

CSE 410 Offline - 2

Raster Based Graphics Pipeline

Overview:

In this assignment, you will develop the raster based graphics pipeline used in OpenGL. The pipeline can be thought of as a series of six stages. You will implement roughly 4 stages of the pipeline.

1. Stage 1: modeling transformation
2. Stage 2: view transformation
3. Stage 3: projection transformation
4. Stage 4: clipping & scan conversion using Z-buffer algorithm

Your program will output five files: `stage1.txt`, `stage2.txt`, `stage3.txt` and `z-buffer.txt`, `out.bmp`. The first three files will contain the output of the first three stages, respectively. The fourth file will contain Z-buffer values (only those which are less than the max value). And the fifth file will be a bmp image generated by the pipeline.

There will be two input files: `scene.txt` and `config.txt`

The first file will contain the scene description and second file will contain the necessary information for the Z-buffer algorithm.

Scene description:

You will be given a text file named "`scene.txt`". This will contain the following lines:

Line 1: `eyeX eyeY eyeZ`

Line 2: `lookX lookY lookZ`

Line 3: `upX upY upZ`

Line 4: `fovY aspectRatio near far`

Lines 1-3 of `scene.txt` state the parameters of the `gluLookAt` function and Line 4 provides the `gluPerspective` parameters.

The display code contains 7 commands as follows:

1. `triangle` command – this command is followed by three lines specifying the coordinates of the three points of the triangle to be drawn. The points being `p1`, `p2`, and `p3`, 9 double values, i.e., `p1.x`, `p1.y`, `p1.z`, `p2.x`, `p2.y`, `p2.z`, `p3.x`, `p3.y`, and `p3.z` indicate the coordinates.

This is equivalent to the following in OpenGL code.

```
glBegin(GL_TRIANGLE); {  
    glVertex3f(p1.x, p1.y, p1.z);  
    glVertex3f(p2.x, p2.y, p2.z);  
    glVertex3f(p3.x, p3.y, p3.z);  
}glEnd();
```

2. `translate` command – this command is followed by 3 double values (`tx`, `ty`, and `tz`) in the next line indicating translation amounts along X, Y, and Z axes. This is equivalent to `glTranslatef(tx, ty, tz)` in OpenGL.
3. `scale` command – this command is followed by 3 double values (`sx`, `sy`, and `sz`) in the next line indicating scaling factors along X, Y, and Z axes. This is equivalent to `glScalef(sx, sy, sz)` in OpenGL.
4. `rotate` command – this command is followed by 4 double values in the next line indicating the rotation angle in degree (`angle`) and the components of the vector defining the axis of rotation (`ax`, `ay`, and `az`). This is equivalent to `glRotatef(angle, ax, ay, az)` in OpenGL.
5. `push` command – This is equivalent to `glPushMatrix` in OpenGL.
6. `pop` command – This is equivalent to `glPopMatrix` in OpenGL.
7. `end` command – This indicates the end of the display code.

In this assignment, you will generate the output of the first three stages of the raster based graphics pipeline according to the scene description provided in the `scene.txt` file. The output of the stages should be put in `stage1.txt`, `stage2.txt`, and `stage3.txt` file. **The input of the fourth stage will be `stage3.txt` and `config.txt` and the corresponding output should be put in `z-buffer.txt` and `out.bmp` (elaborated later).**

Please check the `scene.txt` carefully to have a more comfortable understanding of the input.

Stage 1: Modeling Transformation

In the Modeling transformation phase, the display code in `scene.txt` is parsed, the transformed positions of the points that follow each `triangle` command are determined, and the transformed coordinates of the points are written in `stage1.txt` file. We maintain a stack S of transformation matrices which is manipulated according to the commands given in the display code. Consider that the display code contains the following commands.

Triangle
Translate
Triangle
Rotate
Scale
Triangle
Rotate
Triangle



The pseudo-code for the modeling transformation phase is as follows:

```
initialize empty stack S
S.push(identity matrix)
while true
    input command
    if command = "triangle"
        input three points
        for each three point P
             $P' \leftarrow \text{transformPoint}(S.\text{top}, P)$ 
            output  $P'$ 
    else if command = "translate"
        input translation amounts
        generate the corresponding translation matrix T
        S.push(product(S.top, T))
    else if command = "scale"
        //do it yourself
    else if command = "rotate"
        //do it yourself
    else if command = "push"
        //do it yourself
    else if command =
        "pop"
        //do it yourself
    else if command =
        "end"
        break
```

Transformation matrix for Translation

```
translate
tx ty tz
```

The transformation matrix for the above translation is as follows:

$$\begin{vmatrix} 1 & 0 & 0 & tx \\ 0 & 1 & 0 & ty \\ 0 & 0 & 1 & tz \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Transformation matrix for Scaling

```
scale
sx sy sz
```

The transformation matrix for the above scaling is as follows:

$$\begin{vmatrix} sx & 0 & 0 & 0 \\ 0 & sy & 0 & 0 \\ 0 & 0 & sz & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Transformation matrix for Rotation

Remember that the columns of the rotation matrix indicate where the unit vectors along the principal axes (namely, \hat{i} , \hat{j} , and \hat{k}) are transformed. We will use the vector form of Rodrigues formula to determine where \hat{i} , \hat{j} , and \hat{k} are transformed and use those to generate the rotation matrix. The vector form of Rodrigues formula is as follows:

$$R(\vec{x}) = \cos \theta \vec{x} + (1 - \cos \theta)(\vec{a} \cdot \vec{x})\vec{a} + \sin \theta(\vec{a} \times \vec{x})$$

In the above formula, $\underline{\mathbf{x}}$ is a unit vector defining the axis of rotation, θ is the angle of rotation, and $\underline{\mathbf{a}}$ is the vector to be rotated.

Now we outline the process of generating transformation matrix for the following rotation:

```
rotate
angle ax ay az
```

We denote the vector (ax, ay, az) by \mathbf{a} . The steps to generate the rotation matrix are as follows:

```
a.normalize()
c1=R(i,a,angle)
c2=R(j,a,angle)
c3=R(k,a,angle)
```

The corresponding rotation matrix is given below:

$$\begin{vmatrix} c1.x & c2.x & c3.x & 0 \\ c1.y & c2.y & c3.y & 0 \\ c1.z & c2.z & c3.z & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Managing Push and Pop

The following table demonstrates how `push` and `pop` works. The state of the transformation matrix stack after execution of each line of the code in the left is shown in the right. Design a data structure that manages `push` and `pop` operations on the transformation matrix stack accordingly.

Code	Stack State after Lines											
	0	1	2	3	4	5	6	7	8	9	10	11
1.Push												
2.Translate ₁												
3.Push												
4.Rotate ₁												
5.Pop												
6.Scale ₁												
7.Push												
8.Rotate ₂									T ₁ S ₁ R ₂		T ₁ S ₁ S ₂	
9.Pop					T ₁ R ₁		T ₁ S ₁	T ₁ S ₁	T ₁ S ₁	T ₁ S ₁	T ₁ S ₁	
10.Scale ₂			T ₁	T ₁	T ₁	T ₁	T ₁	T ₁	T ₁	T ₁	T ₁	
11.Pop	I	I	I	I	I	I	I	I	I	I	I	I

Stage 2: View Transformation

In the view transformation phase, the `gluLookAt` parameters in `scene.txt` is used to generate the view transformation matrix V , and the points in `stage1.txt` are transformed by V and written in `stage2.txt`. The process of generating V is given below.

First determine mutually perpendicular unit vectors l , r , and u from the `gluLookAt` parameters.

```
l = look - eye
l.normalize()
r = l X up
r.normalize()
u = r X l
```

Apply the following translation T to move the eye/camera to origin.

$$\begin{vmatrix} 1 & 0 & 0 & -eyeX \\ 0 & 1 & 0 & -eyeY \\ 0 & 0 & 1 & -eyeZ \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Apply the following rotation R such that the \mathbf{l} aligns with the $-Z$ axis, \mathbf{r} with X axis, and \mathbf{u} with Y axis. Remember that, the rows of the rotation matrix contain the unit vectors that align with the unit vectors along the principal axes after transformation.

$$\begin{vmatrix} r.x & r.y & r.z & 0 \\ u.x & u.y & u.z & 0 \\ -l.x & -l.y & -l.z & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Thus the view transformation matrix $V = RT$.

Stage 3: Projection Transformation

In the projection transformation phase, the `gluPerspective` parameters in `scene.txt` are used to generate the projection transformation matrix P , and the points in `stage2.txt` are transformed by P and written in `stage3.txt`. The process of generating P is as follows:

First compute the field of view along the X (`fovX`) axis and determine r and t .

```
fovX = fovY * aspectRatio
t = near * tan(fovY/2)
r = near * tan(fovX/2)
```

The projection matrix P is given below:

$$\begin{vmatrix} near/r & 0 & 0 & 0 \\ 0 & near/t & 0 & 0 \\ 0 & 0 & -(far+near)/(far-near) & -(2*far*near)/(far-near) \\ 0 & 0 & -1 & 0 \end{vmatrix}$$

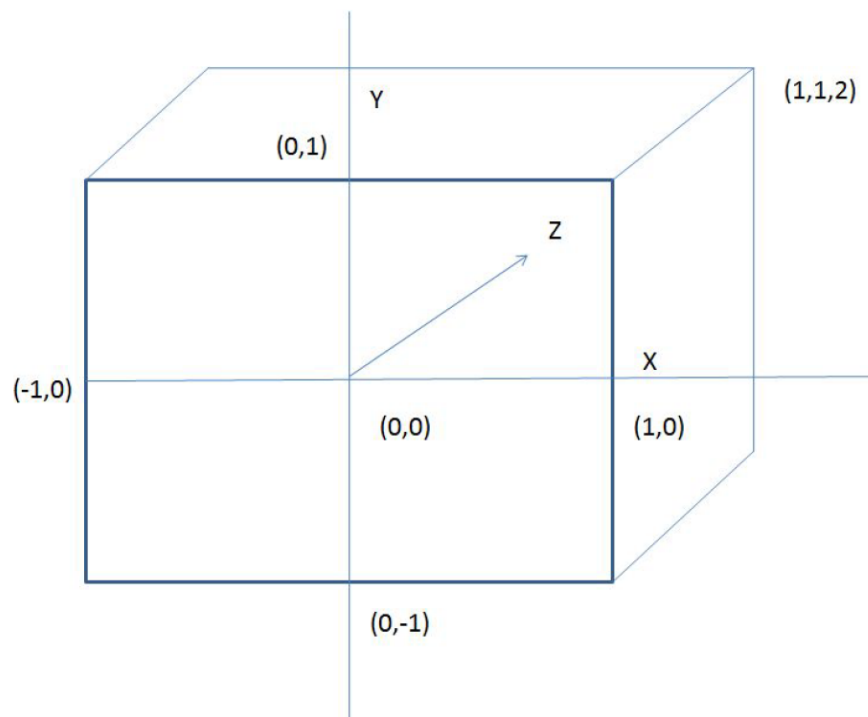
Refer to [1] for understanding the 3rd row of the above projection matrix. Image source: [2].

Stage 4: Clipping & scan conversion using Z-buffer algorithm

In this stage, you have to implement a very simple Hidden Surface Removal algorithm for the objects within a bounding box. You have to work with `triangles only`, as specified in `scene.txt`. The output generated by your program after the third stage, `stage3.txt` and the given input file `config.txt` will work as the input for this stage. However, during implementation it is recommended to test with smaller cases so that you can debug easily.

Config description:

1. The **first line** of file contains **two integers**, representing **Screen_Width** and **Screen_Height** respectively.
2. The **second line** contains a -ve number which specifies the **left limit of X**. You can get the **right limit of X** by negating this value.
3. The **third line** contains a -ve number which specifies the **bottom limit of Y**. You can get the top limit of Y by negating this value.
4. The **fourth line** contains **two real numbers** denoting **front and rear limits of Z** respectively.
5. Example:
500 500
-1.00
-1.00
0.00 2.00
6. Visual representation of the configuration according to the aforementioned example:



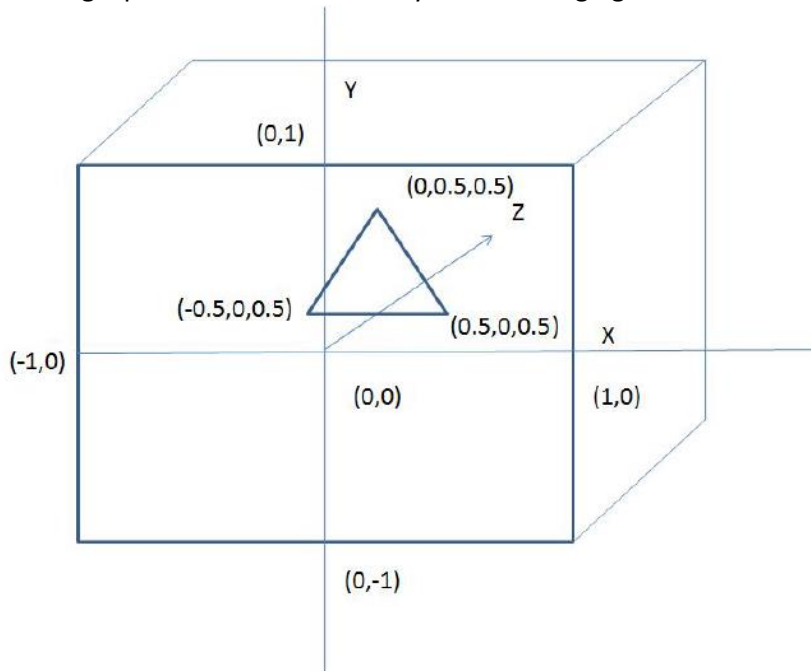
Your only viewing volume is bounded by the box shown above.

Stage 3 description:

The `stage3.txt` file generated by your program will contain each triangle information as three lines specifying the coordinates of the three points of the triangle. Suppose, there is only one triangle and the file contains the following:

```
0.50 0.00 0.50
-0.50 0.00 0.50
0.00 0.50 0.50
```

The triangle position can be shown by the following figure within the viewing volume.



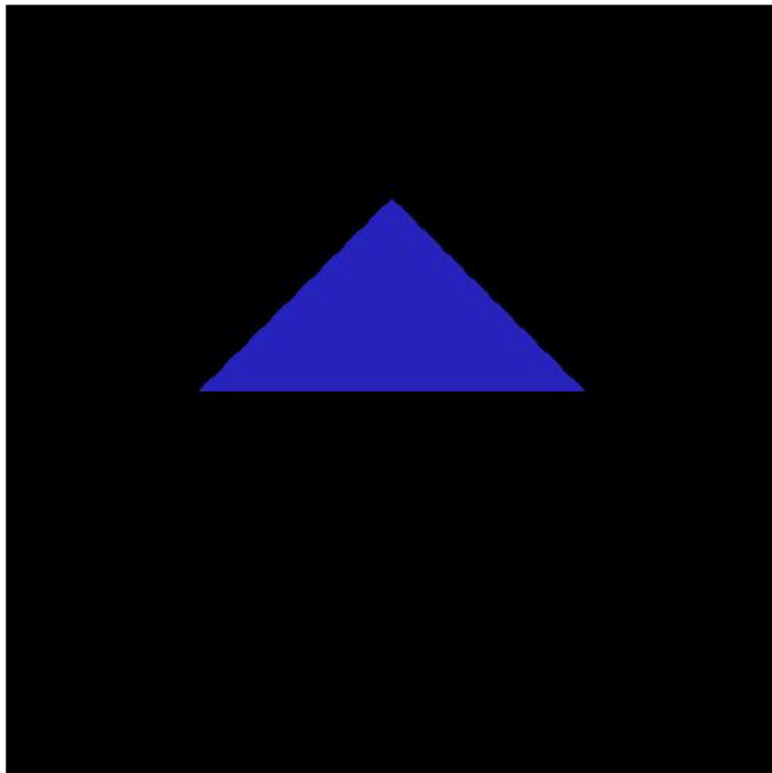
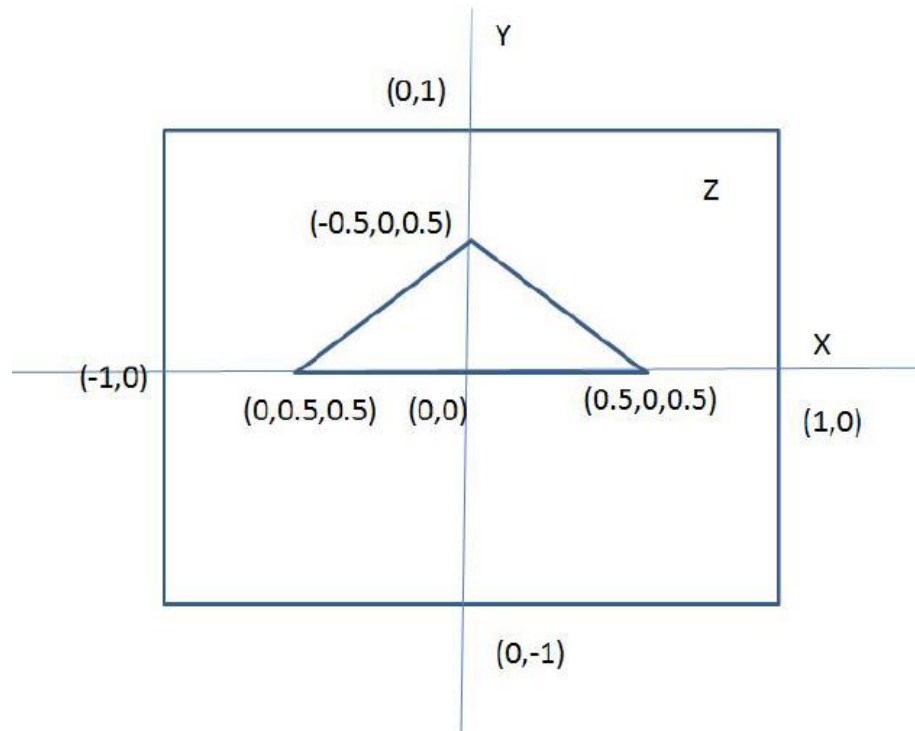
Tasks:

1. Clip everything outside the viewing volume.
2. Considering yourself as a parallel viewer from the XY-plane, generate the image (dimension : Screen_Width X Screen_Height) that can be seen on the XY plane after computing the necessary clipping and depth information of objects (triangles) within this viewing volume.
3. Print Z-buffer values into a file named `z-buffer.txt`. (only those values where `z_buffer[row][col] < z_max`).

*Check "Procedures" for more details and further instructions.

Output:

The output from the viewing plane for the aforementioned configuration and triangle is shown by the following figures (the first one is for your understanding and the second one is the actual output).



You should save the output image in a file named `out.bmp`, and the Z-buffer values in a text file named `z-buffer.txt`.

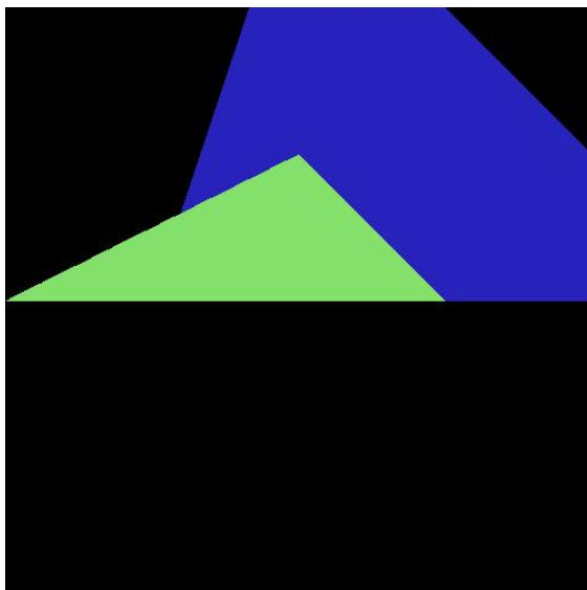
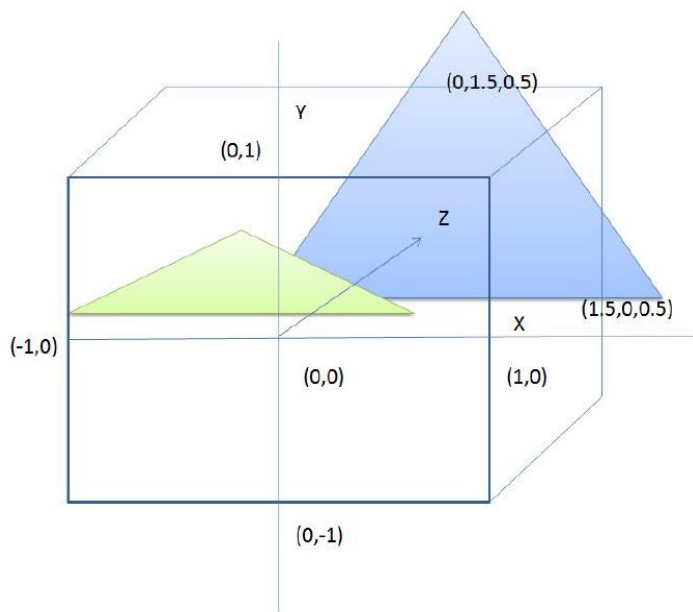
Another Sample:

Suppose. `stage3.txt` contains the following while the `config.txt` is the same as before.

```
1.5 0 0.5
-0.5 0 0.5
0 1.5 0.5

0.5 0 0.25
-1.0 0 0.25
0 0.5 0.25
```

In this case, the output will be as follows.



Procedure:

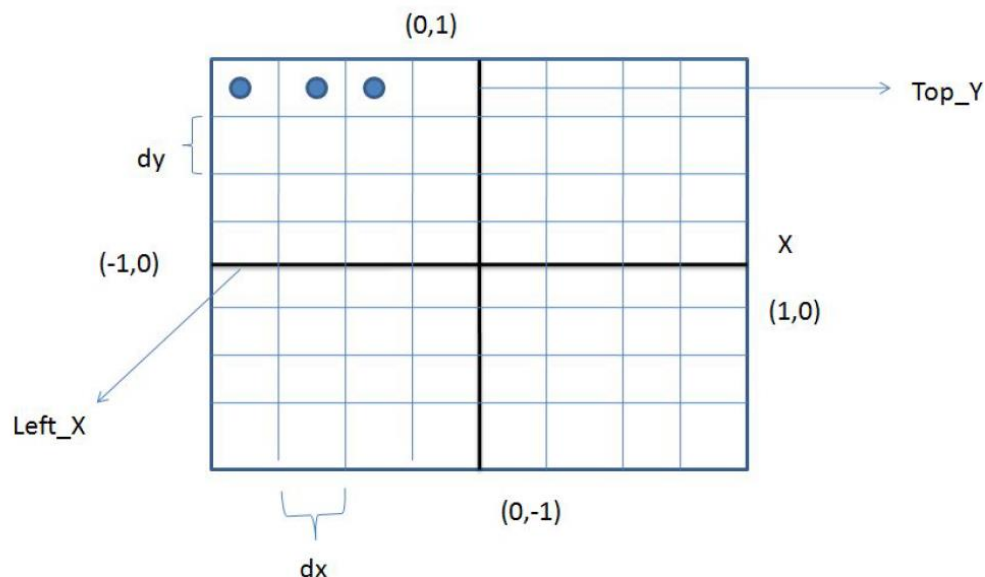
The aforementioned tasks can be divided into the following sub-tasks inside your main function.

1. Read data
2. Initialize Z-buffer and Frame buffer
3. Apply procedure
4. Save
5. Free memory

The description of each of these sub-tasks is as follows.

1. Read data
 - a. Read the `config.txt` file and store the values as `Screen_Width`, `Screen_Height`, limits along the X, Y, Z axes accordingly.
 - b. Read input information from the `stage3.txt` file. This file should contain each triangle information in three consecutive lines where each line contains three coordinate values x, y, z as real numbers.
 - c. Use a suitable data structure to hold this information. Also associate a random color value (R, G, B) with each object (no need to worry about the seed). RGB values are bounded by 0-255.
 - d. An example of a triangle object data structure can be as follows.

```
Triangle{
    Point points[3];
    Color colors[3]; // Color can be primitive/user-defined
}
```
 - e. Print and check whether you have correctly read the information from the files (for debugging purposes).
2. Initialize Z-buffer and Frame buffer.



- a. Create a pixel mapping between the x-y range values and the Screen_Width X Screen_Height range.

$$dx = (\text{right limit} - \text{left limit along X-axis}) / \text{Screen_Width}$$

$$dy = (\text{top limit} - \text{bottom limit along Y-axis}) / \text{Screen_Height}$$

Besides, specify Top_Y and Left_X values.

$$\text{Top_Y} = \text{top limit along Y-axis} - dy/2$$

$$\text{Left_X} = \text{left limit along X-axis} + dx/2$$

- b. During scanning from top to bottom and left to right, check for the middle values of each cell. e.g. $\text{Top_Y} - \text{row_no} * dy$, $\text{Left_X} + \text{col_no} * dx$
- c. Create a Z-buffer, a two dimensional array of Screen_Width X Screen_Height dimension. Initialize all the values in Z-buffer with z_max. In the aforementioned examples, $z_max = 2.0$. The memory for Z-buffer should be dynamically allocated (using STL is allowed).
- d. Create a `bitmap_image` object with Screen_Width X Screen_Height resolution and initialize its background color with black. You can follow the `image_drawing.cpp` code sample for checking how to utilize the image library.

3. Apply procedure

- a. Pseudocode:

for each object : Triangles

Find top_scanline and bottom_scanline after necessary clipping

for row_no from top_scanline to bottom_scanline

Find left_intersecting_column and right_intersecting_column
after necessary clipping

for col_no from left_intersecting_column to right_intersecting_column

Calculate z values

Compare with Z-buffer and z_front_limit and update if required

Update pixel information if required

end

end

end

* Note that you should not update a Z-buffer value if the point's z-coordinate < z_front_limit (invisible to the observer, but ignore its occlusion impact).

- b. Clipping:

- i. Compute the max_y for each triangle. If $\text{max_y} > \text{Top_Y}$, clip (i.e. ignore) the portion above Top_Y and start scanning from Top_Y. Otherwise find the suitable mapping of max_y to a top_scanline below Top_Y. Do a similar checking for min_y and Bottom_Y.
- ii. Compute min_x for each scan line for each triangle. If $\text{min_x} < \text{Left_X}$, clip (i.e. ignore) the portion to the left of Left_X. Otherwise find the suitable mapping of min_x to a column to the right of Left_X ($\text{left_intersecting_column}$). Do a similar checking for max_x and Right_X

4. Save
 - a. Save the image as `output.bmp`
 - b. Save the Z-buffer values in `z_buffer.txt`. Save only those values which are less than `z_max` i.e. for each row and col, `z_buffer[row][col] < z_max`.Check the sample output files for a better understanding.
5. Free memory
 - a. Free image memory
 - b. Free Z-buffer and Frame buffer memory

Do's and Dont's

1. Use homogeneous coordinates. The points should be represented by 4*1 matrices and transformations by 4*4 matrices.
2. While transforming a homogeneous point by multiplying it with a transformation matrix, don't forget to scale the resultant point such that the w coordinate of the point becomes 1.
3. Do not use the matrix form of Rodrigues formula directly to generate the rotation matrix. Use the procedure shown above that uses the vector form of Rodrigues formula.
4. Do not specify `gluLookAt` parameters in `scene.txt` such that the looking direction, i.e., `look-eye`, becomes parallel to the up direction.
5. Make sure that the model is situated entirely in front of the near plane.

Reference

- [1] http://www.songho.ca/opengl/gl_projectionmatrix.html
[2] <http://www.opengl-tutorial.org/beginners-tutorials/tutorial-3-matrices/>