

Careers in Organizations

Literature Review on Internal Labor Market

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Outline

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- 2 Markets
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Introduction

- "Black Box": an IO operation; a unitary agent for profit maximization, an one-multiple contract designer...
- the internal market: an administrative unit within which the **pricing and allocation of labor** is governed by **a set of administrative rules and procedures (institutions)**
 - ① **Market**: pricing-wage and allocation-career/promotion
 - ② **institutions**: design sectors, institutions, policies to incentivize/match human resources
- We will later see the internal labor market featuring both market functioning (especially the lemon) and mechanism design

Empirical Facts-Market

Before introducing the theoretical models, review some common phenomena in internal labor market (BGH,1994)

- Many workers begin employment at the firm at a small number of positions
- dynamic: Nominal wage decreases and demotions are rare (but real wage decreases are not)
- Correlations:
 - ① serial correlations: wage and promotion
 - ② Large wage increases early on in a worker's tenure predict promotions
 - ③ a positive relationship between seniority and wages
 - ④ Promotions tend to be associated with large wage increases, but these wage differences are small relative to the average wage differences across levels within the firm

Empirical Facts-Institutions

- Institutions: tradition v.s. innovative (CIA) (Osterman, 1994, 2000; Lawler et al., 1995)
 - ① (no) problem-solving teams and quality circles (information sharing)
 - ② (no) job rotation
 - ③ much/little effort and resources put into worker screening during the recruitment process
 - ④ incentive pay v.s. hourly pay
 - ⑤ much/little on-the-job training
 - ⑥ high/low job security
- Policies: Peter Principle, compensation profile, mandatory retirement, up-or-out promotion policy, exchange of cadres, skill development etc.
- Sector Divisions and Organization Hierarchies

Theoretical Models

- Theoretical Models:
 - ① identify and model a fundamental factor concerning the operation of internal labor markets
 - ② capture important empirical relationships
- How are wages/careers decided given some properties of firms and workers?
 - ① How does information asymmetry affect the market allocation?
 - ② How to design optimal mechanism to match workers with firms/incentivize workers?
- Key assumptions:
 - ① homo/hetero workers
 - ② multiple careers(hierarchies)
 - ③ complete/incomplete information
 - ④ static/dynamic setting

Candid Models: Markets

- Candid Models (revised from(Waldman,2012)):
 - ① "endogenous growth": human (specific) capital accumulation
 - ② Information: promotions as signals; symmetric learning and insurance
- Now increasing newly-emerged models incorporate these models to better explain more empirical conclusions

Basic Model: Notations

- Bertrand setting: F_0, F_1
- heterogeneous workers: ability $\theta \sim F$
- dynamic setting: q_t, ω_t ($t = 1, 2$)
- workers' utility: $u_A = \omega_1 + \omega_2$
- firms' profit: $\pi_{it} = q_t - \omega_t$

Human Capital Acquisition (Gibbons and Waldman, 1999)

- binary distribution: $\theta \in \{\theta_H, \theta_L\}$, $\Pr(\theta = \theta_H) = p$
- work experience l and effective productivity $\eta_t = \theta f(l) = \theta(1 + gl)$
- two activities: $q^i = d^i + b^i(\eta_t + \epsilon_t)$ ($i = 0, 1$) with $d^0 > d^1 > 0, b^1 > b^0 > 0$
- job assignment $j_t \in \{0, 1\}$ and output $q_t = (1 - j_t)q^0 + j_tq^1$
promotion if $j^1 < j^2$ demotion if $j^1 > j^2$
- public signal: $\phi_0 \subset \{\eta\}$, $\phi_1 = \{q_1, j_1\}$

Human Capital Acquisition (Gibbons and Waldman, 1999)

- ① θ realized and private, ϕ_0 public
- ② ω_1^i : simultaneous offer
- ③ A chooses firm $d_1 \in \{0, 1\}$ and receives $\omega_1^{d_1}$ (suppose $d_1 = 1$)
- ④ F_{d_1} chooses j_1 , output realized and ϕ_1 observed
- ⑤ ω_2^i : simultaneous offer
- ⑥ A chooses firm $d_2 \in \{0, 1\}$ and receives $\omega_2^{d_2}$ ($d_2 = 1$ when indifferent)
- ⑦ F_{d_2} chooses j_2 , output realized

Human Capital Acquisition (Gibbons and Waldman, 1999)

- subgame-perfect equilibrium: $\{\omega_t, d_t, j_t^{d_t}\}$
- $\eta_2^e(\phi) = E(\eta_2|\phi)$, $\phi = \{\phi_0, \phi_1\}$
 - ① Bertrand Assumption matters: wage=expected productivity
$$\omega_2^i(\phi) = (1 - j_2^0)(d^0 + b^0 \eta_2^e(\phi)) + j_2^0(d^1 + b^1 \eta_2^e(\phi))$$
 - ② linear productivity assumption: assignment threshold $\bar{\eta}^e = \frac{d^0 - d^1}{b^1 - b^0}$
 - ③ the first is similar to the second
 - ④ human capital acquisition makes the relative threshold decreasing holding the absolute threshold

Human Capital Acquisition (Gibbons and Waldman, 1999)

- pros: consistent with empirical findings below
 - ① a port of entry into the firm with small p
 - ② Long-term employment relationships are common (depending on the selection!)
firm-specific capital acquisition assumption matters
 - ③ demotions are rare (for the rational updating and human capital acquisition)
 - ④ positive correlation between promotion and wage (wage inequality and wage jumps)
 - ⑤ extensions: multiple stages for serially correlated wage and promotion
- cons:
 - ① innate ability is a one-dimensional fixed attribute
 - ② empirical findings for older workers can only be explained by assuming learning is significant

Promotions as Signals (Waldman, 1984)

- $\theta \in U[0, 1]$
- promotion is publicly observed while output is not
- job assignment: $q_1 = x \in (1/2, 1)$, $q_2(j, \theta, d_2) = (1 + s1_{d_2=d_1})[(1 - j)x + j\theta]$

Promotions as Signals (Waldman, 1984)

- ① ω_1^i : simultaneous offer
- ② A chooses firm $d_1 \in \{0, 1\}$ and receives $\omega_1^{d_1}$ (suppose $d_1 = 1$)
- ③ θ realized and observed by F_1 , output also observed
- ④ (j^1, ω_2^1) offered by F_1, j^1 publicly observed while ω_2^1 not
- ⑤ (j^0, ω_2^0) offered by F_1
- ⑥ A chooses firm $d_2 \in \{0, 1\}$ and receives $\omega_2^{d_2}$ ($d_2 = 1$ when indifferent)
- ⑦ output $q_2(j, \theta, d_2)$ realized

Promotions as Signals (Waldman, 1984)

- PBE: $\{\omega_t^i, d_t, j^i, \mu\}$
- $\omega_2(j^1) = E((1 - j^0)x + j^0\theta | j^1(\theta) = j^1)$
 - ① (Sequential) Bertrand Assumption matters: wage=expected productivity of firm 0
 $\omega_2^0 = \omega_2^1 = \omega_2(j^1)$
 - ② (linear) productivity assumption: assignment threshold $\bar{\theta} = \frac{1+2sx}{1+2s}$
 - ③ compared to first best, information asymmetry induces social efficiency

Promotions as Signals (Waldman, 1984)

- pros:

- ① the importance of history of job assignments and resume design
- ② large wage increases upon promotion
- ③ wage increases are small relative to wage differences across adjacent job levels.

- cons:

- ① no promotion is completely determined by observable characteristics
- ② not easily explain why the size of wage increases early at a job level forecast speed of promotion

Candid Models: Institutions

- Candid Models (revised from (Lazear and Oyer,2012)):
 - ① Contest Design: induce optimal average efforts, selection
 - ② Contract Design: tradeoff between incentives and insurance
$$y = e + \epsilon \text{ and decompse } \frac{\partial \omega}{\partial y}$$
 - ③ Training Programs, Career Life Design, Organization of Work (Job Design)

Contest Competitiveness (FNS, 2020)

- Incentives vs Discouragement is the key tradeoff when increasing competition in contest theory
 - ① Incentives: Increasing competition naturally increases contestants' incentives to exert high effort
 - ② Discouragement: Contestants' gains from exerting effort are reduced for beating their rivals harder
 - ③ the competitiveness of the competition:
 - ① the number of contestants (scaling up and contestant entry)
 - ② the reward structure (prize inequality)
- With homogeneous contestants and convex effort costs, increasing competitiveness means decreasing average effort.

Increasing competition \Rightarrow More spread-out distributions(extreme effort levels)
 \Rightarrow Decreasing expected effort under convex costs

Contest Competitiveness (FNS, 2020)

- Setup:

- ① $n \geq 1$: homogeneous risk-neutral contestants
- ② x_i : efforts, $c(x_i) : R_+ \rightarrow R_+$: effort cost (differentiable, strictly increasing and convex)
- ③ $v = (v_1, v_2, \dots, v_n) \in R_+^n$: an ordered vector of prizes
where $0 = v_1 \leq v_2 \leq \dots \leq v_n$ and $v_1 < v_n$, $F_v(x)$: distribution function
- ④ $\pi_v(p) = \sum_{i=1}^n v_i \binom{n-1}{i-1} p^{i-1} (1-p)^{n-i}$: the expected reward

- Formalization

- ① Price Inequality: $w, v \in P^n$ and $\sum_{i=1}^k w_i = \sum_{i=1}^k v_i$. Vector w is more unequal than v if w is more unequal than v in the Lorenz order.
that is $\sum_{i=1}^k w_i \leq \sum_{i=1}^k v_i$, for all $k = \{1, \dots, n\}$
- ② Scaling: Let $s > 1$ be an integer; $w \in P^{ns}$ is a scaling of $v \in P^n$ if $w_k = v_{\lfloor k/s \rfloor}$ for all $k \in \{1, \dots, ns\}$

Contest Competitiveness (FNS, 2020)

- ① a unique symmetric equilibrium in mixed strategies:

$$\pi \circ F_v(x) - c(x) = 0, x \in [0, c^{-1}(v_n)]$$

$$\rightarrow F_v(x) = (\pi^{-1} \circ c)(x)$$

- ② Suppose vector w is more unequal than (a scaling of) v . For any concave, strictly increasing function, u , of individual contestant effort $E[u(X^v)] \leq E[u(X^w)]$

- ③ Intuition: contestants face a direct incentive to increase effort but all contestants increasing effort cannot be sustained in equilibrium

\Rightarrow requiring an increase in the payoff from intermediate effort levels and a decrease in the payoff from high effort levels

\Rightarrow increasing the likelihood contestants make extreme efforts (more spread-out distributions)

\Rightarrow cost convexity comes into play

Mandatory Retirement (Waldman, 1984)

- Solution to moral hazard problem: pay less when young, more when old.
inducing the desire for a long-term contract thus voluntarily avoid shirking
voluntary in ex-ante sense while mandatory in ex-post sense (T)
- Notations:
 - ① $W^*(t)$ wage, $V^*(t)$ VMP (constant), $\tilde{W}(t)$ reservation wage (increasing)
 - ② T such that $\tilde{W}(t) = V^*(t)$, $\int_0^T W^*(t)e^{-rt}dt = \int_0^T V^*(t)e^{-rt}dt$

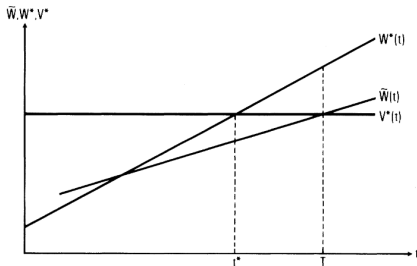


FIG. 1

Mandatory Retirement (Waldman, 1984)

- two cheating: $\tilde{g}(t)$ (bankrupt), $\theta_i \sim f(\theta_i)$ worker's benefit with cost $c(t)$

- expected rent:

$$R(t) = e^{rt} \int_t^T \left\{ W^*(\tau) - \tilde{W}(\tau) - \tilde{g}(\tau) e^{r\tau} \int_\tau^T [W^*(\delta) - \tilde{W}(\delta)] e^{-r\delta} d\delta \right\} e^{-r\tau} d\tau$$

- cheating at t : $\theta_i > R(t)$ determines $\tilde{f}(t)$

- $\max \int_0^T \left\{ W^*(t) + \tilde{f}(t) [\theta - e^{rt} \int_t^T W^*(\tau) e^{r\tau} d\tau] - \tilde{g}(t) e^{rt} \int_t^T W^*(\tau) e^{r\tau} d\tau \right\} e^{-rt} dt$

- $Wealth = \int_0^T [V^*(t) - \tilde{f}(t) \int_t^T V^*(\tau) e^{r\tau} d\tau - \tilde{f}(t)c(t) - \tilde{g}(t) \int_t^T V^*(\tau) e^{r\tau} d\tau] e^{rt} dt - \epsilon$

- the boundary condition: $V^*(T) - \tilde{f}(T)c(T) = \tilde{W}(T)$

- Important Insights:

- Mandatory: $W^*(T) > \tilde{W}(T)$, Steeper Wage Path \Rightarrow Less Shirking

- $\tilde{g}(t)$ increases: higher payment, shorter T

- Endogenous $\tilde{g}(t)$ - tradeoff between reduced worker cheating against increased firm cheating as $W^*(t)$ becomes more end weighted (Mandatory Still)

Further Readings

- Survey Literature: The Handbook of OE (Personnel Economics by Lazear and Oyer, Internal Labor Market by Waldman)
- Specific Models:
 - ① wage and promotion dynamics: Harris and Holmstrom(1982), Weiss (1984).
Rongzhu Ke et.al(2018)
 - ② human resources practices: Becker(1962, 1964), Lazear and Rosen(1981),
Rosen(1982), Bernhardt (1995), Wu and Fu(2022)
 - ③ Gibbons, Waldman, Powell