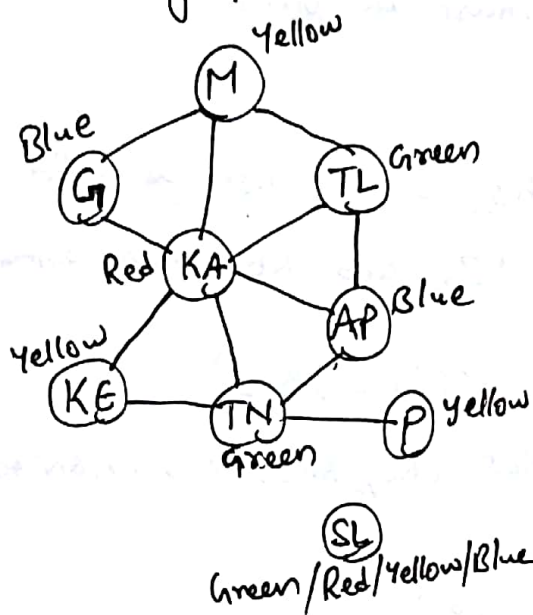


Assignment - 5

1) (a) Constraint graph:



variables: M, G, TL, KA, AP, TN, SL, KE, P

Constraint: Color the graph such that no 2 adjacent states have same color.

(b) Backtracking search with MVR and Degree heuristic

Color: {Red, Green, Blue, Yellow}

Level 1: Max constraint, legal values,

KA. assigned Red (has max constraint = 6)

Level 2: TN assigned Green (Max constraint = 4)

Level 3: AP assigned Blue (Max constraint = 3, legal val = 2)

Level 4: TL assigned Green (Max constraint = 3, legal val = 2)

Level 5: M assigned Yellow (Max constraint = 3, legal val = 2)

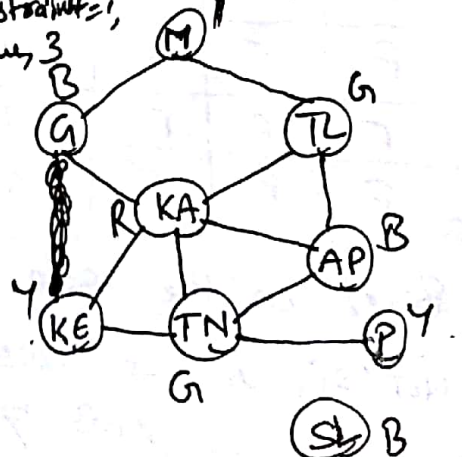
Level 6: G assigned Blue (Max constraint = 2, legal val = 2)

Level 7: KE assigned Yellow (Max constraint = 2, legal val = 2)

Level 8: SL assigned Red (Max constraint = 0, legal value = 4)

Level 9: P assigned Yellow (Max constraint = 1, legal value = 3)

(c) Constraint graph solution:



$$2) A \Leftrightarrow B$$

means

$A \Rightarrow B$  AND  $B \Rightarrow A$  (Biconditional Elimination)

i.e.  $A \Rightarrow B$  AND  $B \Rightarrow A$  must be valid.

For  $KB_1 \Leftrightarrow KB_2$ ,

$KB_1 \Rightarrow KB_2$  AND  $KB_2 \Rightarrow KB_1$  must be valid.

i.e.  $KB_1$  must entail  $KB_2$  and  $KB_2$  must entail  $KB_1$ .

fun CHECK\_EQUIVALENCE( $KB_1, KB_2$ )

return (TT\_ENTAILS? ( $KB_1, KB_2$ ) AND TT\_ENTAILS? ( $KB_2, KB_1$ ))

$$3) \textcircled{a} \text{ Yes } KB \text{ entail } S_1 \text{ (} KB \models S_1 \text{)}$$

i.e. whenever  $KB$  is true,  $S_1$  is always true.

A	B	C	KB	$S_1$
T	T	T	T	T
T	F	T	T	T

$$\textcircled{b} \text{ Checking } \neg(KB) \text{ entail } \neg(S_1) \text{ (} \neg KB \models \neg S_1 \text{)}$$

A	B	C	$\neg(KB)$	$\neg(S_1)$
T	T	F	T	F
T	F	F	T	F
F	T	T	T	T
F	T	F	T	T
F	F	T	T	T
F	F	F	T	T

Based on the table values,

$\neg(S_1)$  is not TRUE whenever  $\neg(KB)$  is True  
 $\neg KB \not\models \neg S_1$

7) Constants: John, Bill

Predicates: tall, taller

Proposition:

tall(John): tall\_John

tall(Bill): tall\_Bill

taller(John, Bill): taller\_John\_Bill

taller(John, John): taller\_John\_John

taller(Bill, John): taller\_Bill\_John

taller(Bill, Bill): taller\_Bill\_Bill

KB taller(John, Bill): taller\_John\_Bill

$\forall x$  taller(x, Bill)  $\Rightarrow$  tall(x):

taller\_Bill\_Bill  $\Rightarrow$  tall\_Bill

taller\_John\_Bill  $\Rightarrow$  tall\_John

5) Let A be true, if it rains on May 1, 2017

Let B be true, if John must give Mary a check of 10,000\$ on May 2, 2017

Let C be true if Mary must mow the lawn on May 3, 2017

(a) Propositional logical statement:

$$A \Rightarrow B$$

$$B \Rightarrow C$$

(b) Logical statement

$$\neg A \wedge B \wedge C$$

(c) The contract was violated.

According to the contract John must give a check of \$10,000 to Mary if it rains on May 1, 2017. But even though it didn't rain on May 1, 2017, John gave a check of 10,000\$ to Mary.

4) Symbols:  $A, B, C, D$

The two cases of false in KB are

A	B	C	D	KB
T	T	T	T	F
T	F	T	T	F

CNF is the product of sums.

$$\Rightarrow \overline{(A \cdot B \cdot C \cdot D)} \cdot \overline{(A \cdot \bar{B} \cdot C \cdot \bar{D})}$$

$$\Rightarrow (\bar{A} + \bar{B} + \bar{C} + \bar{D}) \cdot (\bar{A} + B + \bar{C} + D)$$

$$\Rightarrow ((\neg A) \cup (\neg B) \cup (\neg C) \cup (\neg D)) \cap ((\neg A) \cup B \cup (\neg C) \cup D)$$

//

6) Constants: John, Mary, Smartphone, Laptop and Shadow.

predicates:

$Dog(x)$ :  $x$  is a dog

$Gave(x, y, z)$ :  $x$  gave  $y$  to  $z$

$Male(x)$ :  $x$  is a male

$Female(x)$ :  $x$  is a female

KB:-  $Dog(Shadow)$

$Gave(John, Shadow, Mary)$

$Male(Shadow) \Rightarrow Gave(Mary, Smartphone, John)$

$\neg Male(Shadow) \Rightarrow Gave(Mary, Laptop, John)$

$\exists x, \exists y, Gave(John, x, y) \wedge Male(x) \wedge Dog(x)$

$Gave(Mary, Laptop, John)$  //