

Detected Resonant Frequencies (0-200 Hz):

16  
44  
52  
88  
176  
190

Estimated Damping Ratios:

Mode near 16.00 Hz  $\rightarrow \zeta = 0.1250$   
Mode near 44.00 Hz  $\rightarrow \zeta = 0.0455$   
Mode near 52.00 Hz  $\rightarrow \zeta = 0.0385$   
Mode near 88.00 Hz  $\rightarrow \zeta = 0.0341$   
Mode near 176.00 Hz  $\rightarrow \zeta = 0.0284$   
Mode near 190.00 Hz  $\rightarrow \zeta = 0.0263$

Normalized Mode Shapes (0-200 Hz):

Mode at 16.00 Hz:

X:  $0.750 \angle 174.5^\circ$   
Y:  $0.234 \angle -177.7^\circ$   
Z:  $1.000 \angle -5.4^\circ$

Mode at 44.00 Hz:

X:  $1.000 \angle -7.6^\circ$   
Y:  $0.551 \angle -85.3^\circ$   
Z:  $0.897 \angle 174.1^\circ$

Mode at 52.00 Hz:

X:  $1.000 \angle -115.4^\circ$   
Y:  $0.068 \angle 71.2^\circ$   
Z:  $0.795 \angle 66.2^\circ$

Mode at 88.00 Hz:

X:  $0.254 \angle -175.7^\circ$   
Y:  $1.000 \angle 145.3^\circ$   
Z:  $0.176 \angle 12.9^\circ$

Mode at 176.00 Hz:

X: 0.201∠-159.3°

Y: 1.000∠136.7°

Z: 0.168∠169.6°

Mode at 190.00 Hz:

X: 0.574∠-141.7°

Y: 0.475∠57.6°

Z: 1.000∠51.5°

=== Modal Parameter Summary (0-200 Hz) ===

**Freq\_Hz Damping Phi\_X Phi\_Y Phi\_Z**

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16	0.125	-0.74618+0.072004i	-0.23356-0.009204i	0.9956-0.093658i
44	0.045455	0.99117-0.13262i	0.045264-0.54936i	-0.892+0.092867i
52	0.038462	-0.42953-0.90305i	0.021824+0.064194i	0.32008+0.7272i
88	0.034091	-0.25376-0.019038i	-0.82253+0.56873i	0.17136+0.039128i
176	0.028409	-0.18815-0.07101i	-0.72721+0.68642i	-0.16514+0.030209i
190	0.026316	-0.4502-0.35542i	0.25414+0.40118i	0.62262+0.78253i

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Estimated Damping Ratios:

0.1250

0.0455

0.0385

0.0341

0.0284

0.0263

=== Modal Summary (0-200 Hz) ===

Mode 1: f=16.00 Hz, Damping=0.1250, k\_dyn\_X=1400318.13 N/m, k\_dyn\_Y=4491036.04 N/m, k\_dyn\_Z=1049742.83 N/m

Mode Shape (X,Y,Z): 0.750∠174.5°, 0.234∠-177.7°, 1.000∠-5.4°

Mode 2: f=44.00 Hz, Damping=0.0455, k\_dyn\_X=26083589.57 N/m, k\_dyn\_Y=47319624.35 N/m, k\_dyn\_Z=29084391.48 N/m

Mode Shape (X,Y,Z): 1.000∠-7.6°, 0.551∠-85.3°, 0.897∠174.1°

Mode 3: f=52.00 Hz, Damping=0.0385, k\_dyn\_X=6521094.45 N/m, k\_dyn\_Y=96177777.55 N/m, k\_dyn\_Z=8207496.63 N/m

Mode Shape (X,Y,Z): 1.000∠-115.4°, 0.068∠71.2°, 0.795∠66.2°

Mode 4: f=88.00 Hz, Damping=0.0341, k\_dyn\_X=177070025.15 N/m, k\_dyn\_Y=45060333.28 N/m, k\_dyn\_Z=256355651.13 N/m

Mode Shape (X,Y,Z): 0.254∠-175.7°, 1.000∠145.3°, 0.176∠12.9°

Mode 5: f=176.00 Hz, Damping=0.0284, k\_dyn\_X=533551100.58 N/m, k\_dyn\_Y=107297084.92 N/m, k\_dyn\_Z=639136796.47 N/m

Mode Shape (X,Y,Z): 0.201∠-159.3°, 1.000∠136.7°, 0.168∠169.6°

Mode 6: f=190.00 Hz, Damping=0.0263, k\_dyn\_X=361927460.80 N/m, k\_dyn\_Y=437136515.47 N/m, k\_dyn\_Z=207598713.02 N/m

Mode Shape (X,Y,Z): 0.574∠-141.7°, 0.475∠57.6°, 1.000∠51.5°