

## Reduction of Order by roots

- Homogeneous Linear equations with Constant coefficients:  
→ general solution of  $ay'' + by' + cy = 0$  is found by Solving Equation " $am^2 + bm + c = 0$ " for roots  $m_1$  &  $m_2$
- Case 1:  $b^2 > 4ac$ ,  $m_1$  &  $m_2$  are real & distinct  
$$Y = C_1 e^{m_1 x} + C_2 e^{m_2 x}$$
- Case 2:  $b^2 = 4ac$ ,  $m_1$  &  $m_2$  are real & equal  
$$Y = C_1 e^{m_1 x} + C_2 e^{m_1 x}$$
- Case 3:  $b^2 < 4ac$ ,  $m_1$  &  $m_2$  are conjugate complex numbers  
$$Y = e^{\alpha x} (C_1 \cos(\beta x) + C_2 \sin(\beta x))$$
- Given  $ay'' + by' + cy = 0$  we get  $am^2 + bm + c = 0$   
$$m_1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad m_2 = \frac{-b - \sqrt{b^2 - 4ac}}{2a}$$

end