



FACULTY OF INFORMATION TECHNOLOGY AND ELECTRICAL ENGINEERING  
DEGREE PROGRAMME IN ELECTRONICS (MASTER'S)

**Course Name: Radio Engineering 1**  
**Homework #5**

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Soln.

- ① We can determine the stability of the transistor by using  $A, K$  parameters which is defined below with  $M$ .

- i)  $|A| < 1$
- ii)  $K > 1$
- iii)  $M > 1$

$$\text{Here, } |A| = |S_{11} S_{22} - S_{12} S_{21}|$$

$$= (0.70 \angle -155)(0.66 \angle -55) - (0.07 \angle 32)(0.07 \angle 77)$$

$$= -0.33 + j0.03$$

$$= 0.33 \angle 174.4^\circ$$

$|A| < 1$ , valid

$$\text{Now, } K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |A|^2}{2 |S_{12} S_{21}|}$$

$$= \frac{1 - 0.70^2 - 0.66^2 + 0.33^2}{2 \cdot |0.21|}$$

$$= 0.4364$$

$K < 1$  not valid

As we can see that  $K < 1$ , Unconditionally stable is not true for the transistor. So, the instability depends on matching of the input and output, i.e. so, it can become unstable for certain passive source or load impedance. From Potan it is state that, "If a two port network is unconditionally stable then it will not oscillate for any passive source and load impedance."

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(5) Input stability circle :-

$$\text{Center, } c_s = \frac{(s_{11} - As_{22})^*}{|s_{11}|^2 - |A|^2} = \frac{0.70 \angle -155^\circ - [(0.33 \angle 174.4^\circ)(0.66 \angle 55^\circ)]^*}{0.70^2 - 0.33^2}$$

$$= \frac{0.5 \angle +165.45^\circ}{0.380}$$

$$= 1.34 \angle +165.45^\circ$$

$$\text{Radius, } R_s = \left| \frac{s_{12} s_{21}}{|s_{11}|^2 - |A|^2} \right| = \frac{(0.7 \angle 32^\circ)(3 \angle 77^\circ)}{0.7^2 - 0.33^2}$$

$$= -0.179 + j0.52$$

$$= 0.55$$

$$\therefore R_s = 0.55$$

$$c_s = 1.34 \angle +165^\circ$$

Output Circle :-

$$c_L = \frac{(s_{22} - As_{11})^*}{|s_{22}|^2 - |A|^2} = \frac{(0.66 \angle -55^\circ - (0.33 \angle 175^\circ)(0.70 \angle 155^\circ))^*}{0.66^2 - 0.33^2}$$

$$= 1.3 \angle 67.3^\circ$$

So

$$\& \cdot R_L = \left| \frac{s_{12} s_{21}}{|s_{22}|^2 - |A|^2} \right| = \frac{(0.07 \angle 32^\circ)(3 \angle 77^\circ)}{0.66^2 - 0.33^2}$$

$$= 0.64 \angle 100^\circ$$

∴

So

$R_L = 0.64$
$c_L = 1.3 \angle 67.3^\circ$



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$$\textcircled{C} \quad Z_L = 5 + 75j$$

$$1. \quad Z_L = \frac{5+75j}{50} = 0.1 + 1.5j \quad (\text{Nonnormalized})$$

Reflection:

$$\Gamma_L = \frac{Z_L - 1}{Z_L + 1} = \frac{0.1 + 1.5 - 1}{0.1 + 1.5 + 1}$$

$$= 0.04 \angle 67.2^\circ$$

Now, the input reflection co-efficient of the transition is,

$$\left. \begin{aligned} \Gamma_{in} &= S_{11} + \frac{S_{12} S_{21} \Gamma_L}{1 - S_{22} \Gamma_L} \\ &= 0.70 \angle -15^\circ + \frac{0.12 \angle 77.5^\circ}{1 - 0.6 \angle 12.5^\circ} \end{aligned} \right\} \text{Here, } \begin{aligned} S_{12} S_{21} \Gamma_L &= 0.21 \angle 109^\circ \\ 0.04 \angle 67.2^\circ &= 0.2 \angle 176.5^\circ \\ S_{22} \Gamma_L &= 0.66 \angle -57^\circ \\ 0.04 \angle 67.2^\circ &= 0.6 \angle 12.5^\circ \end{aligned}$$

$$\begin{aligned} &= -1.08 - j0.4065 \\ |\Gamma_{in}| &= \sqrt{1.08^2 + (0.4065)^2} \\ &= 1.15 > 1 \end{aligned}$$

So, using part b, we determined that the stable region is situated outside the stability circle. For the given load, reflection co-efficient falls inside the circle, which places the device in an unstable region. In this condition, the magnitude of the input reflection co-efficient becomes larger than the reflected one meaning that the reflected wave is larger than the incident wave in input.

