Agenda

1) what is recursion
2) some basic questions

Importance

1) Trees and graphs
2) DP

Recursion : Function calling itself.

How to apply recursion

$$Sum(N) = 1+2+3+\dots+N$$

$$Sum(N-1) = 1+2+3+\dots+N-1$$

$$Sum(N) = Sum(N-1) + N$$

Solving the main problem using just smaller problem of same type.

3 magical steps to apply recursion

1) **Assumption** : what is the function doing.
2) **Main logic** : solving same problem using just smaller problem of same type (sub-problem)
3) **Base condition** : when to stop recursion.

Q.1 Given N, find sum of N natural numbers.

```
int sum(int N) {
    if(N==1) {
        return 1;
    }

    int temp = sum(N-1);
    return temp + N;
}

void main() {
    int N = scn.nextInt();
    sopln(sum(N));
}
```

Assumption: Given N, find sum of N natural no.

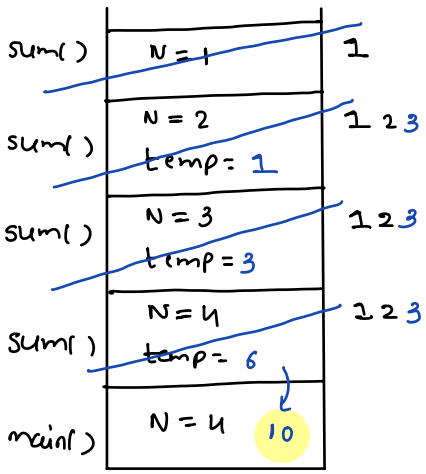
Main logic:

$$sum(N) = sum(N-1) + N$$

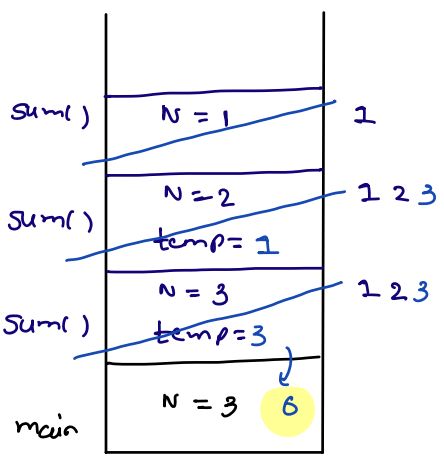
Base condition: Smallest problem whose answer is known.

if (n==1) → 1

```
int sum(int N) {
    if(N==1) {
1       return 1;
    }

2   int temp = sum(N-1);
3   return temp + N;
}

void main() {
    int N = scn.nextInt();
    sopln(sum(N));
}
```




```
int sum(int N) {
    if(N==1) {
1       return 1;
    }

2   int temp = sum(N-1);
3   return temp + N;
}

void main() {
    int N = scn.nextInt();
    sopln(sum(N));
}
```



Q. 2 Given N, find factorial of N.

```
int factorial (int N) {
    if (N == 0) {
        return 1;
    }
    int temp = factorial (N-1);
    return temp * N;
}
```

Assumption: Given N, find factorial of N.

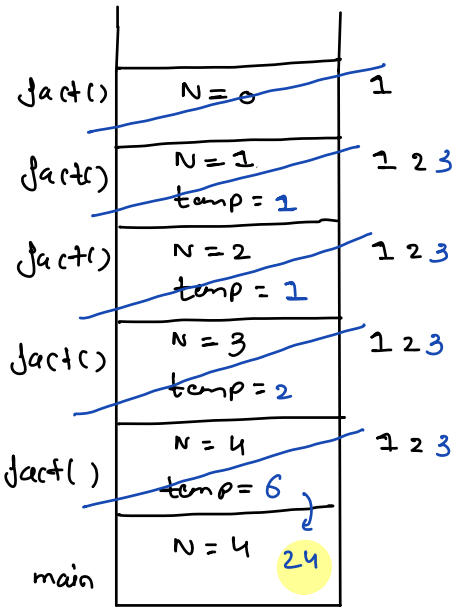
Main logic:

factorial (N) = factorial(N-1) * N

Base condition:

if (N == 0) → 1

```
int factorial (int N) {
    if (N == 0) {
1       return 1;
    }
2   int temp = factorial (N-1);
3   return temp * N;
}
```



Q-3 Given N, find N^{th} fibonacci number.

0	1	2	3	4	5	6	7	8 ....
0	1	1	2	3	5	8	13	21

```
int fib (int N) {
    if (N == 0 || N == 1) {
        return N;
    }
    int temp1 = fib(N-1);
    int temp2 = fib(N-2);
    return temp1 + temp2;
}
```

Assumption : Given N, find N^{th} fibonacci no.

Main logic :

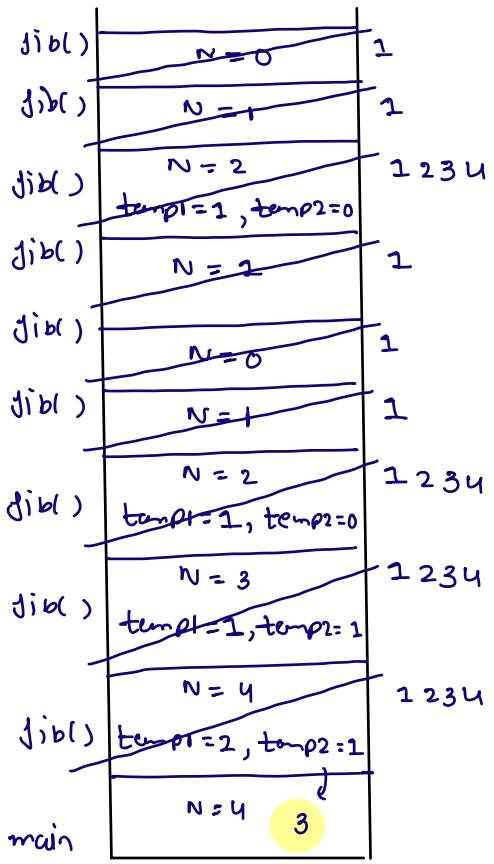
$fib(N) = fib(N-1) + fib(N-2)$

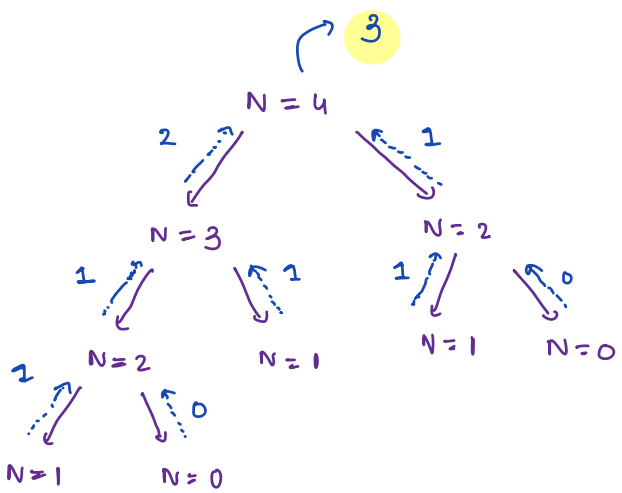
Base condition:

if (N == 0) → 0

if (N == 1) → 1

```
int fib (int N) {
    if (N == 0 || N == 1) {
1       return N;
    }
2   int temp1 = fib(N-1);
3   int temp2 = fib(N-2);
4   return temp1 + temp2;
}
```





Euler diagram
(cover it
in next
sessions)

Q.4 Given N, print increasing from 1 to N.

N = 5 , O/P : 1 2 3 4 5

N = 4 , O/P : 1 2 3 4

```
void Inc (int N) {
    if (N == 0) {
        return;
    }
    Inc (N-1);
    SOPln(N);
}
```

Assumption: Given N, print increasing 1 to N.

Main logic:

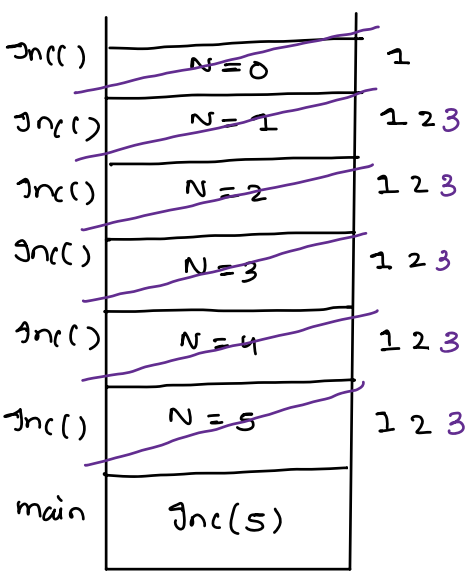
Inc(N) ⇒ Inc(N-1) + SOPln(N)

(Inc(N): 1 to N; Inc(N-1): 1 to N-1)

Base condition

if(N==0)

```
void Inc (int N) {
    if (N == 0) {
1       return;
    }
2   Inc (N-1);
3   SOPln(N);
}
```



O/P: 1 2 3 4 5

```
void fun(int N) {
    if (N == 0) {
        return;
    }
    SOPln(N);
    fun(N-1);
}
```

do tracing yourself

Q.5 Given string, check if it is palindromic or not.

Str: bata ans = false

Str: abcba ans = true

ch(s) != ch(e)

return false

ch(s) == ch(e)

if string from s+1 to e-1 is palindromic or not.

question

```
boolean palindrome (string str) {
    return check (str, 0, str.length()-1);
}
```

helper

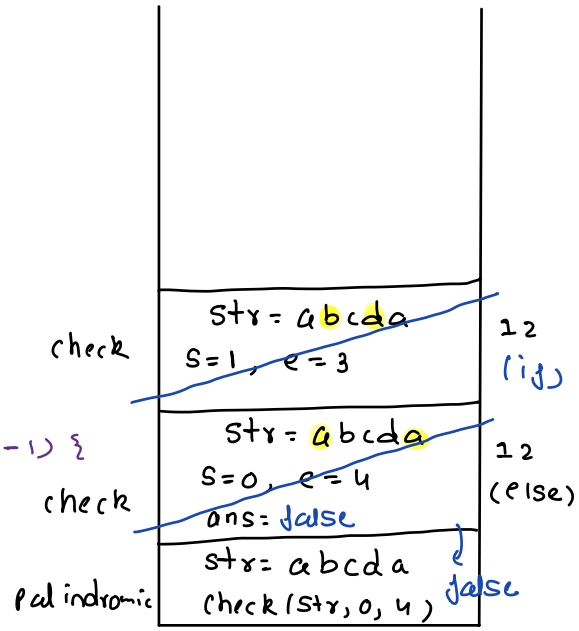
```
boolean check (string str, int s, int e) {
    if ( s==e || s>e) {
        return true;
    }
    if (str.charAt(s) != str.charAt(e)) {
        return false;
    }
    else {
        boolean ans = check (str, s+1, e-1) {
        return ans;
    }
}
```

a	b	c	b	a
0	1	2	3	4
		s		
		e		

a	b	b	a
0	1	2	3
	e	s	

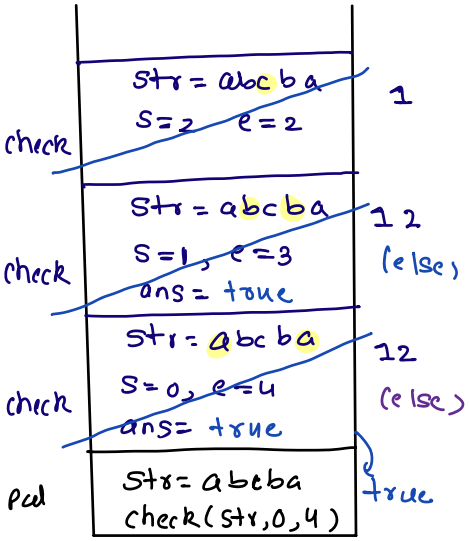
```
if ( s==e || s>e) {
    return true;
}
```

```
boolean check (string str, int s, int e) {
    if (s == e || s > e) {
1       return true;
    }
    if (str.charAt(s) != str.charAt(e)) {
        return false;
    }
2   else {
        boolean ans = check (str, s+1, e-1) {
        return ans;
    }
}
```



str: a b c d a
0 1 2 3 4

```
boolean check (string str, int s, int e) {
    if (s == e || s > e) {
1       return true;
    }
    if (str.charAt(s) != str.charAt(e)) {
        return false;
    }
2   else {
        boolean ans = check (str, s+1, e-1) {
        return ans;
    }
}
```



str: a b c b a
0 1 2 3 4

Doubts

longest consecutive sequence

A = 100 1 3 15 99 97 16 2 4 5 98

Cons. Seq: 1 2 3 4 5

97 98 99 100

15 16

ideal: using sorting

Arrays.sort(A); // nlogn

A = 1 2 3 4 5 15 16 97 98 99 100

5 2 4

A = 100 1 3 15 99 97 16 2 4 5 98

100 → ~~T~~ F
1 → T
3 → ~~T~~ F
15 → T
99 → ~~T~~ F
97 → T
16 → ~~T~~ F
2 → ~~T~~ F
4 → ~~T~~ F
5 → ~~T~~ F
98 → ~~T~~ F

HashMap

ele vs are you starting pt. of any sequence

i) In map put A[i] vs true

ii) put false infront of those A[i]'s which can't be start of your seq.

if A[i]-1 is present in map then A[i] can't be a sequence start.

(iii) to avel the map and try to create ans from real start points.

```
for( int sp : map.keySet() ) {
    if ( map.get(sp) == true ) {
        // sp is a correct starting point
        int len = 0;
        while (map.containsKey(sp+len)) {
            len++;
        }
        ans= Math.max(ans, len);
    }
}
```

O(n)

100 → ~~T~~ F

1 → T

3 → ~~T~~ F

15 → T

99 → ~~T~~ F

97 → T

16 → ~~T~~ F

2 → ~~T~~ F

4 → ~~T~~ F

5 → ~~T~~ F

98 → ~~T~~ F

ans = 5

sp = 15

len = 2

(15, 16)

sp = 97

len = 4

(97, 98, 99, 100)

sp = 1

len = 0 , 1+0 => T

len = 1, 1+1 => T

len = 2, 1+2 => T

len = 3, 1+3 => T

len = 4, 1+4 => T

len = 5, 1+5 => F

A = 2 3 4 1 5 7 10 8 9

2 → ~~T~~ F

3 → ~~T~~ F

4 → ~~T~~ F

1 → T

5 → ~~T~~ F

7 → ~~T~~ F

10 → ~~T~~ F

8 → ~~T~~ F

9 → ~~T~~ F

SP = 1

den = 10

ans = 10