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Abstract:

In the realm of digital image processing, the pursuit of clarity and detail amidst inherent noise is a fundamental challenge. This project delves into the intricacies of image enhancement through the development and application of various filtering techniques aimed at noise reduction and image sharpening. We explore the implementation of Average and Median filters, which serve to diminish the effects of noise by smoothing the image through the calculation of local statistical measures. The Sobel operator is employed to accentuate edges, thereby enhancing image features, and facilitating a crisper visual perception. Furthermore, we delve into the frequency domain with Fourier transforms to selectively amplify specific spatial frequencies, contributing to the sharpness of the image. A Gaussian filter with a 5x5 kernel is meticulously designed to provide a subtle yet effective blurring effect, which mitigates noise while preserving essential details. Additionally, a Low-Pass filter is crafted to attenuate high-frequency noise, rendering a smoother image appearance. This comprehensive study not only demonstrates the practical application of these filters through a user-friendly graphical interface but also presents a comparative analysis of their effects on image quality. The project culminates in a software tool that embodies the synthesized knowledge, providing an intuitive platform for image processing and analysis.

Data Samples

In this project, we were given **two images by our teacher** to help us test our image-cleaning program. The first is a very grainy and noisy image, perfect for trying out filters like the Median, Average, and Gaussian that are meant to make images clearer by removing noise. The second sample image, we used it to see how well filters that enhance image details work, specifically the edge-highlighting Sobel Mask and the High-Pass Filter using Fourier transform techniques. To dig deeper, **I also picked six more grayscale pictures**—half with varying noise levels

to push our noise-reduction filters further and the rest to test the detail-enhancing filters' effectiveness.

Samples from the professor = 2

Samples from Internet = 6

Average Filter Explanation and Testing Results

The average filter is a simple yet **effective tool in image processing used for noise reduction**. It operates by taking a **neighborhood of pixels around a target pixel and calculating their average value**. This average value is then assigned to the target pixel.

Here's how the algorithm works: For each pixel in the image, the filter considers a square group of pixels around it. **In our tests**, we used a **5x5 dimension**, meaning each target pixel was averaged with the **24 surrounding pixels**. The filter sums up the values of these **25 pixels** (the target and its neighbors) and then divides this total by 25 to get the average. This average is what replaces the original pixel value.

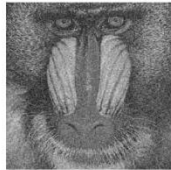
For this project, I conducted four different tests using four distinct images with noise. One of these images was provided by my instructor, and the other three were downloaded from the internet for additional testing. After applying the average filter with a 5x5 dimension to these images, **I observed that it indeed removes noise effectively. However, a notable side effect was that the images became quite blurry**. This blurring occurs because the filter replaces each pixel's value with the average of its neighbors, **leading to a loss of fine details in the image**. This effect is particularly noticeable around edges and in areas with subtle textures, where the averaging process tends to smooth out the distinct features.



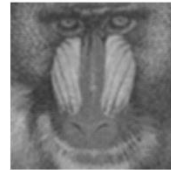
Original Image



1(a) Average filter



Original Image



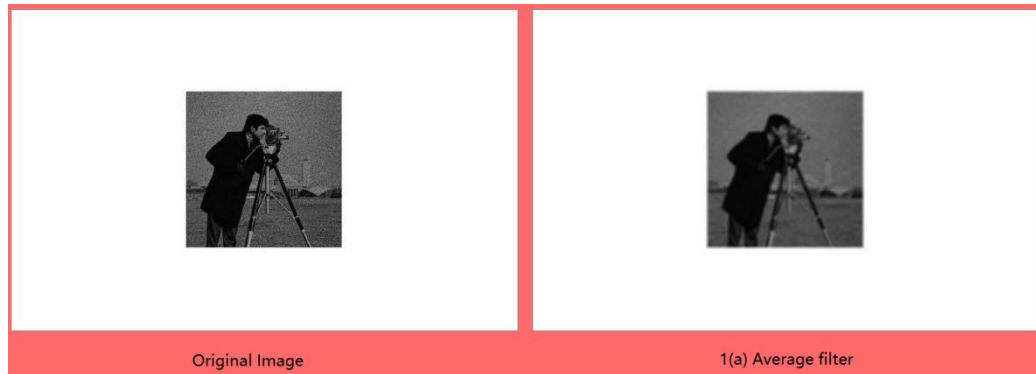
1(a) Average filter



Original Image



1(a) Average filter



Median Filter Explanation and Testing Results:

The median filter is a **robust tool for noise reduction in image processing**, distinguished by its approach of **selecting the median value from a neighborhood of pixels**. Unlike the average filter, which computes the mean value, the median filter operates by sorting the pixel values within a specified window and choosing the value that falls in the middle of this sorted sequence.

The process involves the following steps:

Select a Neighborhood of Pixels: The median filter examines a square group of pixels around the target pixel. In our tests, **I used a 5x5 window**, encompassing the target pixel and its **24 neighbors**.

Sort the Pixel Values: The values of these pixels are arranged in ascending order.

Find the Median Value: The median, being the middle value in the sorted list, is determined. For a 5x5 window, this would be the **13th value when arranged from lowest to highest**.

Replace the Target Pixel with the Median: This median value is then assigned to the target pixel, replacing its original value.

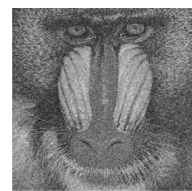
After implementing the median filter with a 5x5 dimension on various images, it became clear that its performance in noise removal **surpassed that of the average filter.** It effectively minimized noise while better preserving the fine details of the images. Although a slight blur is introduced, the median filter's impact on image clarity is less severe than that of the average filter, making it a more suitable choice for maintaining the integrity of the image's details while reducing noise.



Original Image



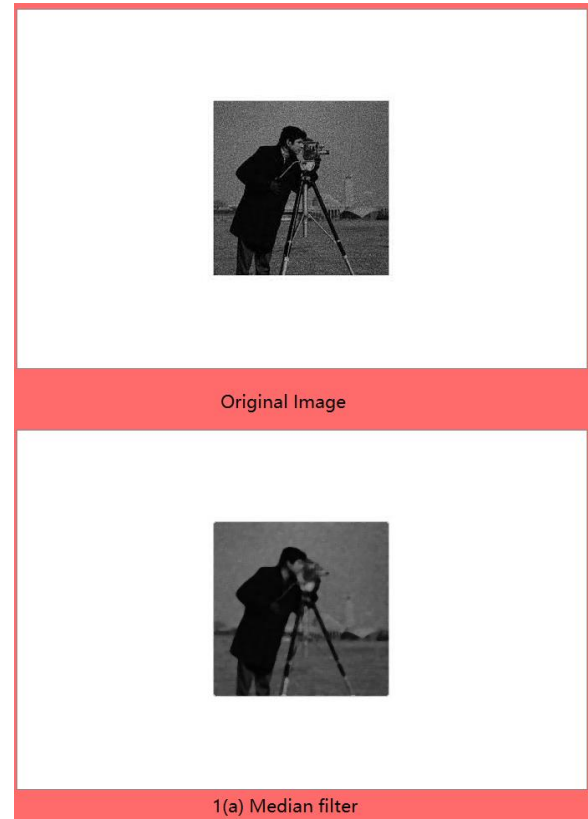
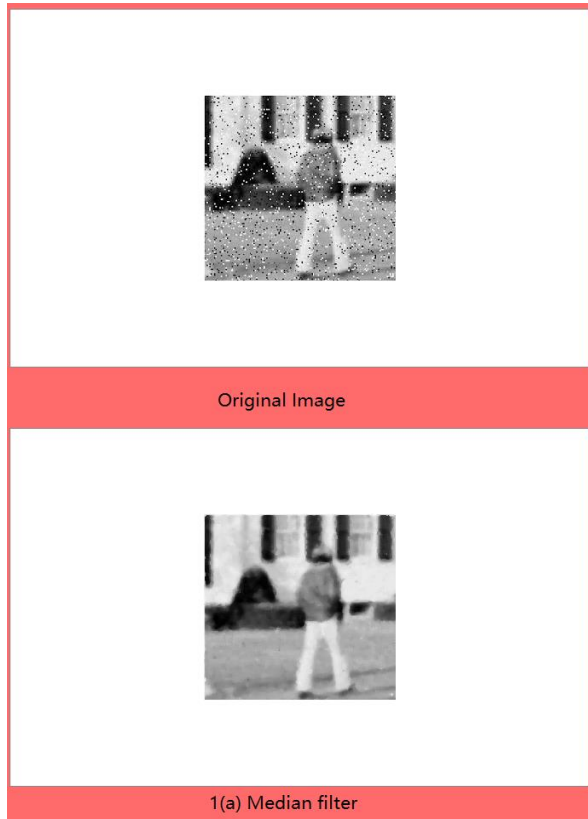
1(a) Median filter



Original Image



1(a) Median filter



Low-Pass Filter in the Frequency Domain Explanation

A Low-Pass Filter (LPF) in the frequency domain is an interesting technique in image processing that's **used to reduce high-frequency components (like noise and fine details) in an image**. Here's how it functions:

Frequency Domain Conversion: First, the image is transformed from the spatial domain to the frequency domain using a mathematical operation known as the Fourier Transform. This process converts the image so that instead of representing pixel intensities, it represents how frequently different patterns occur in the image.

Applying the Filter: A low-pass filter works by **allowing only the lower frequencies to pass through while attenuating (reducing the strength of) the higher frequencies**. The lower frequencies represent the general layout and smooth variations in the image, while the higher frequencies represent the finer details and noise.

Filter Shape and Radius: The filter typically has a circular (radial) shape in the frequency domain. The radius of this circle determines the cut-off frequency. A **smaller radius** means a tighter circle, **which allows fewer high-frequency components to pass**, resulting in a smoother (but potentially blurrier) image. Conversely, a **larger radius allows more high-frequency components** through, **preserving more details but also potentially more noise**.

Transform Back to Spatial Domain: After applying the LPF, the image is converted back to the spatial domain using the **Inverse Fourier Transform**. This step reconstructs the image from its frequency representation, now altered by the LPF, to a form we can visually interpret.

Mask Design and Radius Adjustment: The LPF uses a circular mask in the frequency domain. The values within this mask's radius are **set to 1, allowing those frequencies to pass through unchanged**. This means that the larger the radius, **the more high-frequency components (like sharp edges and noise) are allowed through**. In contrast, values outside this radius **are set to 0, effectively blocking those frequencies**. A smaller radius thus allows fewer high frequencies to pass, leading to more noise reduction but also increased blurring.

Testing with Different Radius: In my experiments, **I adjusted the radius of the LPF to 15, 39, 45, and 60** to observe its impact on noise reduction and image clarity. With a **radius of 15**, the noise was significantly reduced, but the resulting image was **very blurry**, making it hard to discern details. Increasing the **radius to 30 still resulted in noticeable blurring**. At a **radius of 45, the balance improved**; the finer details of the image were more visible, and the filter effectively **reduced noise**. However, when **the radius was set to 60**, the image clarity improved with **minimal blur, but the noise reduction was less effective**.

Conclusion: My tests indicate that while the low-pass filter in the frequency domain is an intriguing technique, **it's not as effective as the median filter for noise reduction. It also involves a more complex process**, requiring additional steps to manipulate and transform the image into and out of the frequency domain. Therefore, although it can be a useful tool, it might not always be the most practical choice for simple noise reduction tasks.

Radio=15



1(b) Fourier transform

Radio=30



1(b) Fourier transform

Radio=45



1(b) Fourier transform

Radio=60



1(b) Fourier transform

Sobel Mask Explanation and Testing Results

The Sobel mask is a widely used image processing technique, **particularly effective for edge detection**. It emphasizes the transitions in intensity, which are typically found at the boundaries between different objects within an image.

Functionality of Sobel Mask: The Sobel mask works by convolving the image with two separate kernels, one for detecting changes in brightness horizontally, and another for detecting them vertically. These convolutions highlight the gradients or changes in intensity, effectively outlining the edges.

Testing with Different Image Samples: For my testing, I selected four different images to apply the Sobel mask and observe its effectiveness in various contexts. I initially used a 5x5 Sobel filter, which provided a good balance between edge detection and maintaining image clarity.

Adjusting Mask Dimensions: I experimented with different dimensions of the Sobel mask to see how they would affect the outcome. When the mask was set to smaller dimensions like 3x3, the results were more pronounced, with clear and distinct edges. This smaller size seemed to capture the fine details more effectively. However, as I increased the mask size to 19x19, the edges became less distinct, appearing wider and more blurred, similar to a blurring effect. The larger mask seemed to blend the transitions in intensity over a broader area, losing some of the precision in edge detection.

Conclusion: The tests showed that while the Sobel mask is excellent for highlighting edges, the size of the mask significantly influences the results. Smaller masks like 3x3 provided sharper and more distinct edge detection, making them more suitable for images where fine details are important. In contrast, larger masks may be useful for a more generalized edge detection but can lead to a loss of sharpness and clarity in the edges.

5x5 mask



Original Image



2(a) Sobel mask

3x3 mask

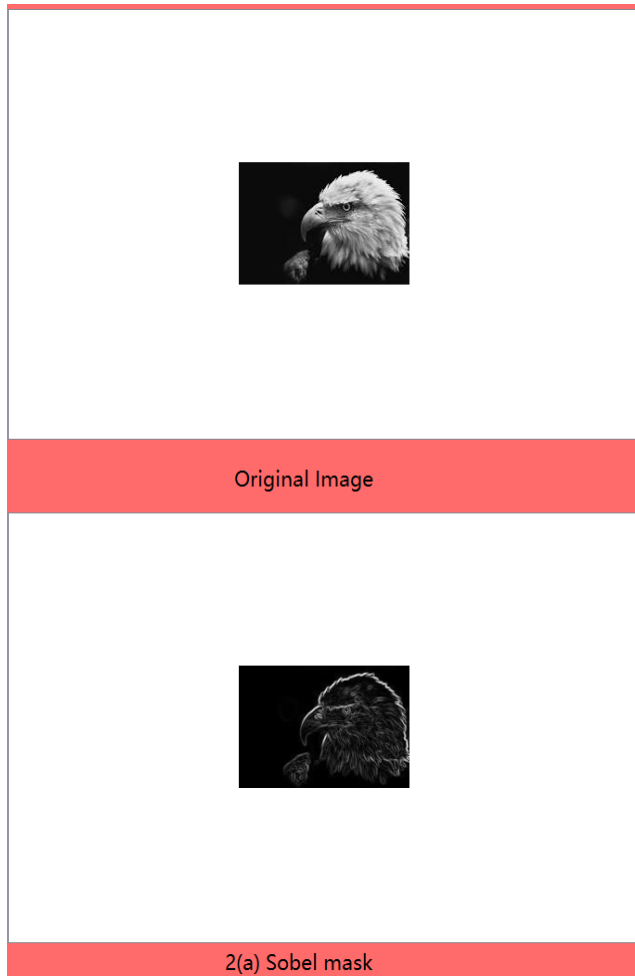


Original Image

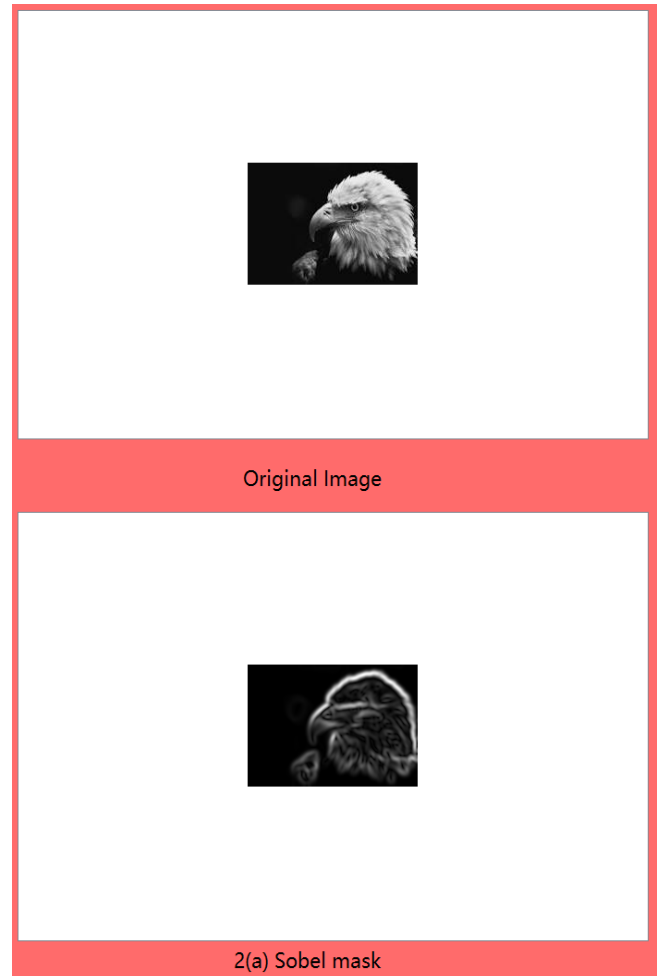


2(a) Sobel mask

3x3 mask



19x19 mask



High-Pass Filter in the Frequency Domain Using Fourier Transform Explanation and Testing Results

The High-Pass Filter (HPF) in the frequency domain, implemented using the Fourier Transform, functions as the **opposite of the Low-Pass Filter**. It is designed to allow high frequencies to pass while **blocking low frequencies**.

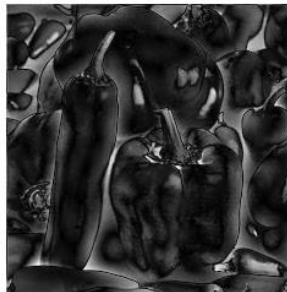
Functionality of High-Pass Filter: In the context of an image, **high frequencies correspond to the edges and fine details**, while **low frequencies represent smooth, slow-changing areas**. The HPF uses a circular mask in the frequency domain, similar to the LPF, but with a crucial difference: **the values inside the**

radius of the HPF are set to 0, effectively blocking low-frequency components, while **the values outside the radius are set to 1**, allowing high-frequency components to pass through.

Testing with Varying Radio: I conducted tests by adjusting the radius of the HPF to **5, 20, and 30**, and observed how these changes impacted the definition of edges in the images. With a smaller radius, more high frequencies are allowed to pass, which resulted in broader and less finely defined edges. As I increased the radius to **20 and then 30, the edges became finer**, but there was an introduction of a **slight blur**, especially at the higher radius.

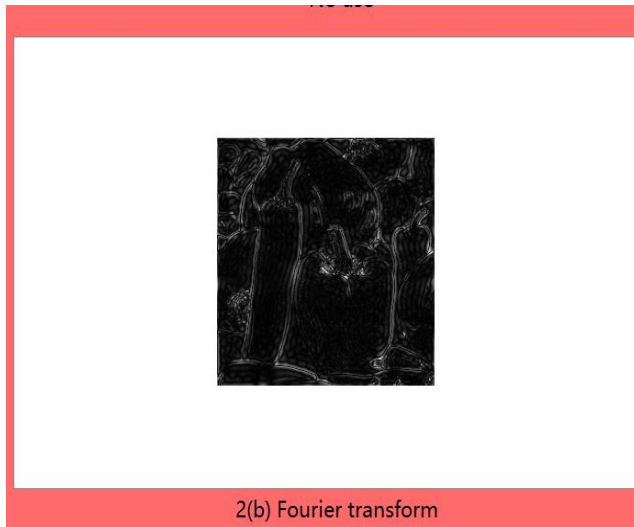
Conclusion: Based on my tests, I conclude that while the high-pass filter can be used for sharpening edges, **its effectiveness is radius-dependent**. Smaller radio led to less fine edge definition, and larger radio **introduce a blur**. Comparatively, the **Sobel mask proved to be more effective and easier to use for sharpening edges**. The Sobel mask delivered clearer results without the blur, offering a more precise refinement of edges. This makes it a preferable choice for tasks requiring sharp and clear edge definition in images.

Radio=5



2(b) Fourier transform

Radio=20



Radio=30



Gaussian Filter with a 5x5 Mask in the Spatial Domain Explanation and Testing Results

The Gaussian filter, applied in the spatial domain with a **5x5 mask**, is a fundamental tool in image processing known for its effectiveness in noise reduction and image smoothing.

Functionality of Gaussian Filter: This filter applies a Gaussian blur to an image. **It works by convolving the image with a Gaussian kernel**, a type of weighted average where pixels closer to the **center of the mask are given more weight**. The shape of the Gaussian function is determined by the **standard deviation (σ , sigma)**, which controls the extent of smoothing.

Testing with Different Sigma Values: The key to adjusting the Gaussian filter is altering the sigma value. **In my tests, I initially set sigma to 1.0**, resulting in a narrower and taller Gaussian curve. This configuration gives more weight to the central pixels in the kernel, **effectively reducing noise while maintaining a reasonable level of detail in the image**. However, to explore the filter's range, **I then exaggerated sigma to 50**. This significantly widened the Gaussian curve and lowered its peak, which meant that distant pixels in the kernel were given more

weight. Consequently, this resulted **in a much smoother image but introduced considerable blurring and loss of fine details.**

Conclusion: The tests highlight the Gaussian filter's versatility in noise reduction and smoothing, with the sigma value playing a crucial role in determining the filter's impact. A lower sigma value like 1.0 offers a balance between noise reduction and detail preservation, while a much higher sigma value leads to pronounced blurring, suitable for aggressive smoothing but at the expense of image details. This demonstrates the Gaussian filter's adaptability to different image processing needs, depending on the desired balance between noise reduction and clarity.

Sigma=1.0



Original Image



Gaussian Filter(Spatial Domain
Low-pass)

Sigma=50.0



Original Image



Gaussian Filter(Spatial Domain
Low-pass)

Gaussian Low-Pass Filter in the Frequency Domain Using Fourier Transform Explanation and Testing Results

The Gaussian Low-Pass Filter (LPF) in the frequency domain, applied using the Fourier Transform, is a sophisticated method for smoothing images while reducing **high-frequency noise**.

Functionality and Application: This filter works by applying a Gaussian blur in the frequency domain. The process starts by transforming the image from the spatial domain to the frequency domain using the Fourier Transform. A Gaussian function, characterized by its **standard deviation (sigma)**, is then applied as a filter. The size of the filter is adjusted to match the size of the image.

Testing with Different Sigma Values: In my tests, I experimented with various sigma values to understand their impact on the filtering effect. With a smaller **sigma, like 10.0, the Gaussian bell curve is narrow with a sharp peak**. Since the filter size matches the image, this sharp, narrow curve significantly affects the image, **leading to a loss of details and a blurry output**. **Increasing sigma to 20.0**, the bell curve widens slightly, allowing the image to retain a bit more detail, but still resulting in noticeable blurring.

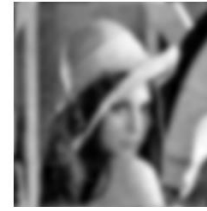
Finally, setting sigma to 50.0 produced a more balanced effect. The Gaussian curve becomes much wider with a shorter peak, which means the intensity of the filter's effect is more diffused across the image. This leads to a gentler smoothing effect, **slightly reducing noise while maintaining more of the image's clarity and details**.

Conclusion: The tests demonstrate that the effectiveness and impact of the Gaussian LPF in the frequency domain are largely dictated by the sigma value. A smaller sigma results in a stronger filter effect with more blurring, whereas a larger sigma offers a more subtle effect, smoothing the image while preserving more details. This highlights the filter's adaptability, showing how adjustments to sigma can tailor the balance between noise reduction and detail preservation to suit various image processing needs.

Sigma=10.0



Original Image



Gaussian Filter(Frequency Domain
Low-pass)

Sigma=20.0



Original Image



Gaussian Filter(Frequency Domain
Low-pass)

Sigma=50.0



Original Image



Gaussian Filter(Frequency Domain
Low-pass)

Conclusion

In this exploration of image processing filters, **the median filter emerged as the most effective for noise reduction**, closely followed by **the Gaussian low-pass filter in the frequency domain**. The median filter excelled in preserving image details while minimizing blur and noise, benefiting from its simpler application in the spatial domain compared to the more complex frequency domain process of the Gaussian filter.

For edge enhancement, the Sobel mask proved superior, especially with smaller kernel sizes like 3x3, which produced sharp, well-defined edges. In contrast, the high-pass filter in the frequency domain tended to blur edges as they became finer.

This project has not only deepened my understanding of fundamental image processing techniques but has also sparked a curiosity to explore more advanced and contemporary filters. The experience gained in manipulating these basic filters lays a foundation for future investigations into innovative image processing methods.