

HUM 475

Md. Hasin Abrar (1605082)

$$Y = 6A^3 - 3B^2 - 441A + 162B + 36$$

Taking partial derivative with respect to A and B;

$$\frac{\partial Y}{\partial A} = 18A^2 - 441$$

$$\text{and } \frac{\partial Y}{\partial B} = -6B^2 + 162$$

$$\text{again, } \frac{\partial^2 Y}{\partial A^2} = 36A$$

$$\text{and } \frac{\partial^2 Y}{\partial B^2} = -12B$$

So, in order to find the critical points,

$$\frac{\partial Y}{\partial A} = 0$$

$$\Rightarrow 18A^2 - 441 = 0$$

$$\Rightarrow A = \pm \sqrt{\frac{441}{18}} = \pm \frac{7}{\sqrt{2}}$$

$$\text{and } \frac{\partial Y}{\partial B} = 0$$

$$\Rightarrow -6B^2 + 162 = 0$$

$$\Rightarrow B = \pm 3\sqrt{2}$$

Plugging these values into  $\frac{\partial^2 Y}{\partial A^2}$  and  $\frac{\partial^2 Y}{\partial B^2}$  we get,

$$\frac{\partial^2 Y}{\partial A^2} = \pm \frac{252}{7} \quad \text{and} \quad \frac{\partial^2 Y}{\partial B^2} = \mp 54\sqrt{2}$$

$$\text{At } (A, B) = \left(\frac{7}{\sqrt{2}}, -3\sqrt{2}\right), \quad \frac{\partial^2 Y}{\partial A^2} \cdot \frac{\partial^2 Y}{\partial B^2} > 0$$

So,  $\left(\frac{7}{\sqrt{2}}, -3\sqrt{2}\right)$  is a relative ~~min~~ minimum

$$\text{At } (A, B) = \left(-\frac{7}{\sqrt{2}}, 3\sqrt{2}\right), \quad \frac{\partial^2 Y}{\partial A^2} \cdot \frac{\partial^2 Y}{\partial B^2} > 0 \quad \text{minimum}$$

So,  $\left(-\frac{7}{\sqrt{2}}, 3\sqrt{2}\right)$  is a relative ~~maximum~~.

$$\text{At points } \left(\frac{7}{\sqrt{2}}, 3\sqrt{2}\right) \text{ and } \left(-\frac{7}{\sqrt{2}}, -3\sqrt{2}\right), \quad \frac{\partial^2 Y}{\partial A^2} \cdot \frac{\partial^2 Y}{\partial B^2} < 0.$$

So, these points are relative maximum.