Manual or Automatic

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Abstract

In the Motor Trend magazine, we looked for a answer about which trasmission is better for ratio mile per gallon (mpg). This report go throught the mtcar dataset supplied by R, with some Exploratory data analisys and differents models that helped to discover wich trasmission has a better impact to mpg.

Getting and Cleaning Data

```
##
                           cyl
                                             disp
         mpg
                                                               hp
                             :4.000
##
                                               : 71.1
                                                                : 52.0
    Min.
            :10.40
                     Min.
                                       Min.
                                                         Min.
                                       1st Qu.:120.8
##
    1st Qu.:15.43
                      1st Qu.:4.000
                                                         1st Qu.: 96.5
##
    Median :19.20
                     Median :6.000
                                       Median :196.3
                                                         Median :123.0
            :20.09
                             :6.188
                                               :230.7
                                                                 :146.7
##
    Mean
                     Mean
                                       Mean
                                                         Mean
##
    3rd Qu.:22.80
                     3rd Qu.:8.000
                                       3rd Qu.:326.0
                                                         3rd Qu.:180.0
            :33.90
                             :8.000
##
    Max.
                     Max.
                                       Max.
                                               :472.0
                                                         Max.
                                                                 :335.0
##
         drat
                            wt
                                            qsec
                                                               vs
##
    Min.
            :2.760
                     Min.
                             :1.513
                                       Min.
                                               :14.50
                                                         Min.
                                                                 :0.0000
##
    1st Qu.:3.080
                     1st Qu.:2.581
                                       1st Qu.:16.89
                                                         1st Qu.:0.0000
##
    Median :3.695
                     Median :3.325
                                       Median :17.71
                                                         Median : 0.0000
            :3.597
                             :3.217
                                               :17.85
                                                                :0.4375
##
    Mean
                     Mean
                                       Mean
                                                         Mean
##
    3rd Qu.:3.920
                     3rd Qu.:3.610
                                       3rd Qu.:18.90
                                                         3rd Qu.:1.0000
                             :5.424
                                               :22.90
##
    Max.
            :4.930
                     Max.
                                       Max.
                                                         Max.
                                                                 :1.0000
##
                                              carb
           am
                            gear
##
                              :3.000
                                                :1.000
    Min.
            :0.0000
                       Min.
                                        Min.
##
    1st Qu.:0.0000
                       1st Qu.:3.000
                                        1st Qu.:2.000
##
    Median :0.0000
                       Median :4.000
                                        Median :2.000
    Mean
            :0.4062
                       Mean
                               :3.688
                                        Mean
                                                :2.812
##
    3rd Qu.:1.0000
                       3rd Qu.:4.000
                                        3rd Qu.:4.000
                               :5.000
    Max.
            :1.0000
                       Max.
                                        Max.
                                                :8.000
```

The summary show that all features are numeric, let's investigate further.

str(df)

```
'data.frame':
                    32 obs. of 11 variables:
    $ mpg : num
                 21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
##
##
    $ cyl : num
                 6 6 4 6 8 6 8 4 4 6 ...
                 160 160 108 258 360 ...
##
    $ disp: num
    $ hp : num
                 110 110 93 110 175 105 245 62 95 123 ...
##
    $ drat: num
                 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
##
                 2.62 2.88 2.32 3.21 3.44 ...
    $ wt
         : num
    $ qsec: num
                 16.5 17 18.6 19.4 17 ...
                 0 0 1 1 0 1 0 1 1 1 ...
##
    $ vs
           num
          : num
                 1 1 1 0 0 0 0 0 0 0 ...
```

```
## $ gear: num 4 4 4 3 3 3 3 4 4 4 ...
## $ carb: num 4 4 1 1 2 1 4 2 2 4 ...
#am unique values
table(df$am)
##
## 0 1
## 19 13
#cyl unique values
table(df$cyl)
##
## 4 6 8
## 11 7 14
#vs unique values
table(df$vs)
##
## 0 1
## 18 14
#gear unique values
table(df$gear)
##
## 3 4 5
## 15 12 5
#carb unique values
table(df$carb)
##
## 1 2 3 4 6 8
## 7 10 3 10 1 1
There are different factor variable, they are going to be factorize.
## 'data.frame':
                   32 obs. of 11 variables:
## $ mpg : num 21 21 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 ...
## $ cyl : Factor w/ 3 levels "4", "6", "8": 2 2 1 2 3 2 3 1 1 2 ...
## $ disp: num 160 160 108 258 360 ...
## $ hp : num 110 110 93 110 175 105 245 62 95 123 ...
## $ drat: num 3.9 3.9 3.85 3.08 3.15 2.76 3.21 3.69 3.92 3.92 ...
## $ wt : num 2.62 2.88 2.32 3.21 3.44 ...
## $ qsec: num 16.5 17 18.6 19.4 17 ...
## $ vs : Factor w/ 2 levels "0", "1": 1 1 2 2 1 2 1 2 2 2 ...
## $ am : Factor w/ 2 levels "0","1": 2 2 2 1 1 1 1 1 1 1 ...
## $ gear: Factor w/ 3 levels "3", "4", "5": 2 2 2 1 1 1 1 2 2 2 ...
## $ carb: Factor w/ 6 levels "1","2","3","4",..: 4 4 1 1 2 1 4 2 2 4 ...
#sum of N/A values
sum(is.na(df))
## [1] 0
head(df,5)
```

mpg cyl disp hp drat wt qsec vs am gear carb

##

```
## Mazda RX4
                      21.0
                                160 110 3.90 2.620 16.46
## Mazda RX4 Wag
                      21.0
                             6
                                160 110 3.90 2.875 17.02
                                                                    4
                                                                         4
## Datsun 710
                      22.8
                                     93 3.85 2.320 18.61
                                258 110 3.08 3.215 19.44
## Hornet 4 Drive
                      21.4
                                                                    3
                                                                         1
                             6
## Hornet Sportabout 18.7
                             8
                                360 175 3.15 3.440 17.02
                                                                         2
```

Now df is clean and there are any missing values.

Exploratory data Analisys

```
## Estimate Std. Error t value Pr(>|t|)
## am0 17.14737 1.124603 15.24749 1.133983e-15
## am1 24.39231 1.359578 17.94109 1.376283e-17
```

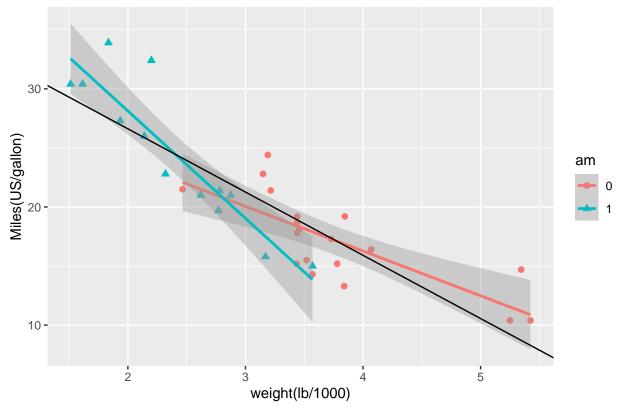
Comparing mpg to automatic and manual, it seems that automatic cars consume less than 18 per mile, while manual it's around 24/25 mpg. Let's see how horse-power and weight influence those statistics.

Horse power and weight investigation

Weight:

```
## `geom_smooth()` using formula 'y ~ x'
```

mpg according to weight over trasmission



The graph show a relation between weight and mpg over transmission, less a car weight more mpg does the car, if it's applied transmission information too, it seems that lower weight cars that have manual transmission, they consume in general less respect to automatic cars, while this assumption is not true if we talk about medium size car, but any light cars data with automatic transmission are given for prove the first assumption.

let's check this assumption:

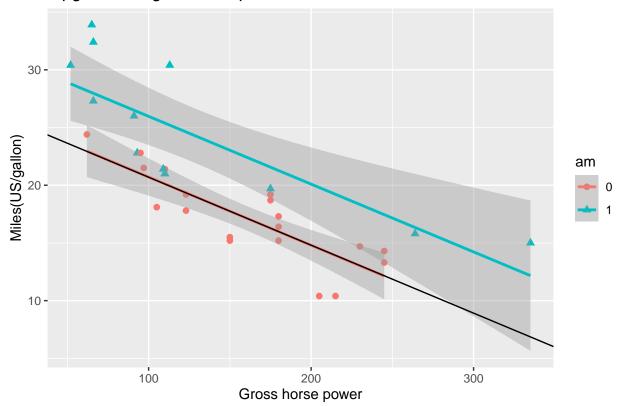
```
## Estimate Std. Error t value Pr(>|t|)
## wt -3.785908 0.7856478 -4.818836 4.551182e-05
## am0 31.416055 3.0201093 10.402291 4.001043e-11
## am1 46.294478 3.0101489 15.379465 3.488923e-15
## wt:am1 -5.298360 1.4446993 -3.667449 1.017148e-03
```

the automatic trasmission seems to consume more than manual adjusting with weight

Horse_power:

```
## `geom_smooth()` using formula 'y ~ x'
```

mpg according to horse-power over trasmission



The graph show a relation between *gross horse-power* and *mpg* over *transmission*, it seems that more horse power has the car less mpg are. Transmission to influence the mpg, and it show that automatic cars use less mpg when horse power grow then manual ones.

let's check this assumption:

```
summary(lm(mpg ~ hp*am -1, data = df))
```

```
##
## Call:
## lm(formula = mpg ~ hp * am - 1, data = df)
##
## Residuals:
## Min    1Q Median   3Q Max
## -4.3818 -2.2696   0.1344   1.7058   5.8752
##
## Coefficients:
```

```
Estimate Std. Error t value Pr(>|t|)
## hp
        ## am0
        26.6248479 2.1829432 12.197 1.01e-12 ***
        31.8425012 1.5288820
                             20.827 < 2e-16 ***
## am1
## hp:am1 0.0004029 0.0164602
                             0.024
                                     0.981
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2.961 on 28 degrees of freedom
## Multiple R-squared: 0.9825, Adjusted R-squared:
## F-statistic: 393.5 on 4 and 28 DF, p-value: < 2.2e-16
```

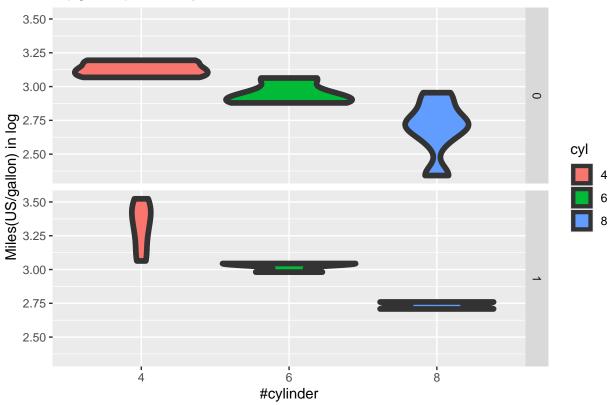
Comparing cylinderrs, C-shape engine, gear and carb to mpg over trasmission before start let's check which features seems to influence the mpg prediction and them coefficients

```
##
           Estimate Std. Error
                                 t value
                                          Pr(>|t|)
## cyl4 23.87913244 20.06582026 1.1900402 0.25252548
## cyl6 21.23043717 18.33416483 1.1579713 0.26498157
## cyl8 23.54296946 18.22249667 1.2919728 0.21591810
## disp
        0.03554632 0.03189920 1.1143329 0.28267339
## hp
        1.18283018 2.48348458 0.4762784 0.64073922
## drat
        -4.52977584 2.53874584 -1.7842573 0.09461859
## wt
       0.36784482 0.93539569 0.3932505 0.69966720
## qsec
         1.93085054 2.87125777 0.6724755 0.51150791
## vs1
## am1
         1.21211570 3.21354514 0.3771896 0.71131573
## gear4 1.11435494 3.79951726 0.2932886 0.77332027
## gear5 2.52839599 3.73635801 0.6767007 0.50889747
## carb2 -0.97935432 2.31797446 -0.4225044 0.67865093
## carb3 2.99963875 4.29354611 0.6986390 0.49546781
## carb4 1.09142288 4.44961992 0.2452845 0.80956031
## carb6 4.47756921 6.38406242 0.7013668 0.49381268
## carb8 7.25041126 8.36056638 0.8672153 0.39948495
```

Cylinders seems to have more impact respect to other features.

Warning: Ignoring unknown parameters: coloir





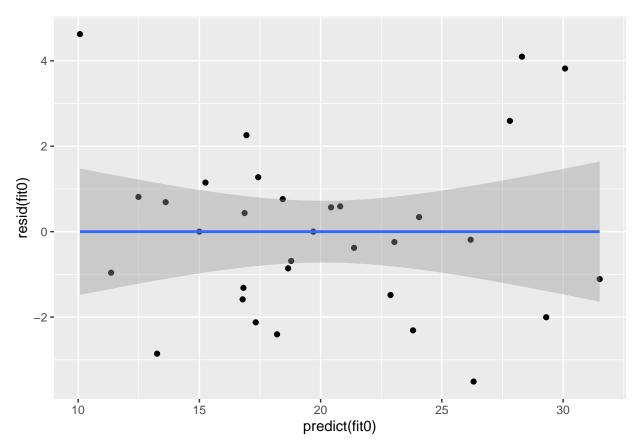
Checking variance of mpg compare to #cylinders over transmision it's seems that automatic transmision as flatter variance then manual transmission does on 4 cyl while the opposite occur for 6 and 8 cyl.

Diagnostic

```
Std. Error
                                     t value
                                               Pr(>|t|)
            Estimate
## cyl4
         23.87913244 20.06582026
                                   1.1900402 0.25252548
         21.23043717 18.33416483
                                   1.1579713 0.26498157
  cyl6
  cyl8
         23.54296946 18.22249667
                                   1.2919728 0.21591810
## disp
          0.03554632
                      0.03189920
                                   1.1143329 0.28267339
## hp
         -0.07050683
                      0.03942556
                                  -1.7883534 0.09393155
##
  drat
          1.18283018
                      2.48348458
                                   0.4762784 0.64073922
         -4.52977584
                      2.53874584 -1.7842573 0.09461859
##
  wt
## qsec
          0.36784482
                      0.93539569
                                   0.3932505 0.69966720
                      2.87125777
##
  vs1
          1.93085054
                                   0.6724755 0.51150791
##
  am1
          1.21211570
                      3.21354514
                                   0.3771896 0.71131573
  gear4
          1.11435494
                      3.79951726
                                   0.2932886 0.77332027
  gear5
          2.52839599
                      3.73635801
                                   0.6767007 0.50889747
  carb2 -0.97935432
                      2.31797446
                                  -0.4225044 0.67865093
  carb3
                      4.29354611
                                   0.6986390 0.49546781
##
          2.99963875
          1.09142288
                      4.44961992
                                   0.2452845 0.80956031
          4.47756921
                      6.38406242
                                   0.7013668 0.49381268
## carb6
          7.25041126
                      8.36056638
                                  0.8672153 0.39948495
```

Looking the coefficients it's seems that all features are necessary, so we need to first the *residual plot* for look throught the data pattern and then check over *vif* for look variance on features.

Residual plot Now that we know the main features that influence mpg overam lets look the residual plot ## `geom_smooth()` using formula 'y ~ x'



residual plot have a pattern that suggest a linear regresion should fit the pattern, but we still need to investigate over outliers for check if some data can be adjust for fit in a better way the model.

```
GVIF Df GVIF^(1/(2*Df))
## cyl 128.120962
                    2
                              3.364380
## disp
        60.365687
                    1
                              7.769536
                              5.312210
## hp
         28.219577
                    1
          6.809663
                              2.609533
## drat
                    1
         23.830830
                              4.881683
## wt
## qsec
         10.790189
                    1
                              3.284842
## vs
          8.088166
                              2.843970
## am
          9.930495
                    1
                              3.151269
## gear 50.852311
                    2
                              2.670408
## carb 503.211851
                   5
                              1.862838
##
             GVIF
                         Df GVIF^(1/(2*Df))
## cyl 11.319053 1.414214
                                   1.834225
                                   2.787389
## disp
         7.769536 1.000000
## hp
         5.312210 1.000000
                                   2.304823
## drat
         2.609533 1.000000
                                   1.615405
         4.881683 1.000000
                                   2.209453
         3.284842 1.000000
## qsec
                                   1.812413
         2.843970 1.000000
                                   1.686407
## vs
## am
         3.151269 1.000000
                                   1.775181
```

```
## gear 7.131081 1.414214 1.634138
## carb 22.432384 2.236068 1.364858
```

Model selection

In this section we are interest in find the best model for mpq and then check which am is better.

Now i will check which feature is better to exclude by the use of anova function and the pre-knoledge obtain with vif test.

```
## Analysis of Variance Table
##
## Model 1: mpg ~ am
## Model 2: mpg ~ am + vs + qsec
## Model 3: mpg ~ am + vs + qsec + hp + wt
## Model 4: mpg ~ am + vs + qsec + hp + wt + drat
## Model 5: mpg ~ am + vs + qsec + hp + wt + drat + disp
## Model 6: mpg ~ am + vs + qsec + hp + wt + drat + disp + gear
## Model 7: mpg ~ am + vs + qsec + hp + wt + drat + disp + carb
## Model 8: mpg ~ am + vs + qsec + hp + wt + drat + disp + cyl
## Model 9: mpg ~ (cyl + disp + hp + drat + wt + qsec + vs + am + gear +
##
      carb) - 1
##
    Res.Df
              RSS Df Sum of Sq
                                          Pr(>F)
## 1
        30 720.90
## 2
        28 315.89 2
                        405.01 25.2286 1.589e-05 ***
## 3
        26 159.82 2
                        156.07 9.7216 0.001961 **
## 4
        25 158.56 1
                          1.26 0.1569 0.697630
## 5
        24 149.45 1
                          9.11 1.1351 0.303548
## 6
        22 146.57 2
                          2.88 0.1795 0.837437
## 7
        19 134.15 3
                         12.42 0.5157 0.677744
## 8
        22 139.02 -3
                         -4.87
                                0.2024 0.893093
## 9
        15 120.40 7
                         18.62 0.3314 0.927349
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

the best suitable model with linear regression seems to be m5 the best.

Aswer and conclusion

```
b_m \leftarrow lm(mpg \sim am + vs + qsec + hp + wt + drat + disp -1 , data = df)
summary(b m)$coefficients
##
          Estimate Std. Error
                                t value
                                          Pr(>|t|)
## am0
       12.49804962 12.48038774 1.0014152 0.326616519
## am1
       15.52206608 12.21052872 1.2712034 0.215839083
## vs1
        ## gsec 0.87148931
                  0.61331436
                             1.4209504 0.168194583
## hp
       -0.02282191
                  0.01525893 -1.4956426 0.147781592
       -3.94973602 1.26261038 -3.1282303 0.004567014
## drat 0.95532814
                  1.40737217 0.6788028 0.503756614
## disp 0.01373930 0.01135852 1.2096028 0.238211942
```

Answer Automatic transmission seems to be the best transmission respect to mpg because consume around 12 mpg with a variance of 12, respect to manual transmission that consume 15 mpg with 12 of mpg variance.