Problem 2

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[15]: import numpy as np
      spambase = np.loadtxt('spambase.data', delimiter=',')
[16]: np.random.shuffle(spambase)
      y = spambase[:, -1].astype(int)
      X = np.zeros(np.array(spambase.shape) - np.array([0, 1]), dtype=int)
      X[spambase[:, :-1] > np.median(spambase[:, :-1], axis=0)[None, :]] = 1
[17]: X_train, y_train = X[:2000, :], y[:2000]
      X_{val}, y_{val} = X[2000:, :], <math>y[2000:]
[18]: eta = y_train.sum() / 2000 # P[y=1]
      theta = np.array([
          X_train[np.logical_not(y_train), :].sum(axis=0) / (eta*2000),
          \# P[xi = 1 \mid y = 0] \text{ over } i = 1, ..., d
          X_train[y_train.astype(bool), :].sum(axis=0) / (eta*2000)
          \# P[xi = 1 \mid y = 1] \text{ over } i = 1, ..., d
      ]).T
      one_minus_theta = 1 - theta
      \# P[xi = 0 \mid y = 0], P[xi = 0 \mid y = 1]
[19]: def y_hat(x):
          P = np.array([
              eta * theta[x.astype(bool), y].prod() * one_minus_theta[np.
       →logical_not(x), y].prod() for y in range(2)
          ]) \# P[y] * prod(P[xi | y]) over y = 0, 1
          return P.argmax()
[20]: y_test = np.array([
          y_hat(X[-i-1, :]) for i in range(X.shape[0] - 2000)
      ])[::-1]
      error = np.abs(y_val - y_test).mean()
      error
[20]: 0.08419838523644751
[21]: y_naiv = int(y_train.mean() > 0.5)
      error_naiv = np.abs(y_val - y_naiv).mean()
      error_naiv
```

[21]: 0.4002306805074971