

DAY 20:

ASSIGNMENT 2:

Task 2: Longest Common Subsequence

Implement `int LCS(string text1, string text2)` to find the length of the longest common subsequence between two strings.

ANSWER:

```
public class LongestCommonSubsequence {

    public static int LCS(String text1, String text2) {

        int m = text1.length();
        int n = text2.length();
        int[] dp = new int[n + 1];

        // Build the dp array in bottom-up manner
        for (int i = 1; i <= m; i++) {
            int prev = 0; // This will be dp[j-1] from the previous row
            for (int j = 1; j <= n; j++) {
                int temp = dp[j]; // Store the current dp[j] to update it later
                if (text1.charAt(i - 1) == text2.charAt(j - 1)) {
                    dp[j] = prev + 1;
                } else {
                    dp[j] = Math.max(dp[j], dp[j - 1]);
                }
                prev = temp; // Update prev to the current dp[j] for the next iteration
            }
        }

        return dp[n];
    }
}
```

```

public static void main(String[] args) {
    String text1 = "abcde"; // Example string 1
    String text2 = "ace"; // Example string 2

    System.out.println("Length of LCS = " + LCS(text1, text2));
}
}

```

Explanation:

1. Initialization:

- $dp[j]$ will hold the length of the LCS of the substrings $text1[0..i-1]$ and $text2[0..j-1]$.
- Initialize $dp[j] = 0$ for all j because the LCS with any empty string is 0.

2. Filling the DP Array:

- Iterate over each character of $text1$ (outer loop) and $text2$ (inner loop).
- Use a variable $prev$ to store the value of $dp[j-1]$ from the previous row, which is needed to calculate $dp[j]$ for the current row.
- If $text1[i-1] == text2[j-1]$, then the characters match, and the LCS up to i and j is $prev + 1$.
- If the characters do not match, then the LCS up to i and j is the maximum of the LCS without the current character of $text1$ ($dp[j]$) or without the current character of $text2$ ($dp[j-1]$).

3. Result:

- The result will be in $dp[n]$, which represents the length of the LCS of $text1$ and $text2$.

This solution is more space-efficient, using $O(n)$ space instead of $O(m \times n)$ by leveraging a rolling array approach. The time complexity remains $O(m \times n)$, where m and n are the lengths of $text1$ and $text2$, respectively.