# Howere work 1 - Solution Guide

# Assignment on Continuous-Time and Discrete-time Signals \*

Signals and Systems (ELC 321)
Department of Electrical and Computer Engineering
The College of New Jersey.

# Instructions:

- 1. The assignment questions are extracted from the Text (Signals, Systems, and Transforms, Fifth edition)
- 2. Figure reference in this assignment refers to the Text's Figure label
- 3. When using MATLAB to plot signals, scale your time axis such as to allow sufficient amount of the signal to be plotted. Use subplot to give 3 or 4 plots per page, label the axes of your plots accordingly e.g. Time (sec) on the x-axis and x(t) on the y-axis; the title should be the problem number, for example 2a).
- You do not need to submit the Matlab codes for this assignment but the generated figures must be printed out and submitted alongside your detailed solutions.
- Due Date: February 14, 2014.

Problem 1 (10 Marks). For the signal x(t) of Figure P2.1a plot lise Madlab to plot the following functions

a) 
$$x(3t-6)$$
, and

$$-4x(t)+2$$
.

Problem 2 (10 Marks). For the general case of transformations of discrete signals, given signals x[n] and  $x_i[n]$  can be expressed as 

$$x_t[n] = Ax[an + n_o] + B$$

Ξ

where a is rational and  $n_o$  is an integer.

a) Solve this expression for x[n].

b) Suppose that for the signal of Figure p9.7

$$x_1[n] = 0.5x_3[-n+1] + 2$$

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sketch  $x_3[n]$ .

Problem 3 (20 Marks). For each of the signals

- 1.  $x[n] = 2\mu[n]$ , and
- 2. x[n] = cos[0.1n].
- (a) Determine mathematically whether the signal is even, odd, or neither, and
- (b) Find the even part and the odd part of each of the signals.
- (c) Use Mattab to plot the signals, their even and odd parts.

Problem 4 (20 Marks). For each of the signals

- 1. x(t) = -4t, and
- 2.  $x(t) = -\mu(t-1) + \mu(-t-1)$ .
- $(a) \ \mathit{Determine}$  mathematically whether the signal is even, odd, or neither, and
- (b) Find the even part and the odd part of each of the signals
- (c) Use Matlab to plot the signals, their even and odd parts.

Problem 5 (10 Marks). Consider the signal

$$x(t) = \cos(\pi t) + 5c^{-j15t} + \sin(7t)$$

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If the signal is periodic, find its

- a) fundamental period Ta, and its
- b) fundamental frequency  $\omega_o$ .

Otherwise, prove that the signal is not periodic.

Problem 6 (20 Marks). A continuous-time signal  $x(t) = \cos(\pi t)$  is sampled enery T seconds resulting in the discrete-time signal x(n) = x(nT). Determine whether the sampled signal is periodic for

- I. T = 0.125s,
- 2. T = 0.130s.

For the sampled signal that is periodic, find

- a) the number of periods of x(t) in one period of x[n].
- b) the number of samples in one period of x[n].

<sup>\*</sup>Dr. Ambrose A. Adegbege

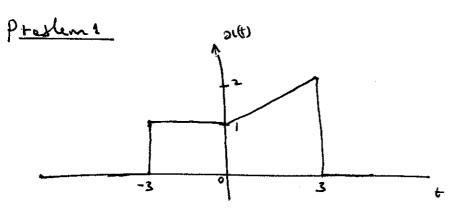
Problem 7 (10 Marks). Prove the time-scaling property of the Dirac delta function

$$\int_{-\infty}^{\infty} \delta(at - t_o)dt = \frac{1}{|a|} \int_{-\infty}^{\infty} \delta(t - \frac{t_o}{a})dt$$
 (4)
Hence or otherwise, evaluate the following integral
$$\int_{-\infty}^{\infty} \sin[t - \frac{2\pi}{6}]\delta(2t - \frac{2\pi}{3})dt$$
 (5)

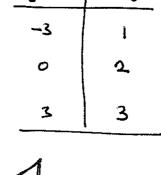
$$\int_{-\infty}^{\infty} sin[t-\frac{\pi}{6}]\delta(2t-\frac{2\pi}{3})dt$$

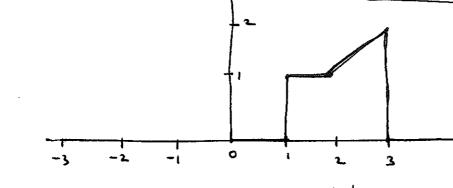
(5)





Let 7 = 3t-6 Then  $t = (\overline{c} + b)/3$ 





Dr (34- 4)

wt y(t) = -4 >1(t)+2

-a 161 =	-7 ***	1-4	esatt) + 2		
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		-4+		-1	
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2(4)	A&)
0	2
1	-2
2_	- 6

Let m= antro Such that

$$n = \frac{1}{a} (m - n_0)$$

susstituty into (1) gives

which yields

$$SICMJ = \frac{1}{A} \left[ SI_{+} \left[ \frac{1}{A} \left( M - n \delta \right) - B \right] \right]$$

Replacing on with a gives the find result

or 
$$CuJ = \frac{1}{A} \left( 3C_{+} \left[ \frac{1}{a} (n-n_{0}) \right] - B \right)$$
.

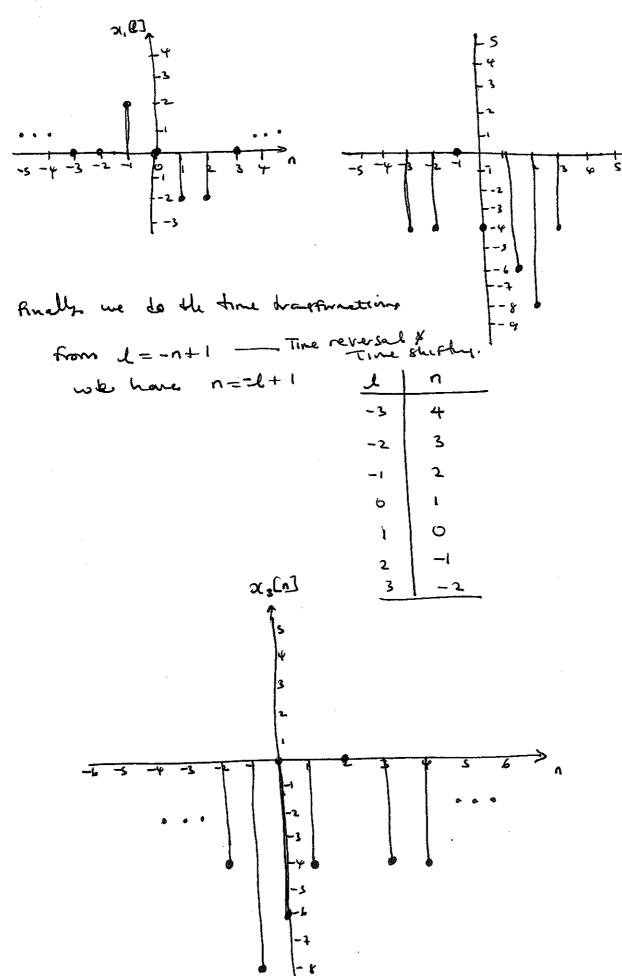
lut m=-n+1 => n=-m+1

$$x_3(m) = 2(x, (-m+i) - 2)$$

$$x_3[n] = 2 \left( x_1[-n+1] - 2 \right)$$

This involves both time- and amplitude transformations we do amplitude transformation FIFA 1. e

L	x,(2]	7(4)
-3	0	-4
-2	Ø	-4
t	2	0
O	0	-4
1	-1	-6
2	_2	- 8
3	0	-4



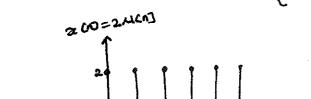
$$9, \quad 9(0) = 21(0) = \begin{cases} 2 & 1 & 1 & 70 \\ 0 & 1 & 1 & 40 \end{cases}$$

$$3(C-n) = 2M(-n) = \begin{cases} 2; & n = 0 \\ 0; & n > 0 \end{cases}$$

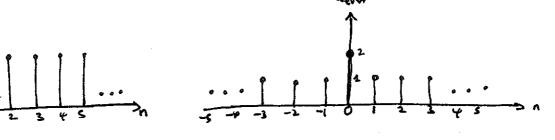
$$2(evn Cn) = \frac{1}{2} (2(n) + 2(-n)) = \frac{1}{2} (2(n) + 2(-n)) = 2(n) + 2(-n)$$

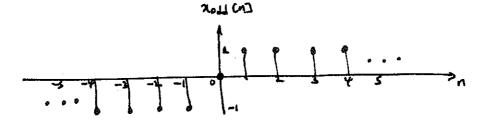
$$= \begin{cases} 2 & n = 0 \\ 1 & n \neq 0 \end{cases}$$

The odd part 4



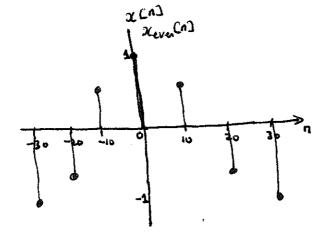
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Sme x C-n] = 21 Cn], the signal is an even signal

 $C_{II}$ 



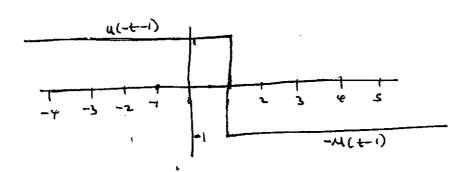
## problem 4

Problem 4 Continued

$$2(t) = -M(t-i) + M(t-i) = -(-M(t-i) + M(-t-i) = -x(t)$$

by 
$$\alpha_{\text{even}}(t) = 0$$
  $\alpha_{\text{odd}}(t) = \alpha_{\text{even}}(t)$ 

Сп



### Preblem 5

$$a_1(t) = (os(\pi t)) = cos(\omega t)$$

is periodic with wi= 7 and Ti= 2

az(t) = 5e-jist = 5e-jwt is periodic with w2=15 and T2= 27/s

730 = Sin(74) = Sin(w+) is periodic with w3=7 and T3= 2x cheeking in the condition in sitt to be periodic

Since à 15 au irrahaal number, the ratio or the periods one not rationals Therefore Signal 2(4) is not periodic i.e apariodic.

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Problem 6 Q(1) = (us(T+)
              |x(t)|_{t=nT} = \cos(\pi nT) \equiv \cos(\omega_0 nT) = \cos(2\pi(\frac{\tau}{\tau_0})n)
      The period To as sets is aslained from
                            コユスニス コ て。= 2
         For periodic signal
                          I = R - soatio or integers
      So for 7=0.125
                 we have \frac{K}{N} = \frac{0.12S}{2} = \frac{1}{16}
              Heree De COD es persodic with N=16
        ai Sure NT= KTO
                         => 16 T = To
                    N=16
        a_{1}
       b1 for 7=0.130
                     \frac{T}{T_0} = \frac{K}{N} \Rightarrow \frac{K}{N} = \frac{0.130}{2} = \frac{13}{200} - \text{periodic with}
\frac{T}{N} = \frac{13}{N} \Rightarrow \frac{13}{N} = \frac{13}{200} - \frac{13}{N} = \frac{13}{200}
                          12=13
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