

Q.1 Given an array, find the max sum subarray of length k.

A =     3     9     4     -2     5     13     -7     8         k=4  
         0     1     2     3     4     5     6     7

S	e	ans
0	3	14
1	4	16
2	5	20
3	6	9
4	7	19

i) go to each subarray of length k, find its sum and the overall best is the ans.

```
int solve (int [] A, int k) {
```

k = 3

```
int s = 0, e = k - 1;
```

A =  $\begin{bmatrix} 2 & 4 & -1 & 9 & 5 & 8 \\ 0 & 1 & 2 & 3 & 4 & 5 \end{bmatrix}$

```
int n = A.length;
```

```
int ans = Integer.MIN_VALUE;
```

```
while (e < n) {
```

```
int sum = 0;
```

```
for (int i = s; i <= e; i++) {
```

```
sum += A[i];
```

```
if (sum > ans) {
```

```
ans = sum;
```

```
}
```

```
s++;
```

```
e++;
```

```
}
```

```
return ans;
```

s	e	sum
0	2	0 to 2
1	3	1 to 3
2	4	2 to 4
3	5	3 to 5
4	6	

TC:  $O(n^2)$

SC:  $O(1)$

$$TC: \left( \begin{array}{c} \text{no. of subarray of} \\ \text{length } k \end{array} \right) = k$$

A =      a      b      c      d      e      f      g      h  
             0      1      2      3      4      5      6      7

k	no. of subarrays	
1	8	n
2	7	n-1
3	6	n-2

$$n - (k-1) \Rightarrow n - k + 1$$

$$TC: \left( \begin{array}{c} \text{no. of subarray of} \\ \text{length } k \end{array} \right) = k$$

$$\begin{array}{c}
 (n-k+1) * k \\
 \begin{array}{ccc}
 \swarrow k=1 & | & \searrow k=\frac{n}{2} \\
 n & n & (n-\frac{n}{2}+1) * \frac{n}{2} \approx n^2
 \end{array}
 \end{array}$$

ii) prefix sum

```
int solve (int [] A, int k) {
```

```
    int s=0, e=k-1;
```

```
    int n=A.length;
```

```
    int ans= Integer.MIN_VALUE;
```

```
    int [] ps= prefixSum(A);
```

```
    while (e < n) {
```

```
        int sum=0;
```

```
        if (s==0) {
```

```
            sum= ps[e];
```

```
        }
```

```
        else {
```

```
            sum= ps[e] - ps[s-1];
```

```
        }
```

```
        if (sum > ans) {
```

```
            ans = sum;
```

```
        }
```

```
        s++;
```

```
        e++;
```

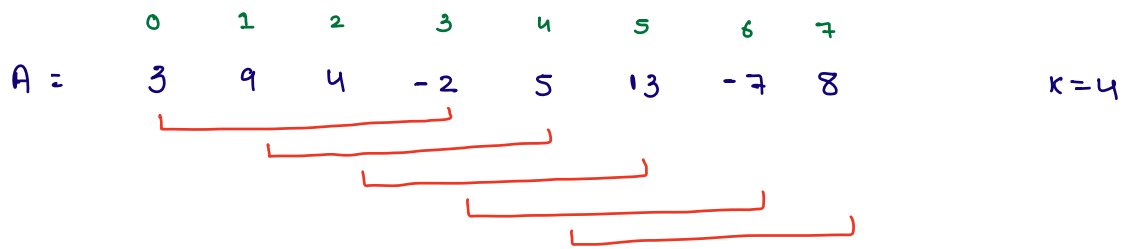
```
    }
```

```
    return ans;
```

```
}
```

Tc:  $O(n)$

Sc:  $O(n)$



carry forward + fixed length subarray  $\Rightarrow$  sliding window

s	e	Sum
0	3	$A[0] + A[1] + A[2] + A[3]$
1	4	$\cancel{A[0]} + A[1] + A[2] + A[3] - \cancel{A[0]} + A[4]$
2	5	$\cancel{A[1]} + A[2] + A[3] + A[4] - \cancel{A[1]} + A[5]$
3	6	$\cancel{A[2]} + A[3] + A[4] + A[5] - \cancel{A[2]} + A[6]$
4	7	$\cancel{A[3]} + A[4] + A[5] + A[6] - \cancel{A[3]} + A[7]$

$$\text{sum} - A[s-1] + A[e]$$

```
int solve (int [] A, int k) {
```

k=3

```
int n = A.length;
```

```
int sum = 0;
```

// moved the first window

```
for (int i = 0; i < k; i++) {
```

```
    | sum += A[i];
```

```
int ans = sum;
```

```
int s = 1, e = k;
```

```
while (e < n) {
```

```
    | sum = sum - A[s-1] + A[e];
```

```
    | if (sum > ans) {
```

```
        | ans = sum;
```

```
    | }
```

```
    | s++, e++;
```

```
    | }
```

```
return ans;
```

}

A = [ 2 3 -4 5 7 1 ]  
0 1 2 3 4 5

ans = ~~4/8~~  
13

s	e	sum
		1
1	3	1 - 2 + 5 = 4
2	4	4 - 3 + 7 = 8
3	5	8 - (-4) + 1 = 13
4	6	

Tc:  $O(n)$

Sc:  $O(1)$

Q.2 Given a row and col wise sorted matrix, find if  $k$  is present in it or not.

$A =$

	0	1	2	3	4
0	10	20	30	40	50
1	12	22	35	45	58
2	18	25	44	54	68
3	38	48	55	59	72

$k = 49$

i) brute force : travelling entire matrix      TC:  $O(n \cdot m)$

$A =$

	0	1	2	3	4
0	<del>10</del>	<del>20</del>	<del>30</del>	40	50
1	<del>12</del>	<del>22</del>	35	45	<del>58</del>
2	18	25	44	54	<del>68</del>
3	38	48	55	<del>59</del>	<del>72</del>

$k = 49$

$A =$

	0	1	2	3	4
0	<del>10</del>	<del>20</del>	30	40	50
1	<del>12</del>	<del>22</del>	35	<del>45</del>	<del>58</del>
2	<del>18</del>	25	44	<del>54</del>	<del>68</del>
3	38	48	<del>55</del>	<del>59</del>	<del>72</del>

$k = 38$

$k = 49$

	0	1	2	3	4
0	10	20	30	40	50
1	12	22	35	45	58
2	18	25	49	54	68
3	38	48	55	59	72

i	j
0	4
0	3
1	3
2	3
2	2
2	2

$\rightarrow 49$

boolean search (int [][] A, int k) {

int n = A.length;

int m = A[0].length;

int i = 0, j = m - 1;

while ( i < n && j >= 0 ) {

if (A[i][j] == k) {

return true;

}

else if (A[i][j] > k) {

j--;

}

else if (A[i][j] < k) {

i++;

}

}

return false;

}

TC :  $O(n)$



try run

```

while( i < n && j >= 0 ) {
    if (A[i][j] == k) {
        return true;
    }
    else if (A[i][j] > k) {
        j--;
    }
    else if (A[i][j] < k) {
        i++;
    }
}
return false;

```

$k = 49$

$j$

	0	1	2	3	4
0	<del>10</del>	<del>20</del>	<del>30</del>	40	50
1	<del>12</del>	<del>22</del>	<del>35</del>	45	<del>58</del>
2	18	25	49	54	68
3	38	48	55	<del>59</del>	<del>72</del>

$i$

```

while( i < n && j >= 0 ) {
    if (A[i][j] == k) {
        return true;
    }
    else if (A[i][j] > k) {
        j--;
    }
    else if (A[i][j] < k) {
        i++;
    }
}
return false;

```

$k = 21$

$j$

	0	1	2	3	4
0	<del>10</del>	20	30	40	50
1	12	22	<del>35</del>	<del>45</del>	<del>58</del>
2	18	25	49	<del>54</del>	<del>68</del>
3	38	<del>48</del>	<del>55</del>	<del>59</del>	<del>72</del>

$i$

$i = 3, j = -1$

↳ out of loop

Q.3 Given a 2D matrix of  $N \times N$ , print its outermost boundary in clockwise direction.

A =

	0	1	2	3	4
0	10	20	25	15	12
1	19	18	13	28	101
2	15	5	6	7	34
3	9	94	38	10	28
4	6	7	8	12	55

10 20 25 15 12 101 34  
 28 55 12 8 7 6 9  
 15 19

$$n = 5$$

A =

	0	1	2	3	4
0	10	20	25	15	12
1	19	18	13	28	101
2	15	5	6	7	34
3	9	94	38	10	28
4	6	7	8	12	55

print  $n-1$  ele L to R

print  $n-1$  ele T to B

print  $n-1$  ele R to L

print  $n-1$  ele B to T

```
void boundary (int [][] A) {
```

```
    int n = A.length;
```

```
    int i = 0, j = 0;
```

```
    // print n-1 values left to right
```

```
    for (int k = 1; k <= n-1; k++) {
```

```
        sop (A[i][j] + " ");
```

```
        j++;
```

```
    }
```

```
    // print n-1 values top to bottom
```

```
    for (int k = 1; k <= n-1; k++) {
```

```
        sop (A[i][j] + " ");
```

```
        i++;
```

```
    }
```

```
    // print n-1 values right to left
```

```
    for (int k = 1; k <= n-1; k++) {
```

```
        sop (A[i][j] + " ");
```

```
        j--;
```

```
    }
```

```
    // print n-1 values bottom to top
```

```
    for (int k = 1; k <= n-1; k++) {
```

```
        sop (A[i][j] + " ");
```

```
        i--;
```

```
    }
```

Q.4 Given a 2D matrix of  $N \times N$ , print it in **Spiral manner**.

A =

	0	1	2	3	4	5
0	10	12	44	55	18	6
1	20	19	15	25	36	38
2	41	42	49	54	48	55
3	8	6	17	2	5	9
4	13	2	3	40	78	3
5	18	19	20	21	10	7

i	j	n
0	0	6
1	1	4
2	2	2
3	3	0

	0	1	2	3	4
0	10	20	25	1	12
1	19	18	13	28	101
2	15	5	6	7	34
3	4	94	38	10	28
4	6	7	8	12	55

i	j	n
0	0	5
1	1	3
2	2	1

```
void spiral (int [][ ] A) {
```

```
    int n = A.length;
```

```
    int i = 0, j = 0;
```

```
    while ( n > 1 ) {
```

```
        // print n-1 values left to right
```

```
        for (int k = i; k <= n-1; k++) {
```

```
            |      sop (A[i][j] + " ");
```

```
            |      j++;
```

```
        }
```

```
        // print n-1 values top to bottom
```

```
        for (int k = i; k <= n-1; k++) {
```

```
            |      sop (A[i][j] + " ");
```

```
            |      i++;
```

```
        }
```

```
        // print n-1 values right to left
```

```
        for (int k = i; k <= n-1; k++) {
```

```
            |      sop (A[i][j] + " ");
```

```
            |      j--;
```

```
        }
```

```
        // print n-1 values bottom to top
```

```
        for (int k = i; k <= n-1; k++) {
```

```
            |      sop (A[i][j] + " ");
```

```
            |      i--;
```

```
        }
```

```
        i++, j++;
```

```
        n = n-2;
```

```
    }
```

```
    if (n == 1) {
```

```
        sop (A[i][j] + " ");
```

```
    }
```

Doubts  
=

$$A = \begin{bmatrix} 6 & 9 & 8 & 10 \\ \cancel{1} & \cancel{2} & \cancel{1} & \cancel{4} \end{bmatrix}$$

0      1      2      3

$$A_{\text{sr}} = \begin{bmatrix} 5 & 2 & & 1 \\ \emptyset & \emptyset & 0 & -2 \\ 0 & 1 & 2 & 3 \end{bmatrix}$$

(1 based)

$$2 \quad 3 \quad 2 \quad \rightarrow \quad 1 \quad 2 \quad 2$$

$$1 \quad 4 \quad 5 \quad \rightarrow \quad 0 \quad 3 \quad 5$$

$$4 \quad 4 \quad 1 \quad \rightarrow \quad 3 \quad 3 \quad 1$$

$$[5 \quad 7 \quad 7 \quad 6]$$

Ans  $\rightarrow$  add<sup>n</sup> of  $A[i] + Arr[i]$

$$s = A[i][0] - 1;$$

$$e = A[i][1] - 1;$$

$$val = A[i][2];$$

$$A[s] += val;$$

$$A[e+1] += -val; \quad (\text{if } e+1 < n)$$

$$A = \begin{bmatrix} 1 & 2 & 1 & 4 \end{bmatrix}$$

0      1      2      3

+2      +2

+5      +5      +5      +5

+1

---

6      9      8      10

Revise



Assign | HW



do similar ques on other platform

↳ Leetcode

↳ hfh

2, 4 → 2

0, 3 → 3

2, 4 → 5

0 1 2 3 4 5 6

0 0 0 0 0 0 0

2 2 2

3 3 3 3

5 5 5

---

3 3 7 7 7 0 0

$2, 4 \rightarrow 2$  ↙  
 $0, 3 \rightarrow 3$  ↙  
 $2, 4 \rightarrow 5$  ↙  
 $2 \rightarrow \begin{matrix} 10 \\ 10 \end{matrix}$   
 $3 \rightarrow \begin{matrix} 11 \\ 10 \end{matrix}$   
 $5 \rightarrow \begin{matrix} 101 \\ 210 \end{matrix}$

0   1   2   3   4   5   6  
 0   0   0   0   0   0   0

	0	1	2	3	4	5	6
0	1	1	2	2	1	0	0
1	1	1	2	2	1	0	0
2	0	0	1	1	1	0	0
3							
4							
5							
6							
⋮							
⋮							
⋮							
32							
	3	3	7	7	7	0	0

for (0) {

s, e, val

for (32) → bits of val

}

for (32) {

for (ps → 0 to N)

}

TC:  $O(N)$