

Contest Duration: 2025-07-12(Sat) 08:00 (<http://www.timeanddate.com/worldclock/fixedtime.html?iso=20250712T2100&p1=248>) - 2025-07-12(Sat) 09:40 (<http://www.timeanddate.com/worldclock/fixedtime.html?iso=20250712T2240&p1=248>) (local time) (100 minutes)

[Back to Home \(/home\)](#)

[🏠 Top \(/contests/abc414\)](#) [☰ Tasks \(/contests/abc414/tasks\)](#)

[🗨️ Clarifications \(/contests/abc414/clarifications\)](#) [🚀 Submit \(/contests/abc414/submit\)](#)

[☰ Results ▾](#) [⬇️ Standings \(/contests/abc414/standings\)](#)

[⬇️ Virtual Standings \(/contests/abc414/standings/virtual\)](#)

[🔧 Custom Test \(/contests/abc414/custom\\_test\)](#)

[📖 Editorial \(/contests/abc414/editorial\)](#)

[🗨️ Discuss \(https://codeforces.com/blog/entry/144653\)](https://codeforces.com/blog/entry/144653)



## E - Count $A \% B = C$ (/contests/abc414/tasks/abc414\_e) Editorial by [spheniscine \(/users/spheniscine\)](/users/spheniscine)

Note that for the tuples  $(a, b, c)$  we wish to count, if  $a < b$ ,  $a = c$ , therefore we can rule out those. This leaves  $\binom{N}{2} = N(N-1)/2$  possible tuples where  $a > b$ , with the only exceptions being where  $c = 0$ , therefore we must filter out the tuples where  $b$  divides  $a$ .

If we fix  $b$ , there are  $\lfloor N/b \rfloor - 1$  tuples where  $b$  divides  $a$  to subtract. To do this efficiently, we want to enumerate through triples  $(l, r, q)$  such that:

- For all integers  $l \leq b < r$  [note the half-open range],  $q = \lfloor N/b \rfloor$
- All  $q$  are distinct, and segments  $[l, r)$  would cover the range  $[1, N]$  without overlapping.

We claim that there are at most  $O(\sqrt{N})$  such triples. Proof: there are at most  $\sqrt{N}$  possible triples where  $q \leq \sqrt{N}$ . If  $q > \sqrt{N}$ ,  $l < \sqrt{N}$ , therefore there are again at most  $\sqrt{N}$  triples.

We can enumerate through these triples via the following algorithm:

- Start with  $l := 1$ .
- While  $l \leq n$ :
  - $q := \lfloor N/l \rfloor$
  - $r := \lfloor N/q \rfloor + 1$
  - yield  $(l, r, q)$
  - reassign  $l := r$

2025-07-15 (Tue)  
22:38:11 -04:00

This is a variant of a common technique of enumerating floored quotients of  $N$  in  $O(\sqrt{N})$  time (link to yosupo.jp library checker ([https://judge.yosupo.jp/problem/enumerate\\_quotients](https://judge.yosupo.jp/problem/enumerate_quotients)))

For each  $(l, r, q)$  triple, we can thus subtract  $(r - l)(q - 1)$  from the answer.

posted: a day ago

last update: a day ago

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Telegram)

<https://atcoder.jp/contests/abc414/editorial/13468> (Flang%3Den&title=Editorial%20-%20Contest%202025%20(AtCoder%20Beginner%20Contest%20414))

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[Rule \(/contests/abc414/rules\)](/contests/abc414/rules) [Glossary \(/contests/abc414/glossary\)](/contests/abc414/glossary)

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2025-07-15 (Tue)  
22:38:11 -04:00