## Assignment 4: Fourier Series and Transform\*

Signals and Systems (ELC 321)
Department of Electrical and Computer Engineering
The College of New Jersey.

## **Instructions:**

- 1. The assignment questions are extracted from the Text (Signals, Systems, and Transforms, Fifth edition)
- 2. When using MATLAB to plot signals, scale your time or frequency axis such as to allow sufficient amount of the signal to be plotted. Use subplot to give 3 or 4 plots per page; label the axes of your plots accordingly e.g Time (sec) on the x-axis and x(t) on the y-axis; the title should be the problem number, for example 2a).
- 3. No submission is required for this assignment.
- 4. Due Date: Not Applicable.

**Problem 1** (50 Marks). The block diagram of Figure 1 is an electronic oscillator for generating pure sinusoidal signal of a particular frequency, say  $\omega_o$ . The block comprises of a square wave generator and a filter. The square wave generator can be realized using the circuit in Figure 2.

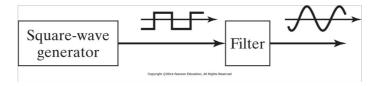


Figure 1: Square Wave Generator

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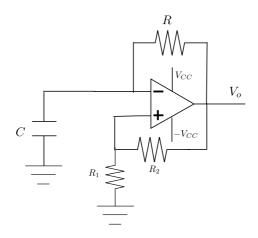


Figure 2: Square Wave Generator

a) Simulate the square wave generator in Pspice to obtain a square wave output. Set  $V_{CC} = 5V$  and use appropriate component values to obtain a period of 5 Secs. Include the plots of the capacitor voltage and the output voltage  $V_o$  in your report. Hint: The period T is given by the relation

$$T = 2RC \ln \left(\frac{1+\alpha}{1-\alpha}\right) \text{ with}$$

$$\alpha = \frac{R_1}{R_1 + R_2}$$
(2)

$$\alpha = \frac{R_1}{R_1 + R_2} \tag{2}$$

You may fix  $\ln\left(\frac{1+\alpha}{1-\alpha}\right) = 1$  and then compute the values  $R_1, R_2, R$  and C to achieve your desired Period of 5 seconds.

- b) Express the square-wave obtained in step (a) into its exponential Fourier series.
- c) Use Matlab to plot truncated form of the Fourier series obtained in step (b) using the following number of harmonics:
  - (a) 3-Harmonics, i.e only include terms up to  $3\omega_o$  in your Fourier series.
  - (b) 9-Harmonics
  - (c) 21-Harmonics, and
  - (d) 45-Harmonics

Problem 2 (50 Marks). Figure 3 shows a half-wave rectifer circuit with sinusoidal signal input  $V_S(t) = A\sin(\omega t)$  as shown in Fig 4. The voltage measured across the load resistor  $R_L$  is shown in Fig 5 assuming ideal diode behavior.

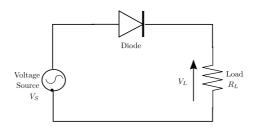


Figure 3: Half-wave Rectifier Circuit

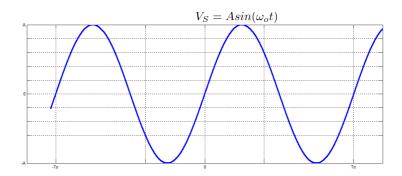


Figure 4: Sinusoidal Input

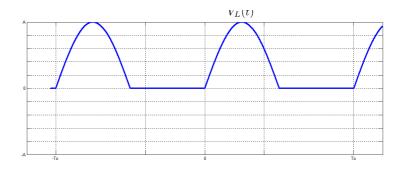


Figure 5: Half-wave rectified Signal

- a) Determine the period  $T_o$  of both the input and output signals shown in Figs 4 and 5.
- b) Express the input sinusoidal signal as an exponential Fourier series.
- c) Express the half-wave rectfied signal of Fig. 5 as an exponential Fourier series. Deduce the average value of the half-wave rectified signal.

**Problem 3** (50 Marks). The pulsed sinusoid of Figure 6 is formed by multiplying a sinusoidal signal x(t) of Fig. 7 by a rectangular pulse of Fig. 8

sometimes called a window. This pulsed-waveform has many applications expecially in electronic communication systems and in detection systems such as radar and sonar.

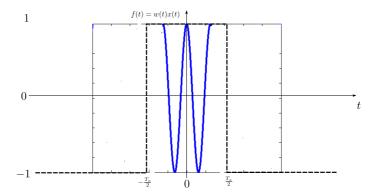


Figure 6: Pulsed Cosine waveform

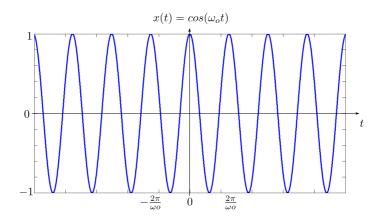


Figure 7: Cosine waveform

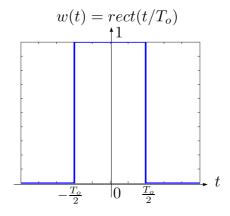


Figure 8: Rectangular Pulse

- a) Determine the Fourier transform of the cosine waveform  $x(t) = cos(\omega_o t)$  shown in Fig. 7 and plot its magnitude spectrum.
- b) Find the Fourier transform of the rectangular pulse of Fig. 8 and plot its magnitude spectrum using Matlab
- c) Determine the Fourier tranform of the pulsed cosine waveform of Fig.6 and plot the magnitude spectrum using Matlab.