

## Agenda

- i) Design min Stack
- ii) Nearest Smaller
  - ↳ on left
  - ↳ on right
- iii) Largest Area histogram

Q.1 Design a Stack that supports push, pop, top and min functions in  $O(1)$  time.

10 5 9 18 12 3 7 17

```
MinStack st = new MinStack();
```

```
st.push(10)
```

```
st.push(5)
```

```
st.push(9)
```

```
st.push(18)
```

```
st.push(12)
```

```
st.push(3)
```

```
st.push(7)
```

```
st.min() → 3
```

```
st.pop()
```

```
st.pop()
```

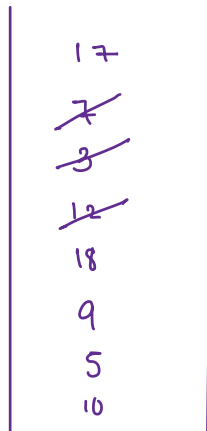
```
st.min() → 5
```

```
st.top() → 12
```

```
st.pop()
```

```
st.push(17)
```

```
st.top() → 17
```



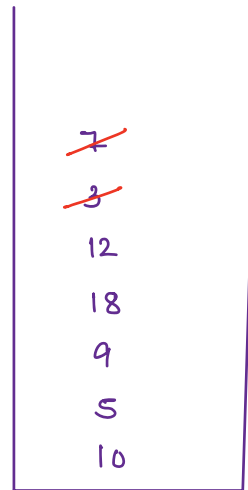
```
class MinStack {
```

```
    void push(int x)
    void pop()
    int top()
    int min()
```

```
}
```

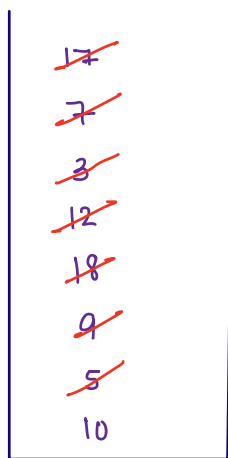
↓  
10 5 4 18 12 3 7 17

min = ~~10~~ / ~~5~~ / ~~4~~ / 3

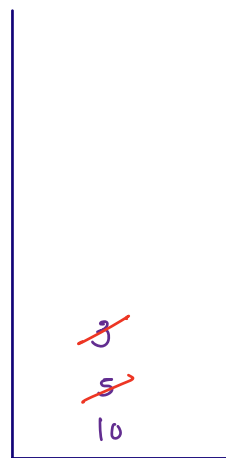


Idea: Manage min by creating a separate stack.

↓  
10 5 4 18 12 3 7 17



valst

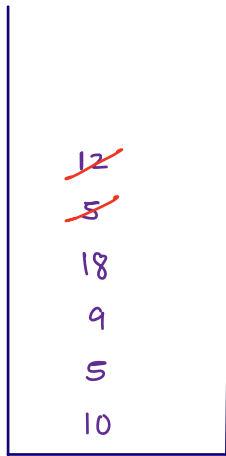


minst

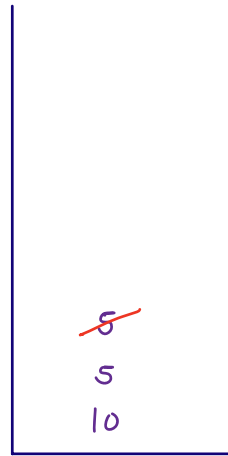
min till now

→ minst.peek()

↓  
10 5 9 18 5 12 3 7 3 17



valst



minst

```
class minStack {
```

→ two stacks { valst, minst }

```
void push(int x) {
```

→ maintain size 0

→ add x to valst

→ add x to minst (  $x \leq \text{minst}.\text{peek}()$  )

```
}
```

```
void pop() {
```

→ maintain size 0

→ pop from valst : (temp)

→ pop from minst (  $\text{minst}.\text{peek}() == \text{temp}$  )

```
}
```

```
int top() {
```

→ maintain size 0

→ return valst.peek()

```
}
```

```
int min() {
```

→ maintain size 0

→ return minst.peek()

```
}
```

```
}
```

```
class Solution {

    Stack<Integer>valst = new Stack<>();
    Stack<Integer>minst = new Stack<>();

    public void push(int x) {
        if(valst.size() == 0) {
            valst.push(x);
            minst.push(x);
        }
        else {
            valst.push(x);

            //should I add x in minst as well
            if(x <= minst.peek()) {
                minst.push(x);
            }
        }
    }

    public void pop() {
        if(valst.size() == 0) {
            //nothing
        }
        else {
            int temp = valst.pop();

            //should I pop from minst as well
            if(temp == minst.peek()) {
                minst.pop();
            }
        }
    }

    public int top() {
        if(valst.size() == 0) {
            return -1;
        }
        else {
            return valst.peek();
        }
    }

    public int getMin() {
        if(valst.size() == 0) {
            return -1;
        }
        else {
            return minst.peek();
        }
    }
}
```

Q.2 Nearest / next smaller on left.

A = [10 16 5 9 12 8 25 7 13]  
ans -1 10 -1 5 9 5 8 5 7

A = [18 3 13 14 5 24 4]  
ans -1 -1 3 13 3 5 3

Expected TC:  $O(n)$

A = [10 16 5 9 12 8 25 7 13]  
ans -1 10 -1 5 9 5 8 5 7

for ( $i \rightarrow 1$  to  $A.length-1$ ) {

while ( $st.size() > 0$  &&  $st.peek() \geq A[i]$ ) {

st.pop();

}

if ( $st.size() == 0$ ) {

ans[i] = -1;

}

else {

ans[i] = st.peek();

}

st.push(A[i]);

}

13  
7  
~~25~~  
~~8~~  
~~12~~  
~~9~~  
5  
~~16~~  
~~10~~

TC:  $O(n)$

SC:  $O(n)$

Nearest / next smaller on left (index based)

for every element find its nearest smaller on left's index.

↓

A =		<sup>0</sup>	<sup>1</sup>	<sup>2</sup>	<sup>3</sup>	<sup>4</sup>	<sup>5</sup>	<sup>6</sup>	<sup>7</sup>	<sup>8</sup>
	[	10	16	5	9	12	8	25	7	13]
ans		-1	0	-1	2	3	2	5	2	7

for (i → 1 to A.length-1) {

while (st.size() > 0 && A[st.peek()] >= A[i]) {  
    st.pop();

}

if (st.size() == 0) {

    ans[i] = -1;

}

else {

    ans[i] = st.peek();

}

st.push(i);

}

8
7
<del>8</del>
<del>8</del>
<del>4</del>
<del>2</del>
2
<del>2</del>
<del>0</del>

Q.3 Nearest / next smaller on right.

for every element find the value of nearest / next smaller on right

exact same logic but travel from right to left

↓  
A = [10 16 5 9 12 8 25 7 3]  
ans    5   5   3   8   8   7   7   3   -1

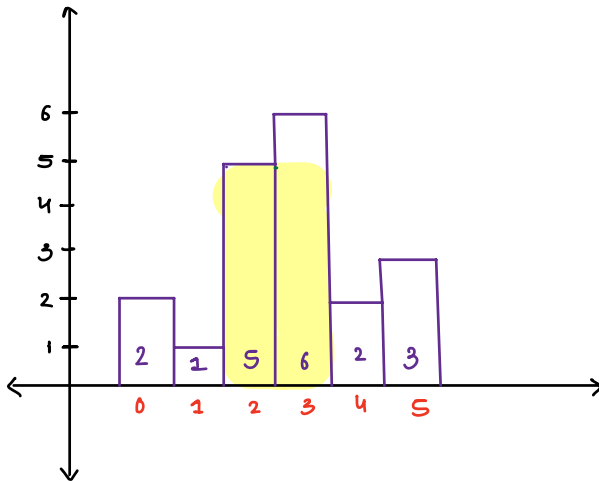
10
<del>16</del>
5
<del>9</del>
<del>12</del>
<del>8</del>
<del>25</del>
<del>7</del>
3

Nearest / next smaller on right (Index based)



#### 0.4 Largest area histogram

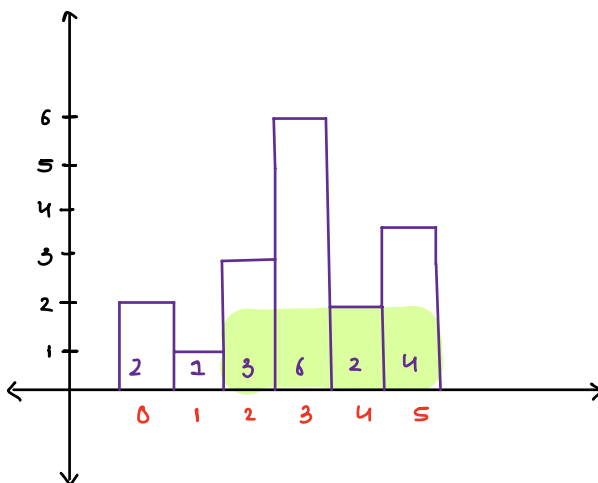
$A = [2 \ 1 \ 5 \ 6 \ 2 \ 3]$



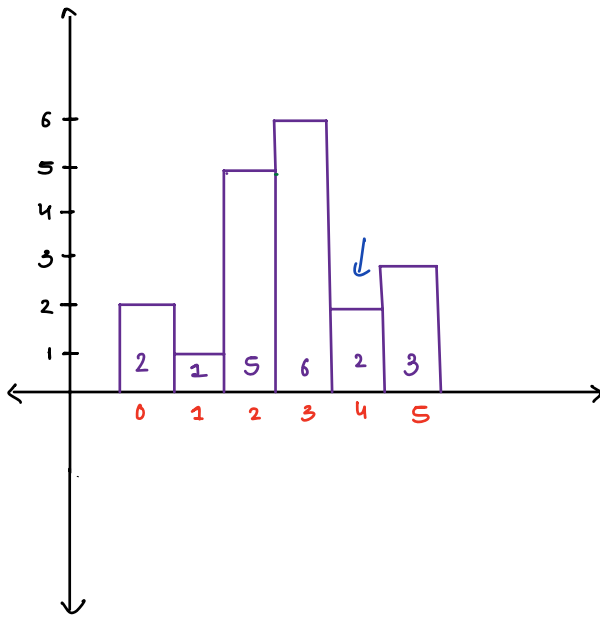
Return the area of  
largest rectangle possible?

$$\text{ans} = 5 \times 2 = 10$$

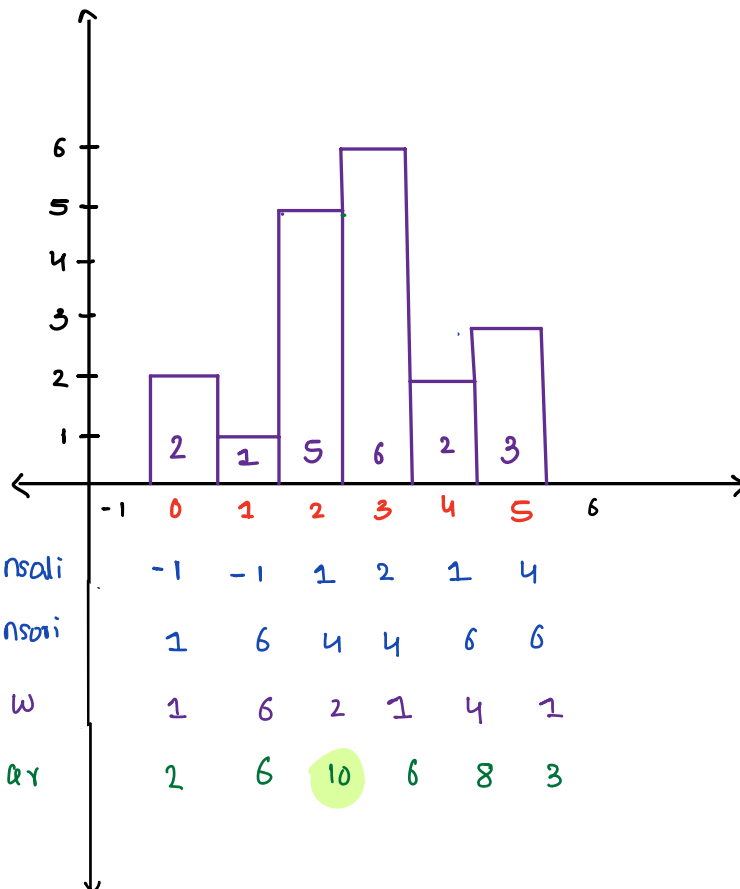
$A = [2 \ 1 \ 3 \ 6 \ 2 \ 4]$



$$\text{ans} = 2 \times 4 = 8$$



i	h	w	ans
0	2	1	2
1	1	6	6
2	5	2	10
3	6	1	6
4	2	4	8
5	3	1	3



$$w = nsr[i] - nsl[i] - 1$$

$$ar = w * A[i]$$

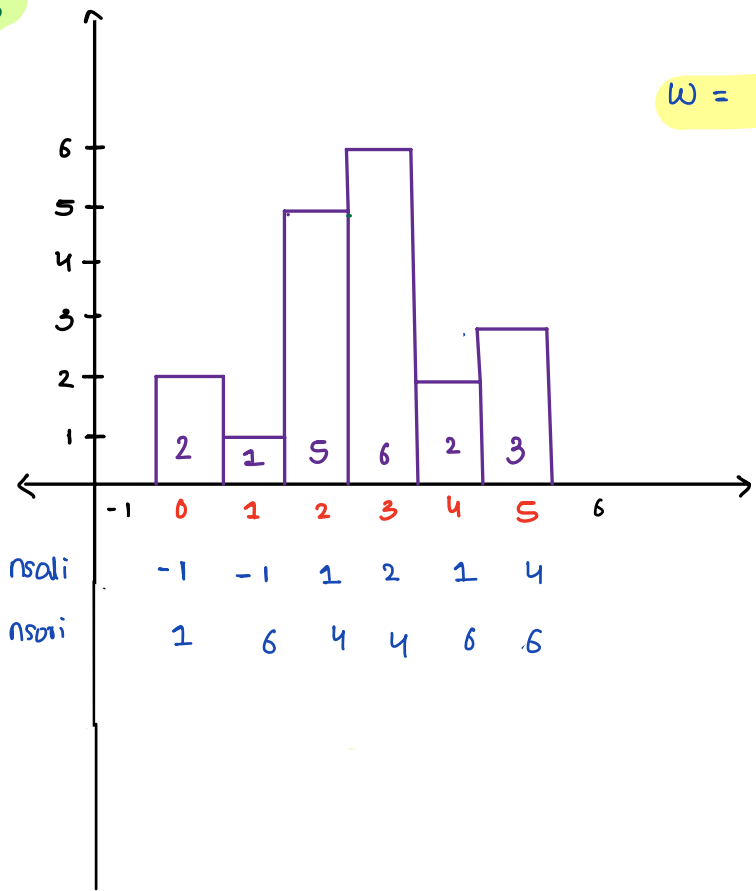
$$max = \text{Math.max}(ar, max)$$

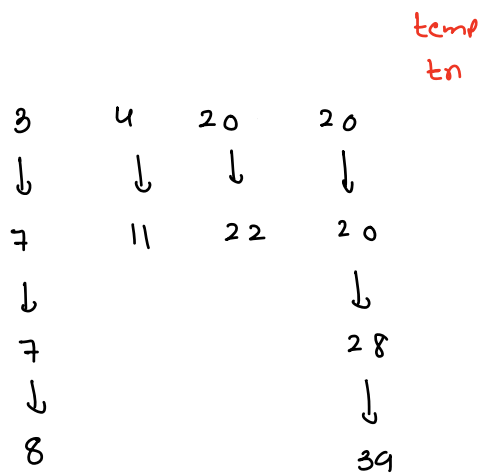
$$TC : O(n)$$

$$SC : O(n)$$

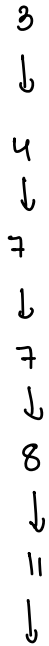
Doubts

$$W = n_{sorted} - n_{sorted} - 1$$





mh



20 → 20 → 20 → 22 → 28 → 39

```

ListNode {
    int val;
    ListNode next;
    ListNode down;
}

```

```

ListNode mh = null;
ListNode temp = head;
while (temp != null) {
    ListNode tn = temp.right;
    temp.next = null;
    mh = mergedTwoSortedLL(mh, temp);
    temp = tn;
}

```