Template

 \mathbf{Y} November 2, 2019

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1 Basic

1.1 .vimrc

```
// vim ~/.vimrc
set nu ai ci si mouse=a ts=2 sts=2 sw=2
nmap<F3>: !gedit % <CR>
nmap<F8>: !time ./% < %<.iin <CR>
nmap<F5>:call CR()<CR>
func: CR()
exec "!g++ % -0 %<"
exec "!g++ % -0 %<"
exec "! ./%<"
endfunc
map<F2>:call SetTitle() <CR>
func SetTitle()
let l = 0
let l = 1 + 1 | call setLine(1, '#include <bits/stdc++.h>')
let l = 1 + 1 | call setLine(1, 'using namespace std;')
endfunc
endfunc
endfunc
```

1.2 head

```
\#define rk(x) upper\_bound(all(V), x) - V.begin()
                                                                                                                                                                                         #define de(x) cout << \#x << "=" << x < end] #define rep(i,a,b) for(int i=(a);i<(b);++i) #define per(i,a,b) for(int i=(b-1);i>=a;--i) #define all(x) (x).begin(),(x).end()
                                                                                                                                                                   #define dd(x) cout << \pm x << \pm x << \pm x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ios::sync_with_stdio(false);
                                                                                                                                                                                                                                                                                                         #define sz(x) (int)(x).size()
                                                                                                             typedef pair<int,int> pii;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           #define lowbit(x) x&(-x)
#include<bits/stdc++.h>
                                                                                                                                       typedef vector<int> vi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       #define inf 0x3f3f3f3f
                                                        typedef long long 11;
                                                                                                                                                                                                                                                                                                                                     #define mp make_pair
                                                                                                                                                                                                                                                                                                                                                                   #define pb push_back
                              using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           const int M = 1e9+7;
                                                                                 typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                       #define se second
                                                                                                                                                                                                                                                                                                                                                                                                                                                   #define endl "\n"
                                                                                                                                                                                                                                                                                                                                                                                           #define fi first
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main(){
```

3 stl

```
#include<pits/stdc+.h>
using namespace std;
int main(){
    int num[6]={1,2,4,7,15,34},x=7;
    sort(num, num+6);// 从小到大排序
    lower_bound(num, num+6,x);// 第一个大手的指针x
    upper_bound(num, num+6,x);// 第一个大于的指针x
    sort(num, num+6, greater<int>());// 从大到小排序
    lower_bound(num, num+6, x, greater<int>());// 第一个小等于的指针x
    upper_bound(num, num+6, x, greater<int>());// 第一个小手的指针x
    return 0;
}
```

DataStructure

2

1 ST

```
// [0, n)
struct ST{
    static const int N = 101010;
    int a[20][N], 1g[N];
    void build(int *v, int n){
        rep(i, 2, n + 1) 1g[i] = 1g[i >> 1] + 1;
        rep(i, 0, n) a[0][i] = v[i];
        rep(i, 1, 1g[n] + 1) rep(j, 0, n - (1 << i) + 1) {
            a[i][j] = max(a[i - 1][j], a[i - 1][j + (1 << i >> 1)]);
        }
    }
}
int qry(int l, int r){
    int qry(int l, int r);
    int i = 1g[r - 1 + 1];
    return max(a[i][l], a[i][r + 1 - (1 << i)]);
}
return max(a[i][l], a[i][r + 1 - (1 << i)]);
}
</pre>
```

Geo

3.1 基础点、向量

```
struct P {
    int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0); }
    P rot90() { return P(-y, x); }
    P rot(db a) { return P(cos(a) * x - sin(a) * y, cos(a) * y + sin(a) * x); }
    P rorm() { return *this / len(); }
    P norm() { return atan2l(det(p1, p2), dot(p1, p2)); } // p1 与 p2 的夹角, 有方 db rad(P p1, P p2) { return atan2l(det(p1, p2), dot(p1, p2)); } // p1 与 p2 的夹角, 有方 自 bool cmp(const pii &a, const pii &b) { // 级角排序 int o = a > pii(0, 0), t = b > pii(0, 0); if(o != t) return o < t;
```

```
db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool isLS(P a1, P a2, P b1, P b2) { // 判断直线线段是否相交 (端点也算) db c1 = det(a2 - a1, b1 - a1), c2 = det(a2 - a1, b2 - a1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return sign(c1) * sign(c2) < 0 & sign(c3) * sign(c4) < 0;
                                                                                                                                                                                                                  auto Rand = [&] () { return rand() % 10000 / 5000 * pi; }; P ans(0, 0); rep(i, 0, n) ans = ans + p[i]; ans = ans / n; db len = 0; rep(i, 0, n) len += (ans - p[i]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      sign(\max(a.s.x,\ a.t.x) - \min(b.s.x,\ b.t.x)) >= 0 \&\& sign(\max(b.s.x,\ b.t.x) - \min(a.s.x,\ a.t.x)) >= 0 \&\&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        sign(max(a.s.y, a.t.y) - min(b.s.y, b.t.y)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sign(max(b.s.y, b.t.y) - min(a.s.y, a.t.y)) >= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       <del>ö</del>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 db ang = Rand();
P np(ans.x + t * sin(ang), ans.y + t * cos(ang));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return P(b0 * c1 - b1 * c0, a1 * c0 - a0 * c1) /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            + c = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db k = 0; rep(i, 0, n) k += (np - p[i]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P isLL(db a0, db b0, db c0, db a1, db b1, db c1) { db d = a0 * b1 - a1 * b0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db s2 = -det(12.b - 12.a, 11.b - 12.a);
return (11.a * s2 + 11.b * s1) / (s1 + s2);
P q1 = (p[2] - p[0]).rot(pi / 3) + p[0];
P q2 = (p[0] - p[1]).rot(pi / 3) + p[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(sign(len - k) > 0) ans = np, len = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        isLL(L 1, db a, db b, db c) { // ax + by }
                                                                                                           return isLL(L(q1, p[1]), L(q2, p[2]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db s1 = det(12.b - 12.a, 11.a - 12.a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     db \dot{u} = \dot{a} * 1.a.x + b * 1.a.y + c;
db v = -(a * 1.b.x + b * 1.b.y + c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return (1.a * v + 1.b * u) / (u + v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool isSSr(const L &a, const L &b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return sign(c1) * sign(c2) <= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       由线
                                                                                                                                                                                                                                                                                                                                                                                   db t = 10000; // modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       直线、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                P isLL(L 11, L 12) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool isSS(L a,L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                    while(t > eps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【线相交判定】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   线段、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 【点到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 【直线交点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                \frac{3}{2}
                                                                                                                                                                                                                                                                                                                                                                                                                                    n_{1} = n_{1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(sign(a[i] * a[i] - a[j] * a[j] - a[k] * a[k] - a[j] * a[k]) >= 0) return p[i];
                                                                                                                                                                                                                                                                                                                                                                                   db Xm = p[m].x, lim = min(solve(l, m, p), solve(m + 1, r, p));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, r + 1) if(fabs(p[i].x - Xm) <= lim) V.pb(p[i]);
rep(i, 0, sz(V)) rep(j, i + 1, sz(V)) {
   if(fabs(V[j].y - V[i].y) >= lim) break;
   T dis = (V[i] - V[j]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // sqrt((a ^ 2 + b ^ 2 + c ^ 2 + 4 * sqrt(3) * area) / 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       o = outC(p[i], p[j], p[k]), r = abs(o-p[k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  sort(all(A), [\&](P, a, P, b)\{return a.x < b.x;\});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(det(p[0], p[1], p[2]) < 0) swap(p[1], p[2]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           o = (p[i] + p[j]) / 2, r = abs(o-p[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(sgn(abs(o-p[k])-r) \le 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(sgn(abs(o-p[j])-r) \le 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(sgn(abs(o-p[i])-r) <= 0) continue;
                                                                                                                                                                namespace NearestPoints { // sz(A) <= 1e5
                                                                                                                                                                                                                          db solve(int l, int r, vector<P> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(n == 1) return p[0];

if(n == 2) return (p[0] + p[1]) / 2;

if(n == 3) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 如果有重点, 大于 2 的直接用模拟退火法
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return solve(0, sz(A) - 1, A);
                                                                                                                                                                                                                                                                       if(1 == r) return le100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        random_shuffle(p , p + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   lim = min(lim, dis);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           }
db solve(vector<P> A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return a.y < b.y;});
                                                                                                                                                                                                                                                                                                                             int m = 1 + r >> 1;
        return det(a, b) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 P o = p[0]; db r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P fermat(vector<P> p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  o = p[i], r = 0; rep(j,0,i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          C Mincir(P *p,int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(k,0,j) {
                                                                                                           // 【点集中最近点对】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<P> V;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return C(o,r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return lim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i,1,n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // 【最小圆覆盖】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db a[3];
```

```
if(sgn((r[i][i+1] - r[i][i])) * (r[t][g+1] - r[t][g])) < 0 || i < t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if(du < 0 && dv >= 0) res[sz++] = pdi(s1 / (s1 + s2) , -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res[sz++] = pdi(getLoc(r[i][j], r[i][j+1], r[t][g]), 1);
res[sz++] = pdi(getLoc(r[i][j], r[i][j+1], r[t][g+1]), -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         db s1 = (r[i][j] - r[t][g]) / (r[t][g+1] - r[t][g]); db s2 = (r[t][g+1] - r[t][g]) / (r[i][j+1] - r[t][g]); if(du >= 0 && dv < 0) res[sz++] = pdi(s1 / (s1 + s2) , 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(g,0,r[t].dn) {
  int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
  int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void ins(int x, int y) { ins(h1, P(x, y)); ins(h2, P(x, -y)); } bool in(int x, int y) { return in(h1, P(x, y)) && in(h2, P(x, -y)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
return (p.y - a.y) / (b.y - a.y);
                                                                                                                                                                                                                                                                                                              if(ao(11->se, 1->se, p)) h.erase(1); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(ao(p, r->se, rr->se)) h.erase(r); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                        auto rr = r; rr++; if(rr == h.end()) break;
                                                                                                                                                                                                                                                                                                                                                                                                         auto r = pos; r++; if(r == h.end()) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res[sz++] = pdi(0,0); res[sz++] = pdi(1,0);
                                                                                                                                                                                                              while(1) {
    auto 1 = pos; if(1 == h.begin()) break;
    auto 11 = 1; if(11 == h.begin()) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   P operator [] (const int&n) {return d[n];}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P d[10]; int dn; // d[dn] = d[0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i,0,n) rep(j,0,r[i].dn){
                                 return ao(1—>se, p, r—>se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             namespace ConvecIntersection{ //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(t == i) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(!du && !dv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sort(res , res + sz);
                                                                                                                        if(in(h, p)) return;
h[p.x] = p;
auto pos = h.find(p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              }} else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             typedef pair<db,int> pdi;
                                                                                        void ins(map<int, P> &h,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int n;pdi res[1000005];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db getLoc(P a,P b,P p){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          const int N = 1005
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(t,0,n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int sz=0;
  auto r = 1–
                                                                                                                                                                                                                                                                                                                                                                        while(1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct Rec {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db work() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       db rt=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // 【凸包交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(sz(qs) > t && sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();
                                                                                                                                                                                                                                                                                                              return min(min(disToSeg(b, a.s), disToSeg(b, a.t)), min(disToSeg(a, b.s), disToSeg(a,
                                                                                        disToS(L 1, P p) { return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.b)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return (b.y - a.y) * 111 * (c.x - b.x) <= (c.y - b.y) * 111 * (b.x - a.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                _`
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             "
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         do (++(det(A[(i + 1) % n]- A[i], A[(j + 1) % n] - A[j]) >= 0 ? j : i)) res = max(res, (A[i] - A[j]).len());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(p.x < h.begin() \rightarrow se.x \mid | p.x > h.rbegin() \rightarrow se.x) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 1, n) (A[i] < A[1]) && (1 = i), (A[r] < A[i]) && (r = i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int i = n - 2, t = sz(qs); i >= 0; qs.pb(ps[i-])) {
                               return fabs(det(1.a, p, 1.b) / (1.b - 1.a).len());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(p.x == 1->se.x) return p.y <= 1->se.y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    sort(all(ps)); vector<P> qs;
for(int i = 0; i < n; qs.pb(ps[i++]))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int n = sz(ps); if(n \le 1) return ps;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // 0(nlogn)
// 插入点,询问点在不在凸包内部(包括边界)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vector<P> convexHull(vector<P> ps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          auto l = h.lower_bound(p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool in(map<int, P> &h, P p) {
                                                                                                                                                    1.a).len(), (p-1.b).len())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db res = (A[1]-A[r]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool ao(P a, P b, P c) { // 包括边界: 小等于
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while(i != 1 || j != r);
                                                                                                                                                                                                                                                                                 if(isSS(a, b)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(!sz(h)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          diameter(vector<P> A)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          qs.pop_back(); return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(n <= 1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          map<int, P> h1, h2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int 1 = 0, r = 0;
db disToL(L 1, P p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int i = 1, j = r;
                                                                                                                                                                                                                                                  disSS(L a, L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n = sz(A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // 【凸包最远点对】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         namespace DCH {
                                                                                                                                                                                        }
// 【线到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【动态凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                    凸包
                                                                                                                                                                                                                                                                                                                                                b.t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【求凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                        3.3
```

```
P p = 1.a - ((1.b - 1.a) * (x / y)), det = (1.b - 1.a) * (sqrt(d) / y); p1 = p - det, p2 = p + det; // dir : 1.a -> 1.b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r + c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               res.pb(c1.0 + (c2.0 - c1.0) ^* c1.r / (c1.r - c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             P det = ((p0 - c.o)^* (-c.r * sqrt(d) / x)).rot90();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    db y = (1.b - 1.a).len2();
db d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
if(sign(d) < 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                         if(sign(dis - fabs(A.r - B.r)) == 1) return 2; if(sign(dis - fabs(A.r - B.r)) == 0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool tanCP(0 c, P p0, P &p1, P &p2) { db x = (p0 - c.o).len2(), d = x - c.r * c.r;
                                                                                                                                                                                                                                                                                                                                              if(sign(dis - (A.r + B.r)) == 1) return 4;
if(sign(dis - (A.r + B.r)) == 0) return 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<P> tanCC(const C &c1, const C &c2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(sign(dis - fabs(c1.r - c2.r) == 0)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(sign(dis - (c1.r + c2.r)) == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P p = (p0 - c.0) * (c.r * c.r / x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool isCL(0 a, L 1, P &p1, P &p2) {
                                                                                                                                                                                                                                                                      // 相离4: 外切3: 相交2: 内切1: 内含0:
int relCC(C A, C B) { // 两圆关系
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               db areaCT(db r,P s,P t) { // 需要除
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db \times = dot(1.a - a.o, 1.b - 1.a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                db dis = (c1.0 - c2.0).len();
                                                                                                                                                                                                                                                                                                                         db \ dis = (A.o - B.o) .len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(d < eps) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          p1 = c.o + p + det;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      det;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 【圆与三角形交面积】
                                                                           return fabs(ans)
  ans += res
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vector<P> res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // 【直线和圆求交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        d = max(d, 0.);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    p2 = c.o + p
                                                                                                                                                                                                                                           // 注意相等关系
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【圆圆切点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return res;
                                                                                                                                                                                                               // 【两圆关系】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【点圆切点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P p1, p2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return 1;
                                                                                                                                                       回
                                                                                                                                                         3.6
                                                                                                                                                                                                           rt += ((r[i][j+1] - r[i][j]) * a + r[i][j]) / ((r[i][j+1]-r[i][j]) * b +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db dB = b.len2(), dC = c.len2(), d = 2 * det(b, c); return A - P(b.y * dC - c.y * dB, c.x * dB - b.x * dC) / d;
                                                                           if(cnt == 0 \& sgn(res[t].fi - res[t+1].fi)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(det(q[0], q1, q2) < 0) swap(q1, q2), f2 = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  = 1;
                                                                                                                                                                                  if(b < 0) continue; if(b > 1) b = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 convexCut(ps, L(q1, q2));
convexCut(ps, L(q2, q[0]));
db res = f1 == f2? area(ps) : -area(ps);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fz = fz + (p[0] + p[i] + p[i + 1]) * t / 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(det(p[0], p1, p2) < 0) swap(p1, p2), f1
                                                                                                                             if(a < 0) \ \ddot{a} = 0; \ if(a > 1) \ break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         polyInter(vector<P> &p, vector<P> &q)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db t = det(p[0], p[i], p[i + 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // if(area(p) < 0) reverse(all(p));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // if(area(q) < 0) reverse(all(q));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vector<P> ps(\{p[0], p1, p2\});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          convexCut(ps, L(q[0], q1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P q1 = q[j], q2 = q[j + 1];
bool f2 = 0;
                                                                                                                                                           db \ b = res[t+1].fi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, n - 1) {
P p1 = p[i], p2 = p[i + 1];
bool f1 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 【平面图欧拉定理】 V + F - E = // 【简单多边形求面积交】
                                                                                                      db a = res[t].fi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(n < 3 \mid | m < 3) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                          P outC(P A, P B, P C) { // 外心
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P baryC(P p[], int n) { // 重心
                                               cnt += res[t].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int n = sz(p), m = sz(q);
int cnt = 0; --sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P \ b = B - A, c = C - A;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P fz(0, 0); db fm = 0;
rep(i, 1, n - 1) {
                                                                                                                                                                                                                                       r[i][j]);
                        rep(t,0,sz) {
                                                                                                                                                                                                                                                                                        return rt / 2;}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(j, 1, m-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return fz / fm;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                多边形
                                                                                                                                                                                                                                                                                                                                                三角形
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fm += t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                 (少) //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      3.5
                                                                                                                                                                                                                                                                                                                                                    3.4
```

```
2;
ans[cnt] += ang * c[i].r * c[i].r / 2 - sin(ang) * c[i].r * c[i].r /
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void set() { rep(i, 0, 4) rep(j, 0, 4) a[i][j] = 0; } void e() { rep(i, 0, 4) a[i][i] = 1; }
                                                                                                                                                                                                                                                                            rep(i, 0, n) ans = ans + p[i]; ans = ans / n;
                                                                                                                                                                                                                                                                                                                                                                                               db tmp = (p[i] - ans).len();
if(ret < tmp) ret = tmp, j = i;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ans = ans + (p[j] - ans) * t;
                                                                                                                                                                                                                                                                                                                                          int j = -1; db ret = -1;
                                                                                                                                                                                                                                                db t = 1; P3 ans(0, 0, 0);
                                                                                                                                                                                       P3 MinSphere(vector<P3> p)
                                                                                                                                                                                                                     int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                          while(t > eps) {
                                                                                                                                                                                                                                                                                                                                                                   rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // 【三维向量变换】
                                                                                                                                                         // 【最小球覆盖】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     db a[4][4];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct Mat {
                                                           bool b1 = sign(s.len2() - r * r) == 1 , b2 = <math>sign(t.len2() - r * r) == 1;
bool f = isCL(C(P(0, 0), r), L(s, t), p1, p2);
if(!f) return r * r * rad(s, t);
```

```
rep(i, 0, 4) rep(j, 0, 4) rep(k, 0, 4) r.a[i][j] += a[i][k] * c.a[k][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Mat translate(db tx, db ty, db tz) { // 平移, 以下矩阵均为左乘
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Mat scale(db a, db b, db c) { // 缩放
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Mat operator * (const Mat &c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(b \& 1) r = r * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Mat r; r.set(); r.e();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Mat kpow(Mat a, int b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Mat r; r.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1, 0, 0, tx, 0, 1, tz, 0, 0, 1, tz, 0, 0, 0, 1, tz, 0, 0, 0, 1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ب
اا
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db p[4][4] = {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          oʻ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                o'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          a = a * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db p[4][4] =
a, 0, 0, 0
0, b, 0, 0
0, 0, c, 0
0, 0, 0, 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while(b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      b >>= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return r;
                        if(sign(dot(s – p1, t – p1)) <= 0 && sign(dot(s – p2, t – p2) <= 0)) return r * r * (rad(s, p1) + rad(p2, t)) + det(p1, p2); else return r * r * rad(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j,0,i) if(c[i]==c[j]) cnt++;
rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            E(){} E(P p,T ang,int delta):p(p),ang(ang),delta(delta){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool overlap(C a, C b) {return sgn(a.r-b.r-abs(a.o-b.o))>=0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool operator < (const E&b) const {return ang<b.ang;}
                                                                                                    } else if(b1) return r * r * rad(s, p1) + det(p1, t);
                                                                                                                            else if(b2) return r r r ad(p2, t) + det(s, p2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ans[cnt] += evt[j].p / evt[j+1].p / 2;
db ang = evt[j + 1].ang - evt[j].ang;
if(ang < 0) ang += pi * 2;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(j,0,2) a[j]=(pts[j]—c[i].o).arg();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(!sz(evt)) ans[cnt] += pi*c[i].r*c[i].r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           memset(ans , 0 , sizeof(T) * (n + 1));
                                                                                                                                                                                                                                                                                                                                                                     ans += areaCT(c.r, u - c.o, v - c.o);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<P> pts=insCC(c[i],c[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     evt.pb(E(pts[0],a[0],1));
evt.pb(E(pts[1],a[1],-1));
                                                                                                                                                                                                                                                                                                         rep(i, 0, n) {
   P u = p[i], v = p[(i + 1) % n];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cnt += a[0] > \bar{a[1]};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cnt+=evt[j].delta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    namespace CircleIntersection{ //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void solve(C *c,int n,T *ans)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                evt.pb(evt.front());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(j, 0, sz(evt)-1) {
                                                                                                                                                                                                                               areaCPoly(C c, vector<P> p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(j,0,n) if(j!=i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  sort(all(evt));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  P p;T ang;int delta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(sz(pts)) {
                                                                                                                                                                                                                                                                                                                                                                                                                      return fabs(ans) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<E> evt;
                                                                                                                                                                                    }
// 【圆与多边形交面积】
                                                                                                                                                        return det(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int cnt=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i,0,n) {
                                                                                                                                                                                                                                                             int n = sz(p);
if(b1 && b2)
                                                                                                                                                                                                                                                                                         db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            struct E{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // 【國文】
```

0 = 0 +

 $isLL(L 1, db a, db b, db c) { // ax + by}$

db u = a * 1.a.x + b * 1.a.y + c;db v = -(a * 1.b.x + b * 1.b.y + c);return (1.a * v + 1.b * u) / (u + v);

 $if(sgn(abs(o-p[i])-r) \le 0) continue;$

C Mincir(P *p,int n){
 random_shuffle(p, p + n);

// 【最小圆覆盖】

P o = p[0]; db r = 0;

rep(i,1,n) {

db s2 = $-\det(12.b - 12.a, 11.b - 12.a)$; return (11.a * s2 + 11.b * s1) / (s1 + s2);

db s1 = det(12.b - 12.a, 11.a - 12.a);

```
rep(i, 0, 3) a[i] = (p[(i + 2) % 3] - p[(i + 1) % 3]).len();

rep(i, 0, 3) {

int j = (i + 1) % 3, k = (i + 2) % 3;

if(sign(a[i] * a[i] - a[j] * a[j] - a[k] * a[k] - a[j] * a[k]) >= 0) return p[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               auto Rand = [&] () { return rand() % 10000 / 5000 * pi; }; P ans(0, 0); rep(i, 0, n) ans = ans + p[i]; ans = ans / n; db len = 0; rep(i, 0, n) len += (ans - p[i]).len();
                                                                                                                                                                                                                                                                                                                                                                                      // sqrt((a ^ 2 + b ^ 2 + c ^ 2 + 4 * sqrt(3) * area) / 2)
                                                                                                                                                                                                              o = outc(p[i], p[j], p[k]), r = abs(o-p[k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db ang = Rand();
P np(ans.x + t * sin(ang), ans.y + t * cos(ang));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \begin{split} &\text{if}(\det(p[0],\ p[1],\ p[2]) < 0)\ \text{swap}(p[1],\ p[2]); \\ &\text{P } q1 = (p[2] - p[0]).\text{rot}(pi \ / \ 3) + p[0]; \\ &\text{P } q2 = (p[0] - p[1]).\text{rot}(pi \ / \ 3) + p[1]; \\ &\text{return isLL}(L(q1,\ p[1]),\ L(q2,\ p[2])); \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db k = 0; rep(i, 0, n) k += (np - p[i]).len(); if(sign(len - k) > 0) ans = np, len = k;
                                                                   if(sgn(abs(o-p[j])-r) <= 0) continue; o = (p[i] + p[j]) / 2, r = abs(o-p[j]); rep(k, 0, j) {
                                                                                                                                                                           if(sgn(abs(o-p[k])-r) \le 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int n = sz(p); assert(n);
if(n == 1) return p[0];
if(n == 2) return (p[0] + p[1]) / 2;
if(n == 3) {
                                                                                                                                                                                                                                                                                                                                                                                                                       // 如果有重点, 大于 2 的直接用模拟退火法
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             直线、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db t = 10000; // modify
0 = p[i], r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                             P fermat(vector<P> p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P isLL(L 11, L 12) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             线段、
                                   rep(j,0,i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while(t > eps) {
                                                                                                                                                                                                                                                                                  return C(o,r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 【直线交点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ans;
                                                                                                                                                                                                                                                                                                                        }
//【费马点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db a[3];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ń
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  3.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inplace_merge(p.begin() + 1, p.begin() + m + 1, p.begin() + r + 1, [&](P a, P b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            };
db rad(P p1, P p2) { return atan2l(det(p1, p2), dot(p1, p2)); } // p1 与 p2 的夹角,有方
                                                                                                                                               \begin{array}{l} \cos^{-1}(1-c_0) \times \times \times \times , & (1-c_0) \times \times \times y - si \times z, & (1-c_0) \times \times \times z + si \times y, & 0, \\ (1-c_0) \times y \times \times + si \times z, & c_0 + (1-c_0) \times y \times y, & (1-c_0) \times y \times z - si \times x, & 0, \\ (1-c_0) \times z \times x - si \times y, & (1-c_0) \times z \times y + si \times x, & c_0 + (1-c_0) \times z \times z, & 0, \\ 0, & 0, & 0, & 1\}; \end{array}
                                                                                                    db 1 = s.len(), x = s.x / 1, y = s.y / 1, z = s.z / 1, si = sin(a), co = cos(a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  P rot90() { return P(-y, x); } P rot(db a) { return P(cos(a) * \times - \sin(a) * \times , \cos(a) * \times + \sin(a) * \times); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db Xm = p[m].x, lim = min(solve(1, m, p), solve(m + 1, r, p));
                                                                                                                                                                                                                                                                                                                     Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, r + 1) if(fabs(p[i].x - Xm) <= lim) V.pb(p[i]);
rep(i, 0, sz(V)) rep(j, i + 1, sz(V)) {
   if(fabs(V[j].y - V[i].y) >= lim) break;
   T dis = (V[i] - V[j]).len();
                                                                   wat rotate(P3 s, db a) { // 绕 s 为轴旋转 a 度, 右手方向
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sort(all(A), [&](P a, P b){return a.x < b.x;});
return solve(0, sz(A) – 1, A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          向
bool cmp(const pii &a, const pii &b) { // 级角排序
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int o = a > pii(0, 0), t = b > pii(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         namespace NearestPoints { // sz(A) <= 1e5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db solve(int l, int r, vector<P> &p) { if(l == r) return 1e100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P norm() { return *this / len(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      .im = min(lim, dis);
                                                                                                                                                                                                                                                                                                                                                                                                                            向量
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(o != t) return o < t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
db solve(vector<P> A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return a.y < b.y;});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int m = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return det(a, b) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                            基础点、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // 【点集中最近点对】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vector<P> V;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return lim;
                                                                                                                                       db p[4][4] = {
                                                                                                                                                                                                                                                                                                                                                                                                                                  _
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct P {
                                                                                                                                                                                                                                                                                                                                                                                                                               3.8
```

```
'n
                                                                                                                                                                                                                                                                                                                           do (++(det(A[(i+1) % n]-A[i], A[(j+1) % n] - A[j]) >= 0 ? j : i)) %= 0 ? j : i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return (b.y - a.y) * 111 * (c.x - b.x) <= (c.y - b.y) * 111 * (b.x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool in(int x, int y) { return in(h1, P(x, y)) && in(h2, P(x, -y)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(p.x < h.begin() -> se.x || p.x > h.rbegin() -> se.x) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void ins(int x, int y) { ins(h1, P(x, y)); ins(h2, P(x, -y)); }
                                                                                                                                                       rep(i, 1, n) (A[i] < A[1]) && (1 = i), (A[r] < A[i]) && (r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(ao(11\rightarrow se, 1\rightarrow se, p)) h.erase(1); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          auto rr = r; rr++; if(rr == h.end()) break;
if(ao(p, r->se, rr->se)) h.erase(r); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(in(h, p)) return;
h[p.x] = p;
auto pos = h.find(p.x);
while(1) {
    auto 1 = pos; if(1 == h.begin()) break; --1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 auto 11 = 1; if(11 == h.begin()) break; --11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                auto r = pos; r++; if(r == h.end()) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P operator [] (const int&n) {return d[n];}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           <= 1->se.y;
                                                                                                                                                                                                                                                                                                                                                                          res = max(res, (A[i] - A[j]).len());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // 插入点, 询问点在不在凸包内部(包括边界)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P d[10];int dn;// d[dn] = d[0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(p.x == 1 \rightarrow se.x) return p.y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool in(map<int, P> &h, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    auto 1 = h.lower_bound(p.x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ao(1—>se, p, r—>se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void ins(map<int, P> &h, P p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            namespace ConvecIntersection{ //
                                                                                                                                                                                                              db res = (A[1]-A[r]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            typedef pair<db,int> pdi,
                                                                                                                                                                                                                                                                                                                                                                                                                                     while(i != l || j != r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool ao(P a, P b, P c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(!sz(h)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int n;pdi res[1000005];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // 包括边界: 小等于
                                                  if(n \ll 1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    namespace DCH {
 map<int, P> h1, h2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       const int N = 1005
                                                                                                         int 1 = 0, r = 0;
                                                                                                                                                                                                                                                                         int i = 1, j = r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              auto r = 1—:
int n = sz(A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct Rec {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      }
// 【动态凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 | / 【凸包交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // O(nlogn)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int i = 0; i < n; qs.pb(ps[i++])) {
   while(sz(qs) > 1 && sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(sz(qs) > t && sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return min(min(disToSeg(b, a.s), disToSeg(b, a.t)), min(disToSeg(a, b.s), disToSeg(a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         db disToS(L 1, P p) { return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : <math>min((p - return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : <math>min((p - return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : <math>min((p - return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : <math>min((p - return sign(dot(1.a, p, 1.a)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? disToL(1, p) : min((p - return sign(dot(1.a, p, 1.a)) == 1 ? d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                           bool isSSr(const L &a, const L &b){ db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s); db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool isLS(P a1, P a2, P b1, P b2) { // 判断直线线段是否相交 (端点也算) db c1 = det(a2 - a1, b1 - a1), c2 = det(a2 - a1, b2 - a1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return sign(c1) * sign(c2) < 0 && sign(c3) * sign(c4) < 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sign(max(a.s.y, a.t.y) - min(b.s.y, b.t.y)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sign(max(a.s.x, a.t.x) - min(b.s.x, b.t.x)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sign(max(b.s.x, b.t.x) - min(a.s.x, a.t.x)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(int i = n - 2, t = sz(qs); i >= 0; qs.pb(ps[i-]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sign(max(b.s.y, b.t.y) - min(a.s.y, a.t.y)) >= 0;
                                                                                                                                                       return P(b0 * c1 - b1 * c0, a1 * c0 - a0 * c1) / d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return fabs(det(1.a, p, 1.b) / (1.b - 1.a).len());
                     P isLL(db a0, db b0, db c0, db a1, db b1, db c1) {
    db d = a0 * b1 - a1 * b0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int n = sz(ps); if(n \le 1) return ps;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<P> convexHull(vector<P> ps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return sign(c1) * sign(c2) <= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1.a).len(), (p-1.b).len())
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sort(all(ps)); vector<P> qs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(isSS(a, b)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db diameter(vector<P> A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           qs.pop_back(); return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db disToL(L 1, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool isSS(L a, L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               disSS(L a, L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   口包
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 【凸包最远点对】
                                                                                                                                                                                                                                                                // 【线相交判定】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 【点到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                【线到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   က်
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 【求凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3.10
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if(det(p[0], p1, p2) < 0) swap(p1, p2), f1 = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        db res = f1 == f2 ? area(ps) : —area(ps);
                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(det(q[0], q1, q2) < 0) swap(q1, q2),
                                                                                                                                                   db polyInter(vector<P> &p, vector<P> &q)
                                                                                                                                                                                                                     // if(area(p) < 0) reverse(all(p));
                                                                                                                                                                                                                                           // if(area(q) < 0) reverse(all(q));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vector<P> ps({p[0], p1, p2});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    convexCut(ps, L(q[0], q1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 convexCut(ps, L(q2, q[0]));
                                                                                                                                                                                                                                                                                                                                                                                                          P q1 = q[j], q2 = q[j + 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          convexCut(ps, L(q1, q2));
                                                                                                                                                                                                                                                                                         rep(i, 1, n-1) {
P p1 = p[i], p2 = p[i+1];
                                                                                                      П
Ш
П
                                                                                                                                                                          int n = sz(p), m = sz(q);
if(n < 3 \mid | m < 3) return 0;
                                                                                                  // 【平面图欧拉定理】 V + F
                                                                                                                          【简单多边形求面积交】
                                                                                                                                                                                                                                                                                                                                                                                       rep(j, 1, m-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                  bool f2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return fabs(ans)
                                                                                                                                                                                                                                                                                                                                    bool f1 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             员
                                                                                                                                                                                                                                                                      db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 6
                                              3.12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3.13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(sgn((r[i][j+1] - r[i][j]) * (r[t][g+1] - r[t][g])) < 0 || i < t){
    res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g]) , 1);
    res[sz++] = pdi(getLoc(r[i][j] , r[i][j+1] , r[t][g+1]) , -1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                         int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(cnt == 0 \&\& sgn(res[t].fi - res[t+1].fi)) {
                       if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(b < 0) continue; if(b > 1) b = 1;
                                                                                                                                                                                   res[sz++] = pdi(0,0); res[sz++] = pdi(1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(a < 0) \ a = 0; \ if(a > 1) \ break;
                                           return (p.y - a.y) / (b.y - a.y);
                                                                                                                                        rep(i,0,n) rep(j,0,r[i].dn){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db b = res[t+1].fi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  db a = res[t].fi;
                                                                                                                                                                                                                                if(t == i) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               sort(res , res + sz);
                                                                                                                                                                                                                                                         rep(g,0,r[t].dn) {
                                                                                                                                                                                                                                                                                                                             if(!du && !dv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cnt += res[t].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cnt = 0; —sz;
getLoc(P a, P b, P p){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  r[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(t,0,sz) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return rt / 2;}}
                                                                                                                                                                                                          rep(t,0,n) {
                                                                                                                                                                 int sz=0;
                                                                                           work() {
                                                                                                                  db rt=0;
                                                                    숙용
 ф
```

```
P p = (p0 - c.o) * (c.r * c.r / x);
P det = ((p0 - c.o) * (-c.r * sqrt(d) / x)).rot90();
                                                                                                                                                                     if(sign(dis - fabs(A.r - B.r)) == 1) return 2; if(sign(dis - fabs(A.r - B.r)) == 0) return 1;
                                                                                                                                                                                                                                                                                                       bool tanCP(0 c, P p0, P &p1, P &p2) { db x = (p0 - c.o).len2(), d = x - c.r * c.r;
                                                                                                            if(sign(dis - (A.r + B.r)) == 1) return 4;
if(sign(dis - (A.r + B.r)) == 0) return 3;
// 注意相等关系
// 相离4: 外切3: 相交2: 内切1: 内含0:
int relCC(C A, C B) { // 两圆关系
                                                                                  db dis = (A.o - B.o).len();
                                                                                                                                                                                                                                                                                                                                                              if(d < eps) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                             p1 = c.o + p + det;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             - det;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           p2 = c.o + p
                                                                                                                                                                                                                                                                                // 【点圆切点】
                                                                                                                                                                                                                             return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return 1;
```

```
三角形
4
```

```
return A - P(b.y * dC - c.y * dB, c.x * dB - b.x * dC) / d;
                                                                                                                                                 db dB = b.len2(), dC = c.len2(), d = 2 * det(b, c);
                                                                                                                                                                                                                                                                                                                                                                                   fz = fz + (p[0] + p[i] + p[i + 1]) * t / 3;
                                                                                                                                                                                                                                                                                                                           db t = det(p[0], p[i], p[i + 1]);
                                                                                         P outC(P A, P B, P C) { // 外心
                                                                                                                                                                                                                                    baryC(P p[], int n) { // \equiv \triangle P fz(0, 0); db fm = 0; rep(i, 1, n - 1) {
                                                                                                                        P \ b = B - A, c = C - A;
                                                                                                                                                                                                                                                                                                                                                                                                                                               return fz / fm;
                                                                                                                                                                                                                                                                                                                                                          fm += t;
3.11
```

```
2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ans[cnt] += ang * c[i].r * c[i].r / 2 - \sin(ang) * c[i].r * c[i].r /
                                                                                                                                 rep(j,0,i) if(c[i]==c[j]) cnt++;
rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ans[cnt] += evt[j].p / evt[j+1].p / 2;
db ang = evt[j + 1].ang - evt[j].ang;
if(ang < 0) ang += pi * 2;
                                                                                                                                                                                                                                                                                     rep(j,0,2) a[j]=(pts[j]-c[i].o).arg();
                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!sz(evt)) ans[cnt] += pi^*c[i].r^*c[i].r;
memset(ans , 0 , sizeof(T) * (n + 1));
rep(i,0,n) {
                                                                                                                                                                                                             vector<P> pts=insCC(c[i],c[j]);
                                                                                                                                                                                                                                                                                                             evt.pb(E(pts[0],a[0],1));
evt.pb(E(pts[1],a[1],-1));
                                                                                                                                                                                                                                                                                                                                                                 cnt += a[0] > a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cnt+=evt[j].delta;
       void solve(C *c,int n,T *ans)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      evt.pb(evt.front());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(j, 0, sz(evt)-1) {
                                                                                                                                                                                   rep(j,0,n) if(j!=i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           sort(all(evt));
                                                                                                                                                                                                                                        if(sz(pts)) {
                                                                                                             vector<E> evt;
                                                                                                                                                                                                                                                                  T a[2]
                                                                                      int cnt=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else{
```

7, 3D

<u>.</u>

ans /

```
Mat r; r.set();
rep(i, 0, 4) rep(k, 0, 4) r.a[i][i] += a[i][k] * c.a[k][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void set() { rep(i, 0, 4) rep(j, 0, 4) a[i][j] = 0; }
void e() { rep(i, 0, 4) a[i][i] = 1; }
                                                                                db t = 1; P3 ans(0, 0, 0);
rep(i, 0, n) ans = ans + p[i]; ans =
                                                                                                                                                                                                             db tmp = (p[i] - ans).len();
if(ret < tmp) ret = tmp, j = i;</pre>
                                                                                                                                                                                                                                                                                             ans = ans + (p[j] - ans) * t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Mat operator ^st (const Mat &c) \{
                                                                                                                                                              int j = -1; db ret = -1; rep(i, 0, n) {
                            P3 MinSphere(vector<P3> p) {
                                                       int n = sz(p); assert(n)
                                                                                                                                 while(t > eps) {
                                                                                                                                                                                                                                                                                                                                                                                                                             // 【三维向量变换】
// 【最小球覆盖】
                                                                                                                                                                                                                                                                                                                          t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    db a[4][4];
                                                                                                                                                                                                                                                                                                                                                                             return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               E(){} E(p p,T ang,int delta):p(p),ang(ang),delta(delta){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         };
bool overlap(C a,C b) {return sgn(a.r-b.r-abs(a.o-b.o))>=0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          bool operator < (const E&b) const {return ang<b.ang;}
                                                                     else if(b2) return r r r rad(p2, t) + det(s, p2);
                                                                                                                                                                                                                                                                                                                    ans += areaCT(c.r, u - c.0, v - c.0);
                                                                                                                                                                                                                                                        rep(i, 0, n) {
P u = p[i], v = p[(i + 1) % n];
                                                                                                                                                                                                                                                                                                                                                                                                                                                     namespace CircleIntersection{ //
                                                                                                                                                                            areaCPoly(C c, vector<P> p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       P p;T ang;int delta;
                                                                                                                                                                                                                                                                                                                                                                       return fabs(ans) / 2;
                                                                                                                                 }
// 【圆与多边形交面积】
                                                                                                return det(s, t);
                                                                                                                                                                                                         int n = sz(p);
                                                                                                                                                                                                                                    db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct E{
                                                                                                                                                                                                                                                                                                                                                                                                                      // 【國交】
```

```
3.14
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool b1 = sign(s.len2() - r * r) == 1, b2 = sign(t.len2() - r * r) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           t - p2 <= 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                P p = 1.a - ((1.b - 1.a) * (x / y)), det = (1.b - 1.a) * (sqrt(d) / y); p1 = p - det, p2 = p + det; // dir : 1.a -> 1.b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(sign(dot(s - p1, t - p1)) <= 0 && sign(dot(s - p2, t - return r * r * (rad(s, p1) + rad(p2, t)) + det(p1, p2); else return r * r * rad(s, t); } else if(b1) return r * r * rad(s, p1) + det(p1, t);
                                                                                                                                                            res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r + c2.r));
                                                                                                                                                                                                                                                            res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r - c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                           db x = dot(1.a - a.o, 1.b - 1.a);
db y = (1.b - 1.a).len2();
db d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool f = isCL(C(P(0, 0), r), L(s, t), p1, p2);
if(!f) return r * r * rad(s, t);
                                vector<P> tanCC(const C &c1, const C &c2) {
                                                                                                                                                                                                                                if(sign(dis - fabs(c1.r - c2.r) == 0)) {
                                                                                                                              if(sign(dis - (c1.r + c2.r)) == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         areaCT(db r,P s,P t) { // 需要除
                                                                                                                                                                                                                                                                                                                                                                                                                             bool isCL(0 a, L 1, P &p1, P &p2) {
                                                                                             db dis = (c1.0 - c2.0).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(sign(d) < 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 【圆与三角形交面积】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            d = max(d, 0.);
                                                                    vector<P> res;
                                                                                                                                                                                                                                                                                                                                                                                          // 【直线和圆求交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(b1 && b2)
                                                                                                                                                                                                                                                                                                                                  return res;
// 【圆圆切点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P p1, p2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return 1;
```

bool check(L u, L v, L w) { return w.include(isLL(u, v)); }

deque<L> halfPlane(vector<L> 1) {

sort(all(l)); deque<L> q;

rep(i, 0, sz(1)) {

if(i && sameDir(l[i], l[i - 1])) continue;

if(sameDir(10, 11)) return 11.includer(10.a); return (10.b - 10.a) < (11.b - 11.a);

bool operator < (const L &l0, const L &l1)

 $if(a.quad()\ i=b.quad())$ return a.quad()< b.quad(); return $sign(det(a,\ b))>0$;

bool operator < (const P &a, const P &b) {

```
int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool includer(const P &p) const { return sign(det(b - a, p - a)) > 0; bool include(const P &p) const { return sign(det(b - a, p - a)) >= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     this->a=P(0,0);this->b=P(sign(b),sign(b)*(-a/b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int x=sign(c)*sign(det(P(-c/a,0), P(0,-c/b)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(x==1) this->a=P(-c/a, 0), this->b=P(0,-c/b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool sameDir(L l0, L l1) {  P \ a = 10.a - 10.b, \ b = 11.a - 11.b; \\ return sign(det(a, b)) == 0 \&\& sign(dot(a, b)) == 1; \\ 
                                                                                                               if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), a, b, c));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else this\rightarrowa=P(0,-c/b), this\rightarrowb=P(-c/a,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     this\rightarrowa=P(-c/a, 0);this\rightarrowb=P(-c/a,-sign(a));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            this->a=P(0,-c/b); this->b=P(sign(b),-c/b);
P p1 = p[i], p2 = p[(i + 1) % sz(p)];
int d1 = sign(a * p1.x + b * p1.y + c);
int d2 = sign(a * p2.x + b * p2.y + c);
if(d1 >= 0) q.pb(p1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P det = (b - a).rot90().norm() * len;
                                                                                                                                                                                                                                                                                                                                                                                                           // ax + by + c >= 0, (a != 0 || b != 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return L(a + dét, b + det)
                                                                                                                                                                                                                              \frac{1}{2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else if(sign(b)==0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(sign(c)!=0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                   L(db a, db b, db c) {
                                                                                                                                                                                                                            HalfPlane
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // 向内(右手方向)推
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(sign(a)==0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       L push(db len) {
                                                                                                                                             b = d
                                                                                                                                                                                                                                                                                                                                                                                 struct L {
                                                                                                                                                                                                                                                                                              struct P
                                                                                                                                                                                                                              3.16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db l = s.len(), x = s.x / l, y = s.y / l, z = s.z / l, si = sin(a), co = cos(a); db p[4][4] = \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return
                                                                                                                                                                                                                                                                                                                                         db ty, db tz) { // 平移,以下矩阵均为左乘
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     wat rotate(P3 s, db a) { // 绕 s 为轴旋转 a 度, 右手方向
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mat scale(db a, db b, db c) { // 缩放db p[4][4] = {
a, 0, 0, 0,
0, b, 0, 0,
0, 0, c, 0,
0, 0, 0, 1};
                                                                                                                 Mat r; r.set(); r.e();
                                                                                     Mat kpow(Mat a, int b)
                                                                                                                                           while(b) {
if(b & 1) r = r *
                                                                                                                                                                                                                                                                                                                                            Mat translate(db tx,
                                                                                                                                                                                                                                                                                                                                                                                                1, 0, 0, tx, 0, 1, 0, ty, 0, 0, 1, tz, 0, 0, 1, tz, 0, 0, 0, 1};
                                                                                                                                                                                                                                                                                                                                                                        db p[4][4] = {
                                                                                                                                                                                                a = a * a;
    return r;
                                                                                                                                                                                                                                 b >>= 1;
                                                                                                                                                                                                                                                                                     return r;
```

HalfPlane 3.15

```
void convexCut(vector<P> &p, db a, db b, db c) {
                                                                                                                                                                                                                      if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), 1));
                                                                                                          P p1 = p[i], p2 = p[(i + 1) % sz(p)];
int d1 = sign(det(l.a, l.b, p1));
int d2 = sign(det(l.a, l.b, p2));
                             void convexCut(vector<P> &p, L l) {
                                                                                                                                                                                          if(d1 >= 0) q.pb(p1);
                                                                              rep(i, 0, sz(p)) {
                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, sz(p)) {
// 1: a->b 逆时针方向
                                                                                                                                                                                                                                                                                                    // ax + by + c >= 0
                                                     vector<P> q;
                                                                                                                                                                                                                                                   ) p = d;
```

```
while(cur <= (tmp = area(p[i], p[j], p[(k + 1) % n]))) (++k) %= n, cur = tmp; if(cur <= (tmp = area(p[i], p[(j + 1) % n], p[k]))) (++j) %= n, cur = tmp;
                                                                                 T res = area(a, b, c), cur = res, tmp;
int i = 0, j = 1, k = 2;
a = p[i], b = p[j], c = p[k];
                                                                                                                                                                                                                                                                                              else break;
                                                                                                                                                             while(1) {
                                                                                                                                op
9
while(sz(q) > 1 && !check(q[sz(q) - 2], q.back(), l[i])) q.pop_back();
while(sz(q) > 1 && !check(q[i], q[0], l[i])) q.pop_front();
                                                                                                                                                                while(sz(q) > 2 && !check(q[sz(q) - 2], q.back(), q[0])) q.pop_back();
while(sz(q) > 2 && !check(q[1], q[0], q.back())) q.pop_front();
                                                                                    q.pb(1[i]);
                                                                                                                                                                                                                                                        return q;
```

if(cur > res) a = p[i], b = p[j], c = p[k], res = cur;

3.17 MaxAreaPoly

```
for (int i : vals) area += 1d(1) * sqrt(1d(D) * 1d(D) - 1d(1) * 1d(1)) / 4; 1d hiArea = 1d(hi) * sqrt(1d(D) * 1d(D) - 1d(hi) * 1d(hi)) / 4; if (isReflex) area -= hiArea;
                                                                                                                                                                                                                                                                                                                                                            for (int 1 : vals) tot += 2 * asin(ld(1) / ld(D));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (tooSmall(ma)) numExpand++, ma += (ma - mi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ld hiAng = 2 * asin(ld(hi) / ld(D));
if (isReflex) return ang < hiAng;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else return ang + hiAng >= 2 * PI;
                                                                                                                                                                                                                                                                                                                                                                                                                                           bool isReflex = (getAngle(hi) < PI);
auto tooSmall = [&](ld D) {</pre>
                                                                                                                                                                                                                                                                                                       auto getAngle = [\&](ld D) \rightarrow ld\{
                                                                                                                                                               if (cur > hi) swap(cur, hi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   1d md = mi + (ma - mi) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(tim, 0, 50 + numExpand) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (tooSmall(md)) mi = md;
                                                                                                                                                                                                                                                                              if (sum <= hi) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 };
ld mi = hi, ma = hi + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ld ang = getAngle(D);
                                                   int sum = 0, hi = S[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Id D = mi, area = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else area += hiArea;
ld solve_poly(vi &S) {
                           assert(sz(S) > 0);
                                                                                                          rep(i, 1, sz(S)) {
int cur = S[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int numExpand = 0;
                                                                                                                                                                                                                        vals.pb(cur);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else ma = md;
                                                                                                                                                                                                                                                                                                                                     ld tot = 0;
                                                                                                                                                                                                                                                                                                                                                                                        return tot;
                                                                                                                                                                                               sum += cur;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return area;
                                                                                     vi vals;
```

3.19 MinAreaTri

cur = area(p[i], p[j], p[k]);

} while(i);

if(i == j) (++j) % = n;if(j == k) (++k) % = n;

(++i) %= n;

```
mi = min(mi, area(p[pu - 1], p[pu], p[pv + 1], p[v]));
                                                                                                                                                                                                                                          bool cmp(const P &x, const P &y) { return det(x, y) < 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                   else if(1[m].x == \bar{0} && 1[m].y < \bar{0}) 1[m].y *= -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ma = max(ma, area(p[1], p[pu], p[n], p[v]));
                                                                                                                                                                                                                                                                                                                           rep(i, 1, n + 1) p[i].ind = i, pos[i] = i;

m = 0; rep(i, 1, n + 1) rep(j, i + 1, n + 1) {

l[++m] = p[i] - p[j];

if(l[m].x < 0) l[m].x *= -1, l[m].y *= -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(pu > pv) swap(u, v), swap(pu, pv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(pu == 1 \mid | pv == n) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cout << mi << " " << ma << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int pu = pos[u], pv = pos[v]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int u = l[i].u, v = l[i].v;
                                                         struct P { int x, y, ind, u, v; };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sort(1 + 1, 1 + 1 + m, cmp);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1[m].u = i, 1[m].v = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              swap(pos[u], pos[v]);
                                                                                                                                                                                                                                                                                                    sort(p + 1, p + 1 + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   swap(p[bu], p[bv]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      mi = inf, ma = 0;
rep(i, 1, m + 1) {
                                                                                                                                                   const ll inf = 4e18;
                                                                                         namespace MinAreaTri {
                                                                                                                       const int N = 2020;
                                                                                                                                                                              int n, m, pos[N];
                                                                                                                                                                                                            P p[N], 1[N * N];
// 无重点、三点共线
                                                                                                                                                                                                                                                                      void solve() {
                           // 0(n^2log_2n)
```

3.20 凹四边形计数

11/15

```
// O(n \wedge 2)
void maxAreaTri(P *p, int n, P &a, P &b, P &c) {
```

MaxAreaTri

3.18

```
void solve(const vector<P> &_ps, const vector<pii> &es) {
                                                                                                                                                                                                                                                                                                                                                                                                                   res += det(ps[E[e].se], ps[E[e].fi]); vis[e] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ne[g[i][j].se] = g[i][(j + 1) % sz(g[i])].se;
                                                                                                                                                                                  _ ps[V];
                                                                                                                                               bool cmp(const pii &i, const pii &j) {
   P a = ps[i.fi] - ps[v], b = ps[j.fi]
   int o = P(0, 0) < a, t = P(0, 0) < b;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     init(); ps = _ps;
for(auto e : es) adde(e.fi, e.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, cnte) if(!vis[i]) go(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, sz(ps)) {
    V = i; sort(all(g[i]), cmp);
    rep(j, 0, sz(g[i])) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(res > 0) areas.pb(res / 2);
                                                                                                                                                                                                                                      if(o != t) return o < t;
                                                                                                                                                                                                                                                                        return det(a, b) > 0;
\mathsf{E}[\mathsf{cnte++}] = \mathsf{mp}(\mathsf{u}, \mathsf{v});
                             g[v].pb(mp(u, cnte));
                                                             E[cnte++] = mp(v, u);
                                                                                                                                                                                                                                                                                                                                                                                        while(!vis[e]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                      e = ne[e ^ 1]
                                                                                                                                                                                                                                                                                                                             void go(int e) { db res = 0;
                                                                                                                    int V;
```

while(j >= 2 && det(q[j], q[i]) > 0) —j, ++cnt;

s[i] = s[i + 1] + cnt;

int c = j = k + 1;

per(i, k + 1, n + 1) {

int j = k, cnt = 0;

rep(i, 1, n + 1) q[i] = p[i]; swap(q[1], q[u]); rep(i, 2, n + 1) q[i] = q[i] - p[u]; sort(q + 2, q + n + 1, cmp);

void solve(int u, 11 &ans) {

int k = n; while(k >= 2 && q[k].y <= 0)

rep(i, 2, k + 1) { while(c <= n && det(q[i], q[c]) > 0) ++c; while(j <= n && det(q[i], q[j]) >= 0) ++j; ans += s[j] + (n - j + 1) * 111 * (c - k - 1);

ll ans = 0; rep(i, 1, n + 1) solve(i, ans);

} 11 solve() {

bool gao(P a) { return a.y > 0 || (a.y == 0 && a.x >= 0); } bool cmp(P a, P b) {

int n; P p[N], q[N]; ll s[N]; namespace CNT {

const int N = 1010;

bool o = gao(a), t = gao(b);

if(o != t) return o > t;

return det(a, b) > 0;

旋转卡壳

```
static const int N = 101010, M = 101010;
                                                                平面图转对偶图
                                                                                                                                             // ps id starts from 0
return ans;
                                                                                                        struct Planar {
                                                                                                                                                              vector<P> ps;
                                                                   3.21
```

```
3.22
```

```
rep(i, 0, n) {
    P t = ps[i] - ps[(i + 1) % n];
    while(det(t, ps[(p + 1) % n] - ps[p]) > 0) (++p) %= n;
    ans = max(ans, (ps[i] - ps[p]).len());
                                                                                                                                                                                                                                             ans = max(ans, (ps[(i + 1) % n] – ps[p]).len());
                                                                                                                    if(n == 2) return (ps[1] - ps[0]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 1, n) if(p[i].y > p[o].y) o = i;
rep(i, 1, m) if(q[i].y < q[t].y) t = i;
                                                                                                                                                                                                                                                                                                                                                                                                                   T solve(P p[], int n, P q[], int m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                          int 0 = 0, t = 0; T ans = inf;
                                                                                                                                                                                                                                                                                                                                          // 【凸包宽度】点 — 边// 【凸包间的最大距离】点 — 点// 【凸包间的最小距离】
                                                  T diameter(vector<P> ps) {
                                                                         n = sz(ps); T ans = 0; if(n <= 1) return 0;
                    // 【凸包直径】点 - 点
// 凸包都是顺时针给出
                                                                                                                                                                                                                                                                                              return ans;
                                                                                                                                                                                                                                                                                                                     void init() {
    rep(i, 0, sz(ps)) g[i].clear();
                                                                                                                                                                                                                                                                                                                                                                    fill_n(vis, cnte, false);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void adde(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                              ps.clear(); cnte = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             g[u].pb(mp(v, cnte));
                                                                                                                      // cnte id starts from
                                                                                                                                                                                                // u -> (v, cnte)
                                                                                                                                                                                                                                                                                                                                                                                                                     areas.clear();
                                                                                                                                                                                                                     vector<pii> g[N];
                                                                                                                                                                                                                                                                      vector<db> areas;
                                                                                                                                               int cnte, ne[M];
                                                                                                                                                                       bool vis[M];
                                                                                                                                                                                                                                               pii E[M];
```

```
BufferedReader reader = new BufferedReader(new InputStreamReader(System.in));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(;tokenizer == null || !tokenizer.hasMoreTokens();){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tokenizer = new StringTokenizer(reader.readLine());
                                                                            PrintWriter writer = new PrintWriter(System.out);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Map<String, Integer> mymap2 = new TreeMap<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Map<String, Integer> mymap = new HashMap<>();
                                                                                                                                                                                                                List<String> mylist2 = new LinkedList<>();
                                                                                                                                                                                  List<String> mylist1 = new ArrayList<>();
                                                                                                                                                                                                                                                                                                                           Queue<String> que = new LinkedList<>();
                                                                                                                                                                                                                                                       List<String> mylist3 = new Vector<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                    Set<String> myset2 = new TreeSet<>();
                                                                                                                                                                                                                                                                                          Vector<String> vec = new Vector<>();
                                                                                                                                                                                                                                                                                                                                                                                                   Set<String> myset = new HashSet<();
                                                                                                                                                                                                                                                                                                                                                            Stack<String> sta = new Stack<>();
                                                                                                           StringTokenizer tokenizer = null;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           String next()throws Exception{
                                                                                                                                              /oid solve()throws Exception{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void run()throws Exception{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        catch(Exception e) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            reader.close();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   writer.close();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (true) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        solve();
public class Main {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 finally {
                                                                 while((tmp = det(a, q[(t + 1) % m] - q[t])) < 0) (++t) %= m;
if(sign(tmp)) ans = min(ans, disToSeg(L(p[o], p[(o + 1) % n]), q[t]));
else ans = min(ans, disSS(L(p[o], p[(o + 1) % n]), L(q[t], q[(t + 1) % m])));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while(det(t, ps[(p + 1) % n] - ps[p]) > 0) (++p) %= n; while(dot(t, ps[(1 + 1) % n] - ps[1]) < 0) (++1) %= n; r = (p + 1) % n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(dot(t, ps[(r + 1) % n] - ps[r]) > 0) (++r) %= n; ll et = abs(det(ps[p], ps[i], ps[(i + 1) % n]));
                                                                                                                                                                                                                                                                                                                                                                  n);
                                                                                                                                                                                                                                                                                                                                                            return min(solve(p, n, q, m), solve(q, m, p,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 ot = abs(dot(t, ps[1] - ps[r]));
ans = min(ans, (db)et * ot / t.len2());
                                      P a = p[(o + 1) \% n] - p[o]; db tmp;
                                                                                                                                                                                                                                                                                                                         T work(P p[], int n, P q[], int m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              P t = ps[i] - ps[(i + 1) % n];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int n = sz(ps); T ans = 1e18;
                                                                                                                                                                                                                                                                                                                                                                                                                              // 【凸包最小面积外接矩形】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【凸包最小周长外接矩形】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int p = 1, l = 1, r; rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  T solve(vector<P> ps) {
                                                                                                                                                                                  'u =% (0++)
                                                                                                                                                                                                                                                         return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ans;
```

Graph

(生成树计数) 矩阵 - 树定理

```
n 个节点的无向图 G ,求一个包含 n-1 条边的边集使得边集的边构成一颗树,问这样的边集的数量度数矩阵
                                     м м=D-A мі, і=的度数і мі, ј=(与有边相连і)?-1:04і=j)矩阵构定理对于图,它的基尔霍夫矩阵的每个代数余子式相等,且等于的生成树的数目。
QMG*/
                            D n*的矩阵n Di, i=的度数i Di, j=0(i!=j)邻接矩阵
```

Java D

0I

```
//提交评测前删除package
                                                        import java.util.*;
                                                                            import java.math.*;
                                       import java.io.*
package mytest;
```

```
/*生成树计数问题
```

Math

public static void main(String args[])throws Exception{

(new Main()).run();

BigInteger nextBigInteger()throws Exception{

return new BigInteger(next());

double nextDouble()throws Exception{

return Integer.parseInt(next());

int nextInt()throws Exception{

return tokenizer.nextToken();

return Double.parseDouble(next())

6.1 FFT

```
const double PI = acos(-1.0);
                           const int _{-M} = N, _{-N} = N;
                                                            template <class V>
```

线性筛素数

6.4

```
for (int i = 1; i < N; i <<= 1)
  for (int j = 0, t = N / (i << 1); j < N; j += i << 1)
  for (int k = 0, 1 = 0, x, y; k < i; k++, 1 += t)
  x = (11) w[f][1] * a[j+k+i] % P, y = a[j+k], a[j+k] = (y+x) % P, a[j+k+i]</pre>
                                                                                                                                                                                                                                                                                                                                                                   int d = __builtin_ctz(N);
w[0][0] = w[1][0] = 1;
for (int i = 1, x = kpow(G, (P-1) / N), y = kpow(x, P-2); i < N; i++) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        W[0][i] = (11) \times W[0][i-1] \% P, W[1][i] = (11) y * W[1][i-1] \% P;
                                                                                                                                                                                                                                             if (f) for (int i = 0, x = kpow(N, P-2); i < N; i++) a[i] = (11)a[i]
rep(i, 0, N) if (i < rev[i]) swap(a[i], a[rev[i]]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void doit(int ^*a, int ^*b, int na, int nb){ // [0, na)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rev[i] = (rev[i>>1] >> 1) | ((i&1) << (d-1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (N = 1; N < na + nb - 1; N <<= 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            work(), FFT(a,0], FFT(b,0);
rep(i, 0, N) a[i] = (11)a[i] * b[i] %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           '/rep(i, 0, N) cout << a[i] << endl;
                                                                                                                                                                                                       (y-x+P) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, na, N) a[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, nb, N) b[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   欧拉函数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FFT(a, 1);
                                                                                                                                                                                                                                                                                                                             void work(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } ntt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         6.3
                                                                        friend cp operator + (cp &a, cp &b) { return cp{ a.x + b.x,a.y + b.y }; } friend cp operator - (cp &a, cp &b) { return cp{ a.x - b.x,a.y - b.y }; } friend cp operator * (cp &a, cp &b) { return cp{ a.x*b.x - a.y*b.y,a.x*b.y + a.y*b.x}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int m = 2; m <= n; m <<= 1) { cp w = get(2 * PI*op / m); tmp[0] = cp{ 1,0 }; for (int j = 1; j < (m >> 1); j++) tmp[j] = tmp[j - 1] * w; for (int i = 0; i < n; i += m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (op == -1) rep(i, 0, n) a[i] = cp{ a[i].x / n,a[i].y / n };
                                                                                                                                                                                                                                                                                                                                                                   for (int i = (n >> 1), j = 1; j < n; j++) {
   if (i < j) swap(a[i], a[j]);
   int k; for (k = (n >> 1); k&i; i ^= k, k >>= 1); i ^=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int j = i; j < i + (m >> 1); j ++) { cp u = a[j], v = a[j + (m >> 1)] * tmp[j - i]; a[j] = u + v, a[j + (m >> 1)] = u - v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<V> multiply(vector<V> A, vector<V> B, int op = 0)
                                                                                                                                                                                                                                             cp get(double x) { return cp{ cos(x), sin(x) }; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               aa = vector<cp>(len), bb = vector<cp>(len);
rep(i, 0, lena) aa[i] = cp{ (double)A[i],0 };
rep(i, 0, lenb) bb[i] = cp{ (double)B[i],0 };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int lena = A.size(), lenb = B.size(), len =
while (len < lena + lenb) len <<= 1;</pre>
                                         struct cp { double x, y; } tmp[\_M * 2 + 5];
                                                                                                                                                                                                                                                                                                                                void FFT(vector<cp> &a, int n, int op) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (op) reverse(all(A));
```

vector <cp> aa, bb;

```
-a^{1}«Euler(n)=n/(1-1/p1)(1-1/p2)(i-)a
                                                                                                    int ans = 1,i; for (i = 2; i * i <= n; i++){ if (n % i == 0){
                                                                                                                                                                                      while (n \% i == 0){
                                                                                                                                                                                                                                                                                              -1;
                 [1, noooo—1]oooookooon»¥µ
*/
                                                                                                                                                                                                                                                                                                                                             //ooooooo • "1. .ŷn~oooo
                                                                                                                                                                                                                                                                                            if (n > 1) ans *= n
                                                                                                                                                                       ans *=i-1;
                                                                                                                                                                                                                       ans *= i;
                                                                                                                                                                                                           n /= i;
                                                                                    int euler(int n){
                                                                                                                                                     n /= i;
                                                                                                                                                                                                                                                                                                                return ans;
                                                                  //oooŷ-ooo
```

LLZ 6.2

FT<11> fft;

rep(i, lena - 1, lena + lenb - 2 + 1) A.pb((11)(aa[i].x + 0.5));

if (!op) rep(i, 0, len) A.pb((ll)(aa[i].x + 0.5)); else

FFT(aa, len, 1), FFT(bb, len, 1); rep(i, 0, len) aa[i] = aa[i] * bb[i];

FFT(aa, len, —1); A.clear();

```
for (; b; b >>= 1,a = a * a % P) if (b & 1) c = c * a %P;
                                                                                                 static const int G = 3, P = 1004535809; I/P = C*2^Nk + 1
                                                                                                                           int N, na, nb, w[2][M], rev[M];
11 kpow(11 a, int b){
<< 1;
                                                                                                                                                                                                                                                                                       void FFT(int *a, int f){
const int M = 1 \ll 17
                                                                                                                                                                                 11 c = 1;
                                                                                                                                                                                                                                    return c;
                        int a[M], b[M];
                                                                            struct NTT{
```