Functional Programming: Assignment 5

Group 60

Lucas van der Laan s1047485

1 Warm-up

1

- const x y :: a -> b -> a
- (\$->) :: a -> (a -> b) -> b
- oper :: (Fractional a) => [char] -> a -> a
- mapMap :: (a -> b) -> [[a]] -> [[b]]
- without :: (a -> Bool) -> [a] -> [a]
- on :: $(b \rightarrow b \rightarrow c) \rightarrow (a \rightarrow b) \rightarrow a \rightarrow a \rightarrow c$

2

- f1: (Input + 1) * 5
- f2: (Input * 5) + 1
- f3: It sets the maximum of the input to 100 and the minimum to 0, if it's inbetween, it will just result the input.
- f4: Returns true if the length of the list is smaller than 5, false otherwise

What if we change f4 to (5<): We now check the other side of the equation, so it will do the opposite, it basically makes it bigger than 5.

What if we change f4 to ((<)5): We now apply < to 5, which means that it will again do bigger than.

3

1.

```
onlyElem :: (Eq a) => a -> [a] -> Bool
onlyElem n = (== 1) . length . filter (== n)
```

2.

```
onlyOnce :: (a -> Bool) -> [a] -> Bool
onlyOnce f = (== 1) . length . filter f
```

3.

```
onlyElem :: (Eq a) => a -> [a] -> Bool
onlyElem n = onlyOnce (== n)
```

4

Tried some stuff, nothing worked.

5

```
and :: [Bool] -> Bool
    and = foldr (&&) True
3
    or :: [Bool] -> Bool
4
    or = foldr (||) False
5
6
    elem :: (Eq a) => a -> [a] -> Bool
    elem n = foldr (\x -> (||) (n == x)) False
    maximum :: (Ord a) \Rightarrow [a] \rightarrow a
10
    maximum [] = error "An empty list has no maxmium"
11
    maximum xs = foldl1 max xs
12
13
    fromList :: (Ord a) => [a] -> Tree a
14
    fromList = foldr insert Leaf
15
16
    fromBits :: [Integer] -> Integer
17
    fromBits = foldr (\xspace x acc -> 2 * acc + x) 0
18
```

I prefer the written out version of recursion, as it is easier to comprehend.

2 Mandatory

6

```
--define using the _list design pattern_

compose :: [a -> a] -> a -> a

compose [] = id

compose (x:xs) = x . compose xs

--define using `foldr`

compose' :: [a -> a] -> (a -> a)

compose' = foldr (.) id
```

It computes the multiplication of all the numbers between 1 and n compose (map (*) [1..n]) 1 => compose ([(x -> x * 1), (x -> x * 2), .. n]) 1 So it then applies all these functions to the new result, with the first doing it on 1

So this becomes 1 * 1 * 2 * 3 * 4 * ... * n

```
--define in terms of *only* `map` and `compose`

foldr' :: (a -> b -> b) -> b -> [a] -> b

foldr' func input xs = compose (map func xs) input
```

7

```
bits :: Int -> [Int]
1
    bits = unfoldr (\x -> if x == 0 then Nothing else Just (x `mod` 2, x `div` 2))
2
3
    zip :: [a] -> [b] -> [(a,b)]
    zip xs ys = unfoldr go seed
5
6
      where
        seed = (xs, ys)
        go (xs, []) = Nothing
8
        go ([], ys) = Nothing
9
        go (x:xs, y:ys) = Just ((x, y), (xs, ys))
10
11
    take :: Int -> [a] -> [a]
12
    take n xs = unfoldr go seed
13
      where
        seed = (n, xs)
15
        go(0, xs) = Nothing
16
        go (n, []) = Nothing
17
        go (n, x:xs) = Just(x, (n-1,xs))
18
19
    primes :: [Integer]
20
    primes = unfoldr go [2..]
21
      where
22
         -- No need for empty list case, since we always put [2..]
23
        go (p:xs) = Just(p, [n | n <- xs, n `mod` p /= 0])
24
```

```
25
    apo :: (t -> Either [a] (a, t)) -> t -> [a]
26
    apo f seed = case f seed of
27
      Left 1
                 -> 1
28
      Right (a,ns) -> a : apo f ns
29
30
     (++) :: [a] -> [a] -> [a]
31
    xs ++ ys = apo go xs
32
      where
33
         go [] = Left ys
34
         go(x:xs) = Right(x, xs)
35
36
    insert :: (Ord a) => a -> [a] -> [a]
37
    insert x = apo go
38
      where
39
         go [] = Left [x]
40
         go (y:ys)
41
           | x \le y = Left (x:y:ys)
           | otherwise = Right (y,ys)
43
44
    unfoldrApo :: (t \rightarrow Maybe (a, t)) \rightarrow t \rightarrow [a]
45
    unfoldrApo f seed = apo go seed
46
      where
47
         go seed = case f seed of
48
          Nothing -> Left []
49
          Just x -> Right x
```

8

See WordState.hs, lines of code are too long.