

U.S.N.

--	--	--	--	--	--	--	--	--	--

# BMS College of Engineering, Bangalore-560019

(Autonomous Institute, Affiliated to VTU, Belgaum)

## July / August 2017 Supplementary Semester Examinations

Course: **Theoretical Foundations of Computation**

Duration: **3 hrs**

Course Code: **15IS3DCTFC/ 15IS3DCTFE**

Max Marks: **100**

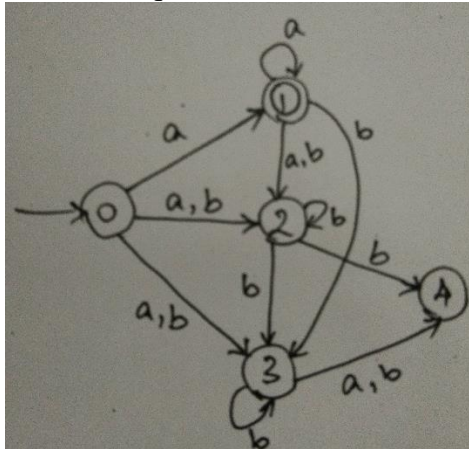
Date: 31.07.2017

**Instructions: 1. Answer any five full questions choosing one from each unit.**

**2. Assume missing data (if any) suitably**

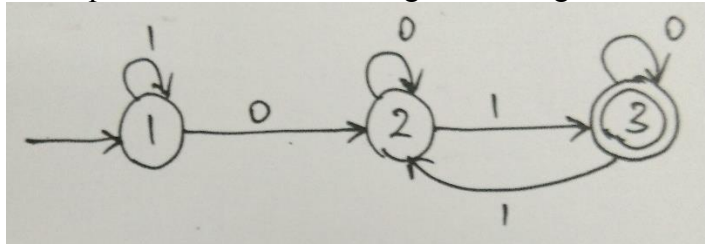
### UNIT 1

1. a) Construct DFA for the languages 10
  - i.  $L = \{ w \mid w \text{ has an even number of } a\text{'s and one or two } b\text{'s} \}$
  - ii.  $L = \{ w \mid w \in \{a,b,c\}^* \text{ and } w \text{ contains the pattern "abac"} \}$
  - iii.  $L = \{ w \mid w \text{ is a binary string divisible by } 4 \}$
- b) Convert the following NFA to its equivalent DFA. 10



### UNIT 2

2. a) What is regular expression? Convert the regular expressions to its equivalent automata. 10
  - i.  $a(ba)^*a^* \cup a(ba)^*b^*$
  - ii.  $(0+1)^*(011+01010)(0+1)^*$
- b) Obtain the regular expression for the following DFA using Kleene's theorem. 10



**OR**

3. a) Show that  $L = \{a^n b^l c^{n+1} \mid n, l \geq 0\}$  is not regular. **04**  
 b) Minimize the following DFA using Table-filling algorithm. **10**

$\delta$	0	1
A	B	E
B	C	F
*C	D	H
D	E	H
E	F	I
*F	G	B
G	H	B
H	I	C
*I	A	E

- c) Show that regular languages are closed under Intersection and Reversal. **06**

### UNIT 3

4. a) Obtain CFG to generate the following languages **06**  
 i.  $L = \{(1010)(0101)^n(1001)(1100)^n \mid n \geq 0\}$   
 ii.  $L = \{0^m 1^m 2^n \mid m \geq 1, n \geq 0\}$   
 b) Consider the CFG with the productions **09**  
 $S \rightarrow S+S \mid S-S \mid S^*S \mid S/S \mid (S) \mid a$   
 Write the leftmost derivation, rightmost derivation and parse tree for the strings  
 i.  $(a+(a+a)) + (a+a)$  ii.  $a+(a^*a)/a-a$   
 c) Explain the YACC Parser-Generator with an example. **05**

### OR

5. a) Show that the following CFG is ambiguous. **10**  
 $S \rightarrow aB \mid bA$   
 $A \rightarrow aS \mid bAA \mid a$   
 $B \rightarrow bS \mid aBB \mid b$   
 Also obtain the leftmost derivation for the string " $a^3 b^2 a b^3 a$ ".  
 b) Eliminate useless symbols from the given grammar **04**  
 $S \rightarrow aAa$   
 $A \rightarrow Sb \mid bCC \mid DaA$   
 $C \rightarrow abb \mid DD$   
 $E \rightarrow aC$   
 $D \rightarrow aDA$   
 c) Find the grammar in CNF equivalent to the grammar **06**  
 $S \rightarrow \sim S \mid [S \supset S] \mid p \mid q$

### UNIT 4

6. a) Design a PDA for the following grammar **06**  
 $S \rightarrow aA$   
 $A \rightarrow aABC \mid bB \mid a$   
 $B \rightarrow b$   
 $C \rightarrow c$   
 b) Define Pushdown Automata. Obtain a PDA to accept the language **08**  
 $L = \{w \mid w \in (a,b)^* \text{ and } n_a(w) > n_b(w)\}$  by a final state.

- c) Obtain CFG for the PDA given below: **06**
- $\delta(q_0, a, Z) = (q_0, AZ)$   
 $\delta(q_0, b, A) = (q_0, AA)$   
 $\delta(q_0, a, A) = (q_1, \varepsilon)$

#### UNIT 5

7. a) Obtain Turing Machine to accept the language **10**  
 $L = \{ ww^R \mid w \in (0,1)^* \}$
- b) Explain Post Correspondence Problem. Let  $A = \{11, 100, 111\}$  and  $B = \{111, 001, 11\}$  **10**  
 Does the pair  $(A, B)$  have PC-Solution? Does it have an MPC solution?

\*\*\*\*\*