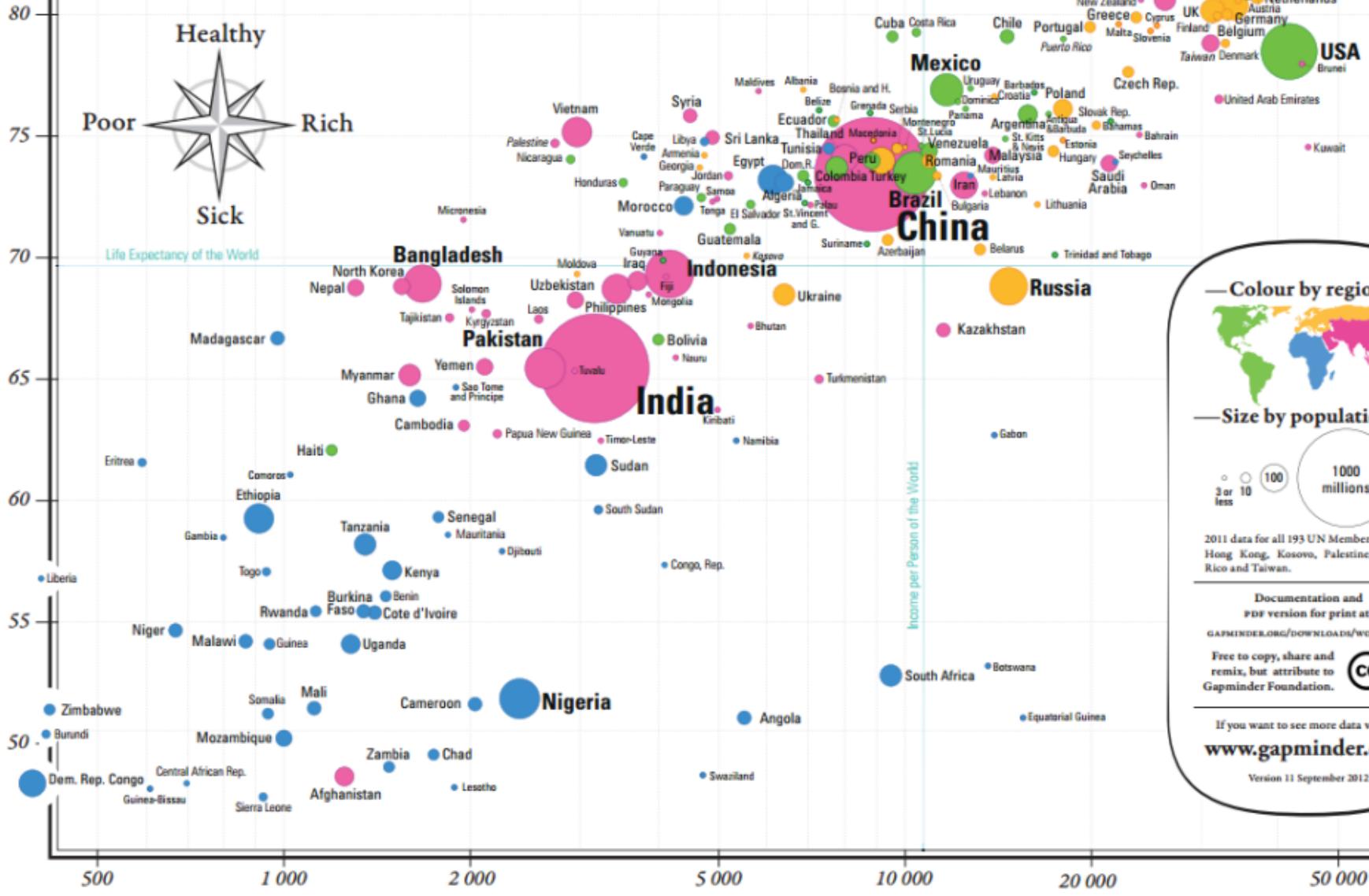
GAPMINDER WORLD 2012

Mapping the Wealth and Health of Nations



Life Expectancy of the World

LIFE EXPECTANCY in years



— Colour by region —



— Size by population —



2011 data for all 193 UN Members and for Hong Kong, Kosovo, Palestine, Puerto Rico and Taiwan.

Documentation and
PDF version for print at:

GAPMINDER.ORG/ DOWNLOADS/WORLD-PDF

Free to copy, share and
remix, but attribute to
Gapminder Foundation.

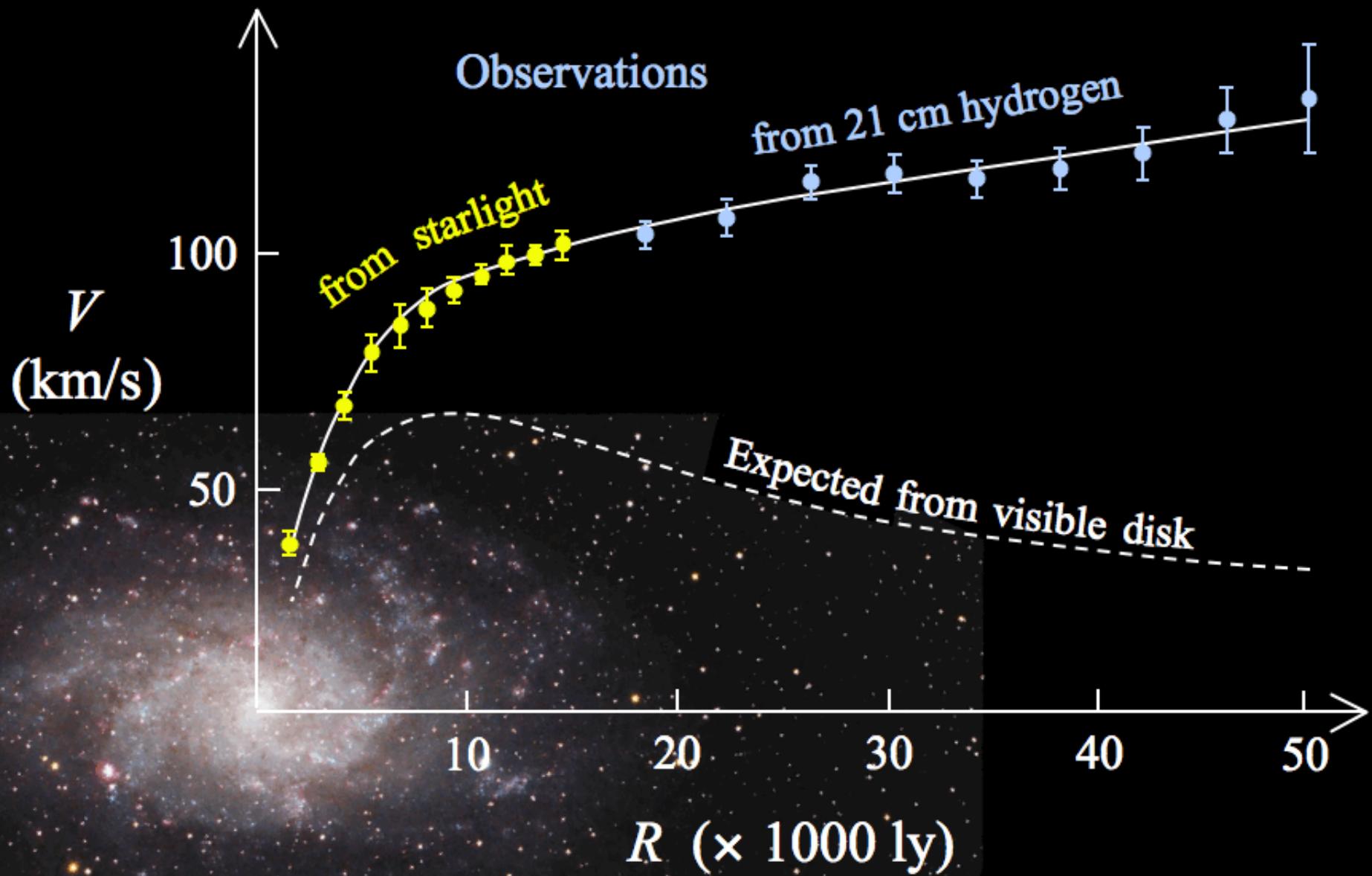


If you want to see more data visit:

www.gapminder.org

Version 11 September 2012

INCOME PER PERSON in US Dollars (GDP/capita, PPP\$ inflation adjusted, log scale)

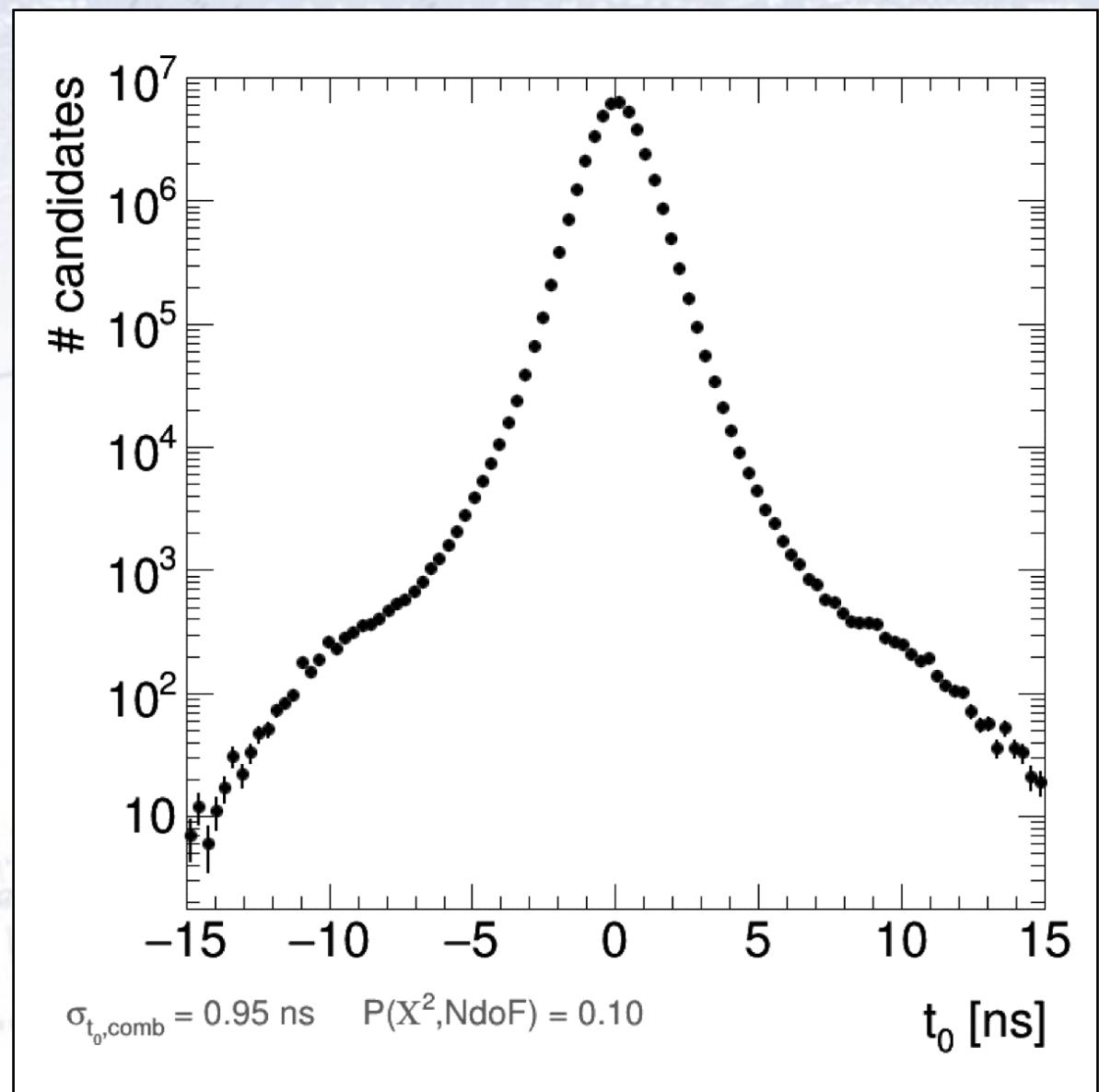


Animations of plots

Once you know how to generate plots en masse, it is surprisingly simple to make short animations illustrating the effect of the changes between plots.

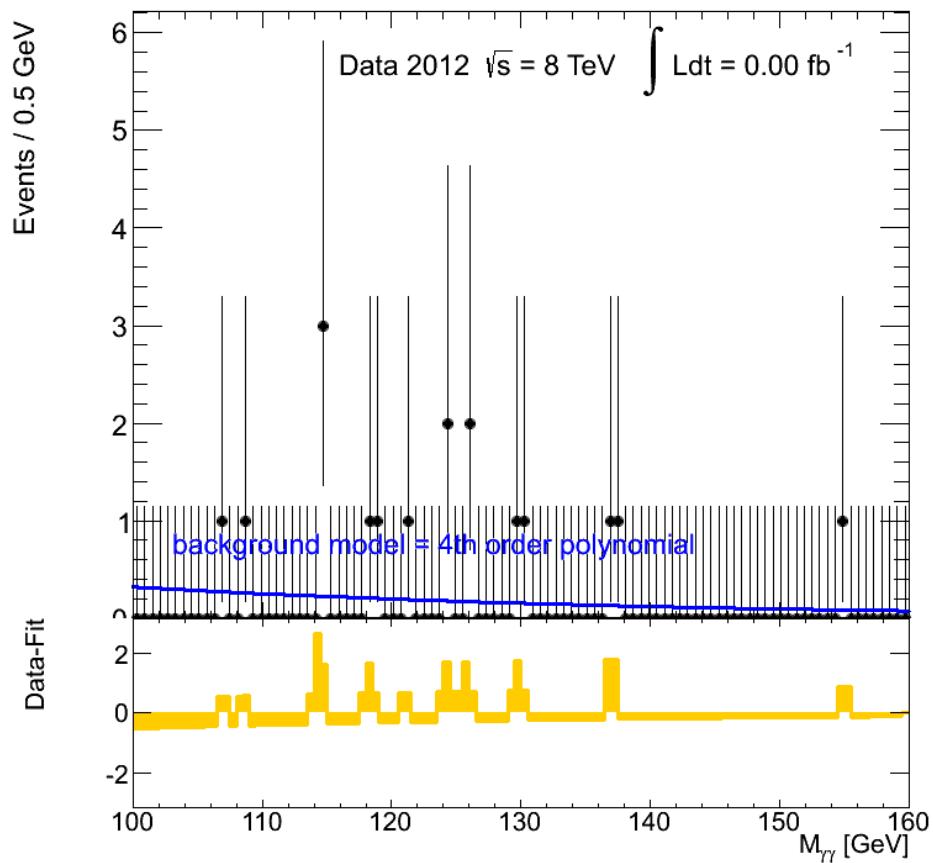
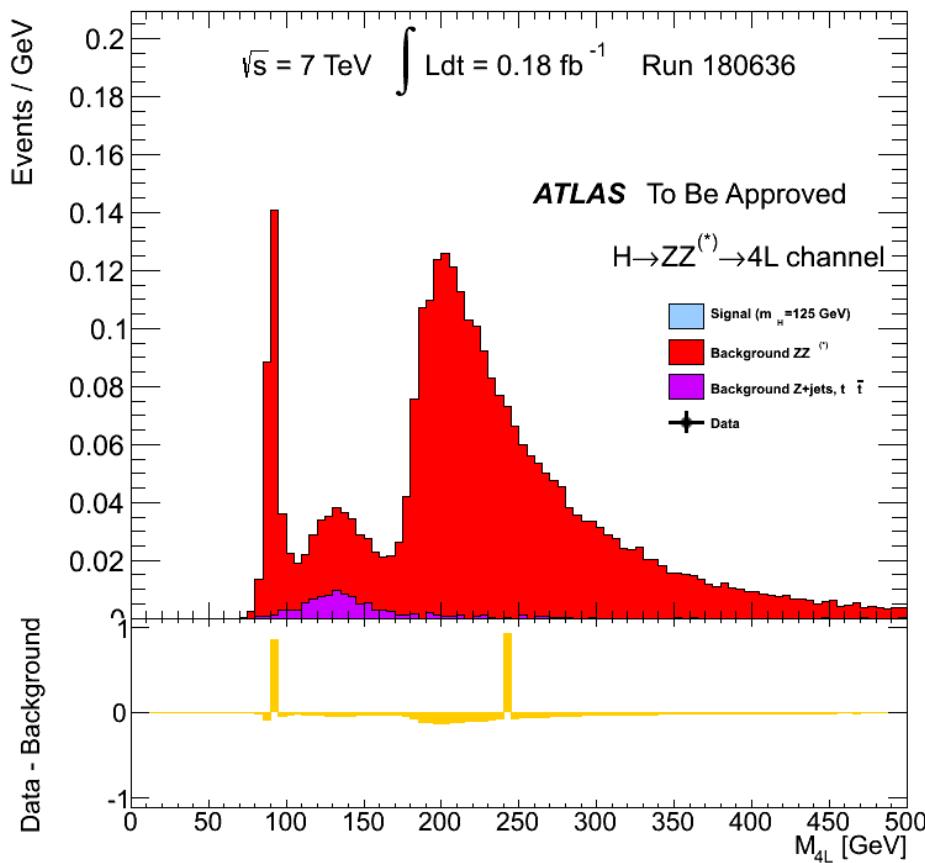
This is a very powerful way to make your points come across, typically well remembered by your audience.

Here is shown the timing of particles in ATLAS, and evidence for observing the small $\pm 5\text{ns}$ satellite bunches.



Animations of plots

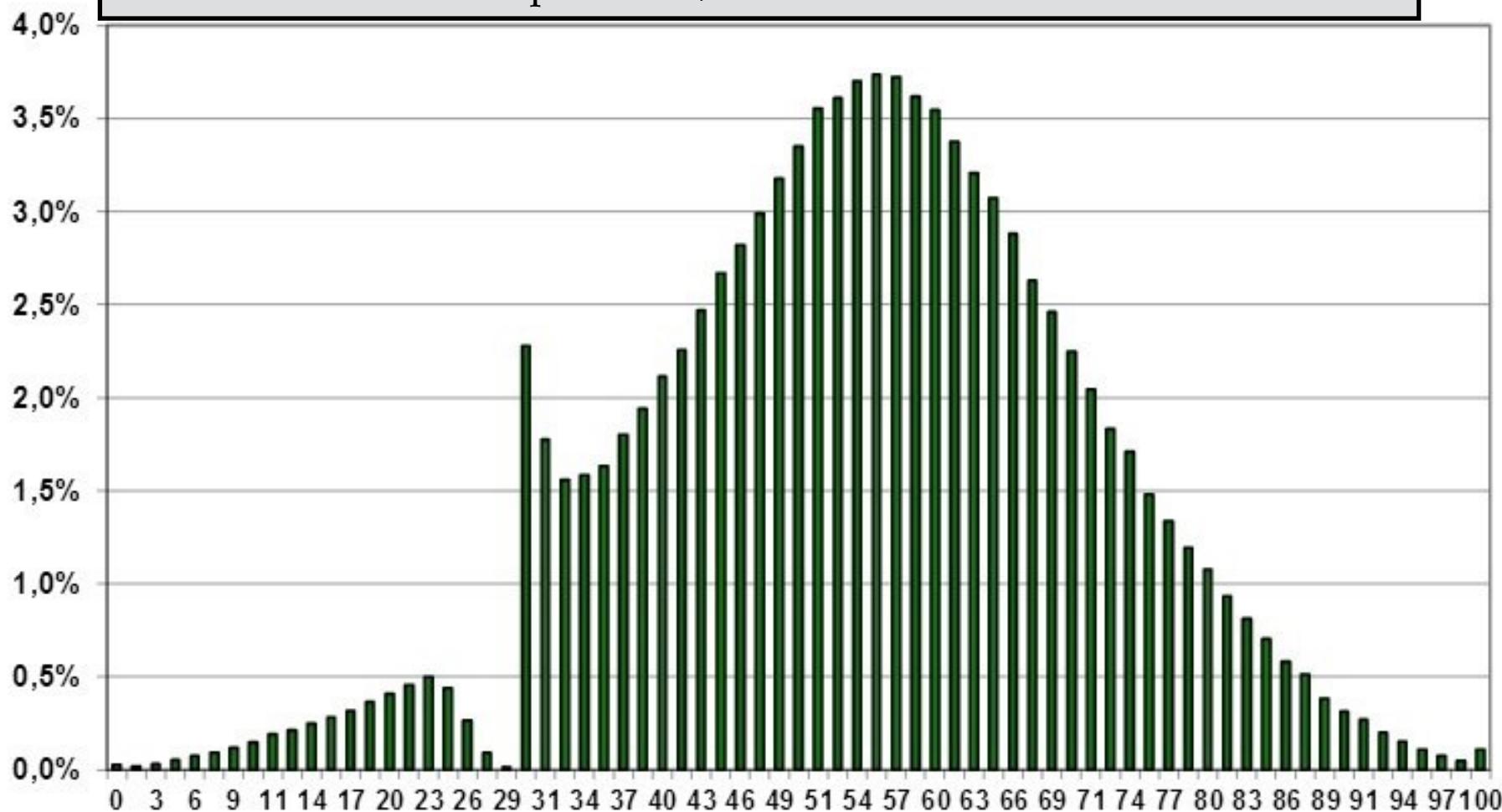
Following the Higgs discovery, the ATLAS collaboration produced the following two animations, which show the buildup of Higgs signal with time / data.



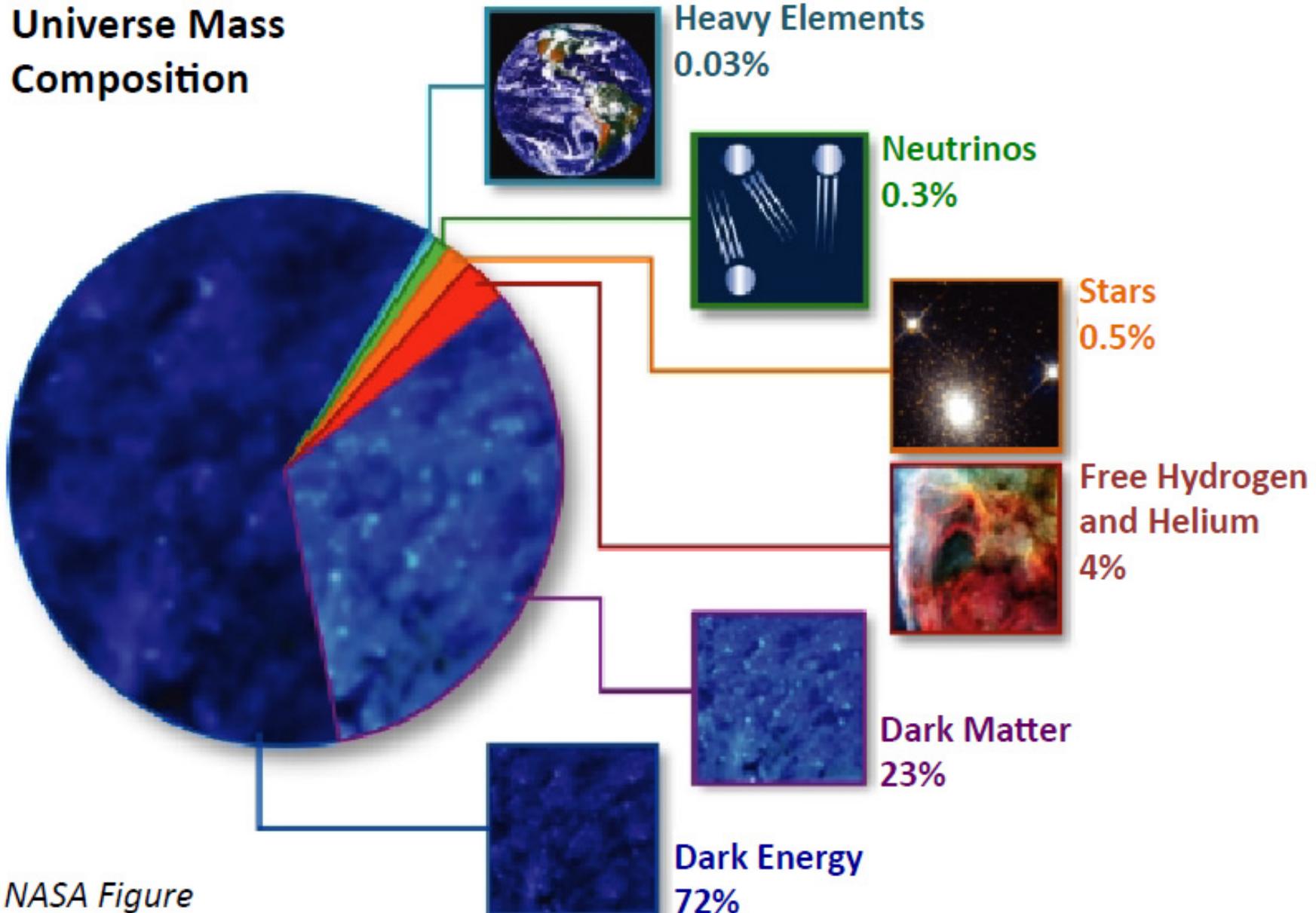
Distributions and social effects

2.1. Poziom podstawowy

Distribution of Matura (high school exit exam) results in Poland in 2013.
The minimum score to pass is 30%.



Universe Mass Composition



Overview

ATLAS Searches* - 95% CL Lower Limits (EPS-HEP 2011)

SUSY

MSUGRA/CMSSM : 0-lep + $E_{T,\text{miss}}$

Simplified model (light $\tilde{\chi}_0^0$) : 0-lep + $E_{T,\text{miss}}$

Simplified model (light $\tilde{\chi}_0^0$) : 0-lep + $E_{T,\text{miss}}$

Simplified model (light $\tilde{\chi}_1^0$) : 0-lep + $E_{T,\text{miss}}$

Simplified model : 0-lep + b-jets + $E_{T,\text{miss}}$

Pheno-MSSM (light $\tilde{\chi}_0^0$) : 2-lep SS + $E_{T,\text{miss}}$

Pheno-MSSM (light $\tilde{\chi}_1^0$) : 2-lep OS_{sf} + $E_{T,\text{miss}}$

GMSB (GGM) + Simpl. model : $\gamma\gamma + E_{T,\text{miss}}$

GMSB : stable $\tilde{\tau}$

Stable massive particles : R-hadrons

Stable massive particles : R-hadrons

Stable massive particles : R-hadrons

RPV ($\lambda_{311} = 0.01, \lambda_{312} = 0.01$) : high-mass e μ

Large ED (ADD) : monojet

UED : $\gamma\gamma + E_{T,\text{miss}}$

RS with $k/M_{Pl} = 0.1$: $m_{\gamma\gamma}$

RS with $k/M_{Pl} = 0.1$: $m_{ee/\mu\mu}$

RS with top couplings $g_L = 1.0, g_R = 4.0 : m_{t\bar{t}}$

Quantum black hole (QBH) : $m_{\text{dijet}}, F(\chi)$

QBH : High-mass σ_{t+x}

ADD BH ($M_{th}/M_D = 3$) : multijet $\Sigma p_T, N_{\text{jets}}$

ADD BH ($M_{th}/M_D = 3$) : SS dimuon $N_{\text{ch. part.}}$

qqqq contact interaction : $F_\chi(m_{\text{dijet}})$

qqqμ contact interaction : $m_{\mu\mu}$

SSM : $m_{ee/\mu\mu}$

SSM : $m_{Te/U}$

Scalar LQ pairs ($\beta=1$) : kin. vars. in eejj, evjj

Scalar LQ pairs ($\beta=1$) : kin. vars. in μμjj, μνjj

4th family : coll. mass in Q₄ $\bar{Q}_4 \rightarrow WqWq$

4th family : d₄ $\bar{d}_4 \rightarrow WtWt$ (SS dilepton)

Major. neutr. ($V_{4\text{-term.}}, \Lambda = 1 \text{ TeV}$) : SS dilepton

Excited quarks : m_{dijet}

Axigluons : m_{dijet}

Color octet scalar : m_{dijet}

ATLAS
Preliminary

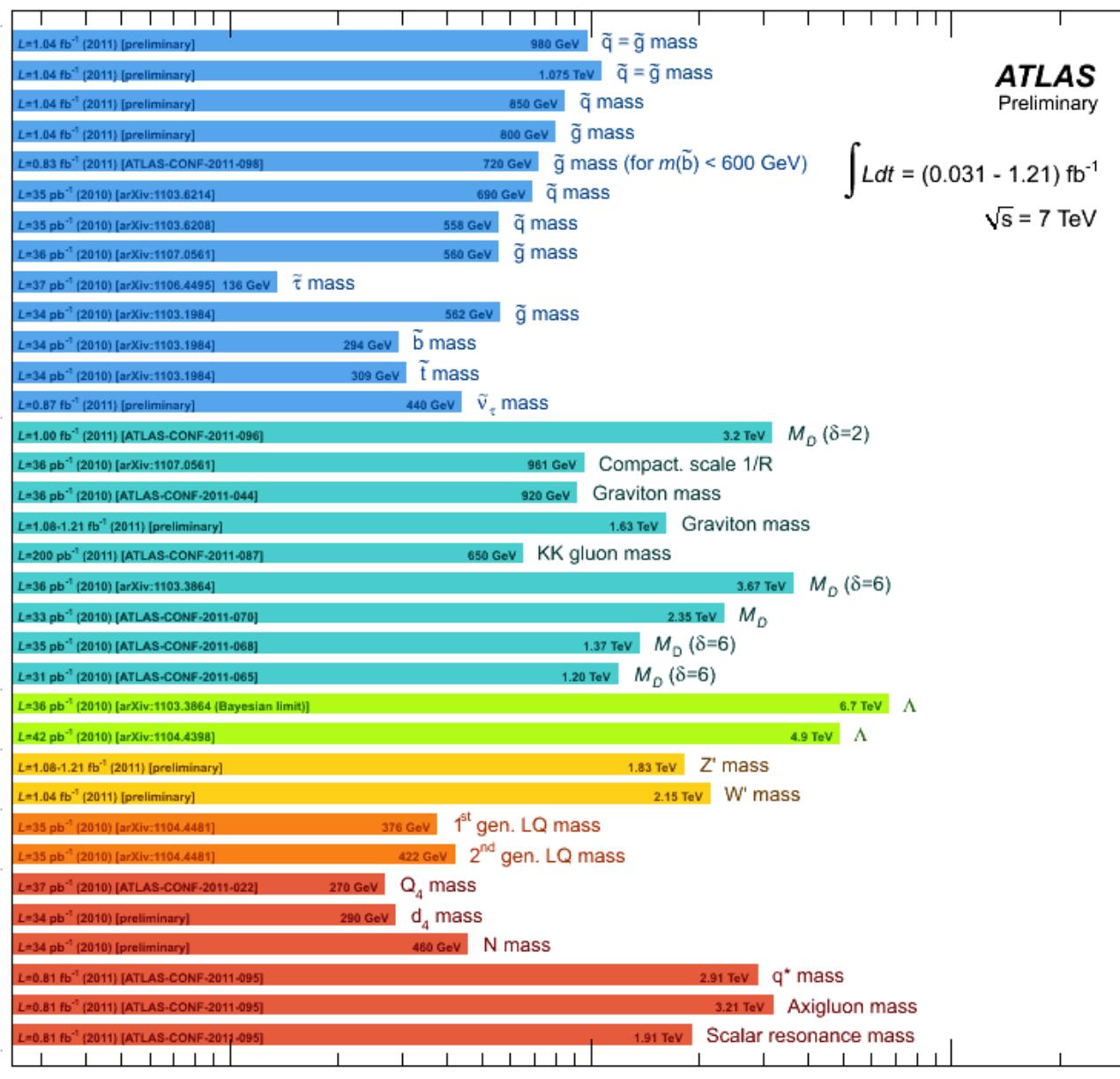
$$\int L dt = (0.031 - 1.21) \text{ fb}^{-1}$$

$$\sqrt{s} = 7 \text{ TeV}$$

Extra dimensions

LQ / Z' / W' Ct. I.

Other



10⁻¹

1

10

Mass scale [TeV]