

$$\int_0^\infty f(x)dx = \sum_{n=1}^N \frac{n-1}{n!} \tag{1}$$