# CSE 5360 003 – Fall 2018 Exam 2, Monday 10/29/2018

Name:	20L0710N	
Student ID:		

(Not providing this information: -10 Points) (Name missing in Individual pages: -5 Points)

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### **Total Exam Points: 100**

#### Score

Question	Points	Max Points
1		15
2		8
3		10
4		15
5		12
6		10
7		15
8		15
9 (Opt.)		10*
Total		100 (110*)

<sup>\*:</sup> Extra Credit Points

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# Question 1 - 15 points

Convert the following statements into conjunctive normal form:

(a) [5 points]:

DEMORGONS

Double Negation

DIST. PROP.

(b) [5 points]:

$$(A \Rightarrow B) \Leftrightarrow C$$

Romera (2)

Menore =)

DE Morans

DOUBLE NECLATION

((A BND NOTB) OR C) AND (NOT C OR (NOTA OR B))

((A OR C) BND (NOTB ORC)) BND (NOTCOR (NOTA OR B))

((A OR C) BND (NOTB ORC)) BND (NOTCOR (NOTA OR B))

((A OR C) BND (NOTB ORC) BND (NOTC OR NOTA)

(c) [5 points]:
A OR (NOT (B ⇒ C))

Renne =>

A OR (NOT (NOTB OR C))

Dellorgans

A OR (NOT (NOT B) AND MOT C)

Double Negation

A OR (B AND NOT C)

Dist Pop.

(A OR B) AND (A OR NOT C)

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# Question 2 – 8 points

For each pair of statements, determine if you can apply resolution to those statements. If you can apply resolution, write at least one statement that can be derived by applying resolution to the given pair of statements. If you can apply resolution, apply it blindly; **do NOT simplify the resulting sentences**. If you cannot apply resolution, just write "cannot apply".

(a) [2 points]:

Statement 1: A OR (NOTE)
Statement 2: B OR D OR E

A DR B OR D

(b) [2 points]:

Statement 1: A OR (NOT B) OR C Statement 2: B OR (NOT C) OR D

A on con wonc) or D.

(c) [2 points]:

Statement 1: A OR B OR (NOT D) Statement 2: A OR C OR (NOT D)

Connot apply

(d) [2 points]:

Statement 1: A OR (NOTB)

Statement 2: A OR B-OR (NOT C)

A on A on (NOT C)

### Question 3 - 10 points

You have a KB and two sentences S1 and S2 that are defined in a domain containing 5 symbols. You check the following using TT-ENTAILS:

$$KB \models S1$$
,  $KB \models S2$ ,  $KB \models (S1 \lor S2)$  and  $KB \models (S1 \land S2)$ 

How many calls to TT-CHECK-ALL are required in total.

If KB  $\vDash$  S1 is true and KB  $\vDash$  S2 is also true does that guarantee that KB  $\vDash$  (S1  $\lor$  S2) and KB  $\vDash$  (S1  $\land$  S2) are also true? Justify your answer.

Each call to 77-ENTAILS requies. (2+1) calls to TT-CHECKS ALL, so in botal we need. Here h=S 4.x (25+1) = 4 x 33 = 132 calls If KB = SI is true then whenever KB is true than SI is true. Similarly Werevan KB is true, 52 is true. So Wenever KB is true, SIVSZ & SINSZ are also true. So, KB = SIVSZ & KB F SINSZ

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# Question 4 – 15 points

John, Harry and Bob sign the following contract on December 31, 2018.

- Bob will give John \$500 if and only if John gets a 4.0 GPA in Spring 2019
- If Bob gives John \$500, John will give Harry a guitar
- If John gave Harry a guitar, Harry will play at the event

The all-inclusive sequence of events at the end of Spring 2019 are the following:

John got a 4.0 GPA. Bob gave John \$500. Harry played at the event.

(HINT: All-inclusive means anything not mentioned here did not happen).

(a) [8 points]: Describe the contract using first-order logic. You also need to list the constants, predicates used and the semantics [father(x,y): x is father of y].

Viedicerts. Coire (X, y, z): X gives y to Z GetA(x): X gets 4.0 GPA in Spring 2019. PlayE(x): x plays at event Constats: Bob, John, 500, Guitar ariables: X, Us, Z Contract Criver (BDb, 500, John) ( Crive (John, Cruitar, Harry) Crire (John, Gruiter, Harry) => Play E (Herry) 9

(b) [7 points]: Describe what happened using first order logic and using notation consistent with your answer in Question 4(a).

(c) [5 points]: Was the contract violated or not? Justify your answer.

Yes. While Bob gove John \$500, John did not give a Guitan to Harry. This is a violation of the second part of the contrack.

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# Question 5 – 12 points

Give the unifier for the following predicates (if possible). If no unifier possible, Justify.

(a) [3 points]: Father(x, Bob), Son(Bob, John)

None Possible. [Father and Son one different predicates]

(b) [3 points]: Gave(x, Laptop, Mary), Gave(Mother(Mary), Laptop, y)



(c) [3 points]: TallerThan(x, Barry), TallerThan(Duncan, y)



(d) [3 points]: Grouped(Tom, Richard, Harry), Grouped(x, Son(y), z)

None Possible. No assignment available. for 9.

# Question 6 – 10 points

Suppose you have a domain in First-Order Logic that has the following:

- 10 constants
- 1 predicate of 3 arguments
- 2 predicates of 2 arguments
- 3 predicates of 1 argument

How many symbols do you need to convert any KB in this domain into a propositional logic KB. Justify your answer.

Possible assignents 1 predicete with 10 assigneds.
2 predicetes with 10 assigneds.
3 predicetes with 10 assigneds. 3 10 + 2×10<sup>2</sup> +3×10 = 1600 + 200 + 30 = 1230 assynds. 12 30 Symbols.

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### Question 7 - 15 points

Consider this first-order logic knowledge base:

big(car)  $\land$  small(bike)  $\forall$ x [ small(x)  $\Leftrightarrow$  fast(x)] fast(bike)  $\Rightarrow$  slower(car, bike)

In this first-order logic knowledge base, fast, slower, slow are predicates, and car, bike are constants. Convert this first-order logic knowledge base into a propositional logic knowledge base, by performing the following two steps:

- (a) Define symbols for the propositional-logic version of the knowledge base and specify what their equivalents are in the original first-order logic knowledge base.
- (b) Define the statements that should be stored in the propositional-logic version of the knowledge base.

The symbols you define should be comprehensive enough to allow us to translate any well-defined inference problem in the original knowledge base to an equivalent problem for the propositional knowledge base. Anything that we can infer from the original first-order logic knowledge base we should also be able to infer from the propositionalized knowledge base, and vice versa.

(a) big (con): big\_can big (bike): big\_car

Small (con): Small car Small (bike): Small-bike

forst (con): forst\_car forst (bike): forst\_bike

Slower (con, con): Slower\_can\_car

Slower (con, bike): Slower\_con\_bike.

Slower (bike, bike): Slower\_bike\_bike

(b) Universally Instantiation.

big (car) n Small (bike)

Small (bike) (=) fast (bike)

Small (car) (=) fast (car)

forst (bike) =) Slower (car, bike).

Converting to Propositional Logic.

big\_car A smoull\_bike.

small\_bike (=) pot\_bike.

Small\_car (=) fast\_car

fast\_bike ) Sover\_car\_bike.

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# Question 8 – 15 points

Is the propositional logic KB obtained in Question 7(b) in Horn Form? If it is not can it be converted into Horn Form. If it can be, use the Horn form representation and Backward Chaining to show that his knowledge base entails slower(car, bike) [Note: Use the symbols obtained in Question 7(a) to convert this statement into propositional logic too. Also Modus Ponens can also be used with

Yes it can be written in Horn Form?

big\_an Small-bike.

Snall\_bike = ) fast\_bike.

fost\_bilce => Snall\_bilco.

Small con => fost-car.

Jost-an => Small-an

fest-bike => slover\_ lar\_bike.

Using Boekward Chairy.

Slover\_car\_bike odd fost\_bike

Jost-Sike.
Slower-Kar-Sike add Small-biko.

Snall\_bike is already tree

So you can use small-bile ) fast-bile to Small-bile to show fest-bike. by Malus Ponons

Now use fest-bile > slower\_car-bile & fest-bile to show slower Car bike by Malus Porens

So slove-con-bile istème.

KB = slower\_Car\_bilce.

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# Question 9 (OPTIONAL) - 10 points Extra Credit

function PL-RESOLUTION( $KB, \alpha$ ) returns true or false inputs: KB, the knowledge base, a sentence in propositional logic  $\alpha$ , the query, a sentence in propositional logic  $clauses \leftarrow$  the set of clauses in the CNF representation of  $KB \land \neg \alpha$   $new \leftarrow \{\}$  loop do

for each  $C_i$ ,  $C_j$  in clauses do  $resolvents \leftarrow \text{PL-RESOLVE}(C_i, C_j)$ if resolvents contains the empty clause then return true  $new \leftarrow new \cup resolvents$ if  $new \subseteq clauses \cup new$ 

The box above shows the PL-RESOLUTION function as defined in the textbook.

#### (a) [5 points]:

This function refers to the empty clause. Specify what this empty clause is, in the context of PL-RESOLUTION. Remember, a propositional logic sentence is defined by defining its symbol (if any), its connective (if any) and its sub expressions (if any). Thus, fully specify what values the empty clause will contain for the symbol, connective, and sub expressions.

Symbol: None Connector: None Sub-Expressive: None

#### (b) [5 points]:

What can you say about the truth value of the empty clause referred to in the PL-RESOLUTION pseudo code? Is it always true, always false? Or sometimes true and sometimes false? Justify your answer.

The empty clause is inherently folse.

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# **SCRATCH**