

Questions 7

1. How do you allocate GSL vectors and matrices?

To allocate a GSL vectors, you type:

```
gsl_vector *v1 = gsl_vector_alloc (size_t n);
gsl_vector *v2 = gsl_vector_calloc (size_t n);
```

To allocate a GSL matrix, you type:

```
gsl_matrix *m1 = gsl_matrix_alloc (size_t n1, size_t n2);
gsl_matrix *m2 = gsl_matrix_calloc (size_t n1, size_t n2);
```

the difference between `alloc` and `calloc`, is that `calloc` initializes all the elements as zeros, where `alloc` doesn't. In the end, you will need to free them, with

```
gsl_vector_free (gsl_vector *v);
gsl_matrix_free (gsl_matrix *m);
```

Problem 20: Implement the Arctangent function using integral representation.

$$\arctan(x) = \int_0^x \frac{1}{z^2 + 1} dz. \quad (1)$$

To facilitate numerical integration reduce the argument to a reasonable interval (e.g. $[0, 1]$) using the formulae (check them),

$$\arctan(-x) = -\arctan(x) \quad (2)$$

$$\arctan\left(\frac{1}{x}\right) = \frac{\pi}{2} - \arctan(x), \quad \text{if } x > 0. \quad (3)$$

prior to integration. Compare with the corresponding function from `<math.h>` or from `GSL`.

The problem was solved by integrating with `gsl/gsl_integrate.h`. First the integrand from eq. 1 was define:

```
double arctan_integrand (double z, void *params){
    return 1/(pow(z,2) + 1);
}
```

and then the GSL integration routine was build:

```
double my_arctan (double x){
    if(x<0) return - my_arctan(-x);
    if(x>1) return M_PI/2 - my_arctan(1/x);
    if(x==0) return 0;
}
```

```

gsl_function f;
f.function = arctan_integrand;
f.params = NULL;

int limit = 100;
double a = 0, b = x, epsabs = 1e-9, epsrel = 1e-9, result, error;
gsl_integration_workspace *w =
    gsl_integration_workspace_alloc (limit);
int status = gsl_integration_qags
    (&f, a, b, epsabs, epsrel, limit, w, &result, &error);
gsl_integration_workspace_free (w);
if (status != GSL_SUCCESS) return NAN;
else return result;
}

```

The three if statements ensures that the function only integrates in the range of $[0, 1]$.

The result of the integration was compared using `atan(x)` from `<math.h>` in the main function, and plottet with points, see fig. 1.

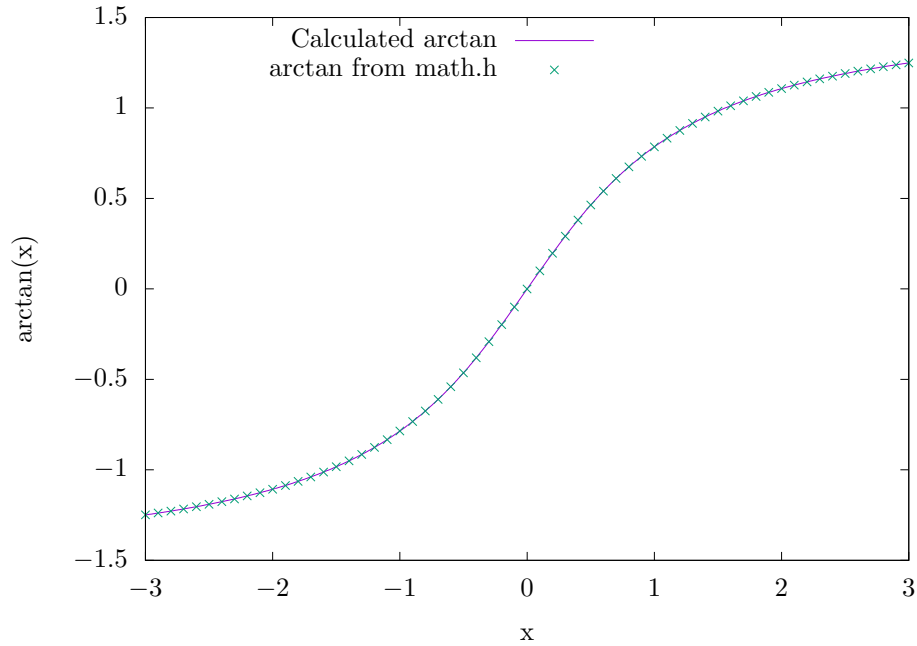


Figure 1: Plot of calculated and exact $\arctan(x)$, every 10th result of the \arctan from `math.h` was plottet as points for clarity.