

Detected Resonant Frequencies (0-200 Hz):

16
52
88
122
146
186

Estimated Damping Ratios:

Mode near 16.00 Hz $\rightarrow \zeta = 0.1250$
Mode near 52.00 Hz $\rightarrow \zeta = 0.0577$
Mode near 88.00 Hz $\rightarrow \zeta = 0.0341$
Mode near 122.00 Hz $\rightarrow \zeta = 0.0410$
Mode near 146.00 Hz $\rightarrow \zeta = 0.0274$
Mode near 186.00 Hz $\rightarrow \zeta = 0.0430$

Normalized Mode Shapes (0-200 Hz):

Mode at 16.00 Hz:

X: $0.019 \angle 157.6^\circ$
Y: $0.021 \angle 123.1^\circ$
Z: $1.000 \angle 167.5^\circ$

Mode at 52.00 Hz:

X: $1.000 \angle 66.8^\circ$
Y: $0.127 \angle -89.2^\circ$
Z: $0.793 \angle -18.1^\circ$

Mode at 88.00 Hz:

X: $0.104 \angle -57.6^\circ$
Y: $1.000 \angle -34.0^\circ$
Z: $0.487 \angle 8.3^\circ$

Mode at 122.00 Hz:

X: $0.069 \angle 77.3^\circ$
Y: $0.049 \angle 64.3^\circ$
Z: $1.000 \angle 76.9^\circ$

Mode at 146.00 Hz:

X: 0.065∠-51.1°

Y: 0.223∠-63.6°

Z: 1.000∠23.4°

Mode at 186.00 Hz:

X: 0.163∠-100.3°

Y: 0.178∠150.3°

Z: 1.000∠17.1°

=== Modal Parameter Summary (0-200 Hz) ===

Freq_Hz Damping Phi_X Phi_Y Phi_Z

16	0.125	-0.017442+0.0071816i	-0.011378+0.017451i	-0.97626+0.21659i
52	0.057692	0.39422+0.91902i	0.0017201-0.12723i	0.75322-0.24661i
88	0.034091	0.055757-0.088008i	0.82882-0.55952i	0.48212+0.070327i
122	0.040984	0.015181+0.06761i	0.021437+0.044454i	0.22603+0.97412i
146	0.027397	0.040688-0.050431i	0.099189-0.20024i	0.91746+0.39783i
186	0.043011	-0.029251-0.16039i	-0.15504+0.088448i	0.95556+0.29478i

Detected Resonant Frequencies (0-200 Hz):

16

52

88

122

146

186

Estimated Damping Ratios:

0.1250

0.0577

0.0341

0.0410

0.0274

0.0430

=== Modal Summary (0-200 Hz) ===

Mode 1: $f=16.00$ Hz, Damping= 0.1250 , $k_{\text{dyn_X}}=8195776.87$ N/m, $k_{\text{dyn_Y}}=7420866.90$ N/m, $k_{\text{dyn_Z}}=154592.23$ N/m

Mode Shape (X,Y,Z): $0.019\angle 157.6^\circ$, $0.021\angle 123.1^\circ$, $1.000\angle 167.5^\circ$

Mode 2: $f=52.00$ Hz, Damping= 0.0577 , $k_{\text{dyn_X}}=14996983.56$ N/m, $k_{\text{dyn_Y}}=117861128.37$ N/m, $k_{\text{dyn_Z}}=18922173.59$ N/m

Mode Shape (X,Y,Z): $1.000\angle 66.8^\circ$, $0.127\angle -89.2^\circ$, $0.793\angle -18.1^\circ$

Mode 3: $f=88.00$ Hz, Damping= 0.0341 , $k_{\text{dyn_X}}=502580997.69$ N/m, $k_{\text{dyn_Y}}=52360875.03$ N/m, $k_{\text{dyn_Z}}=107467134.75$ N/m

Mode Shape (X,Y,Z): $0.104\angle -57.6^\circ$, $1.000\angle -34.0^\circ$, $0.487\angle 8.3^\circ$

Mode 4: $f=122.00$ Hz, Damping= 0.0410 , $k_{\text{dyn_X}}=65415541.11$ N/m, $k_{\text{dyn_Y}}=91847118.55$ N/m, $k_{\text{dyn_Z}}=4532882.38$ N/m

Mode Shape (X,Y,Z): $0.069\angle 77.3^\circ$, $0.049\angle 64.3^\circ$, $1.000\angle 76.9^\circ$

Mode 5: $f=146.00$ Hz, Damping= 0.0274 , $k_{\text{dyn_X}}=488433312.77$ N/m, $k_{\text{dyn_Y}}=141635283.96$ N/m, $k_{\text{dyn_Z}}=31649475.98$ N/m

Mode Shape (X,Y,Z): $0.065\angle -51.1^\circ$, $0.223\angle -63.6^\circ$, $1.000\angle 23.4^\circ$

Mode 6: $f=186.00$ Hz, Damping= 0.0430 , $k_{\text{dyn_X}}=664947086.06$ N/m, $k_{\text{dyn_Y}}=607366525.46$ N/m, $k_{\text{dyn_Z}}=108411531.67$ N/m

Mode Shape (X,Y,Z): $0.163\angle -100.3^\circ$, $0.178\angle 150.3^\circ$, $1.000\angle 17.1^\circ$