

Introduction

These notes are about the analysis of spike trains. It is based on Dayan & Abbott, sections 1.2, 1.4 & 3.2. There is also a set of slides that go with this lecture containing pictures. I offer an error bounty of between 20p and 2 pounds for mistakes. Contact me at conor.houghton@bristol.ac.uk or come up after a lecture.

Decoding spike trains

There are diverse methods for examining spike trains and describing or decoding their activity; they are all useful in different ways and unsatisfactory in others. The methods we will look at here will typically involve histograms, that is, some sort of discretization of time and *binning* of results; this is typically of the field.

Peristimulus time histogram

The idea here is to look at the activity immediately after a stimulus, so the stimulus is repeated as many times as is possible and the spikes that occur different amounts of time after the stimulus are binned together. Thus, a *trial* refers to the responses to a single presentation of the stimulus and

- Superimpose the trials with the stimulus times superposed.
- Divide time into small intervals or bins.
- Plot the spike count in each bin.

This is illustrated in Fig. 1.

A related idea is the *spike triggered average*, this is used when there is a continuous stimulus, such as the current level used to stimulate an electric fish, and the spike triggered average shows the average value of the stimulus at different amounts of time before a spike. The spike triggered average can be interpreted in terms of the sort of linear model we discussed in the case of vision.

Autocorrelogram

This shows how the behavior of a spike train is related to its behavior at a different time; it is used to detect periodic behavior in spike trains: a periodic spike train will have gaps between spikes related to the period. To work out the autocorrelogram

- Divide time into small bins, of length δt say.
- Count how many spikes are separated by a time between $n\delta t$ and $(n+1)\delta t$ and put them in the n th bin.
- Plot the histogram.

This is illustrated in Fig. 2.

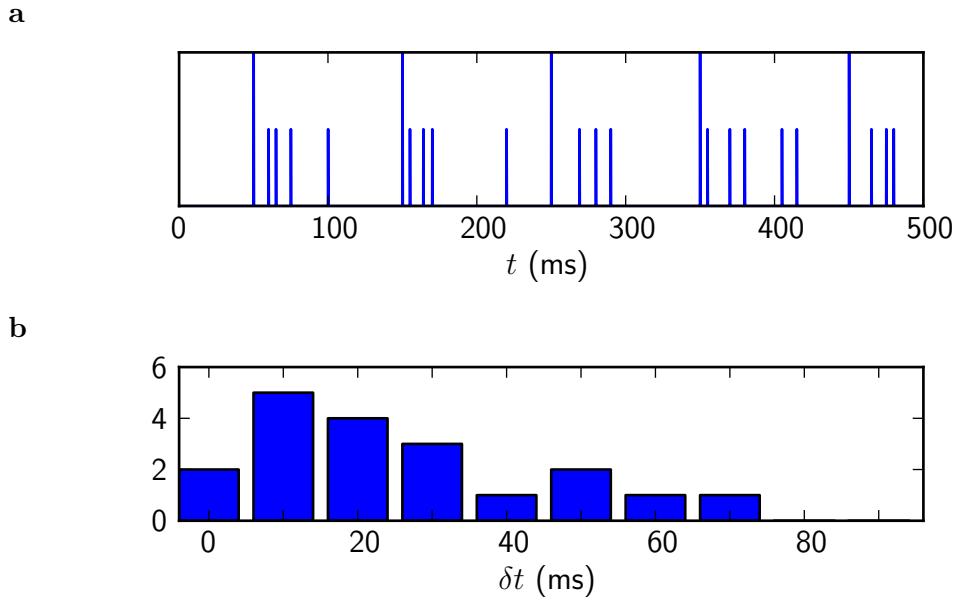


Figure 1: Peristimulus time histogram. **a** represents a spike train and stimulus, with the tall lines marking the stimulus and the short ones the spikes. **b** is the peristimulus time histogram with bin size 10 ms, we see that two spikes came within 1 ms of stimulus and five between 10 and 20 ms.

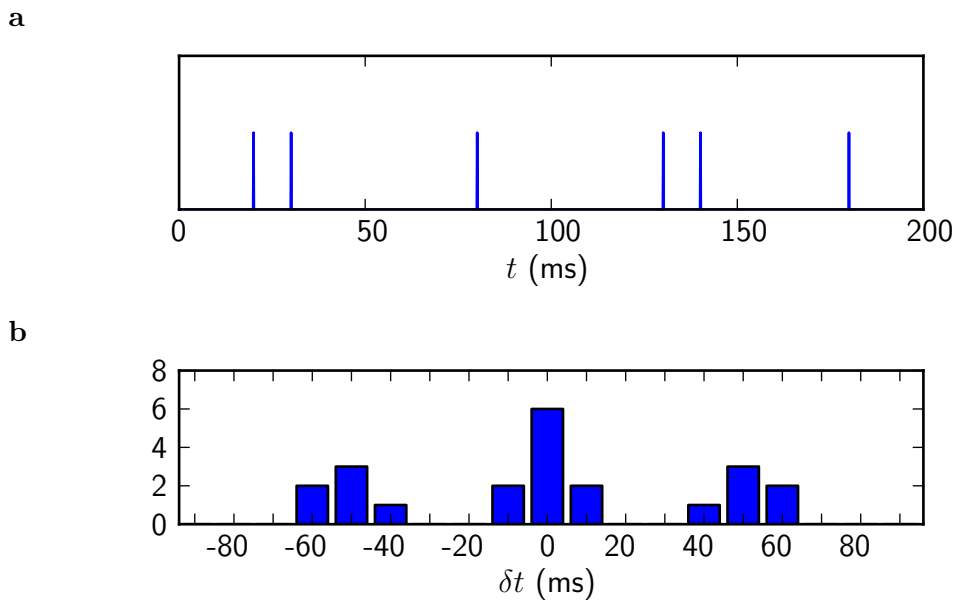


Figure 2: Autocorrelogram. **a** represents a spike train and **b** is the autocorrelogram. All spikes are a time distance of zero from themselves, so the central spike corresponds to the six spikes themselves. The two for $\delta t = 10$ ms tells us that there are two spikes that are one apart. This spike train is roughly periodic and that is matched by the behavior of the autocorrelogram where there are more spike pairs a distance 50 ms apart than, say 30 ms apart.

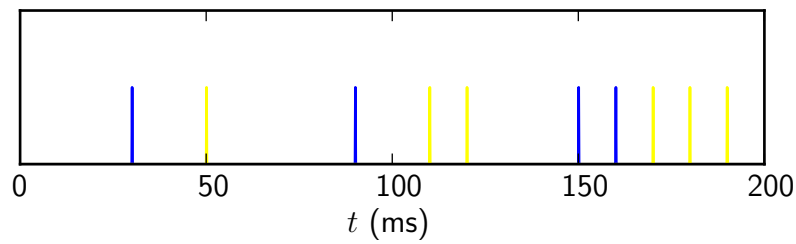
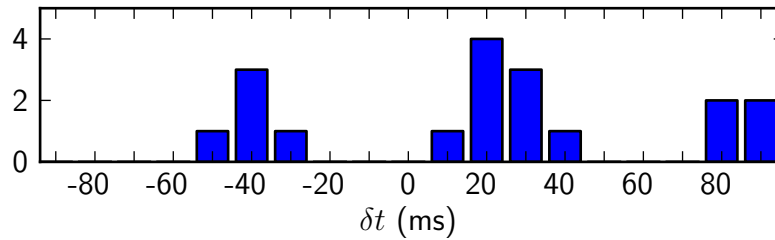
a**b**

Figure 3: Cross correlogram. **a** represents two spike train, one blue with spikes at 30, 90, 150, 160 and one yellow with spikes at 50, 110, 120, 170, 180 and 190. **b** is the crosscorrelogram. These spike trains are both periodic in the same way, which shows up as the repeating bumps in the cross-correlogram and one fires just before the other, so, for example, the four in the 20 ms bin corresponds to the four yellow spikes that occur between 20 and 30 ms after a blue spike. This could indicate that one neuron is causing the other to fire, or that they are responding to the same overall periodicity, but with different lags.

Cross correlogram

A cross correlogram is useful for measuring the relationship between the spiking in two neurons; it might give an indication that one neuron may be influential in causing the other to spike or it might show that both neurons are entrained to the same periodic behavior. It is like the auto-correlogram except that it is gaps between spikes from different spike trains that are measured and plotted. To work out the cross correlogram

- Divide time into small bins, of length δt say.
- Count how many spikes from neuron two are found between $n\delta t$ and $(n+1)\delta t$ compared to the a spike from neuron one.
- Plot the histogram.

This is illustrated in Fig. 3.

Tuning curve

The tuning curve is used to related the response to a family of stimuli parameterized by a single variable, such as the angle of a bar for vision. The tuning curve is a plot of the firing rate against the parameter, so $r(\theta)$ for angle in vision.

Decoding a single neuron

Consider an experiment in which a monkey is shown a screen full of moving dots, some move randomly but some move coherently to either the left or right. The monkey is trained to move its eyes to the left if the dots are moving that way and to right if that's the way the dots are moving. If the monkey gets its determination correct it gets a treat, probably juice. The experimenter can control the coherence of the dots, at one extreme there is no movement one way or another, all the dots move randomly; at the other extreme all the dots are moving the same way.

Britten et al. (Neuroscience (1992) 12:4745-65) managed to record from a direction selective neuron in the monkey brain. Such a neuron has a preferred direction. If the dots were moving the neurons preferred direction it has a high firing rate, if they weren't, it has a low one. However, in this noisy situation the firing rate varied from trial-to-trial, the main thing is that the average is higher for trials in the preferred direction to the other direction. In short, it looks like there are two normal curves, one corresponding to the preferred direction, the other to the other; these curves overlap and overlap more and more as the coherence is lowered, making the motion more random.

One way of describing how different the two distributions are is to use d' . If μ_1 is the average firing rate in the unpreferred direction and μ_2 in the preferred direction and assuming both distributions have the same variance, then

$$d' = \frac{\mu_2 - \mu_1}{\sigma} \quad (1)$$

This is illustrated in Fig. 4.

As an example, imagine that when the dots move left the firing rates are $\{15, 20, 25\}$ and when they move right they are $\{24, 30, 36\}$. Hence

$$\mu_1 = \frac{15 + 20 + 25}{3} = 20 \quad (2)$$

and

$$\mu_2 = \frac{24 + 30 + 36}{3} = 30 \quad (3)$$

Now, they don't have the same variances

$$\sigma_1^2 = \frac{5^2 + 5^2}{2} = 25 \quad (4)$$

and

$$\sigma_2^2 = \frac{6^2 + 6^2}{2} = 36 \quad (5)$$

hence $\sigma^2 = 30.5$. So

$$d' = \frac{30 - 20}{\sqrt{30.5}} = 1.81 \quad (6)$$

This situation can be examined from the point-of-view of an ideal observer, one who can't see the dots, but can see the firing rate of two neurons, these are imagined as identical neurons except one prefers left and the other prefers right. How well would this ideal observer do trying to guess which way the dots are going? Imagine the distribution of firing rates are normal so, say for the cell preferring left if the dots are moving left the firing rate is chosen randomly from

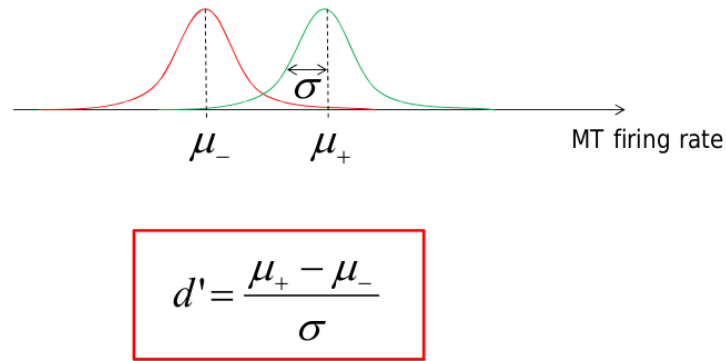


Figure 4: Two different responses from an MT neuron. The green curve corresponds to the distribution of firing rate responses for the preferred direction, the red curve for the other one. d' measures how different they are; it is basically the distance between the two means measured in units of the variance. [This figure was copied from Rafal's original slides.]

$\mathcal{N}(\mu_2, \sigma)$ and if the dots are moving right the firing rate is from $\mathcal{N}(\mu_1, \sigma)$. The other neuron, the one which prefers right, is the same, but the other way around. The idea observer has to then guess the neuron with the higher firing rate is the one whose preferred direction is the one the dots are moving in.

It is easy enough to calculate the chance the ideal observer would come to the correct conclusion based on the firing rates, usually the correct neuron has a higher firing rate than the rate for the other, incorrect, neuron. Lets say the dots are going left, the probability the observer is correct is the probability that the number chosen from the left-preferring neuron is higher than the one from the left neuron. It is

$$P(\text{right}) = P(\mathcal{N}(\mu_+, \sigma) > \mathcal{N}(\mu_-, \sigma)) \quad (7)$$

By some algebra on the distribution it turns out

$$P(\text{right}) = \Phi(d'/\sqrt{2}) \quad (8)$$

where $\Phi(t)$ is the cumulative for the normal distribution; it starts at zero, for low d' it is very hard to distinguish, and rises to one for large d' , which is when you would expect it to be easy to distinguish. In fact, in the Britten et al. paper they show that this curve matches the actual, observed, behavior curves for how often the monkey made mistakes.