

AI1103–Assignment-3

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Download all latex-tikz codes from

https://github.com/AravindCSEiith/Probability-and-Random-variables_AI1103_Assignment-3/blob/main/Assignment_3_AI1103.tex

QUESTION

Let the random variable X have the distribution $P(X = 0) = P(X = 3) = p$, $P(X = 1) = 1 - 3p$ for $0 \leq p \leq \frac{1}{2}$. What is the maximum value of $V(X)$?

- A) 3
- B) 4
- C) 5
- D) 6
- E) none

SOLUTION

Given, for $0 \leq p \leq \frac{1}{2}$,

$$P(X = 0) = p \quad (0.0.1)$$

$$P(X = 1) = 1 - 3p \quad (0.0.2)$$

$$P(X = 3) = p \quad (0.0.3)$$

Now consider $P(X = 1) = 1 - 3p$ for $p = \frac{1}{2}$. We get,

$$P(X = 1) = 1 - 3p \quad (0.0.4)$$

$$= 1 - (3)\left(\frac{1}{2}\right) \quad (0.0.5)$$

$$= 1 - \frac{3}{2} \quad (0.0.6)$$

$$= -\frac{1}{2} < 0 \quad (0.0.7)$$

Probability cannot be negative. But in equation (0.0.7) probability is negative, which is not possible. Therefore, the question is not a proper one.

Answer : Option E