

**Multi-agent cooperation on edge with Spiking Neural Network  
and reinforcement learning**

by

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# Abstract

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# Chapter 1

## Spiking Neural Networks: Models and Learning Algorithms

### 1.1 Neuron model –

The neuron model in this paper is the Leaky Integrate-and-Fire (LIF). The LIF model is a biological model that can be represented as a circuit with a resistor and capacitor and represents a first-order dynamic system [1],

$$R_m C_m \frac{dV_m(t)}{dt} = E_l - V_m(t) + R_m I(t) \quad (1.1)$$

where  $V_m(t)$  is the neuron's membrane potential,  $R_m$  is the membrane resistance,  $C_m$  is the membrane capacitance,  $E_l$  is the resting potential, and  $I(t)$  is the input current. The neuron spikes when its potential reaches the threshold potential ( $V_{th}$ ). The potential of the neuron immediately reaches the reset potential ( $V_{res}$ ) after it spikes.

The spike rate is a parameter that determines how fast the neuron spikes [2].

$$r_{[Hz]} = \frac{1}{t_{isi} [s]} \quad (1.2)$$

where  $t_{isi}$  is the inter-spike interval that can be calculated using the neuron model. When

the potential of a neuron reaches the threshold potential, it fires. Therefore, based on the analytical solution of (1.1), the inter-spike interval time can be written as,

$$t_{isi} = \tau_m \ln \left( \frac{E_l + R_m I - V_{res}}{E_l + R_m I - V_{th}} \right) \quad (1.3)$$

where  $\tau_m$  is the membrane time constant.

According to (1.3), the following condition should be satisfied to have a finite value for  $t_{isi}$ ,

$$E_l + R_m I - V_{th} > 0 \quad (1.4)$$

or

$$I > \frac{V_{th} - E_l}{R_m} \quad (1.5)$$

which means that the input current higher than the above value generates spikes.

After calculating the minimum input for neurons, we must find the maximum input based on the inter-spike interval. Equation (1.3) can be written as,

$$t_{isi} = \tau_m \ln \left( 1 + \frac{V_{th} - V_{res}}{E_l + R_m I - V_{th}} \right) \quad (1.6)$$

Equation (1.6) can be approximated using the Maclaurin series for the natural logarithm function ( $\ln(1 + z) \approx z$ ) as follows,

$$t_{isi} = \frac{\tau_m (V_{th} - V_{res})}{E_l + R_m I - V_{th}} \quad (1.7)$$

Solving for  $I$ , an input current as a function of the inter-spike interval can be obtained,

$$I = \frac{\tau_m (V_{th} - V_{res})}{t_{isi} R_m} + \frac{V_{th} - E_l}{R_m} \quad (1.8)$$

The maximum value for the input current makes the neuron fire at each sample time ( $\Delta t$ ). Therefore, the maximum input current is,

$$I^{max} = \frac{\tau_m (V_{th} - V_{res})}{\Delta t R_m} + \frac{V_{th} - E_l}{R_m} \quad (1.9)$$

In this section, we obtained the minimum and maximum values for input current using (1.5) and (1.9). These equations are used in the learning and encoding processes of the SNN.

# Chapter 2

## Literature review

During the past years, researchers have focused on quadrotor-type UAVs because of their ability to hover, take off vertically, and land in places that conventional fixed-wing aircraft cannot. They can accomplish a wide range of long-distance missions at low costs [3]. Several linear and nonlinear control algorithms have been developed, and the most common approach is hierarchical control that involves an inner and outer loop [4].

In the linear PID controller, one can design the controller feedback gains based on the linear model to achieve desired performance [5][6]. The Linear-Quadratic Regulator (LQR) has demonstrated acceptable results [7], but finding the required control parameters (weight matrices) is a challenging problem.

The  $H_\infty$  approach is widely used [8] for cases with unmodeled dynamics since it eliminates the errors in modelling. However, adjusting the controller parameters is a difficult task that makes the implementation complex to some degree in comparison with the PID and LQR [9].

The quadrotor's control process is a rather complex task because of the nonlinearities and uncertainties (e.g., the moment of inertia of rotors and aerodynamic effects). Sliding Mode Control (SMC) can be used for the flight condition with time-varying disturbances [10] since it quickly compensates for external disturbances and eliminates the effect of uncertainties in modelling [11]. However, chattering and finite-time convergence are always a problem [12].

The backstepping control approach breaks the control law into parts. The control laws are derived using a suitable Lyapunov function [13] to compensate for the problems that exist in the underactuated systems. Although an optimization process can be done to find the optimal gains, it would lead to a time-consuming task if it is done for every drone with different dynamic parameters [14].

All the above-mentioned control algorithms have been developed, considering there is no time delay in the control loop. Drone control in Beyond-Visual-Line-Of-Sight (BVLOS) suffers from many problems caused by random network delays and packet losses [15][16]. Time delay in the feedback loop can make the control system unstable [17].

Control approaches based on the Lyapunov function usually incorporate the time delay into the candidate function [18]. Another approach to compensate for the delay is the Smith predictor, which improves the quadrotors tracking performance by reducing the destabilizing effect of time delay [19]. However, it does not provide any information about the current state of the plant for the remote control station.

In [20], a predictor-based control approach is developed for quadrotor control. The delay was assumed to be constant, and the states of the system were predicted using a discrete-time predictor. A virtual quadrotor model worked in parallel with the actual setup was used to simulate the remote system [21].

Traditional techniques define a model for the time delay or consider it a constant value [22] [23]. Estimating time delay with Machine Learning (ML) algorithms requires high computation capability and sufficient training data, which is unavailable at the beginning of the quadrotor flight [24] [25].

Although previous studies have tried to compensate for time delay by predicting the drone's future states, in the case of 5G networks, the quadrotor's current states should be accessible for the base station to guarantee high communication bandwidth using better beamforming.

Spiking Neural Networks (SNNs) are the third generation of neural networks that have gained attention for their lower power consumption due to their event-driven nature and

sparse representation of data, which is based on real biological neurons [26–28]. The SNNs work based on spikes. Since the spikes are not continuous, only a part of the network is active at a given time. Also, successful hardware implementation of SNNs on neuromorphic chips like TrueNorth [29] and Loihi [30] makes them good candidates for robotic applications.

Studies have shown that the SNN can learn particular tasks autonomously to control robotic platforms. In [31], a Reward Modulated Spike-Timing-Dependent Plasticity (R-STDP) algorithm is used to control a mobile robot. Different States of the mobile robot (e.g., acceleration and deceleration) are defined as different frequencies for the input sensory layer. The SNN learns to navigate autonomously in the environment while avoiding obstacles.

There are several successful implementations of SNNs in learning nonlinear dynamics. In [32], a chaotic reservoir of spiking neurons is trained to control a robotic arm adaptively. The network is able to follow the desired trajectory with few neurons. SNN’s capability in controlling a robotic arm with three degrees of freedom is also studied in [33], where the SNN has 218 neurons. The results are compared with real behavioural and neural data. The results showed that the SNN can adapt the Jacobian matrix when dynamic properties are changed over time.

In [34], an SNN is trained using the R-STDP algorithm and lateral inhibition mechanism to control a mobile robot in an environment with an obstacle. The lateral inhibition helps SNNs switch between target tracking and obstacle avoidance tasks during and after learning. The results showed that the SNNs have the potential to take control in complex scenarios.

In [35], a method based on the reinforcement learning algorithm is proposed to help an invader minimize its distance from a territory before being captured. In [36], an interceptor is used to defend a target from an attacking intruder. This type of differential game is addressed as Defending an Asset, which is solved using Linear Quadratic formulation. In [37], the problem is solved for multi-player cases but split into two simple two-player games.

Multiple attackers-defenders problems with a stationary target are studied in [38]. However, a simple single attacker-single defender case is solved because of the complexity of the numerical solution. Several studies have tried to propose optimal solutions for the ATD

problem. A set of optimal solutions are proposed in [39] considering reduced State space conditions. Using the geometric method, the attacker played an optimal strategy, capturing the target while maximizing its distance from the defender.

# Chapter 3

## Comparison of Cellular Network Controllers for Quadrotors Experiencing Time Delay

### 3.1 Proposed method

In this chapter, a comparative analysis is performed to investigate the performance of linear and nonlinear controllers in quadrotor control operating using cellular or 5G networks. The controller is run on the Ground Control Station for the following reasons:

- *Integrated control system*: The controller uses information provided by the delay estimator and state estimator. All these parts should be run as an integrated system on the Ground Control Station to avoid the interconnection delay among the controller, state estimator, and delay estimator.
- *Low computation time*: Running complex control systems needs high computation capability that the servers can provide on the Ground Control Station.
- *Beamforming*: The beamforming technology needs the user's current position to find the most efficient data delivery route. In the studied control framework, the Ground

Control Station provides the drone's position to the base station.

- *Path planning:* The controller executes the commands that are provided by a path planning algorithm. The proposed framework reduces the transmission delay between the path planning algorithm and the control system.

Fig. 3.1 shows the control framework. The controller sends control commands  $U(t)$  to the quadrotor using the cellular networks. The quadrotor receives control commands and sends back position and orientation  $S(t)$ . The recorded delay history is used for time delay estimation ( $\hat{\tau}_B$ ).

The state estimator estimates the quadrotors current position and orientation  $\hat{S}(t)$  using delay information, control commands, and received data from the quadrotor.

The paper is organized as follows. Section II presents the dynamic model of the quadrotor, and section III provides details about the controllers. Section III is composed of two parts: (a) Linear PD and (b) Backstepping controllers. Section IV discusses the state estimation process based on the dynamic model. Section V presents the delay estimation process, section VI gives details about the numerical simulations and the results, and section VII summarizes the paper.

## 3.2 Quadrotor dynamic model

In this section, the dynamic model of the quadrotor is presented. The quadrotor is a six Degree-of-Freedom (DOF) system controlled by four motors, as shown in Fig. 3.2. It is an underactuated system that makes the control process a challenging task.

An inertial  $\{O_I, x, y, z\}$  and a body-fixed  $\{O_B, x_b, y_b, z_b\}$  reference frame are used to define the rotational and transitional motions [40]. According to rigid body dynamics, the rotational motion can be represented as,

$$\ddot{\phi} = \frac{(I_y - I_z)}{I_x} \dot{\theta} \dot{\psi} + \frac{l}{I_x} U_2 \quad (3.1)$$

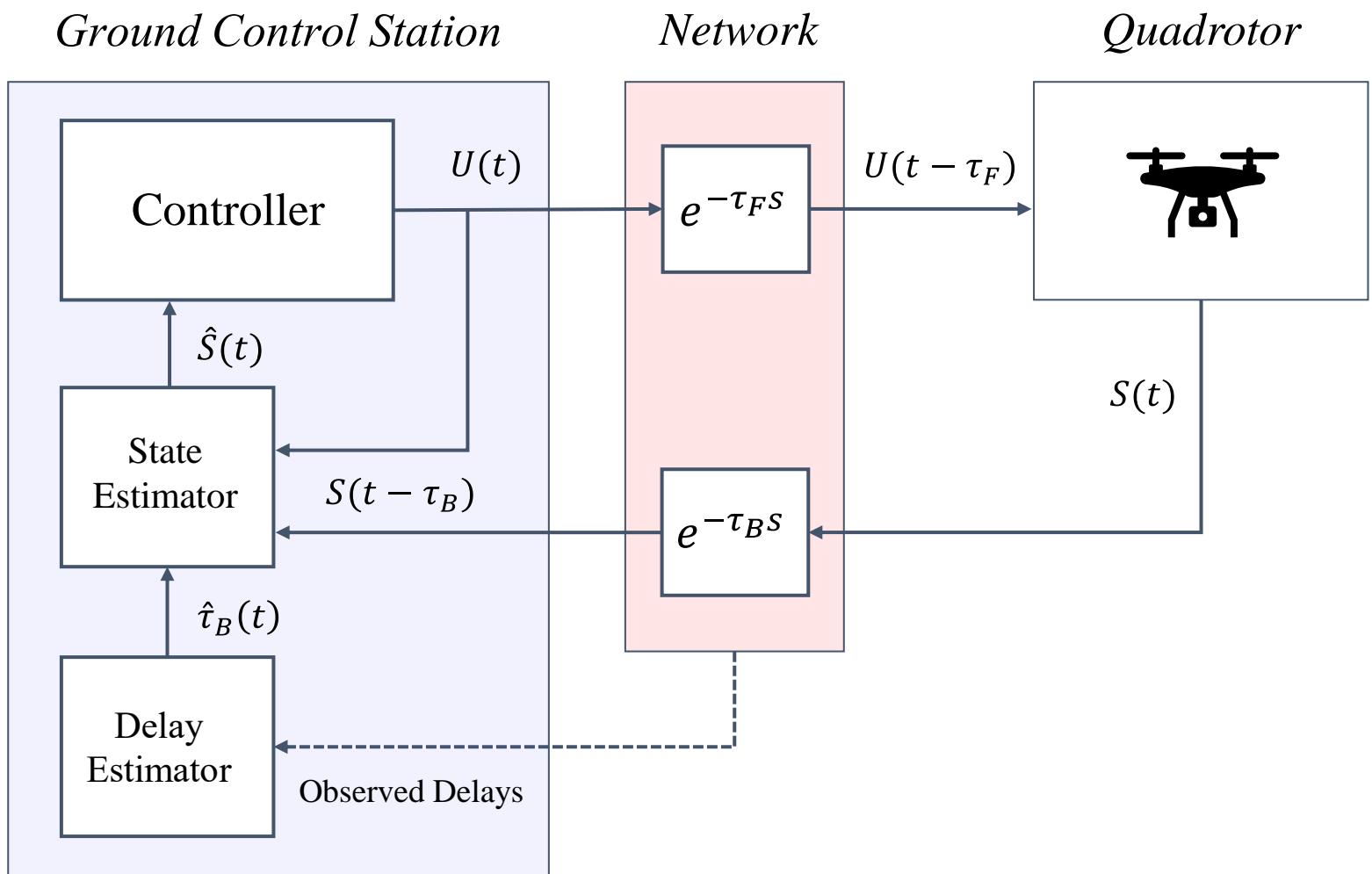


Figure 3.1: Control framework for quadrotor control using cellular networks

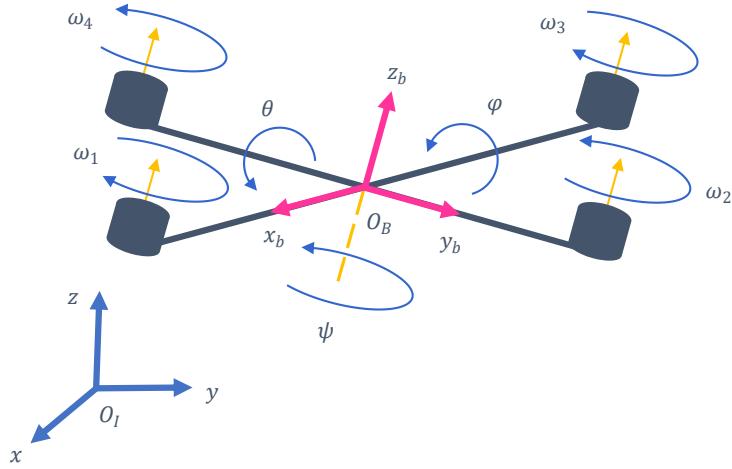


Figure 3.2: Quadrotor's dynamic model

$$\ddot{\theta} = \frac{(I_z - I_x)}{I_y} \dot{\phi} \dot{\psi} + \frac{l}{I_y} U_3 \quad (3.2)$$

$$\ddot{\psi} = \frac{(I_x - I_y)}{I_z} \dot{\theta} \dot{\phi} + \frac{l}{I_z} U_4 \quad (3.3)$$

where,  $\{\phi, \theta, \psi\}$  are the Euler angles (pitch, roll, and yaw),  $I_x$ ,  $I_y$ , and  $I_z$  are the moment of inertia along  $x$ ,  $y$ , and  $z$  axes, respectively. The  $U_i$ s are the control inputs, and  $l$  is the distance between the quadrotor's geometric center and the rotors.

The transitional motion in the inertial frame is given by,

$$\ddot{x} = (\cos \phi \sin \theta \cos \psi + \sin \phi \sin \psi) \frac{U_1}{m} \quad (3.4)$$

$$\ddot{y} = (\cos \phi \sin \theta \sin \psi - \sin \phi \cos \psi) \frac{U_1}{m} \quad (3.5)$$

$$\ddot{z} = -g + (\cos \phi \cos \theta) \frac{U_1}{m} \quad (3.6)$$

where,  $m$  is the mass, and  $g$  is the acceleration due to gravity. The generated force by the motors is considered to be proportional to the square of the angular velocities of the rotors.

Therefore, the control inputs can be represented as,

$$U_1 = b (\omega_1^2 + \omega_2^2 + \omega_3^2 + \omega_4^2) \quad (3.7)$$

$$U_2 = b (\omega_4^2 - \omega_2^2) \quad (3.8)$$

$$U_3 = b (\omega_3^2 - \omega_1^2) \quad (3.9)$$

$$U_4 = d (\omega_2^2 + \omega_4^2 - \omega_1^2 - \omega_3^2) \quad (3.10)$$

where,  $\omega_i$  is the angular velocity of the  $i$ th rotor, and  $b$  and  $d$  are constants.

### 3.3 Controller Design

#### 3.3.1 Linear PD Controller

The PID controller is a widely used linear controller and is defined as,

$$u(t) = K_p e(t) + K_i \int_0^t e(\tau) d\tau + K_d \frac{de(t)}{dt} \quad (3.11)$$

where,  $e(t)$  is the error between the desired state and the current state, and  $K_p$ ,  $K_i$ , and  $K_d$  are PID gains. In this paper, a PD controller is designed to control the rotational and transitional motions. The controller is designed based on the linearized model of the quadrotor.

To simplify the linearization of the system, we assume that the yaw angle is held constant at zero, and as such, the motion along the  $x$ -axis is controlled only by the pitch angle  $\theta$ , and the motion along the  $y$ -axis is controlled only by the roll angle  $\phi$ . We linearized the dynamics for our PD controller design by assuming that the roll and pitch angles are small, which is a reasonable assumption since quadrotors rarely rotate more than 30 degrees during

flight. Also, the angular accelerations of roll and pitch are equal to the torque about the appropriate axis, as such, we write the linear dynamics as  $\ddot{\phi} = T_x/I_{xx}$  and  $\ddot{\theta} = T_y/I_{yy}$ , where  $T_x$  and  $T_y$  are the torques about the  $x$  and  $y$ -axis.

There are two control loops: inner and outer loop. The outer loop controls the desired pitch and roll angles. Since the motions along  $x$  and  $y$  axes depend on the rotation along  $\phi$  and  $\theta$ , the outer loop uses the current position in  $x$  and  $y$  and desired positions to calculate the desired rotations along  $x$  and  $y$  axes as follows [41],

$$\theta_d = K_p(x - x_d) + K_d(\dot{x} - \dot{x}_d) \quad (3.12)$$

$$\phi_d = K_p(y - y_d) + K_d(\dot{y} - \dot{y}_d) \quad (3.13)$$

where,  $\phi_d$  and  $\theta_d$  are desired pitch and roll angles, and  $x_d$  and  $y_d$  are desired positions on  $x$  and  $y$  directions. The  $K_p$  and  $K_d$  control the pitch and roll angles. The inner loop controls the quadrotor's rotation along the  $x$  and  $y$  axes.

According to the PD control law, the control signals can be represented as [42],

$$U_1 = mg + K_{zp}(z_d - z) + K_{zd}(\dot{z}_d - \dot{z}) \quad (3.14)$$

$$U_2 = K_{lp}(\phi_d - \phi) + K_{ld}(\dot{\phi}_d - \dot{\phi}) \quad (3.15)$$

$$U_3 = K_{mp}(\theta_d - \theta) + K_{md}(\dot{\theta}_d - \dot{\theta}) \quad (3.16)$$

$$U_4 = K_{np}(\psi_d - \psi) + K_{nd}(\dot{\psi}_d - \dot{\psi}) \quad (3.17)$$

where,  $K_{zp}$ ,  $K_{zd}$ ,  $K_{lp}$ ,  $K_{ld}$ ,  $K_{mp}$ ,  $K_{md}$ ,  $K_{np}$ , and  $K_{nd}$  are PD gains for the inner loop. The  $z_d$  is the desired position along the  $z$ -axis, and  $\psi_d$  is the desired yaw angle.

The linearized PD controller can be designed based on the second-order dynamic model,

where the bandwidth and damping ratio of the controller are adjustable. Therefore, gains can be calculated based on the inner and outer loop bandwidth.

### 3.3.2 Backstepping Controller

In this section, a nonlinear backstepping control law is designed to be compared with the linear PD controller. As mentioned before, the backstepping controller breaks the control law into several subsystems [43]. There are three subsystems consisting of the altitude ( $z$ ), heading ( $\psi$ ), and horizontal subsystems. The general Lyapunov function for every subsystem based on error variables is defined as [22],

$$V_i = \frac{1}{2}\eta_i^2 \quad (3.18)$$

where,  $\eta_i$  is the error variable for the  $i$ th subsystem.

We define error variables for the  $z$  subsystem as  $\eta_1 = z - z_d$ ,  $\eta_2 = \dot{z} - c_1\eta_1 - \dot{z}_d$ . Then, the control law for altitude control becomes:

$$U_1 = \frac{m}{\cos\phi\cos\theta}(g - \eta_1 - c_2\eta_2 - c_1\dot{z} + c_1\dot{z}_d + \ddot{z}_d) \quad (3.19)$$

where,  $c_1$  and  $c_2$  are constant values that control how fast the quadrotor responds to the input commands in the  $z$ -direction.

For the  $\phi$  subsystem, the error variables are  $\eta_9 = \phi - \phi_d$  and  $\eta_{10} = \dot{\phi} - c_9\eta_9 - \dot{\phi}_d$ . Therefore, the control law is given by:

$$U_2 = \frac{I_x}{l} \left( -\alpha\dot{\theta}\dot{\psi} - c_9\dot{\phi} + c_9\dot{\phi}_d - \eta_9 - c_{10}\eta_{10} + \ddot{\phi}_d \right) \quad (3.20)$$

where,  $\alpha = \frac{I_y - I_z}{I_x}$ , and  $c_9$  and  $c_{10}$  are the constant values that control the response time of the  $\phi$  subsystem [44].

For the  $\theta$  subsystem, the error variables are  $\eta_{11} = \theta - \theta_d$  and  $\eta_{12} = \dot{\theta} - c_{11}\eta_{11} - \dot{\theta}_d$ . Then, the control law for the  $\theta$  subsystem becomes,

$$U_3 = \frac{I_y}{l} \left( -\beta \dot{\phi} \dot{\psi} - c_{11} \dot{\theta} + c_{11} \dot{\theta}_d - \eta_{11} - c_{12} \eta_{12} + \ddot{\theta}_d \right) \quad (3.21)$$

In the above equation, the  $\beta = \frac{I_z - I_x}{I_y}$ , and  $c_{11}$  and  $c_{12}$  are the constant values that control the response time of the  $\theta$  subsystem.

The error variables for the  $\psi$  subsystem are  $\eta_3 = \psi - \psi_d$  and  $\eta_4 = \dot{\psi} - c_3 \eta_3 - \dot{\psi}_d$ . The control law is given by:

$$U_4 = I_z \left( -\gamma \dot{\phi} \dot{\theta} - c_3 \dot{\psi} + c_3 \dot{\psi}_d - \eta_3 - c_4 \eta_4 + \ddot{\psi}_d \right) \quad (3.22)$$

where,  $\gamma = \frac{I_x - I_y}{I_z}$ , and  $c_3$  and  $c_4$  control the response time of the  $\psi$  subsystem.

Since the dynamic model is underactuated and the  $U_1$  is incorporated in  $x$  and  $y$  subsystems, the virtual control signals in  $x$  and  $y$  directions can be calculated based on the mentioned Lyapunov function as follows,

$$u_y = \frac{m}{U_1} (-c_5 \dot{y} + c_5 \dot{y}_d + \ddot{y}_d - c_6 \eta_6 - \eta_5) \quad (3.23)$$

$$u_x = \frac{m}{U_1} (-c_7 \dot{x} + c_7 \dot{x}_d + \ddot{x}_d - c_8 \eta_8 - \eta_7) \quad (3.24)$$

where,  $c_5$  to  $c_7$  are constant coefficients,  $\eta_5 = y - y_d$ ,  $\eta_6 = \dot{y} + c_5 \eta_5 - \dot{y}_d$ ,  $\eta_7 = x - x_d$ , and  $\eta_8 = \dot{x} + c_7 \eta_7 - \dot{x}_d$  are error values for position and velocity.

The desired roll and pitch angles considering yaw angle are  $\phi_d = \sin^{-1}[v(2)]$  and  $\theta_d = \sin^{-1} \left[ \frac{v(1)}{\cos \phi_d} \right]$  where,

$$v = \begin{bmatrix} \cos \psi & \sin \psi \\ \sin \psi & -\cos \psi \end{bmatrix}^{-1} \begin{bmatrix} u_x & u_y \end{bmatrix}^T \quad (3.25)$$

The  $v$  is designed to find the desired orientation along the  $x$  and  $y$  axes that make the quadrotor follow the desired position, velocity, and acceleration in the horizontal subsystem.

## 3.4 State Estimator

Practical networked control systems with feedback loops are prone to face anomalies due to communication imperfections such as time delay. The feedback loop provides information about the plant's current states, and the controller calculates the new commands based on the received information.

When the system experiences a time delay, the controller may become unstable. In order to design a suitable control system, one should use a state estimator that estimates the current states based on the received data from the plant. In this section, the state estimator is given as follows,

$$\dot{\hat{\phi}} = \bar{q}_\phi - k_1 (\hat{\phi}(t - \hat{\tau}_B) - \phi(t - \tau_B)) \quad (3.26)$$

$$\dot{\bar{q}}_\phi = \left( \frac{I_y - I_z}{I_x} \right) \bar{q}_\theta \bar{q}_\psi + \frac{U_2(t)}{I_x} - k_2 (\bar{q}_\phi(t - \hat{\tau}_B) - q_\phi(t - \tau_B)) \quad (3.27)$$

$$\dot{\hat{\theta}} = \bar{q}_\theta - k_3 (\hat{\theta}(t - \hat{\tau}_B) - \theta(t - \tau_B)) \quad (3.28)$$

$$\dot{\bar{q}}_\theta = \left( \frac{I_z - I_x}{I_y} \right) \bar{q}_\phi \bar{q}_\psi + \frac{U_3(t)}{I_y} - k_4 (\bar{q}_\theta(t - \hat{\tau}_B) - q_\theta(t - \tau_B)) \quad (3.29)$$

$$\dot{\hat{\psi}} = \bar{q}_\psi - k_5 (\hat{\psi}(t - \hat{\tau}_B) - \psi(t - \tau_B)) \quad (3.30)$$

$$\dot{\bar{q}}_\psi = \left( \frac{I_x - I_y}{I_z} \right) \bar{q}_\phi \bar{q}_\theta + \frac{U_4(t)}{I_z} - k_6 (\bar{q}_\psi(t - \hat{\tau}_B) - q_\psi(t - \tau_B)) \quad (3.31)$$

$$\dot{\hat{x}} = \bar{q}_x - k_7 (\hat{x}(t - \hat{\tau}_B) - x(t - \tau_B)) \quad (3.32)$$

$$\dot{\bar{q}}_x = \left( \cos \hat{\phi} \sin \hat{\theta} \cos \hat{\psi} + \sin \hat{\phi} \sin \hat{\psi} \right) \frac{U_1(t)}{m} - k_8 (\bar{q}_x(t - \hat{\tau}_B) - q_x(t - \tau_B)) \quad (3.33)$$

$$\dot{\bar{y}} = \bar{q}_y - k_9 (\hat{y}(t - \hat{\tau}_B) - y(t - \tau_B)) \quad (3.34)$$

$$\dot{\bar{q}}_y = \left( \cos \hat{\phi} \sin \hat{\theta} \sin \hat{\psi} - \sin \hat{\phi} \cos \hat{\psi} \right) \frac{U_1(t)}{m} - k_{10} (\bar{q}_y(t - \hat{\tau}_B) - q_y(t - \tau_B)) \quad (3.35)$$

$$\dot{\bar{z}} = \bar{q}_z - k_{11} (\hat{z}(t - \hat{\tau}_B) - z(t - \tau_B)) \quad (3.36)$$

$$\dot{\bar{q}}_z = -g + \left( \cos \hat{\phi} \cos \hat{\theta} \right) \frac{U_1(t)}{m} - k_{12} (\bar{q}_z(t - \hat{\tau}_B) - q_z(t - \tau_B)) \quad (3.37)$$

According to (3.26) to (3.37), the state estimation is based on the quadrotor's dynamic model and the control signal. Therefore, we need to run the controller on the GCS to have access to control signals for state estimation. As mentioned before, the state estimation results are necessary information for beamforming. The Due to space restrictions, details are left to the reader [22]. In (3.26) to (3.37), the  $\tau_B$  and  $\hat{\tau}_B$  are the true and estimated backward delays (the backward and forward delays are assumed to be equal). The  $k_i$ s are the estimator gains, and  $\hat{\phi}$ ,  $\hat{\theta}$ ,  $\hat{\psi}$ ,  $\hat{x}$ ,  $\hat{y}$ , and  $\hat{z}$  are the estimated orientations and positions.

## 3.5 Delay Estimator

Network load, node competition, and congestion affect the communication quality. Therefore, considering the network delay as a constant parameter is not a proper assumption. Whenever a packet is sent over the network, the network state changes. Since the delay distribution follows the Markov model [45], Markov-based models are suitable for delay es-

timation.

In this paper, the delay is assumed to be a discrete-time, discrete-space stochastic process. In order to simulate the network delays during simulation, a fixed predefined transition matrix can be used as follows,

$$p_{ij}(n) = P(\tau_{n+1} = j | \tau_n = i) \quad (3.38)$$

where,  $\tau_n$  and  $\tau_{n+1}$  are current and next time delays, respectively, and the  $i$  and  $j$  are indices corresponding with the time delays. The delays estimator algorithm aims to find the true transition probabilities.

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**Algorithm 1** Time delay estimation using Markov model

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```

1: input  $D_{1 \times \lambda}$ , delay values
2: input  $M_{\lambda \times \lambda}$ , auxiliary matrix
3: input  $\hat{p}_{\lambda \times \lambda}$ , estimated probability matrix
4: for  $n = 1$  to simulation time do
5:   read  $\tau(n - 1)$ 
6:    $i \leftarrow$  index of  $\tau(n - 1)$  in  $D$ 
7:    $j \leftarrow$  index of  $\tau(n - 2)$  in  $D$ 
8:    $M[j, i] \leftarrow M[j, i] + 1$ 
9:   for  $r = 1$  to  $\lambda$  do
10:     $\hat{p}[r, 1 : \lambda] \leftarrow$  Normalize  $r^{th}$  row of the  $M$ 
11:   end for
12:    $ind \leftarrow$  find the index of  $\max(\hat{p}[i, 1 : \lambda])$ 
13:    $\hat{\tau}[n] \leftarrow D[1, ind]$ 
14:    $DEE(n - 1) \leftarrow \sqrt{\frac{\sum_{i=0}^{n-1} (\tau(n-1) - \hat{\tau}(n-1))^2}{n-1}}$ 
15: end for

```

---

The delays are generated based on the fixed predefined transition matrix  $p$ . Delay values are assumed to be known ( $D = \tau_1, \tau_2, \dots, \tau_\lambda$ ), but we do not know which one will happen in the current time step. Therefore, the challenge is to find the transition probabilities matrix  $p$ . The delay estimator gets the previous delay  $\tau(n - 1)$  as the initial value and calculates the transition probabilities matrix using the observed delays' history. Finally, the Delay Estimation Error (DEE) is calculated based on the delay history.

Table 3.1: Gains used in PD and backstepping controllers

	Coefficient	Value	Coefficient	Value
PD	$K_p$	2.5	$K_d$	1
	$K_{lp}$	20.09	$K_{ld}$	0.574
	$K_{mp}$	20.09	$K_{md}$	0.574
	$K_{np}$	43.12	$K_{nd}$	1.232
	$K_{zp}$	2293.2	$K_{zd}$	65.52
Backstepping	$c_1$	20	$c_2$	25
	$c_3$	3	$c_4$	6
	$c_5$	3	$c_6$	6
	$c_7$	3	$c_8$	6
	$c_9$	15	$c_{10}$	30
	$c_{11}$	15	$c_{12}$	30

## 3.6 Results

The performance of the controllers was evaluated using a numerical simulation. The simulation was done in MATLAB R2021 and the total simulation time was 10 seconds with 0.001 second sampling time. The initial condition for orientation, angular velocities, position, and velocities were taken to be  $\mathbf{0}_{12 \times 1}$ . The desired positions in the  $x$ ,  $y$ , and  $z$  directions were 10, 20, and 30  $m$ .

The PD controller was designed using the linearized model of quadrotor dynamics. The gains were calculated using the second-order system model, and the bandwidth for inner and outer loops were 70 rad/s and 5 rad/s, respectively. High bandwidths for controllers can be used because of the small delay values in the 5G network. The  $c_i$ s in the backstepping controller were tuned so that the response time of the controllers are approximately equivalent. The control gains are shown in Table 3.1.

The nonlinear quadrotor model was used for the simulation. The dynamic parameters and state estimator coefficients are shown in Table 3.2.

In order to simulate the delay in the 5G network, a model based on the Markov chain was used to generate delays using the transition matrix. The transition probabilities were

Table 3.2: Quadrotor specifications and state estimator constants

Parameter	Value	Unit
$m$	0.468	$kg$
$I_x$	0.0041	$kg.m^2$
$I_y$	0.0041	$kg.m^2$
$I_z$	0.0088	$kg.m^2$
$l$	0.225	$m$
$k_i \{i \text{ even}\}$	4	-
$k_i \{i \text{ odd}\}$	8	-

set randomly, and the delay values were changed to evaluate the effect of the delay changes on controllers. There were four delays in the experiment  $D = \{6, 7, 9, 10\} \text{ ms}$  with random probabilities. The delay estimator calculated the transition matrix and estimated the time delay based on the maximum probability.

**Exact knowledge of delay** In this case, the delay values and their probabilities were known. Fig. 3.3 shows the state estimator error in estimating the current states in  $x$ ,  $y$ , and  $z$  directions. After three seconds, the state estimator has converged to zero.

Fig. 3.4 shows the control signals calculated on the Ground Control Station according to the estimated quadrotor states. The control signal for both controllers are similar, and as it is shown in Fig. 3.3, the control framework that works based on the PD controller estimates the states similar to the state estimator that works based on the backstepping.

**Delay estimation based on the Markov model** In this case, delays were changed based on the predefined transition matrix. According to Fig. 3.5, the estimation error for the PD and backstepping controllers did not change significantly due to small delay values. The true and estimated transition probability matrices are shown in Table 3.3.

As illustrated in Fig. 3.6, even very small unknown delays affect controller performance. Because of the time delay in the system, tiny oscillations happen in the quadrotor's orientation. For example, since the bandwidth of the PD controller is relatively high (large gains

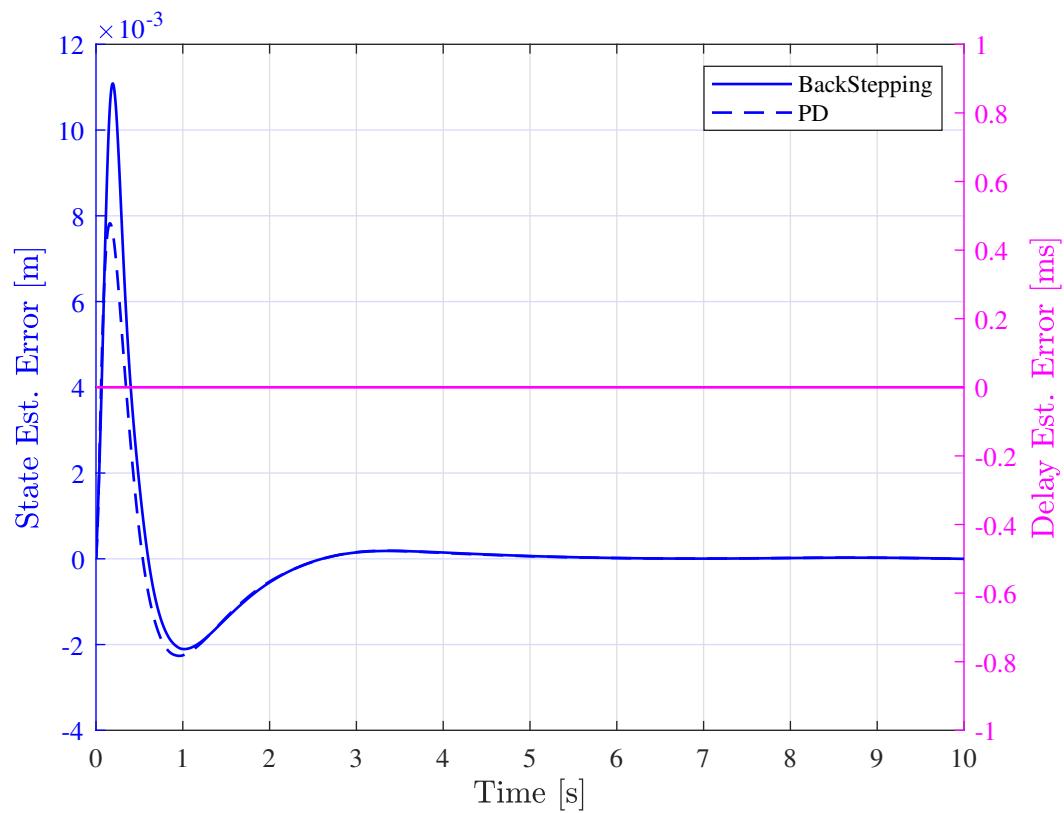


Figure 3.3: State estimation error with perfect delay estimator

Table 3.3: True and estimated transition probabilities

		6 ms	7 ms	9 ms	10 ms
6 ms	True	0.7736	0.0250	0.1643	0.0372
	Estimate	0.7631	0.0259	0.1705	0.0405
7 ms	True	0.0224	0.1972	0.0723	0.7080
	Estimate	0.0349	0.2170	0.0574	0.6908
9 ms	True	0.0360	0.1797	0.0310	0.7533
	Estimate	0.0333	0.1849	0.0258	0.7559
10 ms	True	0.2097	0.0075	0.0305	0.7523
	Estimate	0.2174	0.0072	0.0357	0.7397

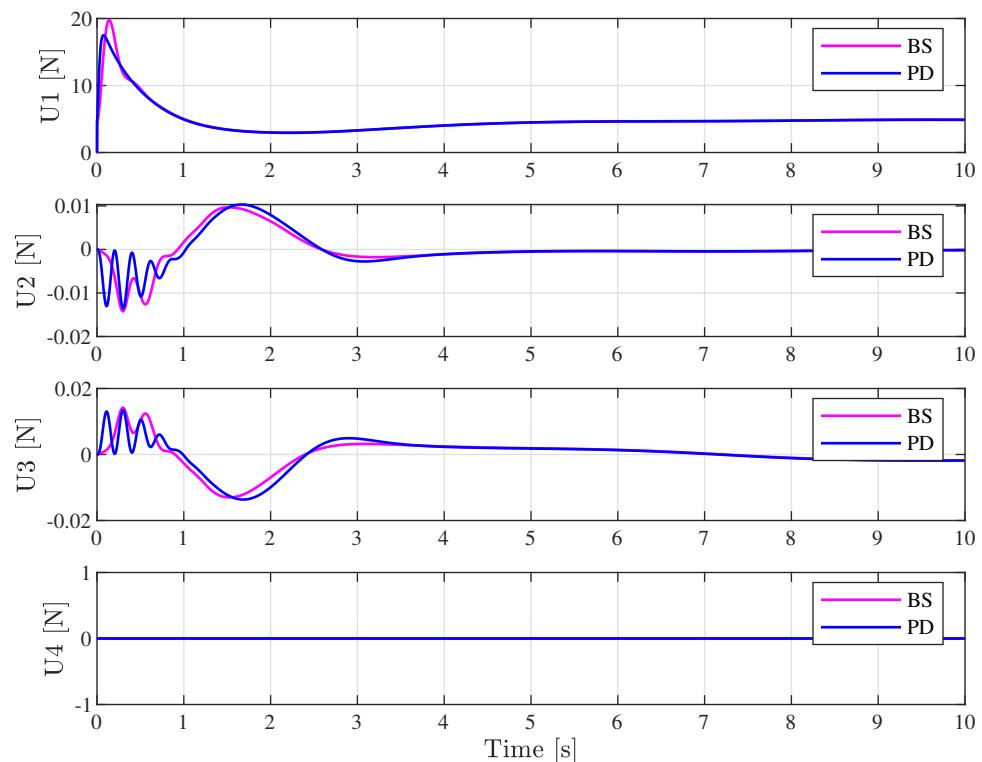


Figure 3.4: Control signals with perfect delay estimator

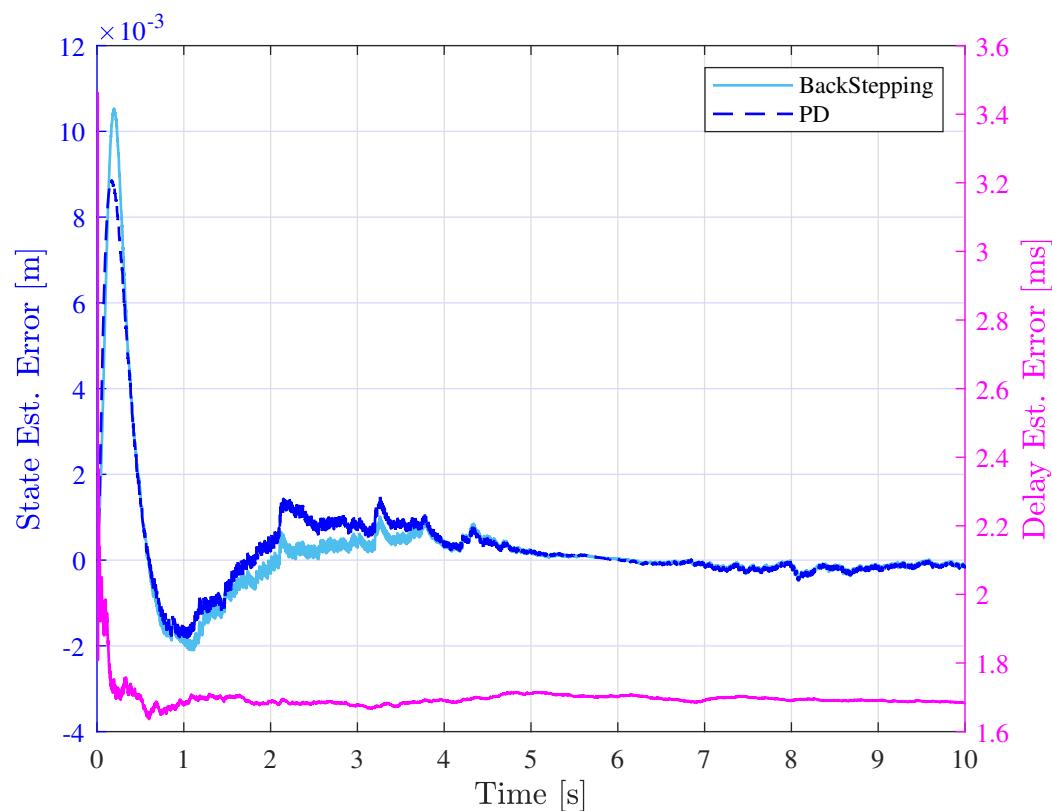


Figure 3.5: State and delay estimation error for  $D = \{6, 7, 9, 10\} \text{ ms}$

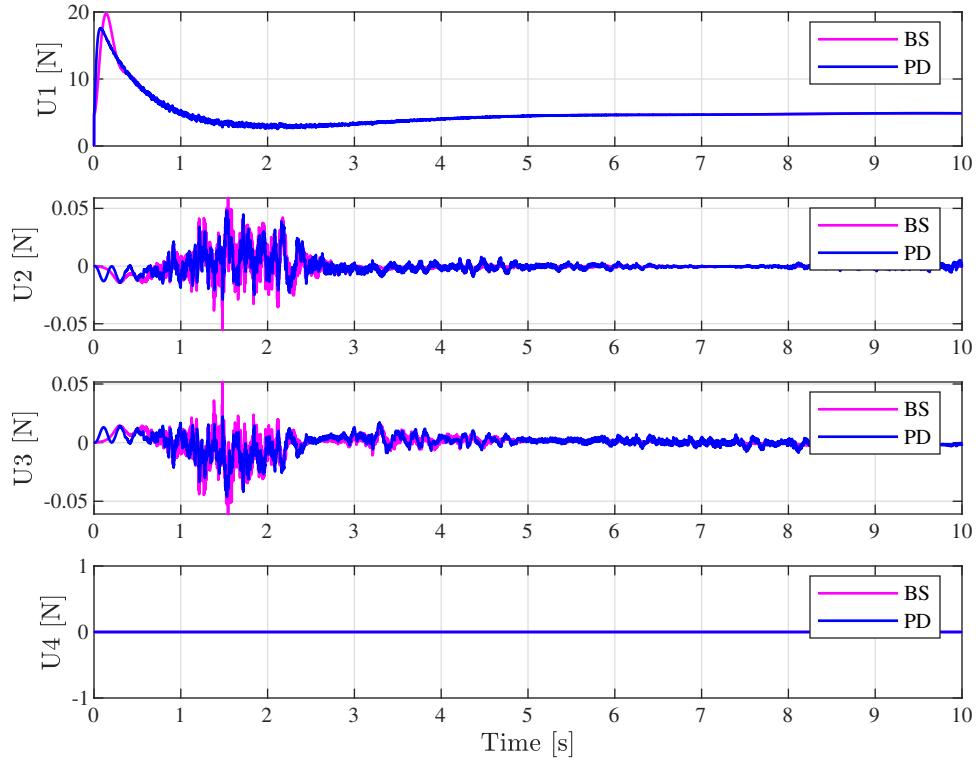


Figure 3.6: Control signals for  $D = \{6, 7, 9, 10\}$  ms

in the control signal), small feedback errors are multiplied by the large gains and generate oscillating control signals.

In order to study the effect of the large changes in delay on the system, the time delays were changed to  $D = \{1, 3, 13, 15\}$  ms. The simulation was done with the true transition probabilities presented in Table 3.3. Fig. 3.7 shows how a slight change in the delay variation increases the estimation error. It also shows that we cannot use the mean value for the delay because large variations in delay negatively affect the response. It takes longer for the state estimator to estimate the current position.

According to Fig. 3.8, large variations in state estimation error affect the backstepping controller so that it generates control signals with higher frequency and amplitude than the PD controller. It should be noted that although one way to solve this problem is to reduce the backstepping controller's coefficients, lower values for coefficients increase the response

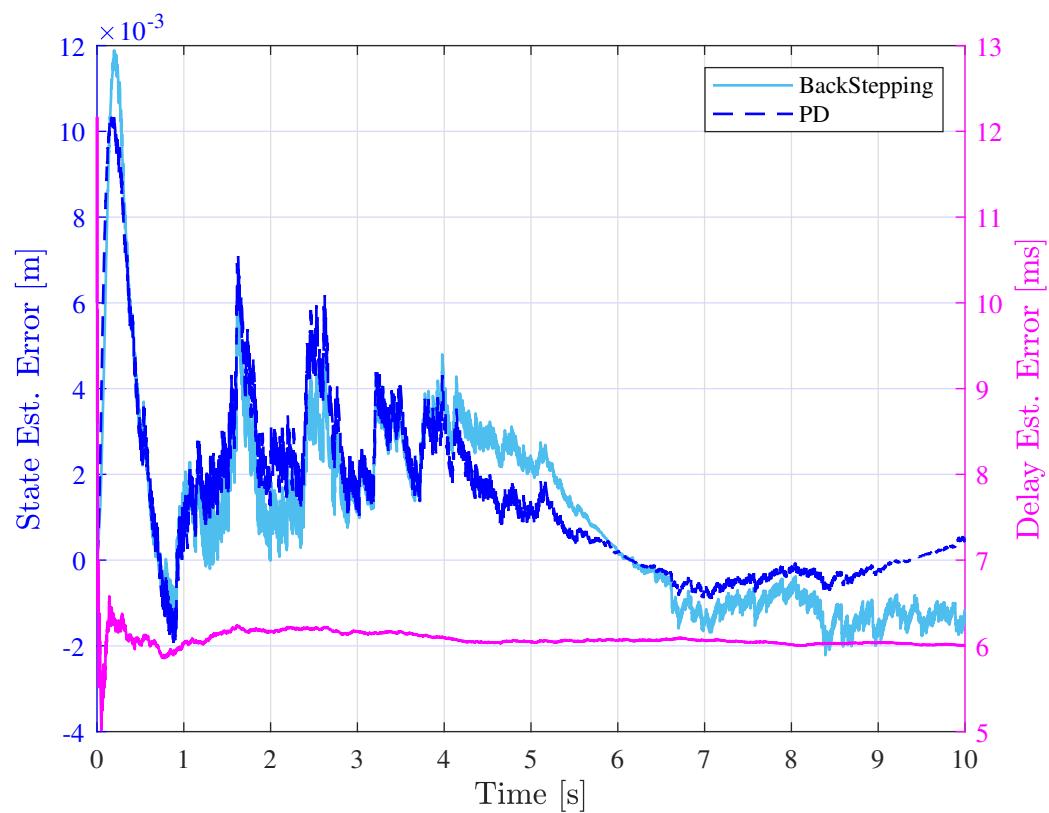


Figure 3.7: State and delay estimation error for  $D = \{1, 3, 13, 15\} \text{ ms}$

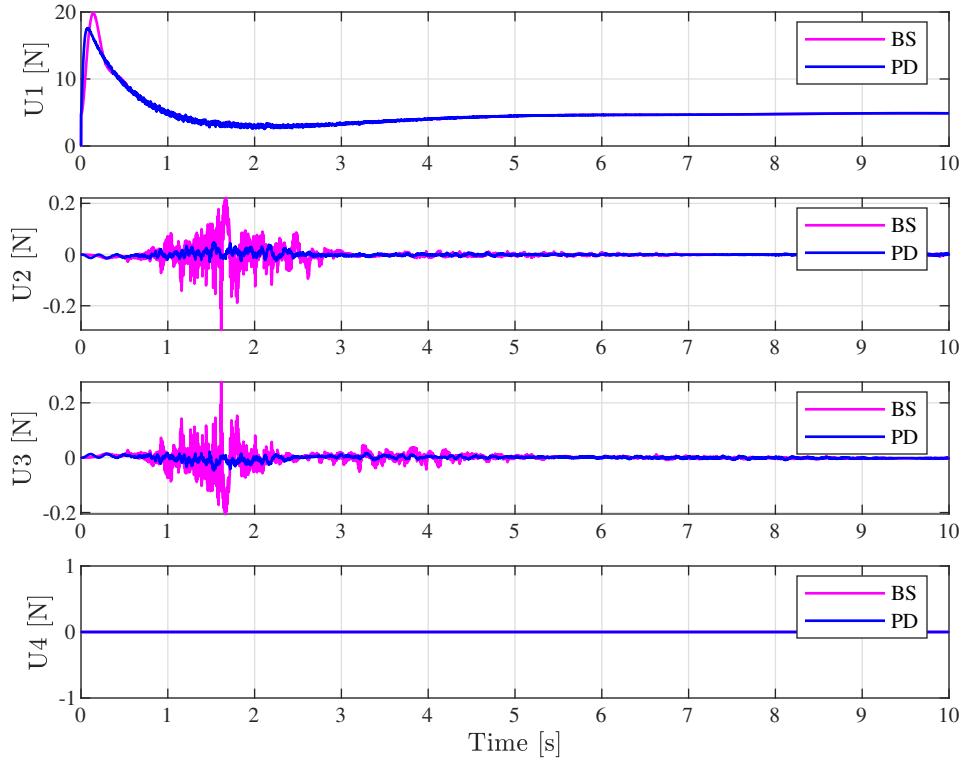


Figure 3.8: Control signals for  $D = \{1, 3, 13, 15\} \text{ ms}$

time and path RMSE.

**Change in delay values and distributions** While the cellular networks provide higher communication bandwidth with lower time delays, the variation in network load in crowded areas like urban environments changes the network properties. During the simulation, the time delays ( $D$ ) and their distributions  $p$  were changed to simulate the changes in network states. The simulation was done with delays between  $1 - 10 \text{ ms}$ , and the time delay values and their transition probabilities were changed six times.

Fig. 3.9 shows the delay estimation error during the simulation. According to the figure, change in delay values and distributions has affected the delay estimation. However, small delay changes between  $1$  to  $10 \text{ ms}$  did not decrease the state estimator's performance. It should be noted that after every change in delay, the DEE was reset, and error was calculated

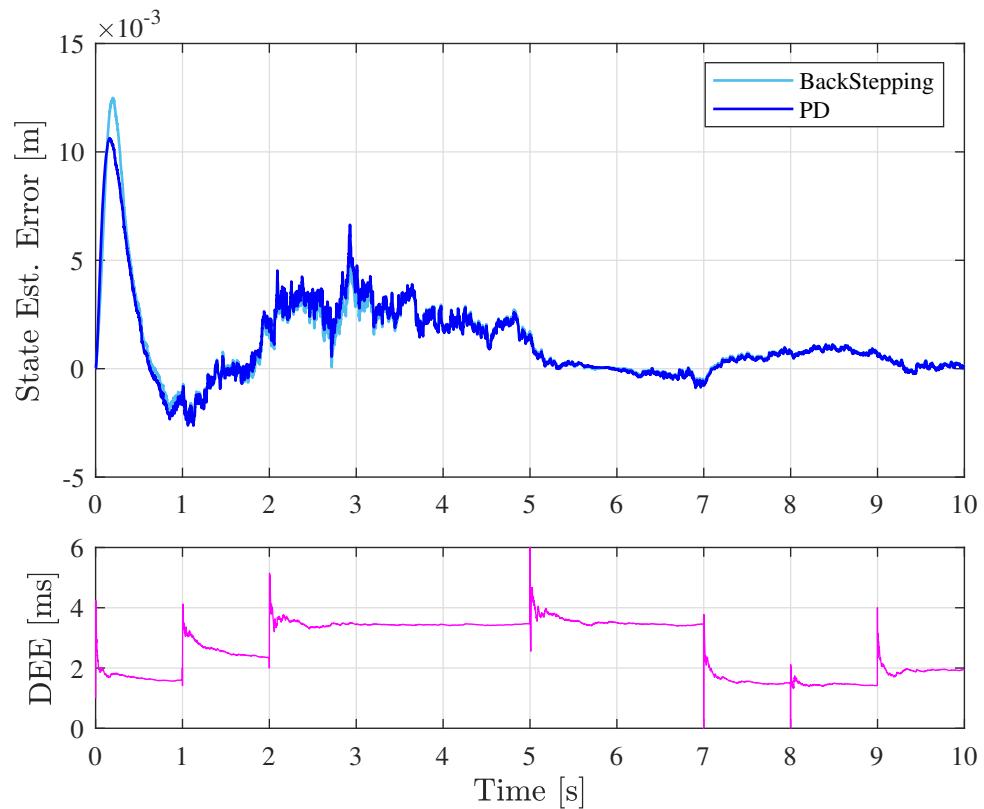


Figure 3.9: State and delay estimation error when delays and their distribution changed  
(Large variations in delay estimation shows the points where the delay values and the transition probabilities are changed)

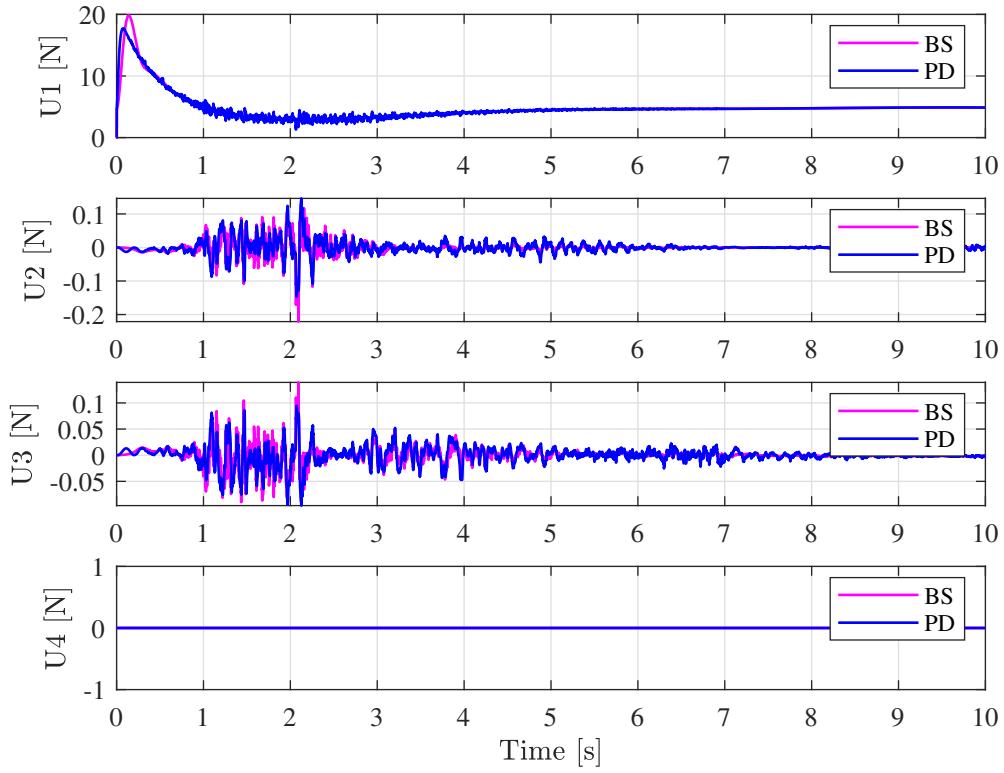


Figure 3.10: Control signals when delays and delay distributions changed

for new time delays.

As shown in Fig. 3.10, errors in estimating time delay caused high-frequency oscillations in the control signal. Although the maximum delay value is not changed, changing delay values between 1 to 10 ms negatively affected the control signal.

According to the results, PD and backstepping controllers have similar performance in quadrotor control. However, in the case of the large variation in time delay, the PD controller generates better control signals. The design process of the backstepping controller is more complicated than the PD controller.

In this paper, the PD gains and backstepping coefficients were set so that the trajectory tracking performance was almost the same. RMSE of the path in  $x$ ,  $y$ , and  $z$  directions were 1.046, 1.138, and 0.131 m for the PD controller, and 1.224, 1.329, and 0.19 m for the backstepping controller. In this case, the forward delay is the major reason for high RMSE

and makes quadrotor follow the path with delay.

In the linear PD controller, the gains can be tuned using inner and outer loop bandwidths. Also, using the theoretical stability analysis based on the linearized model, one can find an equation between time delay and controller's bandwidth. This issue helps the control framework adjust the bandwidth based on the observed time delay.

The bandwidth adaptation in the backstepping controller is a complex task since 12 parameters should be tuned. On the other hand, developing an equation between coefficients and time delay is much more complex than the linear PD controller.

Cellular networks are state-of-the-art communication tools for precise swarm control of drones. The presented control framework can control multiple drones from the GCS while the state estimator provides precise information about each drone's current position and orientation (fully observable system) for real-time centralized multi-agent-based collision avoidance, cooperation, and path planning tasks.

## 3.7 Conclusion

In this paper, a comparative study was done to evaluate the performance of the linear PD and nonlinear backstepping controller in controlling the quadrotor through 5G or other cellular networks. Considering the channel behavior in producing the time delays, the delay estimator estimated the time delays using the Markov model. The estimated time delays were then used to estimate the quadrotor's correct position. The state estimator received the current control signal from the controller. It estimated the correct position using time delay estimation and the measured quadrotor position.

The controllers' performance in three different scenarios was evaluated. Both controllers generated a smooth control signal when the delay was known. There were oscillations in the control signal when the delay was unknown, but the position of the quadrotor was estimated with a very low error. Results showed that increasing the change in delay negatively affects both controllers. Also, when delay values and their distributions changed, the oscillations in control signals increased.

According to the results, there is not a significant difference in controllers' performance. However, large variations in time delay are a considerable problem in the backstepping controller.

# Chapter 4

## Learning a Policy for Pursuit-Evasion Games Using Spiking Neural Networks and the STDP Algorithm

Artificial neural networks have grown in potential over the last decade. From Multi-Layer Perceptron (MLP), as the first generation, to Deep Neural Networks (DNN), as the second generation, they have been implemented in widespread applications to solve complex problems. However, as the networks become more complicated, they become more dependent on devices with high computational capabilities, like general-purpose Graphical Processing Units (GPUs).

The complex combination of neural structures in SNNs helps us implement complex learning systems. One good example of a complex situation is a differential game like the Active Target Defense (ATD) problem [46].

In the ATD, a defender tries to protect a target, while a superior invader with higher velocity than the defender and target tries to reach the target and escape the defender at the same time. In defense strategy, they aid in analyzing movements and determining optimal strategies for aircraft. Law enforcement benefits from these games by minimizing escape possibilities. They are a fundamental component of game theory, providing insights into

strategic decision-making across disciplines like economics and biology. Additionally, these games find applications in Cybersecurity for modeling attacker-defender interactions. [47].

There are three distinct outcomes to the ATD, characterized by two or three termination sets [48]. The first outcome happens when the invader reaches the target while the defender is far from it. The second outcome happens when the defender reaches the target while the invader's distance from the target is larger than the defender's distance. Finally, the third outcome is realized when the invader and defender reach the target at the same time.

## 4.1 The ATD problem and SNN-based solution

The ATD problem has various solving methods, such as Apollonius Circle and Cartesian Ovals (CO). This paper opts for the CO method over the Apollonius Circle because it considers the capture radius and effectiveness against superior invaders [48]. The optimal capture point is considered the minimum distance between the target's position and reachable region if the target is inside the defender's dominant region. The defender's dominant region is a region where the defender can reach the target without letting the invader capture the target.

In this paper, the problem is solved using reinforcement learning. It is considered that each agent knows the relative velocity of other agents. Figure 4.1 shows LOS angles used as the input for the SNNs [49].

The STDP algorithm is used to train two separate SNNs simultaneously that control the invader and defender. The target in this paper moves in the environment, and the SNNs receive the LOS angles (e.g., the defender receives the LOS angle to both the invader and the target) and calculates the steering angle for the agent (Figure 4.2). In this figure, the  $\phi_I^T$  represents the LOS angle to the target relative to the invader.

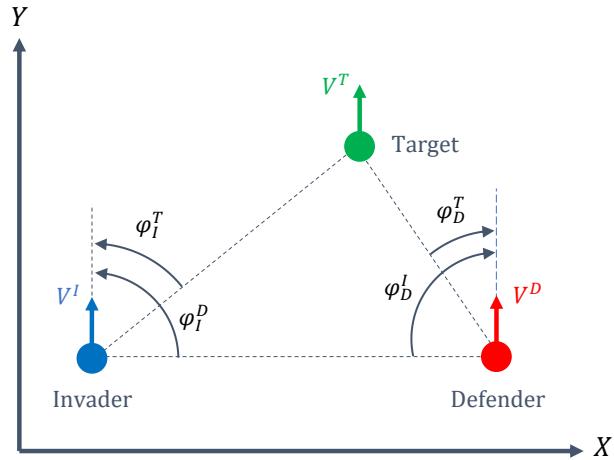


Figure 4.1: Active target defense game with three agents (LOS angles are shown for both agents).

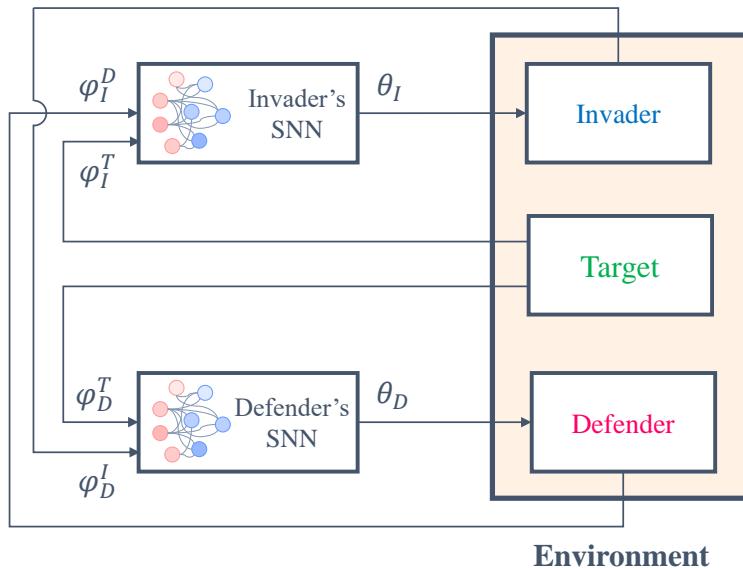


Figure 4.2: Two SNNs simultaneously play and control the invader and defender. Each agent uses the LOS angle and relative velocities for training.

## 4.2 Learning using STDP

Spike-Timing-Dependent Plasticity (STDP) is a biological learning algorithm that is believed to underlie certain learning mechanisms in the brain [50]. The STDP algorithm is based on the idea that if a pre-synaptic neuron fires just before a post-synaptic neuron, the strength of the synapse between the two neurons should be increased. Conversely, if the post-synaptic neuron fires just before the pre-synaptic neuron, the strength of the synapse should be decreased.

In the SNN, the pre-synaptic neurons are input neurons, and post-synaptic neurons are output neurons. The synaptic plasticity is referred to as an eligibility trace ( $C$ ), which is calculated based on the following equation [51],

$$\dot{C}^{i-j} = -C^{i-j}/\tau_C + STDP^{i-j}(\tau)\delta(t - t_{pre/post}) \quad (4.1)$$

where the  $C^{i-j}$  is the eligibility trace for the synaptic connection between neurons  $i$  and  $j$ ,  $\tau$  is the spike timing difference between the input and output spike times,  $\tau_C$  is the time constant for the synaptic plasticity,  $\delta$  is the Dirac function,  $t_{pre/post}$  is the firing time of the pre or post-synaptic neuron, and  $STDP(\tau)$  is a function of the firing time of the input and output neurons as follow,

$$STDP^{i-j}(\tau) = \begin{cases} A_+ \exp\left(\frac{-\tau}{\tau_s}\right) & \text{if } \tau > 0 \\ A_- \exp\left(\frac{\tau}{\tau_s}\right) & \text{if } \tau < 0 \end{cases} \quad (4.2)$$

where  $A_+$  and  $A_-$  are the amplitude of the exponential function, and  $\tau_s$  is the time constant that determines the decaying rate of the STDP function. If  $\tau_s$  goes to infinity, the exponential function becomes 1, and the effect of time in STDP will be lost.

The synaptic weights are changed according to the following equation,

$$\dot{W}^{i-j}(t) = C^{i-j}(t)R(t) \quad (4.3)$$

where  $W^{i-j}$  is the synaptic weight between neurons  $i$  and  $j$ , which is the amount of input

( $I(t)$ ) that the post-synaptic neuron receives when the pre-synaptic neuron spikes, and  $R(t)$  is the reward.

This paper uses the Multiplicative Synaptic Normalization (MSN) method to keep runaway excitation under control. This method keeps pre-existing memories in the network by conserving the proportional difference between smaller and larger synaptic weights. According to (1.9), we can calculate the maximum input for each post-synaptic neuron (output layer).

The MSN normalizes the synaptic weights based on the cumulative input synaptic weights and the maximum input as follows [50],

$$\vec{W}^n(t) = \vec{W}^n(t-1) \left( \frac{I^{max}}{\sum_{\iota=1}^N W^\iota(t)} \right) \quad (4.4)$$

where  $W^n(t)$  is the vector consisting of synaptic weights that send input current to the  $n^{th}$  output neuron, and  $N$  is the total number of input synapses for each output neuron. Therefore, when STDP increases a single synaptic weight, the MSN proportionally decreases the other synaptic weights for the  $n^{th}$  neuron.

The reward for the invader and defender is defined based on the projection of the velocities along the LOS direction. Figure 4.3 shows the projected velocities for the invader and defender, where both agents measure the relative velocities from each other. It means that the invader receives a negative reward when it moves toward the defender and receives a positive reward when it moves toward the target. The defender receives a positive reward when it moves toward the target and invader. Since the velocities are constant, the reward value depends only on the headings that cause the change in relative velocities. Therefore, the LOS toward the other agents determines the reward value.

The reward for the invader considering the target and defender consists of two parts,

$$R_I^T(t) = \eta_I^T (V^I + V^T) \cos(\phi_I^T) \quad (4.5)$$

and

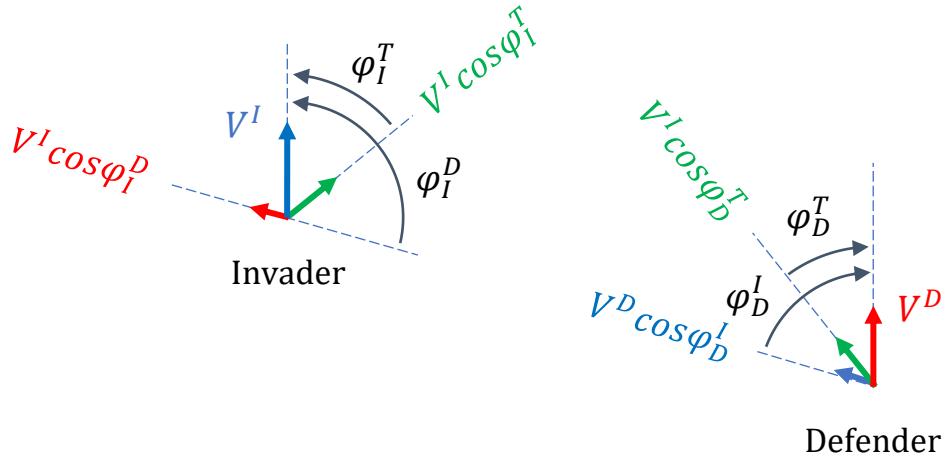


Figure 4.3: Relative velocities and LOS angles used in the reward function

$$R_I^D(t) = \eta_I^D (V^D - V^I) \cos(\phi_I^D) \quad (4.6)$$

The reward for the defender also can be calculated as follows,

$$R_D^T(t) = \eta_D^T (V^D + V^T) \cos(\phi_D^T) \quad (4.7)$$

and

$$R_D^I(t) = \eta_D^I (V^D - V^I) \cos(\phi_D^I) \quad (4.8)$$

In (4.5)-(4.8),  $\eta_I^T$ ,  $\eta_I^D$ ,  $\eta_D^T$ , and  $\eta_D^I$  are constant coefficients. Adjusting these values changes the agent's attention to other agents. For example, in the invader case, increasing the  $\eta_I^T$  and decreasing the  $\eta_I^D$  increases the effect of the target on the output and reduces the defender's effect. The invader then places more importance on getting to the target than evading the defender.

The change in synaptic weights for the invader regarding the target and defender consists of two parts as follows (the same process is true for the defender),

$$\mathbf{W}_I^T(t) = \mathbf{W}_I^T(t-1) + \mathbf{C}_I^T(t) R_I^T(t) \quad (4.9)$$

and

$$\mathbf{W}_I^D(t) = \mathbf{W}_I^D(t-1) + \mathbf{C}_I^D(t)R_I^D(t) \quad (4.10)$$

where  $\mathbf{W}_I^T$  is a  $k \times l$  matrix that represents the synaptic weights corresponding to the target ( $k$  is the number of output neurons and  $l$  is the number of input neurons for the target). The  $\mathbf{W}_I^D$  is a  $k \times m$  matrix that represents the synaptic weights regarding the defender ( $m$  is the number of input neurons for the defender). The eligibility trace matrices  $\mathbf{C}_I^T$  and  $\mathbf{C}_I^D$  are of dimension  $k \times l$  and  $k \times m$ , respectively.

## 4.3 Network structure and encoding method

Figure 4.4 shows the defender’s network structure and encoding process. The invader has the same network with different inputs. The network receives the LOS angles and converts the inputs to Fuzzy Membership Values (FMV) using Gaussian Receptive Fields (GRF) [52]. Since the fuzzy membership values are used just for encoding data into the SNN, the type of the membership function does not affect the computation complexity.

There are  $q$  input neurons, and a membership function is assigned to each neuron. Therefore, there are  $q$  membership functions. The acquired fuzzy membership values are real numbers between 0 and 1 and should be converted to the input currents. This can be done using a linear function and the minimum and maximum inputs.

The acquired fuzzy membership values are converted to the spiking inputs for the neurons using Fuzzy to Spiking (F2S) conversion. If  $FMV = 0$  ( $t_{isi} = \infty$ ), then the input to the desired neuron in the input layer is  $I^{min}$ , and if  $FMV = 1$  ( $t_{isi} = \Delta t$ ,  $\Delta t$  is the sampling time), then the input is  $I^{max}$ . Therefore, the input current for the input neurons can be calculated using the following equation,

$$I_\sigma = (I^{max} - I^{min}) FMV_\sigma + I^{min}$$

or

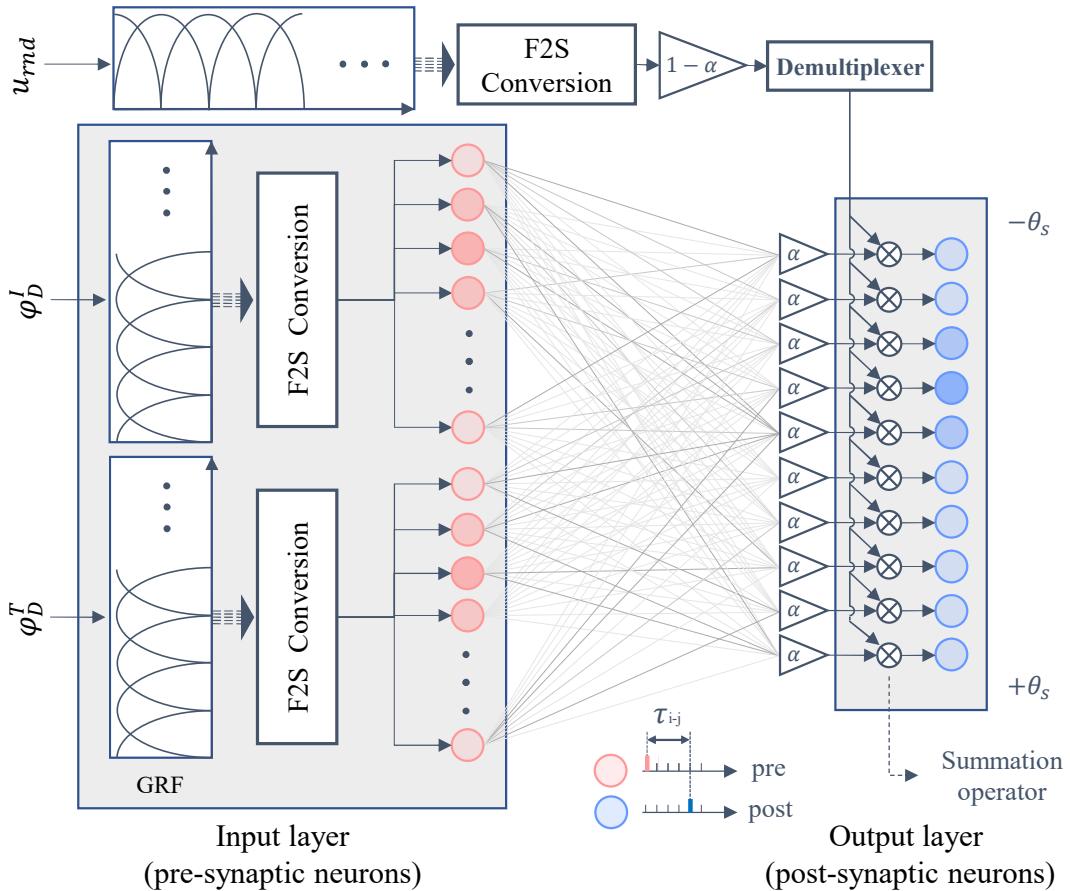


Figure 4.4: Network structure and encoding process for the input layer (Defender). Each neuron is associated with a membership function in GRF. The GRF encodes an input State ( $S^t$ ) at each time step. There is both a training phase when ( $\alpha = 0$ ) and an operating phase when ( $\alpha = 1$ ).

$$I_\sigma = \frac{\tau_m (V_{th} - V_{res})}{\Delta t R_m} FMV_\sigma + \frac{V_{th} - E_l}{R_m} \quad (4.11)$$

where  $\sigma$  is the index of each neuron in the input layer and its corresponding fuzzy membership value in GRF.

The output of the SNN is the steering angle ( $\theta_s$ ) for the agent. The output is calculated using the weighted average method. Each neuron in the output layer represents a specific steering angle. The number of spikes for each output neuron in  $\tau_s$  millisecond represents how much it contributes to the output. The level of contribution is considered 1 for an output neuron that fires at each step time, while it is considered 0 for the output neuron that has not fired. Levels of contributions are then multiplied by the angle that each output neuron represents. Finally, the summation of all the calculated terms is divided by the summation of all levels of contributions.

The output consists of two terms. One term comes from the synaptic weights, and the other term is random noise for exploration. The output of the SNN can be shown as follows,

$$I_{out} = \alpha I_{syn} + (1 - \alpha) I_{rnd} \quad (4.12)$$

where  $\alpha$  is a constant that is 0 during training and becomes 1 after training is completed,  $I_{rnd}$  is a random steering angle that is selected at each time step, and  $I_{syn}$  is the synaptic output (steering angle based on synaptic weights). Therefore, there are two phases: a training phase and an operating phase.

During training, the input State ( $S^t$ ) is encoded into the network, and a random steering angle ( $u_{rnd}$ ) is encoded as a random action using the F2S process into the output layer. These two encoding currents for the input and output layer make input and output neurons fire independently. The STDP adapts the weights for the fired neurons. Since  $\alpha$  is 0 during the training, the  $I_{syn}$  does not affect the SNN's output (Equation 4.12).

In the training process, the output neurons and input neurons are excited separately. The input neurons are fired based on the current State of the agent, whereas the steering angle of the agent is randomly assigned based on the random input to the output neurons, as

**Algorithm 2** Weight training algorithm

---

```

1: for  $t = 0 : \Delta t : t_{final}$  do
2:   input  $\phi_I^T$  and  $\phi_I^D$ 
3:    $\zeta \leftarrow$  number of input neurons
4:    $\kappa \leftarrow$  number of output neurons
5:   for  $i = 0:2\pi/\zeta:2\pi$  do
6:      $Z_T(i, 1) = \exp(-0.5(\phi_I^T - i)/\sigma)$ 
7:      $Z_D(i, 1) = \exp(-0.5(\phi_I^D - i)/\sigma)$ 
8:   end for
9:    $I^T = (I^{max} - I^{min}) Z_T + I^{min}$ 
10:   $I^D = (I^{max} - I^{min}) Z_D + I^{min}$ 
11:  Generate a uniform random number for exploration  $u_{rnd} \in [-\theta_s, \theta_s]$ 
12:   $j = 1$ 
13:  for  $i = -\theta_s:2\theta_s/\kappa:\theta_s$  do
14:     $Z_{rnd}(j, 1) = \exp(-0.5(u_{rnd} - i)/\sigma)$ 
15:     $j \leftarrow j + 1$ 
16:  end for
17:   $I_{rnd} = (I^{max} - I^{min}) Z_{rnd} + I^{min}$ 
18:  for  $j = 1$  to  $\kappa$  do
19:     $I_{syn}(j, 1) = \sum_{i=1}^{\zeta} W^{i-j} \delta(t - t_i)$        $\triangleright t_i$  is the firing time of the  $i^{th}$  input neuron
20:  end for
21:   $I_{in} = \begin{bmatrix} I^T \\ I^D \end{bmatrix}$  Input current
22:   $I_{out} = \alpha I_{syn} + (1 - \alpha) I_{rnd}$  ( $\alpha = 0$  in training phase)
23:   $\mathbf{V}_m(t + \Delta t) = (1 - \frac{\Delta t}{\tau_m}) \mathbf{V}_m(t) + \frac{\Delta t}{\tau_m} \left( \mathbf{E}_l + R_m \begin{bmatrix} I_{in} \\ I_{out} \end{bmatrix} \right)$   $\{\mathbf{V}_m \text{ and } \mathbf{E}_l \text{ are } [\zeta + \kappa] \times 1\}$ 
24:  Find fired neurons in input and output layer
25:  Calculate the  $\boldsymbol{\tau}$  matrix that shows the difference in firing time between the fired
       input neurons and fired output neurons (Figure 4.4)
26:  Calculate STDP for all connection using (4.2)
27:  Calculate C matrix using (4.1) for all the connections
28:  Calculate W matrix using (4.3) for all the connections considering reward from (4.5)
       to (4.8)
29:  for  $i = 1$  to  $\kappa$  do
30:    if sum of the input weights to  $i^{th}$  neuron  $\geq I^{max}$  then
31:      Normalize input weights of  $i^{th}$  neuron using (4.4)
32:    end if
33:  end for
34:  Set voltage of the fired neurons to reset voltage ( $V_{res}$ )
35: end for

```

---

Table 4.1: Parameter values for LIF neuron model [53]

Parameter	Value	Description
$R_m$	40 MΩ	Membrane Resistance
$\tau_m$	30 ms	Membrane time constant
$E_l$	-70 mV	Resting potential
$V_{res}$	-70 mV	Reset potential
$V_0$	-70 mV	Initial membrane potential
$V_{th}$	-50 mV	Threshold membrane potential

shown in Figure 4.8. The training algorithm then evaluates the reward for that given random steering angle. If the reward is positive, then the weight associated with the input neurons to output neurons that fired for that State is strengthened, and if the reward is negative, then the weight for the input to output neurons in (4.2) is weakened. Future research will include an inhibitory effect where the weights can become negative.

After training, the  $\alpha$  changes to 1 and eliminates the effect of random output, and the SNN’s output is calculated based on the synaptic currents. Algorithm 2 shows the training process.

## 4.4 Results

A numerical simulation is conducted to evaluate the SNN’s performance in solving the ATD problem. The simulation is done in MATLAB 2022a, with a 1 *ms* sample time. The simulation parameters for neurons are presented in Table I.

After several simulations, the number of input neurons for invader and defender networks was set to 20. Both agents have 10 neurons in their output layer. The encoding resolution can be enhanced by increasing the number of neurons, although this results in a higher number of synaptic connections. To determine the optimal neuron number in the SNN, an

Table 4.2: Parameter values for STDP

Parameter	Value	Description
$\tau_s$	3 ms	Time constant
$A_{\pm}$	1	Amplitude of the STDP function
$\eta_D^T$	0.90	Reward coefficient
$\eta_D^I$	1.10	Reward coefficient
$\eta_I^T$	1.20	Reward coefficient
$\eta_I^D$	0.80	Reward coefficient

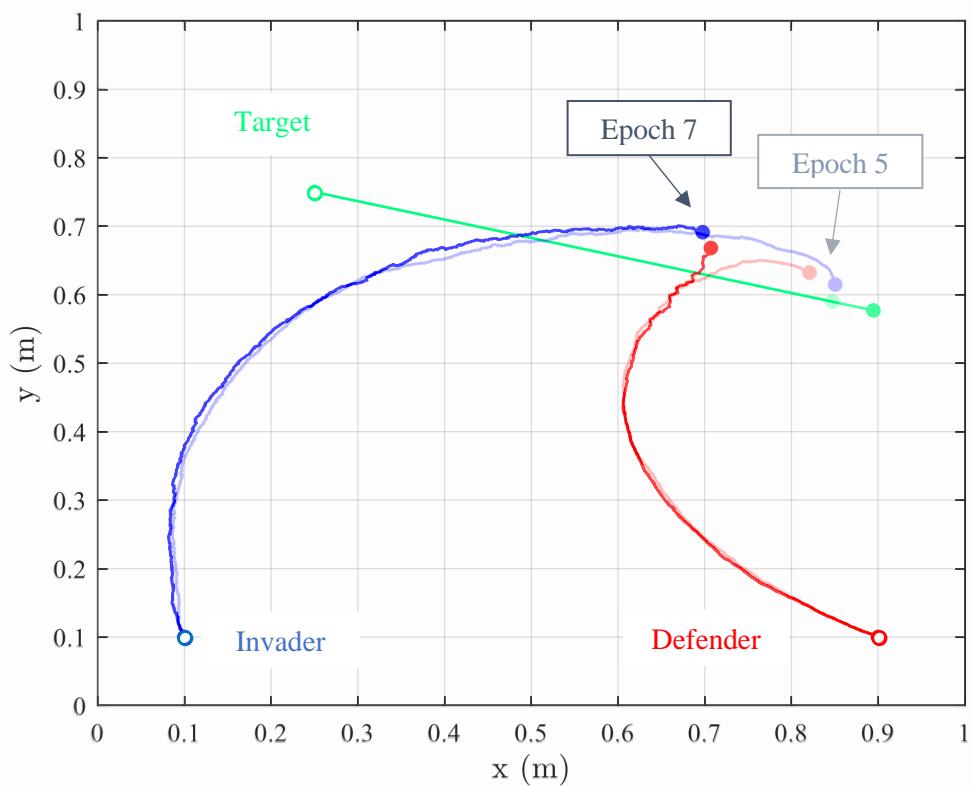


Figure 4.5: SNN's performance during training. Hollow circles show the initial positions.

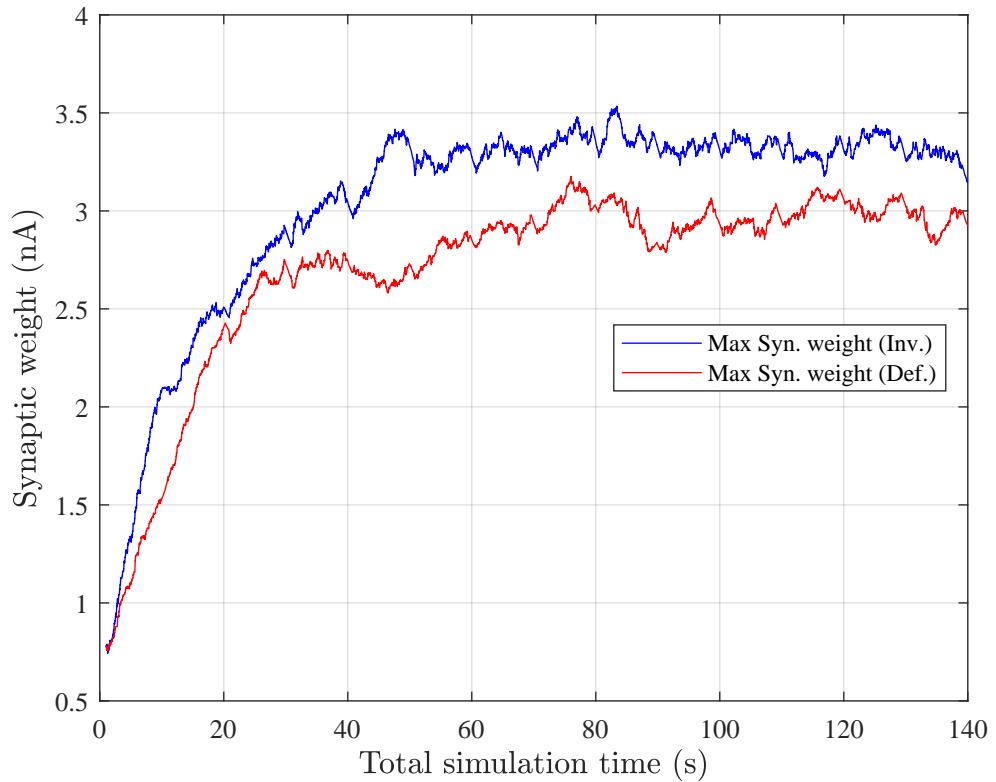


Figure 4.6: Changes in synaptic weights during training. Only Maximum synaptic weights for both agents are shown.

optimization algorithm can be employed. Half of the input neurons for the invader are for the  $\phi_I^T$ , and the other half is for the  $\phi_I^D$ . Half of the defender's input neurons are for the  $\phi_D^T$ , and the other half is for the  $\phi_D^I$ . Since each network contains 20 input neurons, the input layer has 20 Gaussian membership functions.

The output of the activation of each membership function is the input to a neuron associated with that specific membership function. There are 10 input neurons for the 10 membership functions related to each input. Furthermore, no more than 2 membership functions fire for any given input. Therefore, at most, only two neurons are excited and generate an impulse sequence for a given input.

The target's velocity is  $0.15 \text{ m/s}$ . The invader's velocity is  $0.3 \text{ m/s}$ . The  $\gamma$  is  $0.75$ , so the defender's velocity is  $0.225 \text{ m/s}$ . The defender's capture radius ( $\rho$ ) is set to  $0.025 \text{ m}$ . The maximum simulation time for each epoch is 10 seconds. The  $\theta_s$  for invader and defender is  $\pi/4$ , and the  $\sigma$  is set to 1.25. The parameter values for STDP, shown in Table II, are set through several simulations.

The reward coefficients are set manually. The  $\tau_s$  in Table II defines the decaying rate of  $C$  in (4.1) that determines the STDP sensitivity to prior firings. According to (4.2), higher  $\tau_s$  means that the STDP takes into account the activity of the two neurons that have fired in the relatively larger time window. Different studies have considered different values for this parameter.

As mentioned in Section II, the optimal capture point is the closest point from the reachable region to the target position. Figure 4.5 shows the agents during the training process. In epoch 5, the defender is not able to capture the invader, and the invader reaches the target. In epoch 7, the defender learns how to block and capture the invader. The defender has won the game. However, the invader should learn to reach the minimum distance from the target.

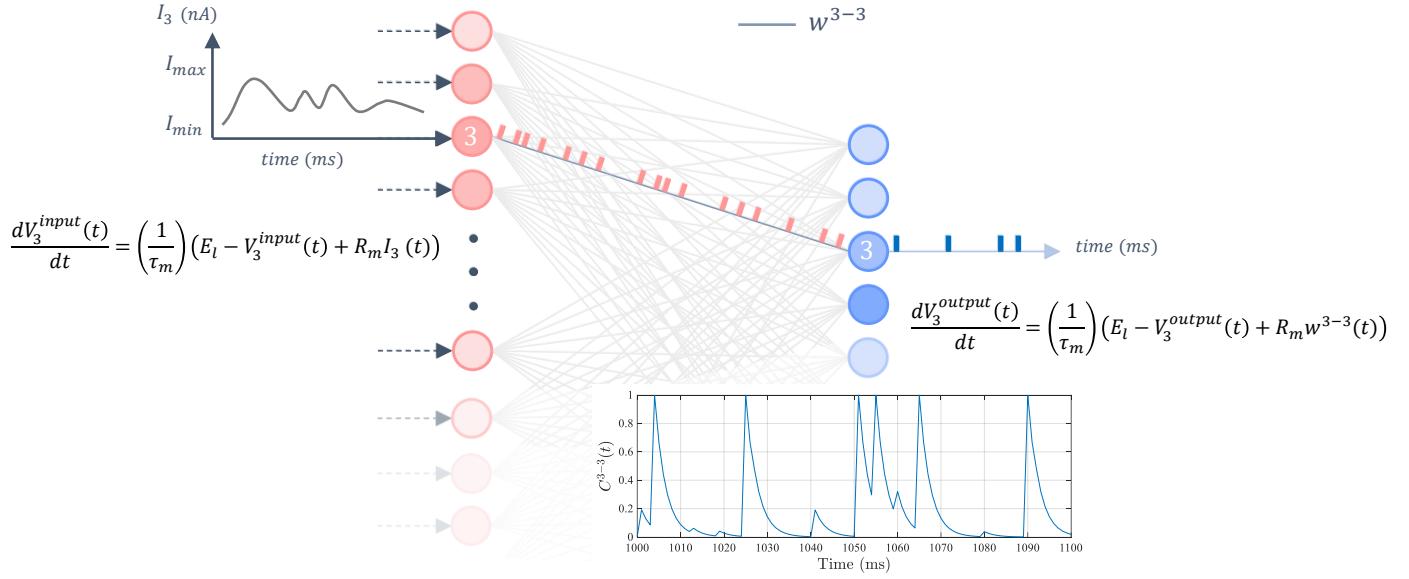


Figure 4.7: An illustration of input current to SNN and synaptic current to the output neurons after training for a single connection.

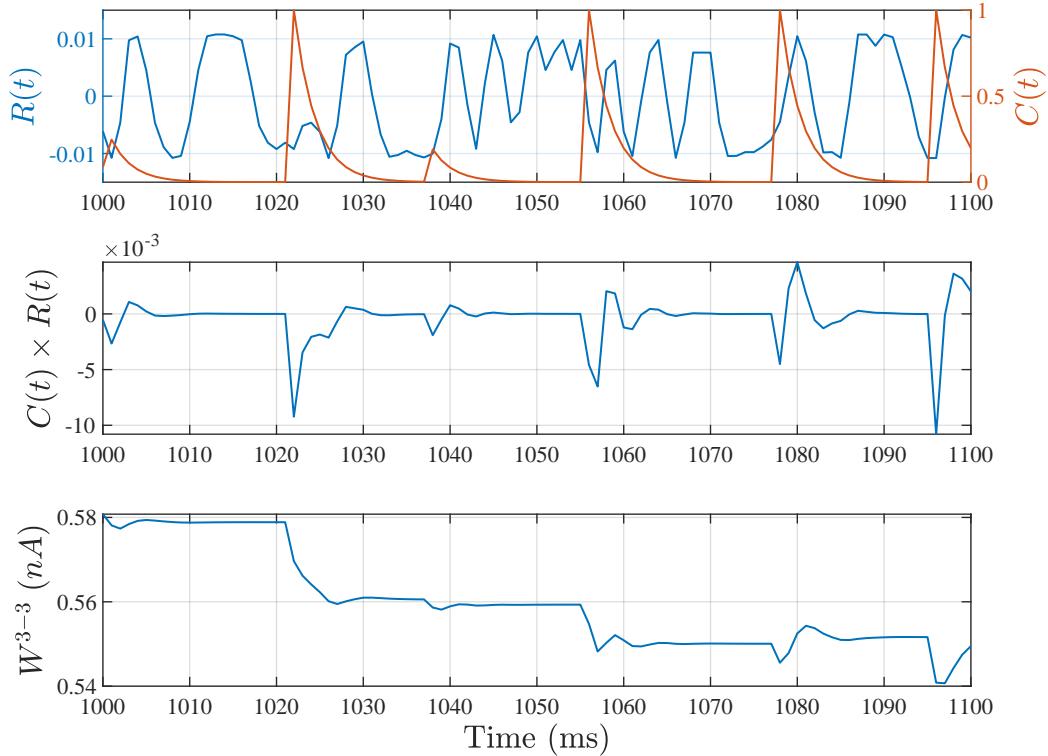


Figure 4.8: Reward, eligibility trace, and weight change during the simulation for  $W^{3-3}$ . The  $C(t)R(t)$  changes the synaptic weight by considering activation strength and reward value.

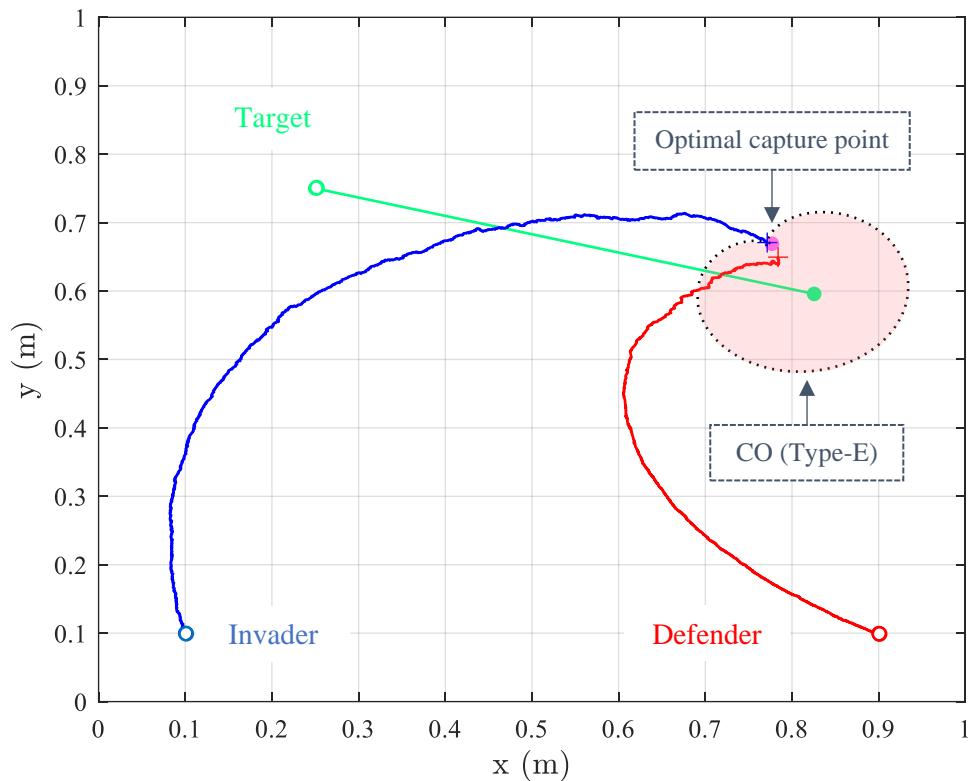


Figure 4.9: SNN’s performance after training. The highlighted region shows the defender’s dominant region. The purple dot is the optimal capture point.

#### 4.4.1 Simulation without noise

Figure 4.9 shows the performance after training. Each epoch has a maximum time of 10 seconds. After 14 epochs, the defender learned to capture the target, while the invader learned to reduce its distance from the target. According to the CO, the target is inside the defender’s dominant region. Therefore, although the invader’s velocity is higher than the defender’s velocity, it cannot reach the target. In this situation, the optimal policy for the invader is to minimize its distance from the target.

According to Figure 4.9, the invader’s SNN can find the optimal [48] capture point for the invader, while the defender’s SNN can protect the moving target against a superior invader. It should be noted that this solution is obtained without a global reference frame. This is important because, in real-world swarm applications, defining a global reference frame is difficult while the learning process is highly dependent on the precise definition of the coordinate system.

Figure 4.6 shows the changes in synaptic weights. Only the synaptic weights with maximum values are shown in this figure because the network has 200 synaptic connections. The minimum value is limited to zero because negative synaptic weights inhibit the post-synaptic neurons. This paper does not consider the inhibition process. According to the figure, after almost 100 seconds of simulation time, the MSN process causes the synaptic weights to converge.

#### 4.4.2 Simulation with noise

In Figure 4.10, we observe the performance of two methods, namely the Spiking Neural Network (SNN) and the Cartesian Oval (CO) method, in the presence of noise. The noise in this experiment is introduced as white Gaussian noise, characterized by a mean of zero and a variance of 0.01. Both SNN and CO receive position data that has been corrupted by this noise.

The results of the simulation reveal that the CO method is highly affected by the presence of noise, making it unable to calculate the optimal capture point accurately. Due to its

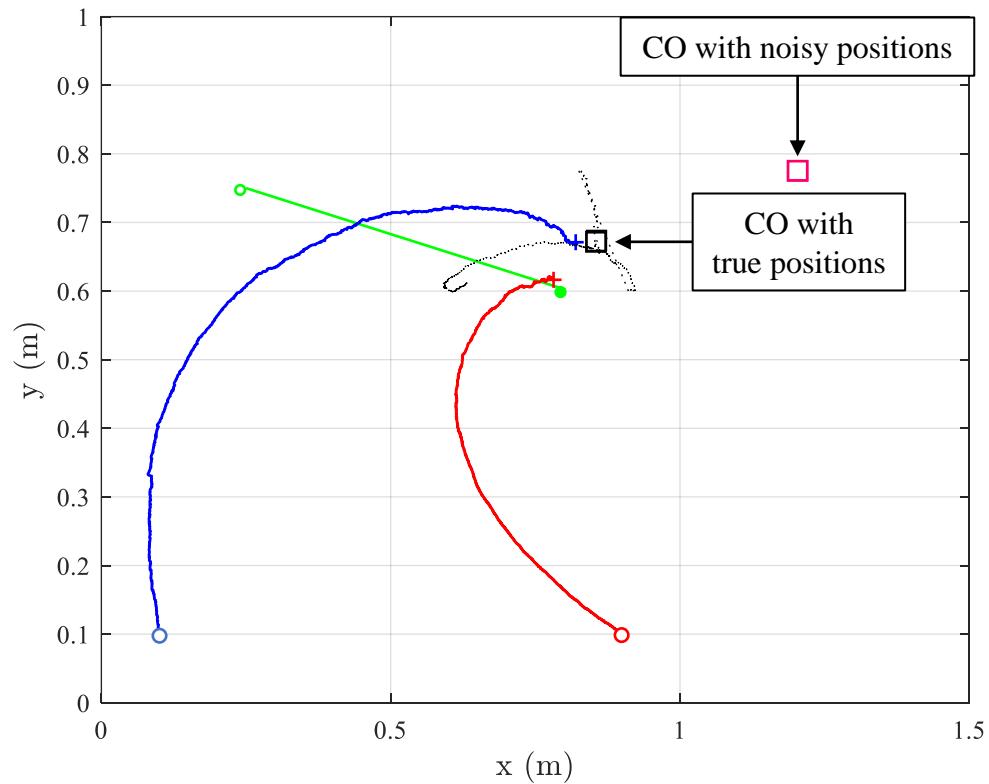


Figure 4.10: SNN's performance in noisy conditions. A white Gaussian noise with a variance of 0.01 is added to the measured inputs.

sensitivity to measurement noise, the CO method exhibits a significant deviation from the desired capture point. On the other hand, the SNN method demonstrates a higher level of robustness against noise. Despite the presence of measurement noise, the SNN method manages to achieve the optimal capture point with an error of only  $0.036\text{ m}$ . This outcome highlights the superior performance of the SNN method in noisy conditions compared to the CO method.

## 4.5 Conclusion

This study focuses on addressing the ATD problem within a dynamic environment involving two agents, where the target is in motion. The approach involves training two Spiking Neural Networks (SNNs) simultaneously to engage in a competitive game. During the game, the target transitions from the invader's dominant region to the defender's dominant region. This shift in the target's location within the defender's dominant region satisfies the necessary conditions for determining the reachable regions for both the invader and defender.

To evaluate the effectiveness of the SNN's solution, a comparison was made with an analytical solution designed for centralized problems. The results demonstrated that the SNN method was capable of identifying the optimal solution for decentralized problems, even under the presence of noise. This result holds significant practical implications, particularly in scenarios where establishing a global coordinate system for all agents proves to be challenging. The obtained solution provided by the SNN approach offers a valuable alternative in such cases, showcasing its potential in real-world applications.

# Chapter 5

## Enhancing Cooperative Multi-agent Reinforcement Learning through the Integration of R-STDP and Federated Learning

### 5.1 Preliminaries

#### 5.1.1 Consensus Flying Problem

The “Consensus Flying Problem” deals with ensuring drones can work together in real-time to agree on their flight paths and positions. When many drones are close together, like in swarms, avoiding crashes is vital. Advanced algorithms and communication methods are needed so drones can exchange information and handle changing situations and unexpected obstacles.

As shown in Figure 5.1, a swarm of agents (follower drones) flies around a leader. The leader is controlled from a remote base station, and the swarm agents should learn to fly safely with the leader. The leader sends its position to all agents, and each agent only sees

two neighboring agents. The swarm aims to learn how to keep a commanded distance from each other and the leader. The commanded distance is provided from the leader. Each agent uses the onboard sensors to find the distance and line of sight from neighboring agents.

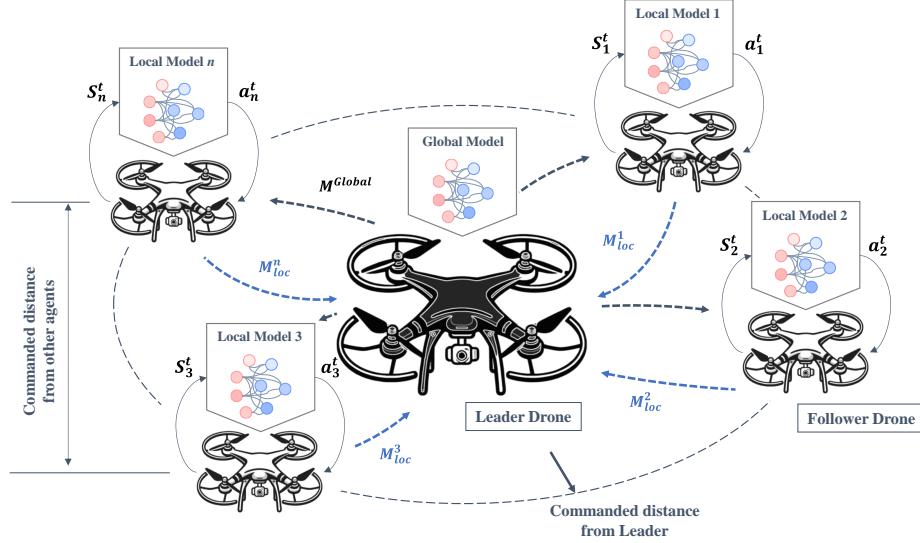


Figure 5.1: The central server (the leader) and the surrounding follower agents (white drones). The follower agents learn to fly in a formation to maintain the commanded distance. The Local models trained individually by follower agents are sent to the leader. The leader aggregates the models and sends back the global model for another round of training of the follower agents.

The follower agents are equipped with an [SNN](#), and their learning algorithm incorporates [Reward-modulated Spike-Timing-Dependent Plasticity \(R-STDP\)](#) and [Federated Learning \(FL\)](#). Each follower agent trains a local network ( $M_{loc}^n$ ) using [R-STDP](#) and sends its model to the leader as the central server. The leader aggregates models and sends back the global model ( $M^{Global}$ ).

### 5.1.2 Neuron Model

The [LIF](#) neuron model provides a simplified yet powerful representation of neuronal dynamics. Fundamentally, using basic electrical circuit elements, the [LIF](#) model captures the

behavior of a neuron's membrane potential in response to incoming currents. Mathematically, the LIF model is characterized by a linear differential equation that describes the voltage response to a current input as follows [54],

$$\tau_m \frac{dV_m(t)}{dt} = V_m(t) + E_L + R_m I_e(t) \quad (5.1)$$

where  $\tau_m$  is the membrane time-constant,  $V_m$  is the membrane potential,  $E_L$  is the reversal potential,  $R_m$  is the membrane resistance, and  $I_e(t)$  is the input current to the neuron. When the neuron's potential reaches the threshold potential ( $V_{threshold}$ ), it spikes, and the potential immediately returns to the resting potential ( $V_{rest}$ ).

For scenarios with constant input current, the Inter-Spike Interval ( $t_{isi}$ ) can be analytically determined by separating variables in the governing differential equation. This allows for the derivation of the  $t_{isi}$  as follows [55],

$$t_{isi} = \tau_m \ln \left( \frac{E_l + R_m I - V_{rest}}{E_l + R_m I - V_{threshold}} \right) \quad (5.2)$$

It is imperative to note that this solution is dependent on an input current magnitude that induces a transition of the membrane potential from  $V_{rest}$  to  $V_{threshold}$ . Through this analytical framework, the LIF model provides insights into the modulation of neuronal spiking dynamics based on constant input currents.

The neuron does not fire when the input current is minimum and  $t_{isi}$  approaches infinity. This occurs when the input current is insufficient to drive the membrane potential to the threshold potential from its resting potential. By setting the  $t_{isi}$  to infinity, one obtains the condition:

$$E_l + R_m I - V_{threshold} = 0 \quad (5.3)$$

or

$$I^{min} = \frac{V_{threshold} - E_L}{R_m} \quad (5.4)$$

where  $I^{min}$  is the minimum input current that makes the neuron reach the potential below

the threshold voltage. Conversely, the lowest possible  $t_{isi}$  defines the maximum input current. For this discussion, we consider this  $t_{isi}$  to be one sample time  $\Delta t$ . By considering  $\ln(1+z) \approx z$ , one can derive the maximum input current that would drive the neuron to spike on every sample time as follows,

$$I^{max} = \frac{\tau_m (V_{threshold} - V_{rest})}{\Delta t R_m} + \frac{V_{threshold} - E_L}{R_m} \quad (5.5)$$

These derived equations determine the range of operation for neurons and establish the boundaries for the maximum weights in the SNN. Specifically, positive synaptic weights indicate the limits of excitement that a neuron can generate. In this context, the minimum input current (or weight) represents the stimulating influence a neuron can exert without triggering an action potential. In contrast, the maximum input current signifies the most powerful stimulating influence possible. Conversely, considering weight values, these currents reflect the minimum and maximum inhibitory effects. In this case, the minimum and maximum input currents determine how much a neuron can inhibit other neurons from firing.

## 5.2 Proposed Method

### 5.2.1 Network Structure

This paper assumes that each agent detects only two neighboring agents in addition to the leader. The information obtained from other agents includes the line-of-sight angle and the distance. Each agent's neural network consists of three sub-layers in the input layer, as shown in Figure 5.2. Two sub-layers correspond to the two neighboring follower agents ( $F_1$  and  $F_2$ ), and the third is dedicated to the leader ( $L$ ). Inputs for these sub-layers are encoded using the Gaussian Receptive Fields (GRF) that use fuzzy membership functions. The network utilizes the difference between the current distance and the commanded distance ( $r_{cmd}$ ) to stimulate the input neurons.

Every input sub-layer is split into two parts. The first part deals with distances greater than the commanded distance, while the second focuses on the space between the agent

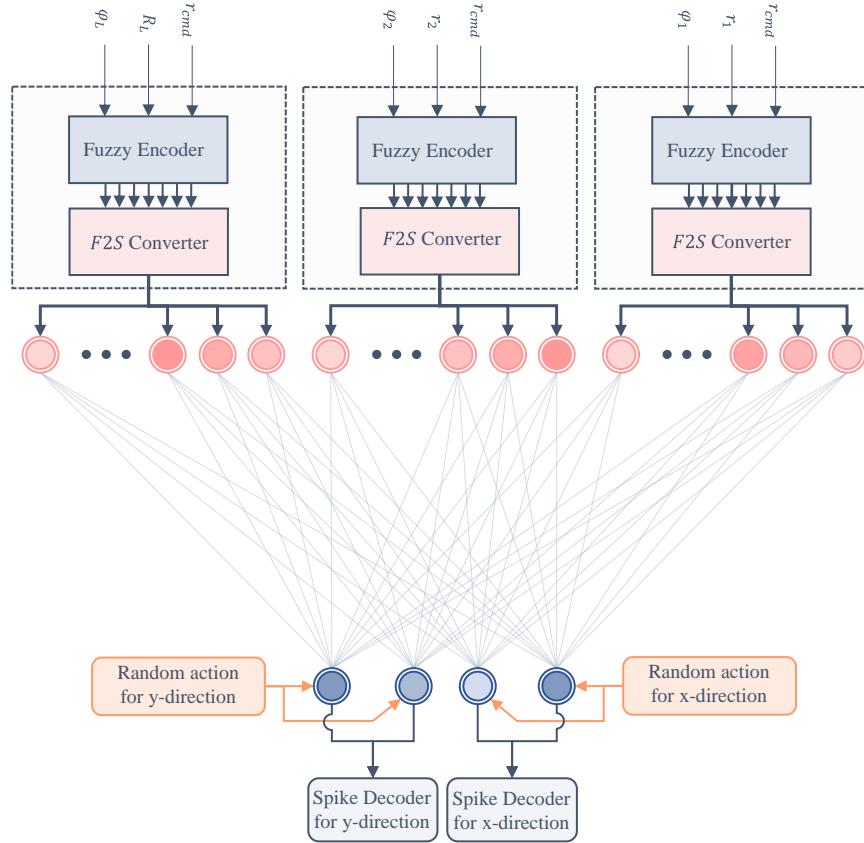


Figure 5.2: SNN structure with encoding and decoding layers. Each sub-layer consists of a fuzzy encoder and a Fuzzy-to-Spiking Converter, with the output layer receiving inputs from synaptic weights and a random action selector. During the training phase, the output layer receives input only from the random action selector, which then shifts to synaptic weight inputs after the training.

and the commanded distance. Within each part, the Line-of-Sight angle is encoded with fuzzy membership functions. The difference between the current and commanded distance is represented as the error that changes the maximum amplitude of the fuzzy membership functions. We transform this difference into an amplitude value using the  $\tanh$  function so that it is bounded between 0 and 1. An error of zero leads to an amplitude of zero, and as the error increases towards infinity, the amplitude approaches one. Consequently, the encoding function for the input layer is expressed as follows,

$$\mu_I(\phi_i, r_i) = |\tanh(r_{cmd} - r_i)| \cdot \exp\left(-\frac{(\phi_i - \zeta)^2}{2\sigma^2}\right) \quad (5.6)$$

where  $\zeta$  and  $\sigma$  are the Gaussian membership functions' center and standard deviation. The  $r_i$  is the distance from the corresponding agent,  $\phi_i$  is the line-of-sight angle, and  $\mu_I$  is the vector of the membership degrees. The firing strengths from fuzzy encoders are then converted to the spiking input based on the neuron model as follows [56],

$$I_{sub-layer} = (I^{max} - I^{min}) \mu_I(\phi_i, r_i) + I^{min} \quad (5.7)$$

or

$$I_{sub-layer} = \frac{\tau_m (V_{th} - V_{res})}{\Delta t R_m} \mu_I(\phi_i, r_i) + \frac{V_{th} - E_l}{R_m} \quad (5.8)$$

The encoding process is shown in Figure 5.3. The Fuzzy to Spiking (F2S) block uses (5.8) to calculate the inputs for the associated sub-layer.

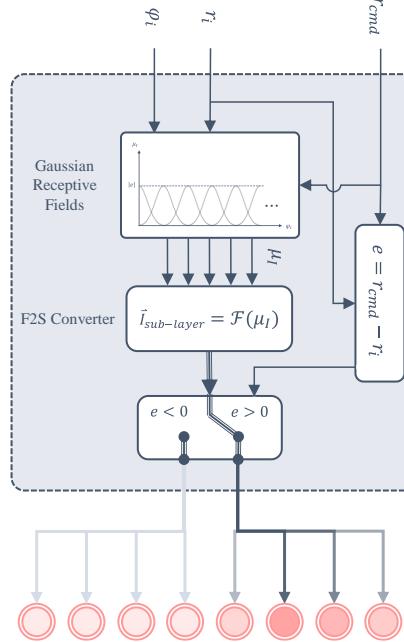


Figure 5.3: The fuzzy encoding principle for the input sub-layer.

The output layer has two sub-layers, and each sub-layer has two neurons. The first sub-layer determines the  $\Delta x$ , and the second one determines  $\Delta y$ . The first neuron of the sub-layers is for negative values, and the second one is for positive values. Each neuron is associated with the output sign, and the magnitude of the  $\Delta x$  and  $\Delta y$  is encoded into the output sub-layers based on the minimum and maximum synaptic weights. Equation (5.8) is used to encode the magnitude of the random action into the output sub-layers. The only difference is that a function called  $(\mu_O)$  is used to normalize the maximum step between 0 and 1 as follows,

$$\mu_x = \frac{\Delta x}{\Delta X_{max}} \quad (5.9)$$

$$\mu_y = \frac{\Delta y}{\Delta Y_{max}} \quad (5.10)$$

where  $\Delta x$  and  $\Delta y$  are selected actions, and  $\Delta X_{max}$  and  $\Delta Y_{max}$  are maximum steps (displacements) in  $X$  and  $Y$  directions. Therefore, two random actions, one for  $\Delta x$  and one for

$\Delta y$ , are generated for the training process.

The decoding of the spiking output is determined by the difference in the firing rates of the output neurons within each sub-layer. Let us denote  $f^{x+}(t)$  and  $f^{x-}(t)$  as the firing rates of the first and second output neurons, respectively, in the x-direction sub-layer at time  $t$ . The equation for decoding this activity can be expressed as:

$$\Delta x_{decoded} = \left[ \sum_{i=t-\Delta T}^t (f^{x+}(i) - f^{x-}(i)) \right] \Delta X_{max} \quad (5.11)$$

A similar process is applied for decoding in the y-direction:

$$\Delta y_{decoded} = \left[ \sum_{i=t-\Delta T}^t (f^{y+}(i) - f^{y-}(i)) \right] \Delta Y_{max} \quad (5.12)$$

The dynamic model of agents can be represented as,

$$\dot{X}(t) = \frac{\Delta x_{decoded}}{\Delta T} \quad (5.13)$$

$$\dot{Y}(t) = \frac{\Delta y_{decoded}}{\Delta T} \quad (5.14)$$

where  $\Delta T$  is the time window the network updates weights.

One of the challenges in robotic applications is ensuring smooth transitions in actions to prevent abrupt and potentially harmful changes. To address this, the recursive random number generation method is used to produce correlated random numbers. This method ensures that the current displacements of the robot are influenced by its previous displacements, leading to smoother transitions. The recursive random number generation can be formulated as,

$$\Pi_t = \gamma \cdot \Pi_{t-1} + (1 - \gamma) \cdot \epsilon_t \quad (5.15)$$

where  $\Pi_t$  is the random action at time  $t$ ,  $\gamma$  is a correlation coefficient, and  $\epsilon_t$  is a random number drawn from a standard distribution (e.g., Gaussian) at time  $t$ . This equation ensures

that the random action at any given time  $t$  is a weighted combination of the previous action and a new random number.

### 5.2.2 Training algorithm

The **R-STDP** algorithm is a learning technique inspired by biological processes in the brain, which is believed to be fundamental to certain learning processes [57]. The algorithm's core principle is that when a pre-synaptic neuron activates just before its post-synaptic counterpart, the synapse's strength connecting them should increase, and vice versa if the post-synaptic neuron fires first.

Within the **SNN** framework, pre-synaptic neurons are the input neurons, and post-synaptic neurons function as the output neurons. The function  $STDP(\tau)$  can be defined as the firing timelines of both input and output neurons [58] as,

$$STDP_{kl}(\tau) = \mathcal{A} \exp\left(-\frac{\tau}{\tau_s}\right) \text{ for } \tau \geq 0 \quad (5.16)$$

where  $\mathcal{A}$  stands as the exponential function's amplitude, and  $\tau$  is the difference between the firing time of the input neuron ( $k$ ) and output neuron ( $l$ ). Meanwhile,  $\tau_s$  acts as the time constant, setting the decay rate for the **R-STDP** function. Should  $\tau_s$  approach infinity, the exponential function converges to 1, neutralizing time's effect on the **R-STDP** function.

The adjustment of synaptic weights follows the given equation:

$$\dot{W}_{kl}(t) = STDP_{kl}(\tau)\mathcal{R}(t) \quad (5.17)$$

where  $\dot{W}_{kl}(t)$  denotes the rate of change of the synaptic weight that connects neurons  $k$  and  $l$ . This weight determines the input that the post-synaptic neuron receives upon the spiking of its pre-synaptic neuron, which is quantified as  $I(t)$ . The term  $\mathcal{R}(t)$  represents the reward that is received at time  $t$ .

$$\mathcal{R}_{Fi}^{Fj}(t) = \mathcal{C}_{Fi}^{Fj} \left[ r_{Fi}^{Fj}(t-1) - r_{Fi}^{Fj}(t) \right] \tanh(r_{Fi}^{Fj}(t) - r_{cmd}^{Fi}) \quad (5.18)$$

$$\mathcal{R}_{Fi}^L(t) = \mathcal{C}_{Fi}^L [r_{Fi}^L(t-1) - r_{Fi}^L(t)] \tanh(r_{Fi}^L(t) - r_{cmd}^L) \quad (5.19)$$

where,  $\mathcal{R}_{Fi}^{Fj}$ ,  $r_{Fi}^{Fj}$ , and  $r_{cmd}^{Fi}$  denote the reward, distance, and commanded distance between two  $i$  and  $j$  follower agents, respectively. Similarly,  $\mathcal{R}_{Fi}^L$ ,  $r_{Fi}^L$ , and  $r_{cmd}^L$  represent the reward, distance, and the commanded distance between the follower agent  $i$  and the Leader ( $L$ ), respectively. The  $\mathcal{C}_{Fi}^{Fj}$  and  $\mathcal{C}_{Fi}^L$  show the reward coefficients and the  $\tanh(r_{Fi}^{Fj}(t) - r_{cmd}^{Fi})$  and  $\tanh(r_{Fi}^L(t) - r_{cmd}^L)$  functions determine the reward's sign according to the agents' relative distance and the commanded distance. The expressions  $r_{Fi}^{Fj}(t-1) - r_{Fi}^{Fj}(t)$  and  $r_{Fi}^L(t-1) - r_{Fi}^L(t)$  specify the magnitude of the instantaneous reward.

If an agent finds itself farther away from the commanded distance than a neighboring agent or the leader, it will be rewarded positively for decreasing its distance. Conversely, moving closer results in a negative reward if the agent is within the commanded distance from a neighboring agent or the leader. This system is designed to encourage the maintenance of a commanded distance: being too far away from the commanded distance invites a penalty. At the same time, positive reinforcement is given for closing the gap between the current distance and the commanded distance.

One of the challenges in R-STDP is the unbounded growth or decay of synaptic weights, which can impede stable and effective learning in neural networks. The following section introduces a novel method focused on learning rate and weight stabilization to address this challenge and enhance the algorithm's applicability. This proposed method, designed to regulate synaptic weight changes, ensures a balanced and controlled learning process. It innovatively incorporates an Adaptive Decay Rate technique designed to maintain stability in synaptic weight adjustments, thereby significantly improving the performance and reliability of R-STDP in SNNs.

### 5.2.3 Weight Stabilization using Reward-Modulated Competitive Synaptic Equilibrium (R-CSE)

Controlling the excessive increase of synaptic weights in SNNs is important to maintain network stability and function. If not controlled, this growth can lead to saturation, affecting the network's ability to learn and adapt. When the network receives fuzzy sets of firing strengths as input, the synaptic weights grow in a pattern influenced by the Gaussian function's shape used for fuzzy encoding. Imposing a limit on synaptic weights disrupts this growth pattern over time, leading to all synaptic weights eventually maxing out. Weight normalization, while preventing excessive growth in one part of the network, can inhibit overall growth; when a synaptic connection reaches its maximum, its activation subsequently diminishes other weights.

Traditional methods like L1 regularization and weight decay employ a constant decay rate, which can slow the network's responsiveness to changes in rewards. Alternatively, the Bienenstock, Cooper, and Munro (BCM) method, a more advanced approach, dynamically adjusts both a threshold and a decay rate in response to input variations. However, this method does not provide a control mechanism for the fuzzy inputs. In this paper, we introduce a method called R-CSE to manage the unbounded growth of synaptic weights while maintaining the gradient in the synaptic weights matrix formed due to differences in firing strength from fuzzy membership functions while dynamically adjusting the network when the reward changes.

Let us define  $\alpha$  as the learning rate matrix. We will also use  $\mathcal{S}$  to represent the set of neurons that fired at time  $t$  in one of the network sections. If we consider  $W_{max}^{\mathcal{S}}(t)$  as the maximum weight among the firing neurons in set  $\mathcal{S}$ , then we can characterize the learning rate using a Sigmoid function. This function gradually transitions from 1 to 0 as the learning process advances, as explained below:

$$\alpha^{\mathcal{S}}(t) = \frac{1}{1 + \exp(|W_{max}^{\mathcal{S}}(t)| - \Psi^{\mathcal{S}})}, \quad \left( \Psi^{\mathcal{S}} = \frac{\mathcal{R}_{max}^{\mathcal{S}}}{\mathcal{R}_{max}^G} I^{max} \right) \quad (5.20)$$

where  $\mathcal{R}_{max}^S$  is the maximum reward in the network section (e.g.,  $\max(\mathcal{R}_{Fi}^{Fj})$ ), and  $\mathcal{R}_{max}^G = \max(\mathcal{R}_{Fi}^{Fj}, \mathcal{R}_{Fi}^L)$ . This model determines the learning rate by the highest synaptic weight among the active input and output neurons. This mechanism is similar to the “winner-takes-all” approach. When a synaptic connection reaches its weight limit, it prevents further changes in the adjacent synaptic weights.

The network contains a variety of reward functions, each with its own maximum and minimum values. The highest reward in specific connections sets the limit for the synaptic weight in that area. The synaptic weight limit is linked to the ratio of the local maximum reward to the global maximum reward. As a result, the network section with the highest local maximum reward ( $\mathcal{R}_{max}^S = \mathcal{R}_{max}^G$ ) attains the maximum synaptic weights ( $\Psi^S = I^{max}$ ), while sections with lower local maximum rewards reach only a proportional fraction of the maximum weight. This proportion is based on the local maximum reward in relation to the global maximum reward. The adjustment of the learning rate transforms into a competitive algorithm, modifying the growth rate of individual synaptic weights by considering partial network parameters.

A significant challenge in learning algorithms is their capacity to adapt to changes in rewards. Commonly, once the learning rate reduces to zero, weight adjustments stop. To address this, a variable decay rate is introduced to prevent weights in each network section from remaining at their peak values indefinitely. In our method, the decay rate is represented as a matrix, and it is calculated using the SoftPlus function, enabling it to adjust according to the current stage of learning. This method ensures that weight modifications continue to respond effectively to changes in the learning environment.

This paper defines the decay rate as a function of the maximum synaptic weight among neurons in the set  $\mathcal{S}$ . This approach is designed to address a critical aspect: when the maximum synaptic weight in  $\mathcal{S}$  reaches its peak ( $|W_{max}^S(t)| = \Psi^S$ ), it is essential that the learning rate remains above zero. This condition is necessary to allow weight change and prevent the learning rate from stagnating at zero. Simultaneously, the learning rate must not exceed the maximum acceptable weight change, which is  $\mathcal{A} \times \mathcal{R}_{max}^G$ . With these considerations, we

propose that the decay rate should be set to  $\mathcal{A}/\lambda \times \mathcal{R}_{max}^G$  when  $|W_{max}^S(t)| = \Psi^S$  and increase to  $\lambda\mathcal{A} \times \mathcal{R}_{max}^G$  when  $|W_{max}^S(t)| = 2\Psi^S$ , where  $\lambda$  is a coefficient that controls the rate of decay when  $|W_{max}^S(t)| > \Psi^S$ . By applying the mentioned condition and solving for the SoftPlus function, the decay rate function can be obtained as follows,

$$\Theta^S = \left( \frac{\eta}{\beta} \right) \log \left( 1 + \exp \left[ \beta \left( |W_{max}^S(t)| - \Psi^S \right) \right] \right) \quad (5.21)$$

where  $\eta = \frac{\mathcal{A}\mathcal{R}_{max}^G \ln(2^{\lambda^2}-1)}{\lambda\Psi^S \log(2)}$  and  $\beta = \frac{\ln(2^{\lambda^2}-1)}{\Psi^S}$ . Therefore, (5.21) can be represented as,

$$\Theta^S = \left( \frac{\mathcal{A}\mathcal{R}_{max}^G}{\lambda \log(2)} \right) \log \left( 1 + \exp \left[ \left( \frac{\ln(2^{\lambda^2}-1)}{\Psi^S} \right) \left( |W_{max}^S(t)| - \Psi^S \right) \right] \right) \quad (5.22)$$

The choice of setting the decay rate to  $\lambda\mathcal{A} \times \mathcal{R}_{max}^G$  when  $|W_{max}^S(t)| = 2\Psi^S$  is based on the feature of reward coefficients. Specifically, when the reward coefficient increases, leading to  $|W_{max}^S(t)| < \Psi^S$ , the  $|W_{max}^S(t)|$  is allowed to increase. Conversely, a decrease in the reward coefficient, resulting in  $|W_{max}^S(t)| > \Psi^S$ , necessitates a higher decay rate to reduce the maximum synaptic weight back to  $\Psi^S$ . Incorporating the **R-CSE** method into (5.17), the enhanced version of the **R-STDP** method is expressed as follows,

$$\dot{\mathbf{W}}(t) = \boldsymbol{\alpha} \odot \mathbf{STDP}(\tau) \odot \mathcal{R}(t) - \boldsymbol{\Theta}_{ij} \odot \text{sgn}(\mathbf{W}) \quad (5.23)$$

where  $\odot$  is the Hadamard product.

When  $|W_{max}^S(t)| < \Psi^S$ , the reward adjusts the synaptic weights, and there is no weight decay to decrease the learning time. When  $|W_{max}^S(t)| > \Psi^S$ , the decay rate changes the synaptic weights and brings the maximum weight to the reward zone, where  $|W_{max}^S(t)| < \Psi^S$  and the networks responds to reward change.

The **R-CSE** method addresses the challenge of unbounded growth in synaptic weights within **SNNs**. By integrating a dynamic decay rate governed by the SoftPlus function, **R-CSE** ensures that synaptic weight adjustments remain responsive to learning stages and reward changes. This method not only preserves the growth pattern induced by fuzzy input firing strengths but also provides a balanced approach to weight adjustment, preventing

saturation and facilitating continual learning adaptability. Moving forward, we will explore the integration of **FL** in the learning process.

### 5.2.4 Federated Learning for Consensus Flying

In **FL**, a key challenge is centralizing various models on one server. This process must effectively combine these models to create a unified global model without compromising the specific adjustments made to each model. A critical strategy involves choosing models that contain substantial information. Another significant aspect is determining the frequency of model aggregation. Shorter intervals between aggregations can enhance learning efficiency but may strain network resources, particularly as the number of participating agents and devices grows. Conversely, longer intervals might slow down the learning process due to delayed updates of the global model. This section proposes an aggregation method for **SNN**. Our focus is on reducing network usage and energy consumption.

Asynchronous **FL** (AFL) has emerged as a significant advancement in federated systems, particularly in response to the challenges posed by device heterogeneity. This approach allows clients to upload their local model updates at different times rather than synchronously [59]. Such a method is particularly beneficial in reducing the negative impacts of device heterogeneity, which can include varying computational capacities and network connectivity among devices. In traditional **FL** setups, delays caused by poor network signals or unexpected client crashes can significantly prolong the time the server takes to receive updates from all clients. By adopting asynchronous aggregation, the server processes and aggregates models as they are received without synchronizing with all clients. This strategy accelerates the training process, making **FL** more efficient and adaptable to diverse client conditions.

Our proposed **FL** model aggregation algorithm aims to establish an efficient and dynamic system for global and local model publishing. This system relies on the similarity between consecutive global and local models and publishes updates only when significant changes are detected, thus avoiding redundant updates and improving overall efficiency. Unlike the uniform model updates in FedAvg [60], our approach allows individual agents to evaluate

and send their local models based on a similarity threshold with the global model, thereby enabling a potentially more effective update process. Our aggregation strategy emphasizes similarity metrics for model updates, which is not commonly emphasized in methods like FedNova [61], adding a layer of context sensitivity to our approach.

In our approach, considering the difference in agents' neural network parameters and maximum and minimum synaptic weights, the weights are normalized to align them on a uniform scale ranging from -1 to 1. This normalization process makes the neural model values comparable across the network. Based on the maximum and minimum synaptic weights outlined in (5.5), and taking into account the highest excitation ( $I^{max}$ ) and inhibition ( $-I^{max}$ ), the normalization of synaptic weights is performed as follows:

$$\bar{\mathbf{W}}_k(t) = \frac{1}{I_k^{max}} [\mathbf{W}_k(t)] \quad (5.24)$$

where  $\mathbf{W}_k(t)$  represents the matrix of synaptic weights,  $\bar{\mathbf{W}}_k(t)$  denotes the normalized synaptic weight matrix for agent  $k \in \{1, 2, 3, \dots\}$ , and  $I_k^{max}$  is the maximum synaptic weight for agent  $k$ .

The global model on the server (Leader) is then computed using a weighted average,

$$\bar{\mathbf{W}}_G(t) = \frac{\sum_{k=1}^N \omega_k \cdot \bar{\mathbf{W}}_k(t)}{\sum_{k=1}^N \omega_k} \quad (5.25)$$

where  $\bar{\mathbf{W}}_G(t)$  is the global normalized model on the central server,  $N$  is the number of agents, and  $\omega_k$  is the aggregation weight for each SNN model, defined as,

$$\omega_k = \frac{1}{\sqrt{mn}} \|\bar{\mathbf{W}}_k(t)\|_F \exp\left(-\frac{t - T_k}{\tau_{cs}}\right) \quad (t \geq T_k) \quad (5.26)$$

where the term  $\|\cdot\|_F$  is the Frobenius norm, and  $m$  and  $n$  are the dimensions of the matrix  $\bar{\mathbf{W}}_k(t)$ , used for normalizing the Frobenius norm.  $T_k$  indicates the time at which agent  $k$  last transmitted its local model to the central server, and  $\tau_{cs}$  is a time constant that reduces the weight to zero if there is no recent update from the agent.

Both agents and the central server employ an event-triggered mechanism for transmit-

ting local and global models. Throughout the training phase, each agent calculates the Euclidean distance between the most recent global model from the central server and its current synaptic weights matrix, as follows,

$$\mathcal{D}_a(\bar{\mathbf{W}}_k(t), \bar{\mathbf{W}}_G(T_{cs}) = \frac{1}{2\sqrt{mn}} \sqrt{\sum_{i=1}^m \sum_{j=1}^n (a_{ij} - b_{ij})^2} \quad (5.27)$$

where  $\mathcal{D}_a$  is the Euclidean distance on the agent side,  $T_{cs}$  is the time when the central server published the global model, and  $a_{ij}$  and  $b_{ij}$  are elements of the latest global model and the current local model, respectively. If this distance exceeds a certain threshold, set between 0 and 1, the agent transmits its model to the central server.

If the  $\mathcal{D}_a$  on the agent  $k$  reaches the threshold and it does not receive any update from the server, the agent sends its model to the server, and then it calculates the  $\mathcal{D}_a$  between current synaptic weights  $\bar{\mathbf{W}}_k(t)$  and the model it recently sent to the server  $\bar{\mathbf{W}}_k(T_k)$  until it receives a new model update from the central server.

The central server follows a similar procedure as the agents, evaluating the distance  $\mathcal{D}_G$  between the current and recently published model at time  $T_{cs}$ ,

$$\mathcal{D}_G(\bar{\mathbf{W}}_G(t), \bar{\mathbf{W}}_G(T_{cs})) = \frac{1}{2\sqrt{mn}} \sqrt{\sum_{i=1}^m \sum_{j=1}^n (a_{ij} - b_{ij})^2} \quad (t \geq T_{cs}) \quad (5.28)$$

Incorporating the proposed **FL** method with the **R-CSE** algorithm, the modified **R-STDP** equation can be represented as follows,

$$\dot{\mathbf{W}}_k(t) = (1 - \delta(t - T_{cs})) [\boldsymbol{\alpha} \odot \text{STDP}(\tau) \odot \mathcal{R}(t) - \boldsymbol{\Theta} \odot \text{sgn}(\mathbf{W}_k(t))] + \delta(t - T_{cs}) I_k^{max} (\bar{\mathbf{W}}_G(t) - \bar{\mathbf{W}}_k(t)) \quad (5.29)$$

where  $\delta$  is the Dirac delta function. Algorithm 3 shows the step-by-step implementation process of the proposed method.

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**Algorithm 3** High-Level Algorithm for the Proposed FL Algorithm

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**Require:** Initialization of Central Server and Agents**Ensure:** Updated Global Model on the Central Server and Local Models on Agents

```

1: Initialize the agents and Central Server with default parameters for model publication
   threshold, Euclidean distance, and model publish status
2: Initialize the Global Model on the Central Server
3: if  $t$  is greater than 0 then
4:   Normalize synaptic weights of local models using (5.24)
5:   Aggregate models from all agents at the Central Server using (5.25)
6:   Calculate the  $\mathcal{D}_G$  between the current and previous global models on the Central
   Server
7:   if  $\mathcal{D}_G >$  the Central Server's threshold then
8:     Publish the global model
9:     set  $T_{cs} = t$ 
10:    end if
11:    for each Agent in the network do
12:      if Central Server publishes a new global model then
13:        Update the local model of the Agent with the global model
14:      else
15:        Agents evaluate their local models against the latest global model ( $\mathcal{D}_a$ ) using
           (5.27)
16:        if  $\mathcal{D}_a >$  the Agent's threshold then
17:          Send the model to the Central Server
18:          set  $T_k = t$ 
19:        end if
20:      end if
21:    end for
22:  end if

```

---

The proposed algorithm allows agents to communicate less often and save energy. It does this by only sending essential updates to the Central Server, which helps when there are many agents with different network models and communication interfaces. This method reduces unnecessary data transmission, making the whole system more efficient. It also decides which agent updates are important based on how much they change the global model.

## 5.3 Results and Discussion

In this section, we conducted a numerical simulation to validate the performance of the proposed method. The simulation involves a group of five agents flying around a leader who is moving in a circular path. Initially, a scenario without implementing [FL](#) was conducted to evaluate the performance of the [SNN](#) in achieving coordinated flight. During this phase, the effect of the change in reward was simulated to examine the [R-CSE](#) method. The results from this phase were then compared to those obtained using a [Fuzzy Actor-Critic Learning \(FACL\)](#) algorithm. In the second part of the simulation, the proposed [FL](#) aggregation algorithm is used, where the leader agent acts as a central server. Finally, the algorithm was tested both before and after changing the rewards.

### 5.3.1 Simulation without FL

In this simulation, we modeled five agents, each equipped with its own [SNN](#) model, capable of reaching a maximum speed of  $1 \text{ m/s}$ . The architecture of each agent's neural network included 72 input neurons. Since each agent was designed to detect three distinct objects within its environment, the input layer was organized into sub-layers, with 24 neurons dedicated to each object. The network's output layer comprised 4 neurons, divided equally to represent  $\Delta x$  and  $\Delta y$  movements. The [SNN](#) model in the simulation is a fully connected network, and the parameters of the [LIF](#) neuron are also represented in Table 5.1.

Table 5.1: Parameter values for LIF neuron model [62]

Parameter	Value	Description
$R_m$	40 MΩ	Membrane Resistance
$\tau_m$	30 ms	Membrane time constant
$E_l$	-70 mV	Resting potential
$V_{res}$	-70 mV	Reset potential
$V_0$	-70 mV	Initial membrane potential
$V_{th}$	-50 mV	Threshold membrane potential

The R-STDP mechanism updated synaptic weights at 10 ms intervals. During these intervals, the learning algorithm adjusted the agent's states based on received data from other agents and the leader while simultaneously generating random outputs as part of an exploration strategy.

Table 5.2: Simulation Parameters

Parameter	Value	Description
$\Delta T$	10 ms	Weight and state update sample time
$\tau_s$	2 ms	Time constant for R-STDP
$\mathcal{A}$	1	Amplitude in R-STDP function
$\lambda$	5	Decay rate coefficient
$\Delta x$ and $\Delta y$	0.01 m	Max step per $\Delta T$
$\sigma$	0.5	Gaussian function's std. deviation
$\Delta t$	1 ms	Minimum inter-spike interval
$I^{min}$	0.5	Lower bound of synaptic weight
$I^{max}$	15.5	Upper bound of synaptic weight
$\gamma$	0.95	Correlation Coefficient

Table 5.2 shows the simulation parameters. The simulation was done in a 10 m by 10 m area, and the leader followed a circular path centered in (5,5) with a 2.5 m radius and a 0.1 m/s speed.

In order to monitor the swarm performance, the minimum and maximum distances of each agent from other agents and the minimum and maximum distances of the swarm from the leader were measured. Figure 5.4 shows the definition of the distances.

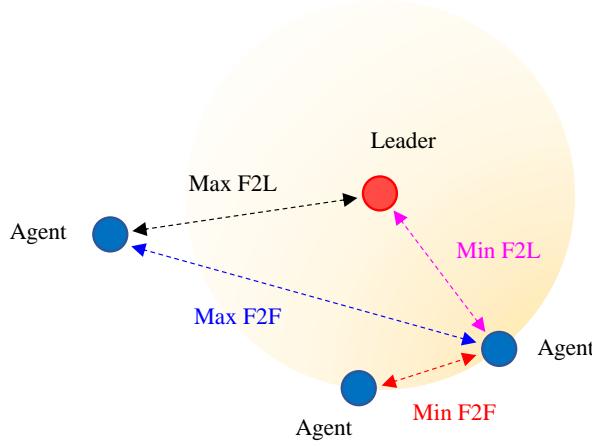


Figure 5.4: The measured distances during the test for evaluating the performance and detecting the collisions.

The simulation included two phases. During the initial phase, the objective was for the agents to learn to maintain the commanded distance from each other and the leader. This phase took 600 seconds for training, and the reward coefficient among followers ( $\mathcal{C}_{Fi}^{Fj}$ ) was set at 0.02, while the coefficient between followers and the leader ( $\mathcal{C}_{Fi}^L$ ) was set at 0.07. These parameters were derived from a series of numerical simulations. A higher value of  $\mathcal{C}_{Fi}^L$  signifies an increased emphasis on the leader's role in the learning process.

To ensure a fair comparison between different learning methods, we have compared our proposed approach with the **FACL** algorithm [63]. We opted for a fuzzy controller as it provides an explanation for how the **SNN** works. The FACL algorithm consists of two components, an actor and a critic. The actor is a fuzzy controller whose output serves as the control signal. The critic is a fuzzy inference system that stores the state value and represents the value function. The actor's output, which is the control signal, is computed as follows:

$$u_t = \sum_{l=1}^L \Phi^l \omega_t^l, \quad (5.30)$$

where  $u_t$  is the control signal at time  $t$ ,  $L$  is the total number of the rules,  $\omega_t^l$  is the output parameter of rule  $l$  at time  $t$ , and  $\Phi^l$  is the firing strength of rule  $l$ , which is calculated as

follows,

$$\Phi^l = \frac{\partial u}{\partial \omega_l} = \frac{\prod_{i=1}^n \mu_i^{F_i^l(x_i)}}{\sum_{l=1}^L (\prod_{i=1}^n \mu_i^{F_i^l(x_i)})}, \quad (5.31)$$

where  $\mu_i^{F_i^l(x_i)}$  is the membership degree of the  $i$ th membership function for rule  $l$ . The critic stores an approximation of the value function. In this paper, we show the critic's output at time  $t$  with  $\hat{V}_t$ , which is as follows,

$$\hat{V}_t = \sum_{l=1}^L \Phi^l \zeta_t^l, \quad (5.32)$$

where  $\zeta_t^l$  is the output parameter of rule  $l$  at time  $t$ . Finding the proper values for  $\omega^l$  and  $\zeta^l$  concerning a reward is the training purpose in the **FACL** algorithm.

To train the followers, five initial sets of  $\omega^l$ 's and  $\zeta^l$  are created and set to zero. Each follower generates an action with (5.30). The value of  $u_t$  is perturbed via a Gaussian noise with a mean of 0 and variance of  $\varsigma$  ( $u'_t = u_t + n(0, \varsigma)$ ). The agents take action  $u'_t$  and move to a new state. The reward function returns a signal corresponding to the quality of the actions. In this section, we implemented the reward functions in (5.18) and (5.19), where the weighting coefficients are set to 1. The temporal difference  $\Delta$  is calculated for each agent as follows,

$$\Delta = \mathcal{R}_t + \Gamma \hat{V}_{t+1} - \hat{V}_t, \quad (5.33)$$

where  $\mathcal{R}_t$  is the reward function and is the summation of (5.18) and (5.19). The actor is updated as follows,

$$\omega_{t+1}^l \leftarrow \omega_t^l + \rho \Delta (u'_t - u_t) \Phi^l. \quad (5.34)$$

The critic is updated as follows,

$$\zeta_{t+1}^l \leftarrow \zeta_t^l + \kappa \Delta \Phi^l. \quad (5.35)$$

In (5.34) and (5.35),  $\kappa$  and  $\rho$  are the critic's and actor's learning rates. Table 5.3 shows the parameters used for the **FACL** algorithm. It should be mentioned that seven membership functions are used for each input, and thus, the total number of rules is  $7 \times 7 \times 7 \times 7 \times 7 \times 7 = 117,649$ .

Table 5.3: Simulation Parameters for the FACL Algorithm

Parameter	Value	Description
$\kappa$	1.0	Critic's learning rate
$\rho$	0.5	Actor's learning rate
$\varsigma$	5	Added exploration noise
$\Gamma$	0.0	Discount factor

Figure 5.5 shows the simulation results for the **R-CSE** method. According to the results, the agents rapidly aligned around the leader within 6.89 seconds, and the maximum distance was reduced from 7.632 meters to the target distance of 2 meters. The swarm completed the formation around the leader in approximately 8.94 seconds, avoiding collisions.

As mentioned in section 3, the input encoding uses the error between current and commanded distance. Therefore, one of the advantages of the encoding and learning method in this paper is that the learned policies are independent of the commanded distance. Since the **SNN** uses the distance error, the commanded distance can be changed after training. Figure 5.7 shows the response of the agents to change in commanded distance after training. According to this figure, when the commanded distance is changed at 30 seconds, the swarm immediately responds to this change in 2.98 seconds without disrupting the formation or any collision.

Figure 5.8 shows the simulation results for the FACL algorithm. The training time was 1000 seconds, and the algorithm converged to the final solution in 667.26 seconds. According to the results, the agents achieved successful formation in approximately 15.85 seconds. Similarly, Figure 5.10 shows the simulation results for the FACL algorithm, where the commanded distance is initially set to 2 m and at  $t = 30$ , the commanded distance changes to 4 m. The results show that it takes 4.35 seconds for the swarm to adapt to the new command. It is worth mentioning that in Figures 5.8 and 5.10, the distances converge to the commanded distance but stay within a bias. Increasing the number of membership functions can reduce the bias, but it increases the training time of the **FACL** algorithm.

After 600 seconds, the leader is changed into an obstacle, and its reward coefficient  $\mathcal{C}_F^L$  is changed to 0.0175. The reward sign function,  $\tanh$  in (5.19), is also changed to -1, so the reward function for the leader is changed as follows,

$$\mathcal{R}_{Fi}^L(t) = -\mathcal{C}_{Fi}^L [r_{Fi}^L(t-1) - r_{Fi}^L(t)] \quad (5.36)$$

When the leader is transformed into an obstacle, the encoding equation for the input layer must be changed. This is because the obstacle has no commanded distance, and the agents need to maintain a commanded distance only from each other. Therefore, the commanded distance from the obstacle encoder in the input layer must be removed. Therefore, (5.6) can then be rewritten as follows:

$$\mu_I(\phi_i) = \exp\left(-\frac{(\phi_i - \zeta)^2}{2\sigma^2}\right) \quad (5.37)$$

The simulation proceeded for an additional 1200 seconds, during which the synaptic weights were adjusted in accordance with the updated reward function. The results of the reward change are shown in Figure 5.11, which indicates that the agents quickly reduced their initial distance to the commanded distance. Simultaneously, the minimum distance from the obstacle, which was the leader, increased over time, indicating that the agents adapted their behavior to maintain a greater distance from the obstacle. Figure 5.12 shows the trajectory of each agent after the reward change.

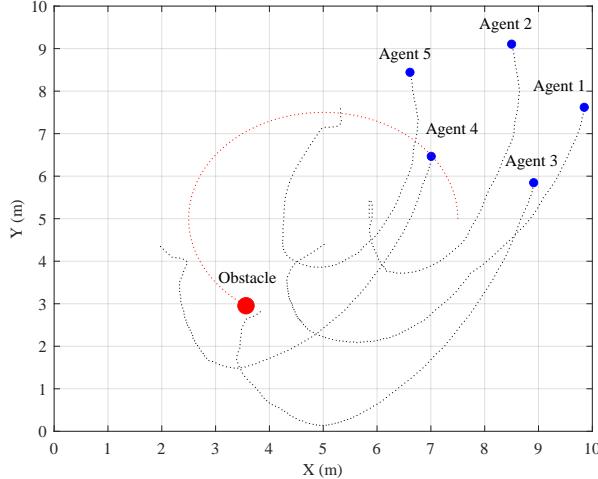


Figure 5.11: Agents' path after reward change (test phase)

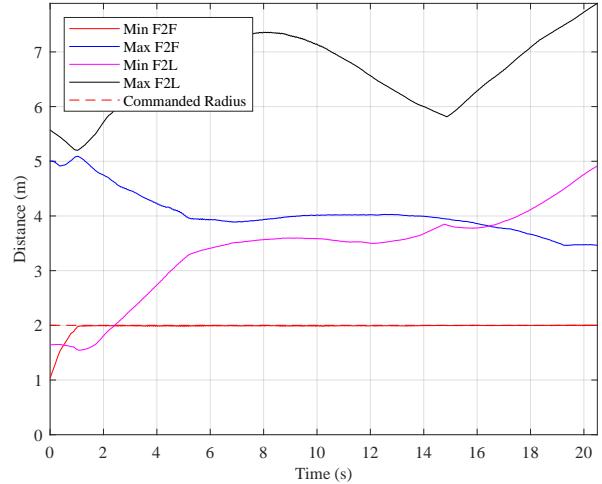


Figure 5.12: Distances after reward change (test phase)

In order to better understand the effect of reward change on SNN, the synaptic weights matrix before and after reward change has been illustrated in Figures 5.13 and 5.14, the vertical axis shows the output neurons. The first output neuron is for negative displacement in the x-direction, while the second output neuron is dedicated to positive displacement in the x-direction. Similarly, the third output neuron corresponds to negative displacement in the y-direction and the fourth output neuron to positive displacement in the y-direction. The horizontal axis shows the input neurons. The neuron IDs from 1 to 24 are for the first sub-layer dedicated to the neighboring follower. The network has two sub-layers for the neighboring follower agents, but only one is shown since they are similar in the case of synaptic weight values. The neuron numbers from 25 to 48 are for the sub-layer dedicated to the leader. The R-CSE method aims to maintain the synaptic weight matrix gradient while adapting to changes in the reward signal.

Considering the numerical values presented in Table 5.2 along with the reward coefficients  $C_{F_i}^{Fj} = 0.02$  and  $C_L^{Fj} = 0.07$ , and  $r_{F_i}^{Fj} = 1 \text{ m/s}$  and  $r_{F_i}^L = 0.1 \text{ m/s}$ , the maximum rewards at each weight update interval ( $\Delta T$ ) for  $\mathcal{R}_{F_i}^{Fj}$  and  $\mathcal{R}_{F_i}^L$  are calculated as  $4 \times 10^{-4}$  and  $7.7 \times 10^{-4}$ , respectively. Consequently,  $\mathcal{R}_{max}^G = \max(\mathcal{R}_{F_i}^{Fj}, \mathcal{R}_{F_i}^L) = 7.7 \times 10^{-4}$ . The  $\Psi^S$

for the follower section in the network is  $\left[ \frac{4 \times 10^{-4}}{7 \times 10^{-4}} \right] 15.5 = 8.0519$ , and for the leader section, it is  $\left[ \frac{7 \times 10^{-4}}{7 \times 10^{-4}} \right] 15.5 = 15.5$ . The  $\eta$  and  $\beta$  for the follower section within the network are  $\frac{\mathcal{AR}_{max}^G \ln(2^{\lambda^2}-1)}{\lambda \Psi^S \log(2)} = 0.0011$  and  $\beta = \frac{\ln(2^{\lambda^2}-1)}{\Psi^S} = 2.152$ , respectively. For the leader section, these values are  $\frac{\mathcal{AR}_{max}^G \ln(2^{\lambda^2}-1)}{\lambda \Psi^S \log(2)} = 5.719 \times 10^{-4}$  and  $\beta = \frac{\ln(2^{\lambda^2}-1)}{\Psi^S} = 1.118$ , respectively.

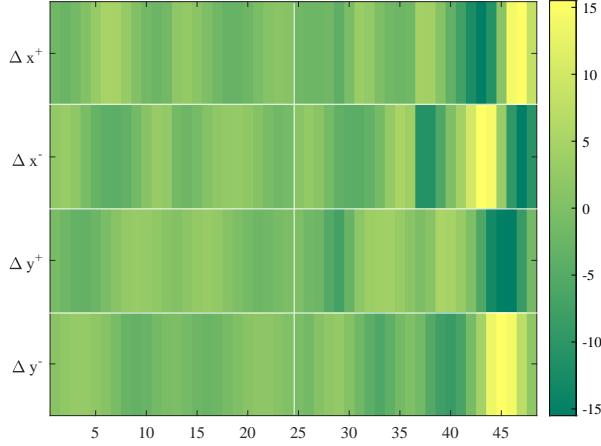


Figure 5.13: Synaptic Weights before Reward change

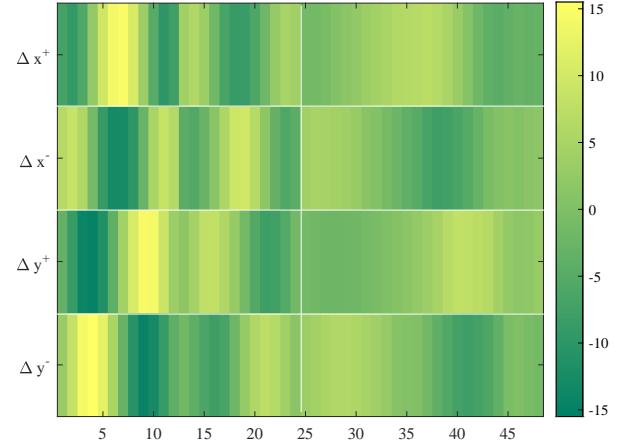


Figure 5.14: Synaptic Weights after Reward change

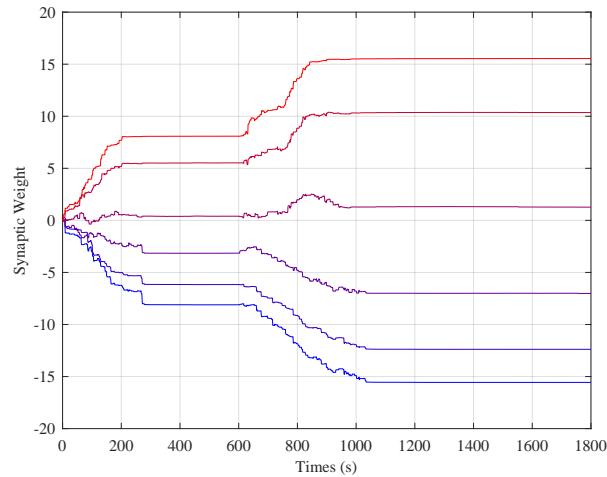


Figure 5.15: Synaptic weights increase after reward change

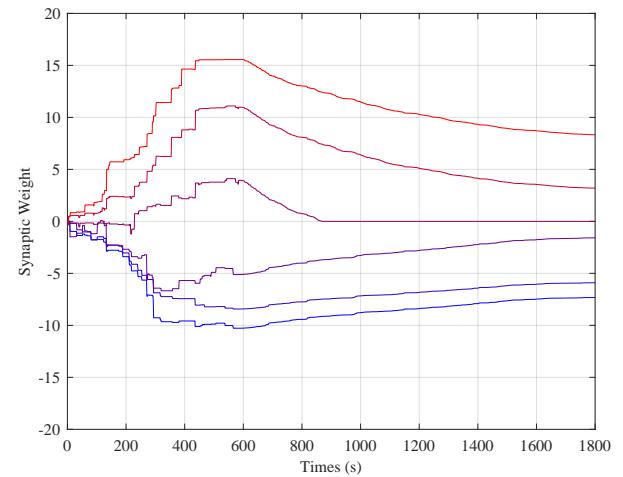


Figure 5.16: Synaptic weights decrease after reward change

According to Figure 5.13, we can see a gradient formed because of the fuzzy nature

of the input. Since the reward coefficients for followers and leaders are different, there is a difference in the maximum allowed synaptic weight for them. The proposed method for controlling the unbounded growth of synaptic weights has successfully stabilized the network while maintaining the fuzzy patterns of the synaptic connections.

Figure 5.14 shows the synaptic weights after the reward change. In this case, since the reward coefficients are changed, the  $\eta$  and  $\beta$  values are changed for the represented sub-layers, and the proposed method has helped the R-STDP algorithm to adjust the weights based on the new situation in the environment.

### 5.3.2 Simulation with FL and R-CSE

In this section, the proposed aggregation algorithm is tested. In this case, the agents only send their models when the Euclidean distance between the current and previously published model or the latest global model reaches a threshold. In the first phase, the simulation was done in 600 seconds, and the agents learned to follow the leader. The threshold for publishing the agents' and server models was 0.0005 and 0.00051, respectively. The reason for choosing the server's threshold a little bit higher than the agents' is that as soon as the first agent sends its model to the server, the Euclidean distance between the current and previously published model by the server reaches 0.0005, and the server distributes the model immediately. Therefore, the serve's threshold is set higher than the agents' threshold so that it waits for the other agents to send their models.

Figure 5.17 shows the distances between agents and the leader before the reward change. According to the figure, the agents converge to the solution faster than the non-federated learning scenario without any error. Figure 5.18 shows the simulation results for the reward change scenario. According to the figure, the proposed aggregation method has improved the learning performance so that the swarm converges to the solution in 6 seconds.

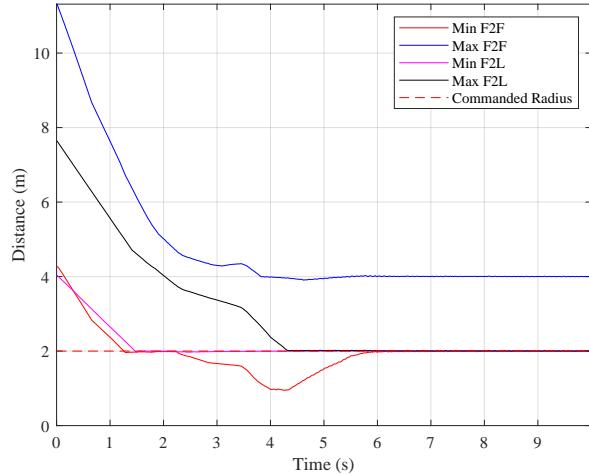


Figure 5.17: Distances during the test phase before reward change in the proposed aggregation method.

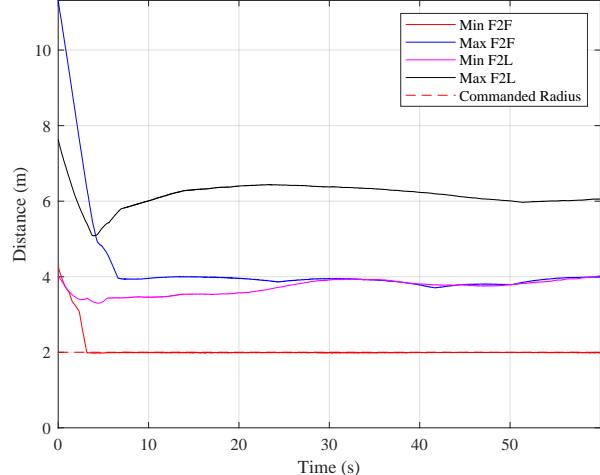


Figure 5.18: Distances during the test phase after reward change in the proposed aggregation method.

The norm of the synaptic weights can represent the changes in the synaptic weights due to the change in the environment during the training process, which can be used as an index to adjust the learning process in SNNs. The proposed aggregation method helps SNN models converge into a single model. Agents communicate with the Central Server (leader) during the training process, and Figure 5.20 shows the communication times. The aggregation sample time is small at the beginning of the training and increases as the SNN models converge to the final solution. The rate of change of the Frobenius norm determines the principle of the aggregation process, which results in small intervals of aggregation when the change rate is high, and larger intervals when it reduces.

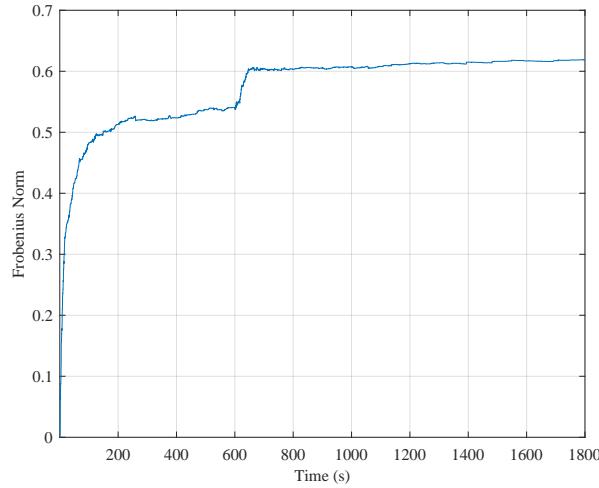


Figure 5.19: Frobenius norm of the agents during the learning phase. The reward changes for the Leader after 600 s.

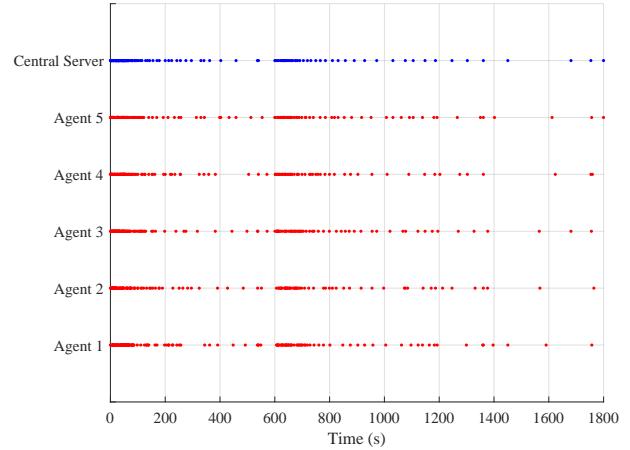


Figure 5.20: Communication times for agents and the Central Server (Leader). Red and blue dots show the times that agents and the Central Server have sent their model, respectively.

Therefore, the aggregation frequency is very high initially, and it reduces after the change in synaptic weights goes to zero because of the learning rate in (5.20). Also, after the reward changes and the leader becomes an obstacle after 600 seconds, the Euclidean distance between the converged and current models increases and reaches the threshold. As soon as the first agent sends its model to the server, the aggregation process starts again, and the agents adjust the associated synaptic weight.

Table 5.4: Comparative Performance Analysis of the Proposed Aggregation Algorithm+[R-CSE](#), [R-CSE](#), and [FACL](#)

	<a href="#">FL+R-CSE</a>	<a href="#">R-CSE</a>	<a href="#">FACL</a>
<b>Learning Time - Training Phase (s)</b>	261.92	554.71	667.26
<b>Max Error After Convergence - Test Phase (%)</b>	0.71	1.95	9.85
<b>Convergence Time - Test Phase (s)</b>	5.81	8.94	15.82

Table 5.4 compares the proposed Federated Learning (FL) algorithm with the non-FL approach and FACL algorithm. The comparison focuses on three critical metrics: learning time, maximum error after convergence, and convergence time. The proposed FL algorithm demonstrates significant improvements in terms of efficiency and accuracy, as evidenced by its considerably shorter learning and convergence times and a notable reduction in error after convergence.

## 5.4 Conclusion

In this paper, we presented a comprehensive approach addressing the challenges of uncontrolled growth in synaptic weights and the limited responsiveness of R-STDP to real-time changes within SNNs. Our proposed solution integrates the R-CSE method with a dynamic aggregation interval in FL, significantly enhancing learning time and performance. The R-CSE method introduces a novel mechanism to manage the unbounded growth of synaptic weights by dynamically adjusting the decay rate through the SoftPlus function. This adjustment is sensitive to the learning stages and rewards changes, ensuring that synaptic weight adjustments remain responsive over time. By addressing the challenge of synaptic weight saturation, the R-CSE method facilitates a balanced approach to weight adjustment, preventing network saturation and promoting continuous learning adaptability. We introduce a novel approach that uses FL in SNN and employs the Frobenius norm to adjust weighted aggregation in FL. Additionally, we include weight decay proportional to the time elapsed since an agent’s last model publication. This improves the efficiency and responsiveness of the learning process. Our model’s dynamic nature of the sample time adjusts based on the Euclidean norm. This metric measures the distance between the weight matrices of the agents and the server, determining reduced intervals for model publication. Our results show that the proposed aggregation method significantly accelerates agents’ learning and performs better than non-federated learning and FACL cases. Moreover, the dynamic aggregation interval effectively reduces communication overhead between the agents and the central server, particularly after model convergence. This reduction is critical in scenarios

where communication bandwidth is limited or costly. Our findings suggest that integrating R-STDP with federated learning, supported by our dynamic aggregation approach, provides a robust framework for advancing multi-agent reinforcement learning systems.

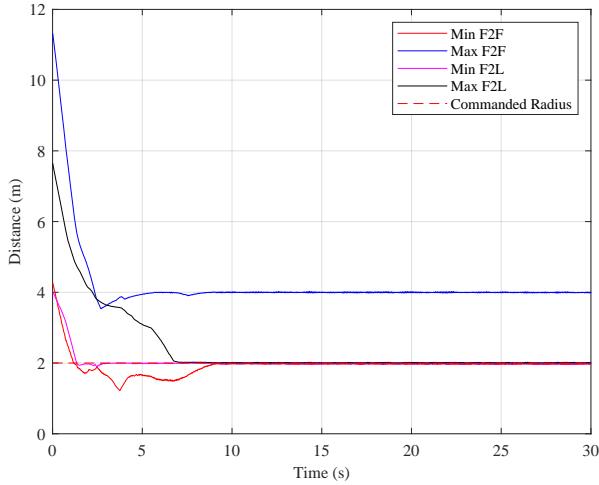


Figure 5.5: Distances during the test phase (R-CSE method)

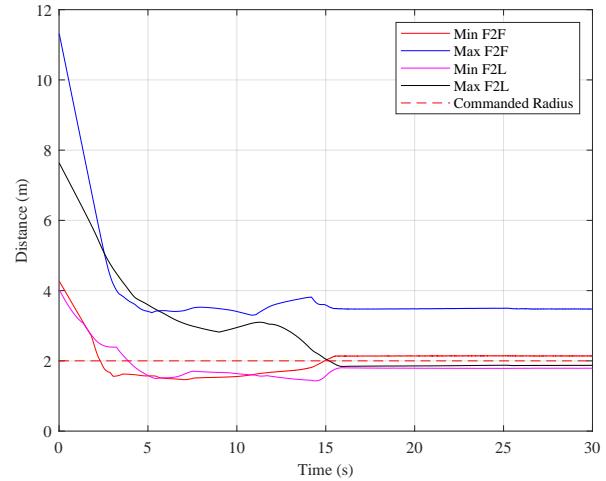


Figure 5.8: Distances during the test phase (FACL method)

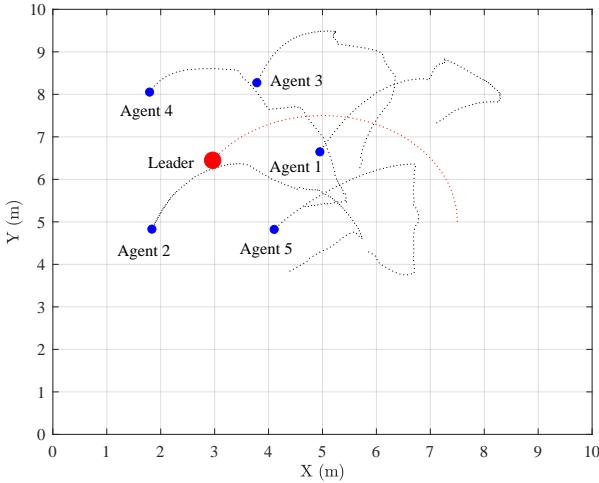


Figure 5.6: Agents' trajectory during the test phase (R-CSE method)

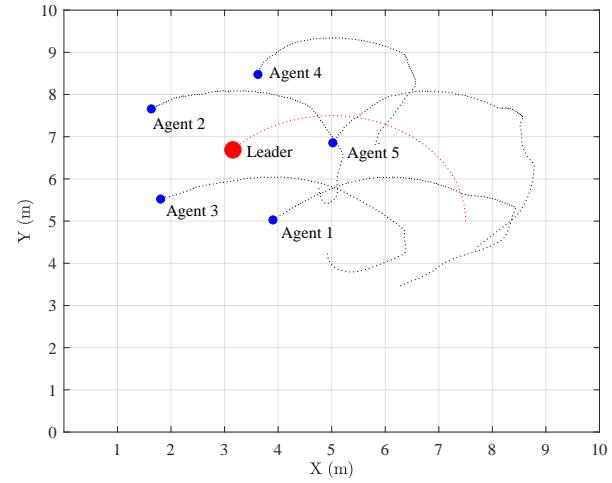


Figure 5.9: Agents' trajectory during the test phase (FACL method)

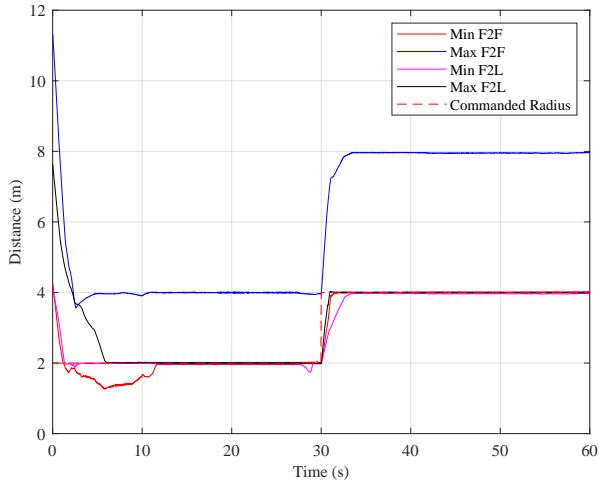


Figure 5.7: Change in commanded distance during the test phase (R-CSE method)

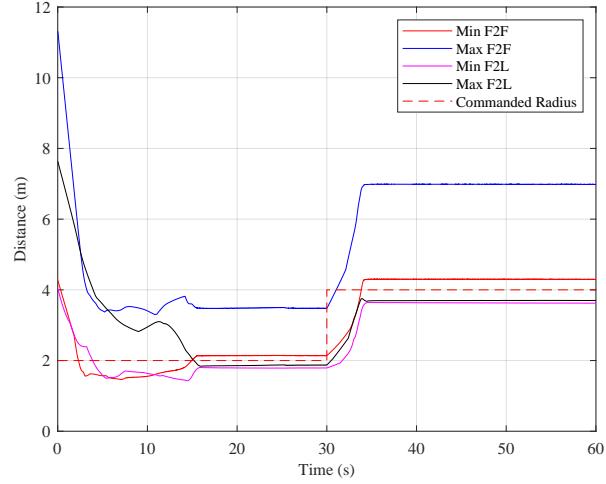


Figure 5.10: Change in commanded distance during the test phase (FACL method)

# **Chapter 6**

## **Proposed Method**

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