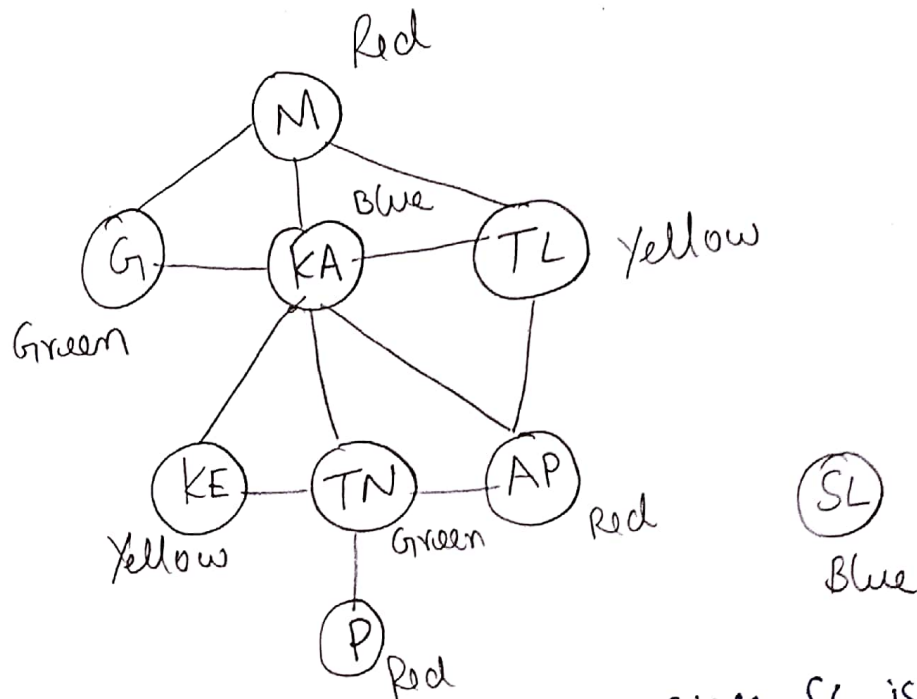


Assignment-5

a)



- 1) We can simplify this problem since SL is not connected to any other nodes, it is an independent subproblem.
- 2) Therefore we can solve the subproblem (M, G, KA, TL, KE, TN, AP, P) and SL subproblem independently.
- 3) We can combine the solution of these two subproblem to find the final solution.

b) MRV: 1st SubproblemLevel 0: all nodes \rightarrow 4 Values (R, G, B, Y)Level 1: M \rightarrow Pick red

$G, KA, TL \rightarrow 3$ possible values (G, B, Y)

$KE, TN, AP, P \rightarrow 4$ possible values (R, G, B, Y)

Level 2:

$M \rightarrow \text{Red}$

$G \rightarrow \text{Green}$

$KA \rightarrow 2$ possible values (B, Y)

$TL \rightarrow 3$ possible values (G, B, Y)

$KE, TN, AP, P \rightarrow 4$ possible values (R, G, B, Y)

Level 3:

$M \rightarrow \text{Red}$

$G \rightarrow \text{Green}$

$KA \rightarrow \text{Blue}$ (Picking randomly)

$TL \rightarrow 2$ possible values (G, Y)

$KE, TN, AP \rightarrow 3$ possible values (R, G, Y)

$P \rightarrow 4$ possible values (R, G, B, Y)

Level 4:

$M \rightarrow \text{Red}$

$G \rightarrow \text{Green}$

$KA \rightarrow \text{Blue}$

$TL \rightarrow \text{Yellow}$

$AP \rightarrow 2$ possible values (R, G)

KE, TN \rightarrow 3 possible values (R, G, Y)
P \rightarrow 4 possible values (R, G, B, Y)

Level 5:

M \rightarrow Red

G \rightarrow Green

KA \rightarrow Blue

TL \rightarrow Yellow

AP \rightarrow Red

KE, TN \rightarrow 2 possible values (G, Y)

P \rightarrow 4 possible values (R, G, B, Y)

Level 6:

M \rightarrow Red

G \rightarrow Green

KA \rightarrow Blue

TL \rightarrow Yellow

AP \rightarrow Red

KE \rightarrow Yellow

TN \rightarrow 1 possible value (G)

P \rightarrow 4 possible value (R, G, B, Y)

Level 7:

M → Red

Gr → Green

KA → Blue

TL → Yellow

AP → Red

KE → Yellow

TN → Green (choosing 1 possible value)

P → 3 possible value (R, B, Y)

Level 8:

M → Red

Gr → Green

KA → Blue

TL → Yellow

AP → Red

KE → Yellow

TN → Green

P → Red

2nd Sub problem

SL → 4 possible values (R, G, B, Y)

Level 1 : SL → Green

C) Degree Heuristic 1st Subproblem:

<u>KA: 6</u>	<u>TN: 4</u>	<u>M: 3</u>	<u>TL: 3</u>	<u>AP: 3</u>	<u>KE: 3</u>	<u>G: 2</u>	<u>P: 1</u>
Level 1	Level 2	Level 3	Level 4	Level 5	Level 6	Level 7	Level 8

Level 0: KA, TN, M, TL, AP, KE, G, P \rightarrow 4 possible values (R, G, B, Y)

Level 1: Select KA \rightarrow Red
G, M, TL, AP, TN, KE \rightarrow 3 possible values (G, B, Y)
P \rightarrow 4 possible values (R, G, B, Y)

Level 2: Select TN \rightarrow Green

KA \rightarrow Red
KE, AP \rightarrow 2 possible values (B, Y)
G, M, TL \rightarrow 3 possible values (G, B, Y)
P \rightarrow 3 possible values (R, B, Y)

Level 3: Select M \rightarrow Blue

KA \rightarrow Red

TN \rightarrow Green

G, TL \rightarrow 2 possible values (G, Y)

KE, AP \rightarrow 2 possible values (B, Y)

P \rightarrow 3 possible values (R, B, Y)

Level 4: Select TL \rightarrow Yellow

KA \rightarrow Red

TN \rightarrow Green

M \rightarrow Blue
AP \rightarrow 1 possible value (B)
KE \rightarrow 2 possible values (B, Y)
G \rightarrow 2 possible values (G, Y)
P \rightarrow 3 possible values (R, B, Y)

Level 5 : Select AP \rightarrow Blue
KA \rightarrow Red
TN \rightarrow Green
M \rightarrow Blue
TL \rightarrow Yellow
KE \rightarrow 2 possible values (B, Y)
G \rightarrow 2 possible values (G, Y)
P \rightarrow 3 possible values (R, B, Y)

Level 6 : Select KE \rightarrow Yellow
KA \rightarrow Red
TN \rightarrow Green
M \rightarrow Blue
TL \rightarrow Yellow
AP \rightarrow Blue
G \rightarrow 2 possible values (G, Y)
P \rightarrow 3 possible values (R, B, Y)

Level 7: Select G \rightarrow Green
KA \rightarrow Red
TN \rightarrow Green

M → Blue

TL → Yellow

AP → Blue

KE → Yellow

P → 3 Possible values (R, B, Y)

Level 8: Select P → Red

KA → Red

TN → Green

M → Blue

TL → Yellow

AP → Blue

KE → Yellow

G → Green

2nd Subproblem

Degree of SL 0

Select SL → Green

Solution:

1st Subproblem solution

KA - Red, TN - green, M - Blue, TL - yellow,
AP - Blue, KE - Yellow, G - Green, P - red

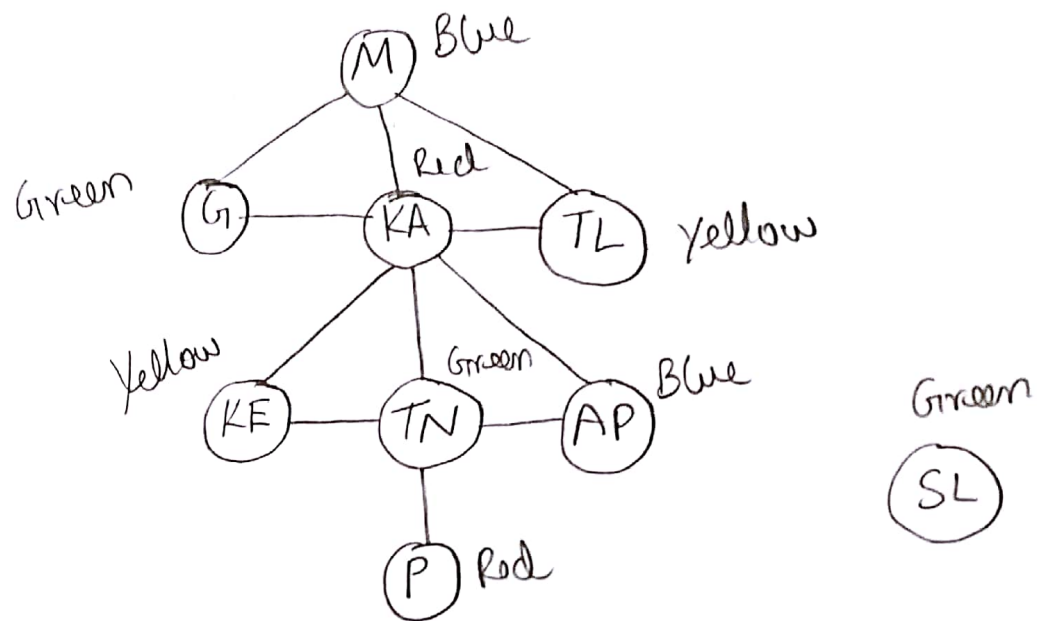
2nd Sub problem solution:

SL - Green

Final Solution

KA - Red, TN - Green, M - Blue, TL - yellow, AP - Blue
KE - Yellow, G - Green, P - Red, SL - Green.

Final Solution



(2)

To show that two logical statements A and B are logically equivalent

Given two knowledge bases KB1 and KB2

- In order to show that $KB1 \Leftrightarrow KB2$, we need to first show $KB1 \Rightarrow KB2$ as well as $KB2 \Rightarrow KB1$
- Let us have two variable symbols and model that are globally defined.

③

Part a:

In order to KB entail S_1 ,
 S_1 should be true in all worlds where
KB is true.

In the given truth table, whenever KB is
true S_1 is also True.

Hence, KB entails S_1 .

Part b:

When we consider $\text{NOT}(KB) \ \& \ \text{NOT}(S_1)$ there
are two cases where KB is True and S_1 is
False (2nd and 4th Row). So, the condition
for entailment doesn't get satisfied.

\therefore , $\text{Not}(KB)$ does not entail $\text{NOT}(S_1)$.

④

A, B, C, D,

Giv: T T T T False

T F T F False

CNF: $(\neg A \vee \neg B \vee \neg C \vee \neg D) \wedge (\neg A \vee B \vee \neg C \vee D)$

// —

⑤

Let A: Rains on May 1, 2017

B: John gives Mary a check for \$10,000 on May 2, 2017

C: Mary moves the lawn on May 3, 2017

Part a : $A \Rightarrow B$
 $B \Rightarrow C$

Part b : \bar{B}
A
C

Part c : The contract was not violated, because when \bar{A} is true $A \Rightarrow B$ holds B is true and C is also true then $B \Rightarrow C$ holds.

⑥

(i) Shadow is a constant

dog() is a predicate

dog(shadow). There is a dog called shadow.

(ii) ~~shadow, Mary~~ John, shadow and Mary are constants

game() is a predicate

game(shadow, Mary, John):

John gave shadow to Mary.

(iii) shadow, Mary, Smartphone, John are constants
game(), male() are predicates
male(shadow) \Rightarrow game(smartphone, John, Mary)
If shadow is male then Mary gave smartphone to John.

(iv) shadow, Mary, John and Laptop are constants
female(): predicate
female(shadow) \Rightarrow game(Laptop, John, Mary):
If shadow is female, then Mary gave laptop to John

(v) Dog, People, John: constants
male(), game(): predicates
game(dog, people, John) \Leftrightarrow male(dog)

If and only if it is a male dog John gives it to people

(vi) Laptop, John, Mary: constants
gave(): predicate
gave(Laptop, John, Mary)

⑦

Given first order logic knowledge base

taller(John, Bill)

$\forall x \text{ taller}(x, \text{Bill}) \Rightarrow \text{tall}(x)$

Given John, Bill are constants
symbols in propositional logic:

a) taller - John - Bill = taller(John, Bill)

we have 2 constants, so $x(\text{John} \text{ (or) } x) \text{ } x \text{ } \text{Bill}$

b) taller(x, Bill) = taller - John - Bill
taller - Bill - Bill

c) tall(x) = tall - John
tall - Bill

d) $(\forall x) \text{ taller}(x, \text{Bill}) \Rightarrow \text{tall}(x)$.

This Statement is represented in propositional logic as follows,

taller - John - Bill \Rightarrow tall - John.

taller - Bill - Bill \Rightarrow tall - Bill.

e) A part from the above, we can also have
 $\text{taller_John_John} = \text{taller}(\text{John}, \text{John})$
 $\text{taller_Bill_John} = \text{taller}(\text{Bill}, \text{John})$

② Statements that should be stored in propositional logic base are

taller_John_Bill

$\text{taller_John_Bill} \Rightarrow \text{tall_John}$

$\text{taller_Bill_Bill} \Rightarrow \text{tall_Bill}$