

### Log-cosh loss:

log-cosh is the logarithm of hyperbolic cosine prediction error. It is smoother than  $L_2$ .

$$L(y, y_p) = \sum_{i=1}^n \log(\cosh(y_i p - y_i))$$



log cosh vs prediction

$$= (0-1.4)^2 \times 0.35 + (1-1.4)^2 \times 0.15$$

$$+ (2-1.4)^2 \times 0.15 + (3-1.4)^2 \times 0.15 + (4-1.4)^2 \times 0.1$$

$$\sigma^2 = 1.84$$

$$\sigma = 1.36$$

Business Moment - III

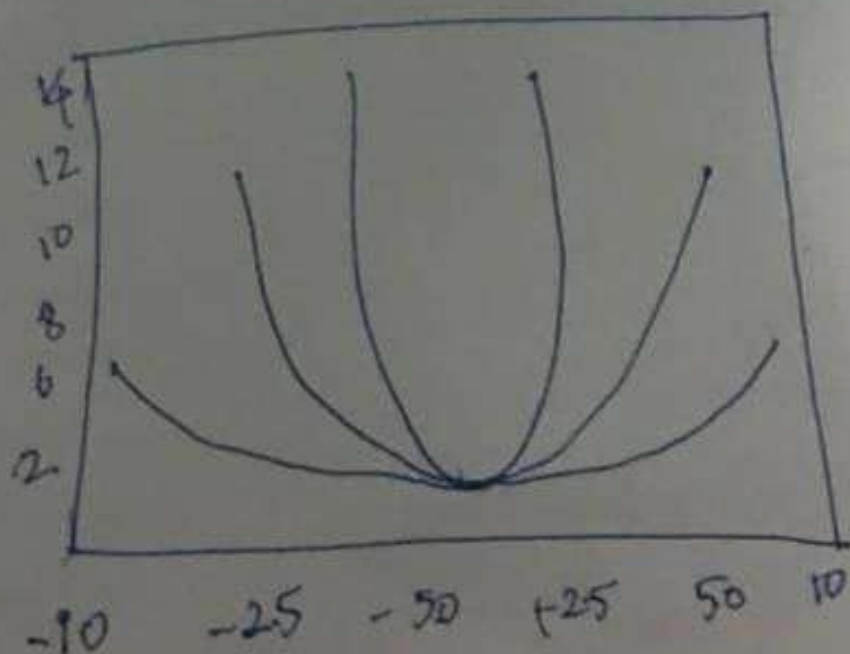
$$S_3 = \sum [(x_i - \mu_2) (\sigma)^3 P(x_i)]$$

$$= \left[ \left( \frac{0-1.4}{1.36} \right)^3 \cdot 0.35 \right] + \left[ \left( \frac{1-1.4}{1.36} \right)^3 \cdot 0.25 \right]$$

$$+ \left[ \left( \frac{2-1.4}{1.36} \right)^3 \cdot 0.15 \right] + \left[ \left( \frac{3-1.4}{1.36} \right)^3 \cdot 0.15 \right]$$

$$+ \left[ \left( \frac{4-1.4}{1.36} \right)^3 \cdot 0.1 \right]$$

$$= 0.568$$



Business Moment - IV:

$$K = \sum \left[ \left( \frac{x_i - \mu_x}{\sigma} \right)^4 \cdot P(x) - 3 \right]$$

$$= \left[ \left( \frac{0 - 1.4}{1.36} \right)^4 \cdot 0.35 \right] + \left[ \left( \frac{1 - 1.4}{1.36} \right)^4 \cdot 0.25 \right]$$

$$+ \left[ \left( \frac{2 - 1.4}{1.36} \right)^4 \cdot 0.15 \right] + \left[ \left( \frac{3 - 1.4}{1.36} \right)^4 \cdot 0.15 \right]$$

$$+ \left[ \left( \frac{4 - 1.4}{1.36} \right)^4 \cdot 0.1 \right] - 3$$

$$K = -0.9762$$

ML & AL Week 2  
Challenge

1.  $x$  Random Variable = No of terms

$P(x)$  = Probability of  $x$

$x$	$P(x)$
0	0.35
1	0.25
2	0.15
3	0.15
4	0.10

Business Moment - I

Central Tendency (Mean)

$$M = \sum (x_i) P(x)$$

$$= [(0 \times 0.35) + (1 \times 0.25) + (2 \times 0.15) \\ + (3 \times 0.15) + (4 \times 0.10)]$$

$$= 0 + 0.25 + 0.30 + 0.45 + 0.4$$

$$M = 1.4$$

Business Moment - II.

Measure of Dispersion Variance

$$= \sum (x_i - \mu_x)^2 \cdot P(x)$$