

CIS 519: Introduction to Machine Learning  
Homework 4

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## PART 1: Problem Set

### Problem 3: TANH Neural Networks

#### Problem (3a):

The advantage of using the tanh function instead of the sigmoid in a neural network is that the sigmoid function saturates to '0' whereas the TANH function saturates to +/- 1. Suppose during training the activity in neural network is close to '0', then the sigmoid function's gradient may go to 0.

#### Problem (3b):

Given

$$y_k(x, \theta) = \sigma \left( \sum_{j=1}^M \theta_{jk}^{(2)} \sigma \left( \sum_{i=1}^d \theta_{ij}^{(1)} x_i + \theta_{0j}^{(1)} \right) + \theta_{0k}^{(2)} \right)$$

Let us find the relation between  $\sigma(a)$  and  $\tanh(a)$ .

$$\begin{aligned} \tanh(a) &= \frac{e^a - e^{-a}}{e^a + e^{-a}} = \frac{1 - e^{-2a}}{1 + e^{-2a}} = 2\sigma(2a) - 1 \\ \sigma(a) &= \frac{1}{2} \tanh\left(\frac{a}{2}\right) + \frac{1}{2} \end{aligned}$$

Rewriting  $y_k(x, \theta)$  in terms of  $\tanh$  we get,

$$\begin{aligned} y_k(x, \theta) &= \sigma \left( \sum_{j=1}^M \theta_{jk}^{(2)} \left( \frac{1}{2} \tanh \left( \frac{1}{2} \sum_{i=1}^d \theta_{ij}^{(1)} x_i + \frac{1}{2} \theta_{0j}^{(1)} \right) + \frac{1}{2} \right) + \theta_{0k}^{(2)} \right) \\ y_k(x, \theta) &= \sigma \left( \sum_{j=1}^M \frac{1}{2} \theta_{jk}^{(2)} \tanh \left( \sum_{i=1}^d \frac{1}{2} \theta_{ij}^{(1)} x_i + \frac{1}{2} \theta_{0j}^{(1)} \right) + \sum_{j=1}^m \frac{1}{2} \theta_{jk}^{(2)} + \theta_{0k}^{(2)} \right) \\ y_k(x, \theta) &= \sigma \left( \sum_{j=1}^M w_{jk}^{(2)} \tanh \left( \sum_{i=1}^d w_{ij}^{(1)} x_i + w_{0j}^{(1)} \right) + w_{0k}^{(2)} \right) \end{aligned}$$

where  $w$  can be obtained from linear transformation as shown below

$$w_{jk}^{(2)} = \frac{1}{2}\theta_{jk}^{(2)}$$

$$w_{ij}^{(1)} = \frac{1}{2}\theta_{ij}^{(1)}$$

$$w_{0j}^{(1)} = \frac{1}{2}\theta_{0j}^{(1)}$$

$$w_{0k}^{(2)} = \sum \frac{1}{2}\theta_{jk}^{(2)} + \theta_{0k}^{(2)}$$

Therefore, the parameters of the two networks differ by linear transformations.

## PART 2: Programming Exercises

### Problem 1: Text Classification and ROC

#### Training Values:

Metric	Naive Bayes	SVM with cosine kernel
Time	0:00:02.931874	0:00:00.771261
Accuracy	0.972231744943	0.960918752143
Precision	0.858908341916	0.880020597322
Recall	0.972231744943	0.960918752143

#### Testing Values:

Metric	Naive Bayes	SVM with cosine kernel
Accuracy	0.849347189234	0.811439857093
Precision	0.791498573934	0.824983579848
Recall	0.849347189234	0.811439857093

The classifier I found to be better is Naive Bayes. This is only true for the selected parameters. The assumption of independence in Naive Bayes classifier is satisfied by the variables of the dataset and the degree of class overlapping is small.

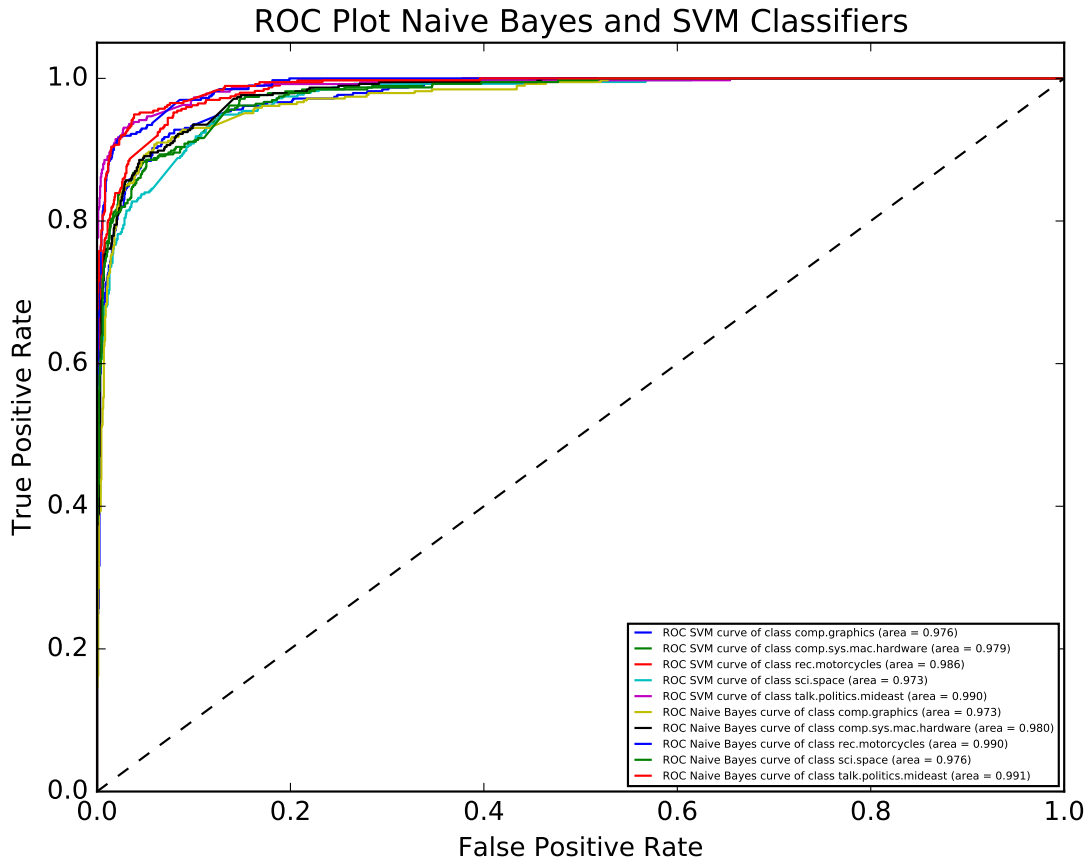


Figure 1: ROC Curves for Naive Bayes and SVM classifiers

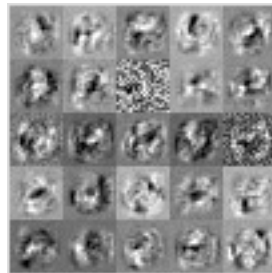
### Problem 2.5: Apply Your Neural Network to Digit Recognition

Optimal Learning Rate = 2.45

Regularization Parameter = 0.001

Maximum Training Performance = 0.957

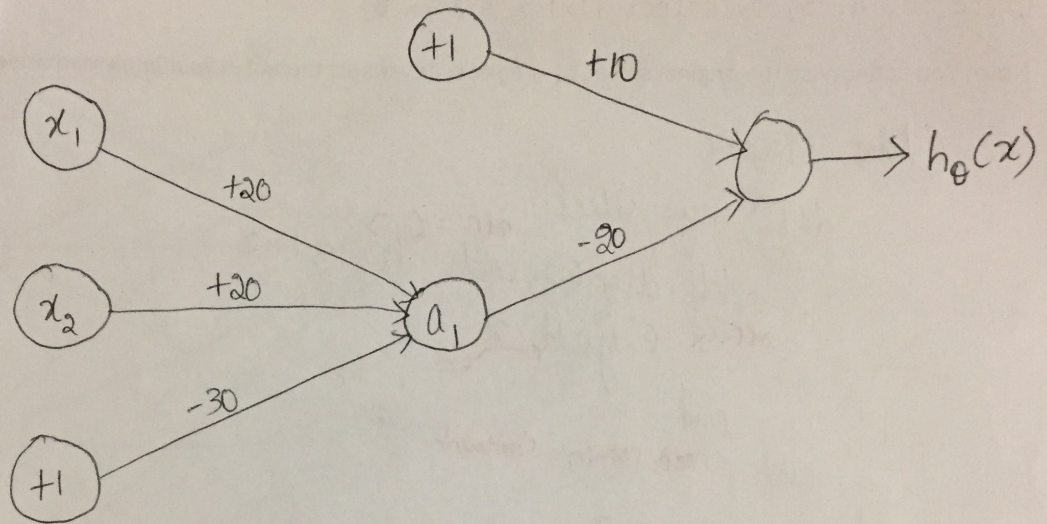
### Problem 2.6: Visualizing the Hidden Layers



## PART 1: Problem Set

### Problem 1: Logical Functions with Neural Networks

Problem 1a:



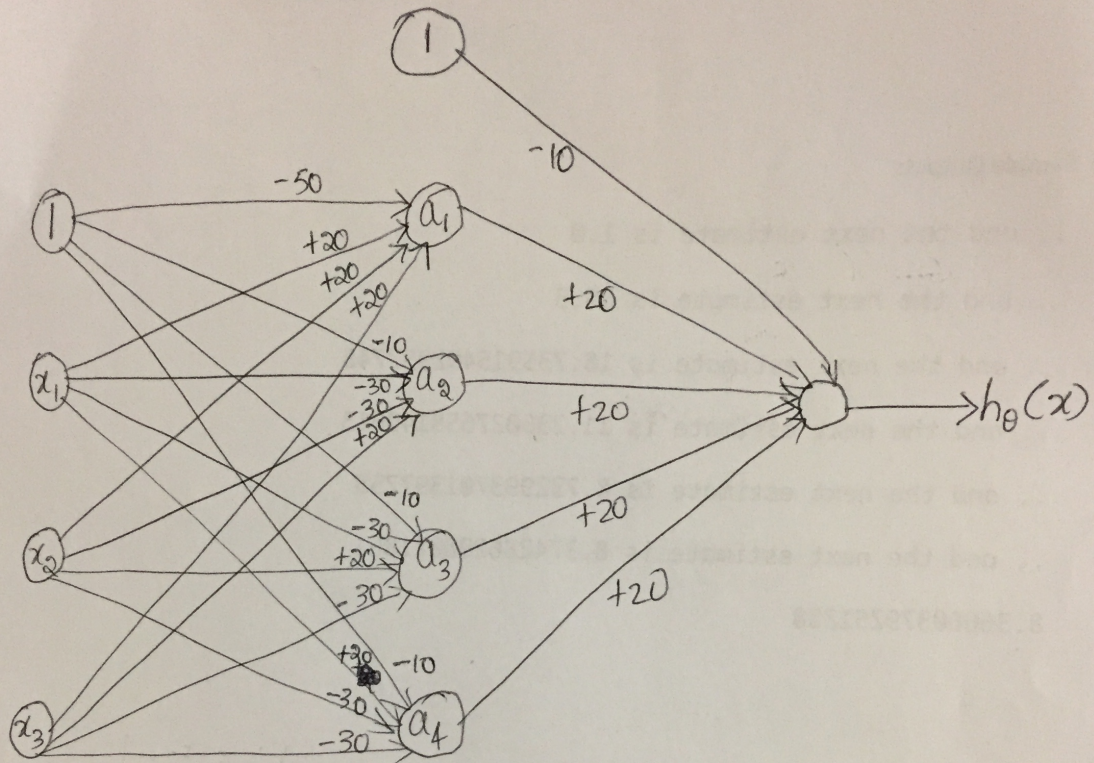
Truth table:

$x_1$	$x_2$	$h_\theta(x)$	Output
0	0	$g(10)$	1
1	0	$g(10)$	1
0	1	$g(10)$	1
1	1	$g(-10)$	0

Figure 2: The NAND<sup>5</sup> of two binary inputs



Problem 1b:



Truth table

$x_1$	$x_2$	$x_3$	Output
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	0
1	1	1	1

Figure 3: The parity<sup>6</sup> of three binary inputs

## **Problem 2: Data Visualization and Feature Engineering**

The two coordinate axes (features) along which you could plot the data to best visualize this dataset are Checking Status and Duration. These two were determined through the algorithms Maximum Corelation, Information Gain and best c val. By analyzing the scatter plot for these in the visualize tab, it is evident that these two are best features to visualize the dataset.