Claims reserving with R: ChainLadder-0.1.5-2 Package Vignette DRAFT

Markus Gesmann*

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Abstract

The ChainLadder package provides various statistical methods which are typically used for the estimation of outstanding claims reserves in general insurance.

The package has implementations of the Mack-, Munich-, Bootstrap, and multi-variate chain-ladder methods, as well as the loss development factor curve fitting methods of Dave Clark and generalised linear model based reserving models.

This document is still in a draft stage. Any pointers which will help to iron out errors, clarify and make this document more helpful will be much appreciated.

^{*}markus.gesmann@gmail.com

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1 Introduction

1.1 Claims reserving in insurance

Unlike other industries the insurance industry does not sell products as such, but promises. An insurance policy is a promise by the insurer to the policyholder to pay for future claims for an upfront received premium.

As a result insurers don't know the upfront cost of their service, but rely on historical data analysis and judgement to derive a sustainable price for their offering. In General Insurance (or Non-Life Insurance, e.g. motor, property and casualty insurance) most policies run for a period of 12 months. However, the claims payment process can take years or even decades. Therefore often not even the delivery date of their product is known to insurers.

In particular claims arising from casualty insurance can take a long time to settle. Claims can take years to materialise. A complex and costly example are the claims from asbestos liabilities. A research report by a working party of the Institute of Actuaries has estimated that the undiscounted cost of UK mesothelioma-related claims to the UK Insurance Market for the period 2009 to 2050 could be around £10bn [GBB $^+$ 09]. The cost for aAsbestos related claims in the US for the worldwide insurance industry was estimate to be around \$120bn in 2002 [Mic02].

Thus, it should come to no surprise that the biggest item on the liability side of an insurer's balance sheet is often the provision or reserves for future claims payments. Those reserves can be broken down in case reserves (or out-standings claims), which are losses already reported to the insurance company and incurred but not reported (IBNR) claims.

Over the years several methods have been developed to estimate reserves for insurance claims, see [Sch11], [PR02] for an overview. Changes in regulatory requirements, e.g. Solvency $\rm II^1$ in Europe, have fostered further research into this topic, with a focus on stochastic and statistical techniques.

2 The ChainLadder package

2.1 Motivation

The ChainLadder [GMZ12] package provides various statistical methods which are typically used for the estimation of outstanding claims reserves in general insurance. The package started out of presentations given by Markus Gesmann at the Stochastic Reserving Seminar at the Institute of Actuaries in 2007 and 2008, followed by talks at Casualty Actuarial Society (CAS) meetings joined by Dan Murphy in 2008 and Wayne Zhang in 2010.

¹See http://ec.europa.eu/internal_market/insurance/solvency/index_en.htm

Implementing reserving methods in R has several advantages. R provides:

- a rich language for statistical modelling and data manipulations allowing fast prototyping
- a very active user base, which publishes many extension
- many interfaces to data bases and other applications, such as MS Excel
- an established framework for documentation and testing
- workflows with version control systems
- code written in plain text files, allowing effective knowledge transfer
- an effective way to collaborate over the internet
- built in functions to create reproducible research reports²
- in combination with other tools such as LATEX and Sweave easy to set up automated reporting facilities
- access to academic research, which is often first implemented in R

2.2 Brief package overview

This vignette will give the reader a brief overview of the functionallity of the Chain-Ladder package. The functions are discussed and explained in more detail in the respective help files and examples.

The ChainLadder package has implementations of the Mack-, Munich- and Bootstrap chain-ladder methods [Mac93a], [Mac99], [QM04], [EV99]. Since version 0.1.3-3 it provides general multivariate chain ladder models by Wayne Zhang [Zha10]. Version 0.1.4-0 introduced new functions on loss development factor (LDF) fitting methods and Cape Cod by Daniel Murphy following a paper by David Clark [Cla03]. Version 0.1.5-0 has added loss reserving models within the generalized linear model framework following a paper by England and Verrall [EV99] implemented by Wayne Zhang.

The package also offers utility functions to convert quickly tables into triangles, triangles into tables, cumulative into incremental and incremental into cumulative triangles.

A set of demos is shipped with the packages and the list of demos is available via:

R> demo(package="ChainLadder")

and can be executed via

²For an example see the project: Formatted Actuarial Vignettes in R, http://www.favir.net/

```
R> library(ChainLadder)
R> demo("demo name")
```

Additionally the ChainLadder package comes with example files which demonstrates how to the ChainLadder functions can be embedded in Excel and Word using the statconn interface[BN07].

For more information and examples see the project web site: http://code.google.com/p/chainladder/

2.3 Installation

We can install ChainLadder in the usual way from CRAN, e.g.:

```
R> install.packages('ChainLadder')
```

For more details about installing packages see [Tea12b]. The installation was successful if the command library(ChainLadder) gives you the following message:

```
R> library(ChainLadder)
```

ChainLadder version 0.1.5-2 by:
Markus Gesmann <markus.gesmann@gmail.com>
Wayne Zhang <actuary_zhang@hotmail.com>
Daniel Murphy <danielmarkmurphy@gmail.com>

Type library(help='ChainLadder') or ?ChainLadder to see overall documentation.

Type demo(ChainLadder) to get an idea of the functionality of this package.

See demo(package='ChainLadder') for a list of more demos.

Feel free to send us an email if you would like to be kept informed of new versions or if you have any feedback, ideas, suggestions or would like to collaborate.

More information is available on the ChainLadder project web-site: http://code.google.com/p/chainladder/

To suppress this message use the statement: suppressPackageStartupMessages(library(ChainLadder))

3 Using the ChainLadder package

3.1 Working with triangles

Historical insurance data is often presented in form of a triangle structure, showing the development of claims over time for each origin period. An origin period could be the year the policy was sold, or the accident year. Of course the frequency doesn't have to be yearly, e.g. quarterly of monthly origin periods are also often used. Most reserving methods of the ChainLadder package expect triangles as input data sets with development periods along the columns and the origin period in rows. The package comes with several example triangles. The following R command will list them all:

```
R> require(ChainLadder)
R> data(package="ChainLadder")
```

Let's look at one example triangle more closely. The following triangle shows data from the Reinsurance Association of America (RAA):

```
R> ## Sample triangle
R> RAA
```

dev										
origin	1	2	3	4	5	6	7	8	9	10
1981	5012	8269	10907	11805	13539	16181	18009	18608	18662	18834
1982	106	4285	5396	10666	13782	15599	15496	16169	16704	NA
1983	3410	8992	13873	16141	18735	22214	22863	23466	NA	NA
1984	5655	11555	15766	21266	23425	26083	27067	NA	NA	NA
1985	1092	9565	15836	22169	25955	26180	NA	NA	NA	NA
1986	1513	6445	11702	12935	15852	NA	NA	NA	NA	NA
1987	557	4020	10946	12314	NA	NA	NA	NA	NA	NA
1988	1351	6947	13112	NA						
1989	3133	5395	NA							
1990	2063	NA								

The objective of a reserving exercise is to forecast the future claims development in the bottom right corner of the triangle and potential further developments. Eventually all claims for a given origin period wil be settled, but it is not always obvious to judge how many years or even decades it will take. We speak of long and short tail business depending on the time it takes to pay all claims.

3.1.1 Plotting triangles

The first thing you often want to do is to plot the data to get an overview. For a data set of class triangle the ChainLadder package provides default plotting

methods to give a graphical overview of the data:

R> plot(RAA)

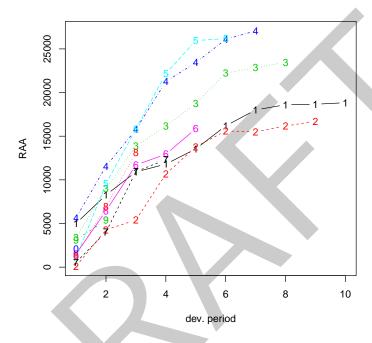


Figure 1: Claims development chart of the RAA triangle, with one line per origin period. Output of plot(RAA)

Setting the argument lattice=TRUE will produce individual plots for each origin period³, see Figure 2.

R> plot(RAA, lattice=TRUE)

You will notice from the plots in Figures 1 and 2 that the triangle RAA presents claims developments for the origin years 1981 to 1990 in a cumulative form. For more information on the triangle plotting functions see the help pages of plot.triangle, e.g. via

R> ?plot.triangle

 $^{^3\}mbox{ChainLadder}$ uses the ${\tt lattice}$ package for plotting the development of the origin years in separate panels.

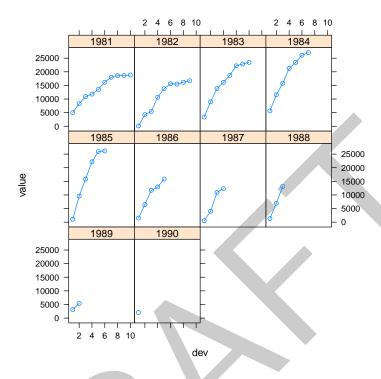


Figure 2: Claims development chart of the RAA triangle, with individual panels for each origin period. Output of plot(RAA, lattice=TRUE)

3.1.2 Transforming triangles between cumulative and incremental representation

The ChainLadder packages comes with two helper functions, cum2incr and incr2cum to transform cumulative triangles into incremental triangles and vice versa:

```
R> raa.inc <- cum2incr(RAA)
R> ## Show first origin period and it
```

R> ## Show first origin period and its incremental development
R> raa.inc[1,]

R> raa.cum <- incr2cum(raa.inc)</pre>

 $\mbox{R>}$ ## Show first origin period and its cumulative development

R> raa.cum[1,]

```
1 2 3 4 5 6 7 8 9 10
5012 8269 10907 11805 13539 16181 18009 18608 18662 18834
```

3.1.3 Importing triangles from external data sources

In most cases you want to analyse your own data, usually stored in data bases. R makes it easy to access data using SQL statements, e.g. via an ODBC connection⁴ and the ChainLadder packages includes a demo to showcase how data can be imported from a MS Access data base, see:

R> demo(DatabaseExamples)

For more details see [Tea12a].

In this section we use data stored in a CSV-file⁵ to demonstrate some typical operations you will want to carry out with data stored in data bases. In most cases your triangles will be stored in tables and not in a classical triangle shape. The ChainLadder package contains a CSV-file with sample data in a long table format. We read the data into R's memory with the read.csv command and look at the first couple of rows and summarise it:

```
R> filename <- file.path(system.file("Database",
                                        package="ChainLadder"),
                           "TestData.csv")
R> myData <- read.csv(filename)</pre>
R> head(myData)
  origin dev
               value lob
1
    1977
            1 153638 ABC
    1978
            1 178536 ABC
3
    1979
            1 210172 ABC
4
    1980
            1 211448 ABC
    1981
            1 219810 ABC
5
6
    1982
            1 205654 ABC
```

R> summary(myData)

ori	igin		de	v	value	:		lob
Min.	:	1	Min.	: 1.00	Min. :	-17657	AutoLiab	:105
1st Qu.	:	3	1st Qu.	: 2.00	1st Qu.:	10324	GeneralLiab	:105
Median	:	6	Median	: 4.00	Median :	72468	M3IR5	:105

⁴See the RODBC package

⁵Please ensure that your CSV-file is free from formatting, e.g. characters to separate units of thousands, as those columns will be read as characters or factors rather than numerical values.

```
Mean
       : 642
                Mean
                        : 4.61
                                  Mean
                                          : 176632
                                                      ABC
                                                                          : 66
3rd Qu.:1979
                3rd Qu.: 7.00
                                  3rd Qu.: 197716
                                                      CommercialAutoPaid: 55
Max.
       :1991
                Max.
                        :14.00
                                  Max.
                                          :3258646
                                                      GenIns
                                                                          : 55
                                                      (Other)
                                                                          :210
```

Let's focus on one subset of the data. We select the RAA data again:

```
R> raa <- subset(myData, lob %in% "RAA")
R> head(raa)
   origin dev value lob
67
               5012 RAA
     1981
             1
68
     1982
                 106 RAA
             1
69
     1983
             1
                3410 RAA
70
     1984
            1
                5655 RAA
71
     1985
             1
                1092 RAA
72
     1986
             1
                1513 RAA
```

To transform the long table of the RAA data into a triangle we use the function as.triangle. The arguments we have to specify are the column names of the origin and development period and further the column which contains the values:

```
R> raa.tri <- as.triangle(raa,
                           origin="origin",
                          dev="dev",
                           value="value")
R> raa.tri
      dev
origin
                                5
                                     6
                                           7
                                                      10
                        898 1734 2642 1828 599
  1981 5012 3257 2638
                                                  54 172
  1982 106 4179 1111 5270 3116 1817 -103 673
                                                 535
                                                      NA
  1983 3410 5582 4881 2268 2594 3479
                                         649 603
                                                  NA
                                                      NA
  1984 5655 5900 4211 5500 2159 2658
                                         984
                                              NA
                                                  NA
                                                      NA
  1985 1092 8473 6271 6333 3786
                                   225
                                         NA
                                              NA
                                                  NA
                                                      NA
  1986 1513 4932 5257 1233 2917
                                    NA
                                         NA
                                              NA
                                                  NA
                                                      NA
  1987 557 3463 6926 1368
                               NA
                                    NA
                                         NA
                                              NA
                                                  NA
                                                      NA
  1988 1351 5596 6165
                                    NA
                                                      NA
                         NA
                               NA
                                         NA
                                              NA
                                                  NA
  1989 3133 2262
                    NA
                         NA
                               NA
                                    NA
                                         NA
                                              NA
                                                  NA
                                                      NA
                    NA
  1990 2063
              MΔ
                         NA
                               NA
                                    NA
                                         NA
                                              NA
                                                  NA
                                                      NA
```

We note that the data has been stored as an incremental data set. As mentioned above, we could now use the function incr2cum to transform the triangle into a cumulative format.

We can transform a triangle back into a data frame structure:

R> raa.df <- as.data.frame(raa.tri, na.rm=TRUE)
R> head(raa.df)

	origin	dev	value
1981-1	1981	1	5012
1982-1	1982	1	106
1983-1	1983	1	3410
1984-1	1984	1	5655
1985-1	1985	1	1092
1986-1	1986	1	1513

This is particular helpful when you would like to store your results back into data base. Figure 3 gives you an idea of a potential data flow between R and data bases.

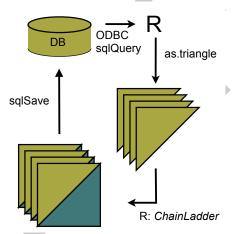


Figure 3: Flow chart of data between R and data bases.

3.1.4 Coping and pasting from MS Excel

Small data sets in Excel can be transfered to R backwards and forwards with via the clipboard under MS Windows.

Copying from Excel to R Select a data set in Excel and copy it into the clipboard, then go to R and type:

R> x <- read.table(file="clipboard", sep="\t", na.strings="")

Copying from R to Excel Suppose you would like to copy the RAA triangle into Excel, then the following statement would copy the data into the clipboard:

```
R> write.table(RAA, file="clipboard", sep="\t", na="")
```

Now you can paste the content into Excel. Please note that you can't copy lists structures from R to Excel.

3.2 Chain-ladder methods

The classical chain-ladder is a deterministic algorithm to forecast claims based on historical data. It assumes that the proportional developments of claims from one development period to the next are the same for all origin years.

3.2.1 Basic idea

The age-to-age link ratios are calculated as the volume weighted average development ratios of a cumulative loss development triangle from one development period to the next C_{ik} , $i, k = 1, \ldots, n$.

$$f_k = \frac{\sum_{i=1}^{n-k} C_{i,k+1}}{\sum_{i=1}^{n-k} C_{i,k}} \tag{1}$$

```
[1] 2.999 1.624 1.271 1.172 1.113 1.042 1.033 1.017 1.009
```

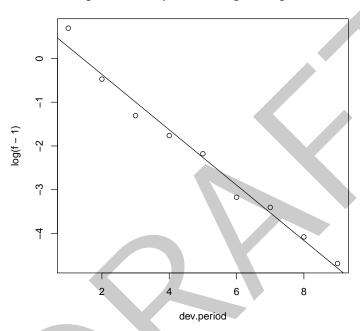
Often it is not suitable to assume that the oldest origin year is fully developed. A typical approach is to extrapolate the development ratios, e.g. assuming a log-linear model.

```
R> dev.period <- 1:(n-1)
R> plot(log(f-1) ~ dev.period, main="Log-linear extrapolation of age-to-age factors")
R> tail.model <- lm(log(f-1) ~ dev.period)
R> abline(tail.model)
R> co <- coef(tail.model)
R> ## extrapolate another 100 dev. period
```

```
R> tail <- \exp(\cos[1] + c((n + 1):(n + 100)) * \cos[2]) + 1
R> f.tail <- \operatorname{prod}(\operatorname{tail})
R> f.tail
```

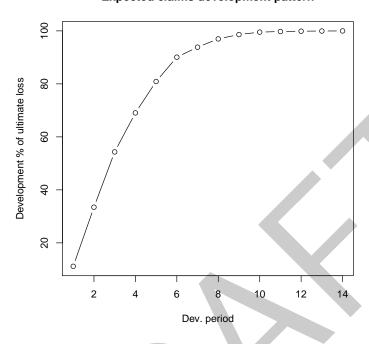
[1] 1.005

Log-linear extrapolation of age-to-age factors



The age-to-age factors allow us to plot the expected claims development patterns.

Expected claims development pattern



The link ratios are then applied to the latest know cumulative claims amount to forecast the next development period.

```
R> f <- c(f, f.tail)
R> fullRAA <- RAA
R> for(k in 1:(n-1)){
+ fullRAA[(n-k+1):n, k+1] <- fullRAA[(n-k+1):n,k]*f[k]
+ }
R> fullRAA[,n] <- fullRAA[,n]*f[n]
R> round(fullRAA)
```

```
dev
origin
                2
                      3
                                  5
                                                                10
             8269 10907 11805 13539 16181 18009 18608 18662 18928
  1981 5012
        106
             4285
                   5396 10666 13782 15599 15496 16169 16704 16942
  1983 3410
             8992 13873 16141 18735 22214 22863 23466 23863 24204
  1984 5655 11555 15766 21266 23425 26083 27067 27967 28441 28847
  1985 1092
             9565 15836 22169 25955 26180 27278 28185 28663 29072
  1986 1513
             6445 11702 12935 15852 17649 18389 19001 19323 19599
             4020 10946 12314 14428 16064 16738 17294 17587 17838
  1987
        557
  1988 1351
             6947 13112 16664 19525 21738 22650 23403 23800 24139
  1989 3133
             5395 8759 11132 13043 14521 15130 15634 15898 16125
```

This approach is also called Loss Development Factor (LDF) method.

Since the early 1990s several papers have been published to embed the simple chain-ladder method into a statistical framework. Ben Zehnwirth and Glenn Branett point out in [Zx00] that the age-to-age link ratios can be regarded as the coefficients of a weighted linear regression through the origin, see also [Mur94].

3.2.2 Mack chain-ladder

Thomas Mack published in 1993 [Mac93b] an article which allows to estimate the standard errors of the chain-ladder forecast without assuming a distribution under certain constrain to the data.

Following Mack [Mac99] let C_{ik} denote the cumulative loss amounts of origin period (e.g. accident year) $i=1,\ldots,m$, with losses known for development period (e.g. development year) $k\leq n+1-i$.

In order to forecast the amounts C_{ik} for k>n+1-i the Mack chain-ladder-model assumes:

CL1:
$$E[F_{ik}|C_{i1}, C_{i2}, \dots, C_{ik}] = f_k$$
 with $F_{ik} = \frac{C_{i,k+1}}{C_{ik}}$ (2)

CL2:
$$Var(\frac{C_{i,k+1}}{C_{ik}}|C_{i1}, C_{i2}, \dots, C_{ik}) = \frac{\sigma_k^2}{w_{ik}C_{ik}^{\alpha}}$$
 (3)

CL3:
$$\{C_{i1}, \ldots, C_{in}\}, \{C_{j1}, \ldots, C_{jn}\},$$
 are independent for origin period $i \neq j$ (4)

with $w_{ik} \in [0;1], \alpha \in \{0,1,2\}$. If these assumptions are hold, the Mack-chain-ladder-model gives an unbiased estimator for IBNR (Incurred But Not Reported) claims.

The Mack-chain-ladder model can be regarded as a weighted linear regression through the origin for each development period: $lm(y ~x + 0, weights=w/x^(2-alpha))$, where y is the vector of claims at development period k+1 and x is the vector of claims at development period k.

R> mack <- MackChainLadder(RAA, est.sigma="Mack") R> mack

MackChainLadder(Triangle = RAA, est.sigma = "Mack")

	${\tt Latest}$	Dev.To.Date	${\tt Ultimate}$	IBNR	Mack.S.E	CV(IBNR)
1981	18,834	1.000	18,834	0	0	NaN
1982	16,704	0.991	16,858	154	206	1.339
1983	23,466	0.974	24,083	617	623	1.010
1984	27,067	0.943	28,703	1,636	747	0.457
1985	26,180	0.905	28,927	2,747	1,469	0.535
1986	15,852	0.813	19,501	3,649	2,002	0.549
1987	12,314	0.694	17,749	5,435	2,209	0.406
1988	13,112	0.546	24,019	10,907	5,358	0.491
1989	5,395	0.336	16,045	10,650	6,333	0.595
1990	2,063	0.112	18,402	16,339	24,566	1.503

Totals

Latest: 160,987.00
Dev: 0.76
Ultimate: 213,122.23
IBNR: 52,135.23
Mack S.E.: 26,909.01
CV(IBNR): 0.52

Access the loss development factors and the full triangle

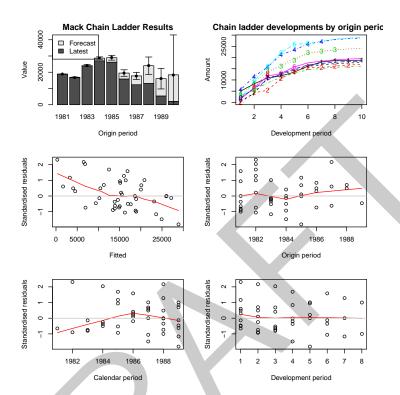
R> mack\$f

[1] 2.999 1.624 1.271 1.172 1.113 1.042 1.033 1.017 1.009 1.000

R> mack\$FullTriangle

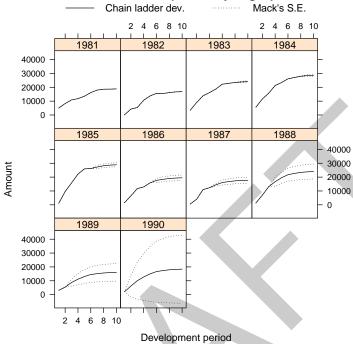
dev 5 8 10 origin 3 4 6 1981 5012 8269 10907 11805 13539 16181 18009 18608 18662 18834 1982 106 4285 5396 10666 13782 15599 15496 16169 16704 16858 1983 3410 8992 13873 16141 18735 22214 22863 23466 23863 24083 1984 5655 11555 15766 21266 23425 26083 27067 27967 28441 28703 9565 15836 22169 25955 26180 27278 28185 28663 28927 1985 1092 1986 1513 6445 11702 12935 15852 17649 18389 19001 19323 19501 1987 557 4020 10946 12314 14428 16064 16738 17294 17587 17749 1988 1351 6947 13112 16664 19525 21738 22650 23403 23800 24019 1989 3133 5395 8759 11132 13043 14521 15130 15634 15898 16045 1990 2063 6188 10046 12767 14959 16655 17353 17931 18234 18402

R> plot(mack)



R> plot(mack, lattice=TRUE)





3.2.3 Bootstrap chain-ladder

 $\mbox{R>}$ # See also the example in section 8 of England & Verrall (2002) on page 55. $\mbox{R>}$

R> B <- BootChainLadder(RAA, R=999, process.distr="gamma") R> B

BootChainLadder(Triangle = RAA, R = 999, process.distr = "gamma")

	Latest	Mean Ultimate	Mean IBNR	SD IBNR	IBNR 75%	IBNR 95%
1981	18,834	18,834	0	0	0	0
1982	16,704	16,876	172	759	171	1,453
1983	23,466	24,116	650	1,400	1,063	3,242
1984	27,067	28,671	1,604	1,899	2,513	4,921
1985	26,180	28,883	2,703	2,332	3,863	6,779
1986	15,852	19,588	3,736	2,474	5,075	8,196
1987	12,314	17,787	5,473	3,167	7,131	11,715
1988	13,112	24,224	11,112	5,014	14,013	20,137
1989	5,395	16,014	10,619	5,997	14,358	21,175
1990	2,063	18,870	16,807	13,570	23,956	43,034

Totals
Latest: 160,987
Mean Ultimate: 213,863
Mean IBNR: 52,876
SD IBNR: 18,705
Total IBNR 75%: 63,655
Total IBNR 95%: 87,192

R> plot(B)

R> # Compare to MackChainLadder

R> MackChainLadder(RAA)

MackChainLadder(Triangle = RAA)

	${\tt Latest}$	Dev.To.Date	Ultimate	IBNR	Mack.S.E	CV(IBNR)
1981	18,834	1.000	18,834	0	0	NaN
1982	16,704	0.991	16,858	154	143	0.928
1983	23,466	0.974	24,083	617	592	0.959
1984	27,067	0.943	28,703	1,636	713	0.436
1985	26,180	0.905	28,927	2,747	1,452	0.529
1986	15,852	0.813	19,501	3,649	1,995	0.547
1987	12,314	0.694	17,749	5,435	2,204	0.405
1988	13,112	0.546	24,019	10,907	5,354	0.491
1989	5,395	0.336	16,045	10,650	6,332	0.595
1990	2,063	0.112	18,402	16,339	24,566	1.503

Totals

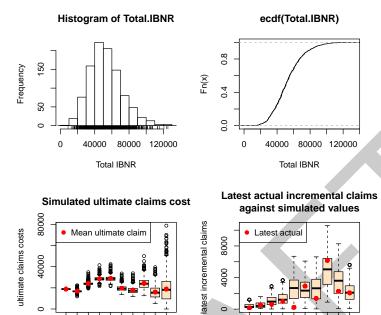
Latest: 160,987.00
Dev: 0.76
Ultimate: 213,122.23
IBNR: 52,135.23
Mack S.E.: 26,880.74
CV(IBNR): 0.52

R> quantile(B, c(0.75, 0.95, 0.99, 0.995))

\$ByOrigin

+-J	-0			
	IBNR 75%	IBNR 95%	IBNR 99%	IBNR 99.5%
1981	0.0	0	0	0
1982	170.8	1453	2990	3607
1983	1062.8	3242	5394	7412
1984	2512.9	4921	7290	9113
1985	3863.3	6779	9786	12052
1986	5075.0	8196	11128	12795
1987	7131.3	11715	14094	16151

```
1988 14013.2
                 20137
                          25022
                                      27061
1989 14358.2
                 21175
                          27265
                                      29882
1990 23955.6
                          56122
                 43034
                                      61632
$Totals
            {\tt Totals}
IBNR 75%:
             63655
IBNR 95%:
             87192
IBNR 99%:
            105033
IBNR 99.5%: 113207
R> # fit a distribution to the IBNR
R> library(MASS)
R> plot(ecdf(B$IBNR.Totals))
R> # fit a log-normal distribution
R> fit <- fitdistr(B$IBNR.Totals[B$IBNR.Totals>0], "lognormal")
R> fit
    meanlog
                 sdlog
 10.810850
               0.370020
 ( 0.011707) ( 0.008278)
R> curve(plnorm(x,fit$estimate["meanlog"], fit$estimate["sdlog"]),
        col="red", add=TRUE)
```



Total IBNR

1984

origin period

Munich chain-ladder 3.2.4

1984

1987

origin period

1990

R> MCLpaid

1981

	lev						
origin	1	2	3	4	5	6	7
1	576	1804	1970	2024	2074	2102	2131
2	866	1948	2162	2232	2284	2348	NA
3	1412	3758	4252	4416	4494	NA	NA
4	2286	5292	5724	5850	NA	NA	NA
5	1868	3778	4648	NA	NA	NA	NA
6	1442	4010	NA	NA	NA	NA	NA
7	2044	NA	NA	NA	NA	NA	NA

R> MCLincurred

C	lev						
origin	1	2	3	4	5	6	7
1	978	2104	2134	2144	2174	2182	2174
2	1844	2552	2466	2480	2508	2454	NA

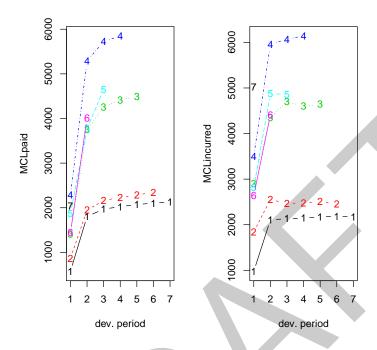
```
3 2904 4354 4698 4600 4644
                                    NA
                                         NA
     4 3502 5958 6070 6142
                                    NA
                                         NA
     5 2812 4882 4852
                              NA
                                    NA
                                         NA
     6 2642 4406
                    NA
                         NA
                              NA
                                    NA
                                         NA
     7 5022
              NA
                    NA
                         NA
                              NA
                                    NA
                                         NA
R> op <- par(mfrow=c(1,2))</pre>
R> plot(MCLpaid)
R> plot(MCLincurred)
R> par(op)
R> # Following the example in Quarg's (2004) paper:
R> MCL <- MunichChainLadder(MCLpaid, MCLincurred, est.sigmaP=0.1, est.sigmaI=0.1)
R> MCL
MunichChainLadder(Paid = MCLpaid, Incurred = MCLincurred, est.sigmaP = 0.1,
    est.sigmaI = 0.1)
 Latest Paid Latest Incurred Latest P/I Ratio Ult. Paid Ult. Incurred
                         2,174
                                           0.980
                                                      2,131
1
        2,131
                                                                     2,174
2
        2,348
                         2,454
                                           0.957
                                                      2,383
                                                                     2,444
3
        4,494
                         4,644
                                           0.968
                                                      4,597
                                                                     4,629
4
        5,850
                         6,142
                                           0.952
                                                      6,119
                                                                     6,176
5
                                           0.958
        4,648
                         4,852
                                                      4,937
                                                                     4,950
6
        4,010
                                           0.910
                                                      4,656
                         4,406
                                                                     4,665
7
        2,044
                         5,022
                                           0.407
                                                      7,549
                                                                    7,650
 Ult. P/I Ratio
1
           0.980
2
           0.975
3
           0.993
4
           0.991
           0.997
5
6
           0.998
7
           0.987
Totals
            Paid Incurred P/I Ratio
          25,525
Latest:
                    29,694
                                0.86
```

R> plot(MCL)

Ultimate: 32,371

0.99

32,688



3.3 Multivariate chain-ladder

3.4 Clark's methods

- 3.4.1 Clark's Cap Cod method
- 3.4.2 Clark's LDF method

3.5 Generalised linear model methods

4 Using ChainLadder with RExcel and SWord

The spreadsheet is located in the Excel folder of the package. The R command

R> system.file("Excel", package="ChainLadder")

will tell you the exact path to the directory. To use the spreadsheet you will need the RExcel-Add-in [BN07]. The package also provides an example SWord file, demonstrating how the functions of the package can be integrated into a MS Word file via SWord [BN07]. Again you find the Word file via the command:

```
R> system.file("SWord", package="ChainLadder")
```

The package comes with several demos to provide you with an overview of the package functionality, see

R> demo(package="ChainLadder")

5 Further resources

Other useful documents and resources to get started with R in the context of actuarial work:

- Introduction to R for Actuaries [DS06].
- An Actuarial Toolkit [MSH+06].
- The book Modern Actuarial Risk Theory Using R [KGDD01]
- Actuar package vignettes: http://cran.r-project.org/web/packages/actuar/index.html
- Mailing list R-SIG-insurance⁶: Special Interest Group on using R in actuarial science and insurance

5.1 Other insurance related R packages

Below is a list of further R packages in the context of insurance. The list is by nomeans complete, and the CRAN Task Views 'Emperical Finance' and Probability Distributions will provide links to additional resources. Please feel free to contact us with items to be added to the list.

- cplm: Monte Carlo EM algorithms and Bayesian methods for fitting Tweedie compound Poisson linear models [Zha11].
- lossDev: A Bayesian time series loss development model. Features include skewed-t distribution with time-varying scale parameter, Reversible Jump MCMC for determining the functional form of the consumption path, and a structural break in this path [LS11].
- favir: Formatted Actuarial Vignettes in R. FAViR lowers the learning curve
 of the R environment. It is a series of peer-reviewed Sweave papers that use
 a consistent style [Esc11].

⁶https://stat.ethz.ch/mailman/listinfo/r-sig-insurance

- actuar: Loss distributions modelling, risk theory (including ruin theory), simulation of compound hierarchical models and credibility theory [DGP08].
- fitdistrplus: Help to fit of a parametric distribution to non-censored or censored data [DMPDD10].
- mondate: R packackge to keep track of dates in terms of months [Mur11].
- lifecontingencies: Package to perform actuarial evaluation of life contingencies [Spe11].

5.2 Presentations

Over the years the contributors of the ChainLadder package have given numerous presentations and most of those are still available online:

- Bayesian Hierarchical Models in Property-Casualty Insurance, Wayne Zhang, 2011
- ChainLadder at the Predictive Modelling Seminar, Institute of Actuaries, November 2010, Markus Gesmann, 2011
- Reserve variability calculations, CAS spring meeting, San Diego, Jimmy Curcio Jr., Markus Gesmann and Wayne Zhang, 2010
- The ChainLadder package, working with databases and MS Office interfaces, presentation at the "R you ready?" workshop, Institute of Actuaries, Markus Gesmann, 2009
- The ChainLadder package, London R user group meeting, Markus Gesmann, 2009
- Introduction to R, Loss Reserving with R, Stochastic Reserving and Modelling Seminar, Institute of Actuaries, Markus Gesmann, 2008
- Loss Reserving with R, CAS meeting, Vincent Goulet, Markus Gesmann and Daniel Murphy, 2008
- The ChainLadder package R-user conference Dortmund, Markus Gesmann, 2008

5.3 Further reading

Other papers and presentation which cited ChainLadder: [Orr07], [Nic09], [Zha10], [MNNV10], [Sch10], [MNV10], [Esc11], [Spe11]

6 Training and consultancy

Please contact us if you would like to discuss tailored training or consultancy.

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