

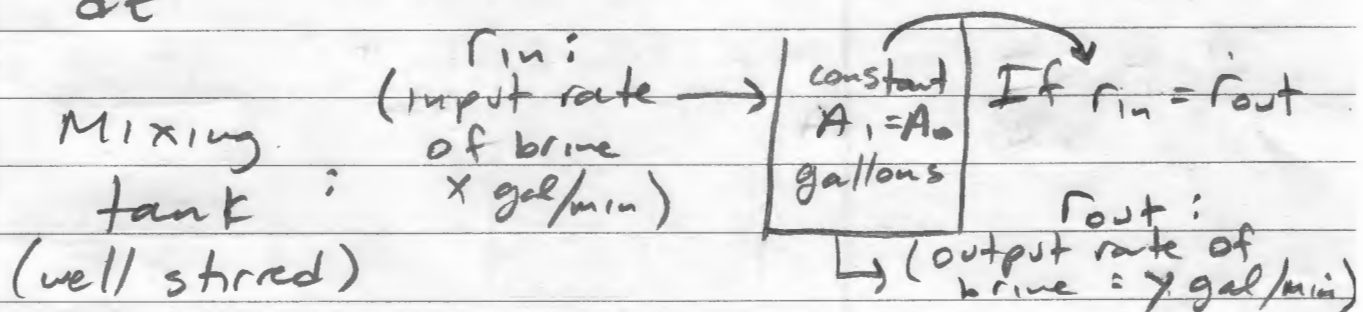
## Mixtures:

$A_0$  = Initial amount of Brine in tank

$A_1$  = Amount of brine in tank at time  $t$

$A(t)$  = amount of salt at time  $t$

$\frac{dA}{dt}$  = Rate at which  $A(t)$  changes



- The solution is pumped out at the same rate as entering the solution

$$\begin{aligned}\frac{dA}{dt} &= (\text{input rate of salt}) - (\text{output rate of salt}) \\ &= R_{in} - R_{out}\end{aligned}$$

$R_{in}$   $\rightarrow$  input rate at which salt enters the tank or input rate of salt

$$R_{in} = \left( \text{inflow concentration of salt} \right) \left( \text{input rate of brine} \right)$$

$$R_{out} = \left( \text{outflow concentration of salt } c(t) \right) \left( \text{output rate of brine} \right)$$

$$c(t) = \frac{A(t)}{A_1} \text{ lb/gal}$$

$$\frac{dA}{dt} = \left( \begin{array}{c} \text{inflow concentration} \\ \text{of salt} \end{array} \right) \left( \begin{array}{c} \text{input rate} \\ \text{of brine} \end{array} \right) - \left( \begin{array}{c} \text{outflow concentration} \\ \text{of salt} + c(t) \end{array} \right) \left( \begin{array}{c} \text{output rate} \\ \text{of brine} \end{array} \right)$$

If  $r_{in}$  and  $r_{out}$  denote the general input and output rates of the brine solutions, then there are three possibilities:

- |                      | <u>Gallons in tank</u>                              |
|----------------------|---|
| ① $r_{in} = r_{out}$ | constant $A_1$                                      |
| ② $r_{in} > r_{out}$ | increasing  |
| ③ $r_{in} < r_{out}$ | decreasing<br>(at the net rate $r_{in} - r_{out}$ ) |

Case ②:  $r_{in} > r_{out}$  and # gallons of brine in tank is increasing then it is accumulating liquid at a rate of  $(r_{in} - r_{out})$  gal/min. After  $t$  minutes there are  $A_1 = A_0 + (r_{in} - r_{out})t$  gallons

Case ③:  $r_{in} < r_{out}$  and # gallons of brine in tank is decreasing then it is losing liquid at a rate  $(r_{in} - r_{out})$  gal/min. After  $t$  minutes there are  $A_1 = A_0 + (r_{in} - r_{out})t$  gallons where  $r_{in} - r_{out}$  is negative.