

1 Assignment No. 4: Merge k Ordered Lists Efficiently

Allocated time: 2 hours

1.1 Implementation

You are required to implement **correctly** and **efficiently** an $O(n \log k)$ method for **merging k sorted sequences**, where n is the total number of elements. (Hint: use a heap, see *Seminar no. 2* notes).

Implementation requirements:

- Use linked lists to represent the k sorted sequences and the output sequence

Input: k lists of numbers $\langle a_1^i, a_2^i, \dots, a_{m_i}^i \rangle$, $\sum_{i=1}^k m_i = n$

Output: a permutation of the union of the input sequences: $a'_1 \leq a'_2 \leq \dots \leq a'_n$

1.2 Minimal requirements for grading

- Interpret the chart and write your observations in the header (block comments) section at the beginning of your *main.cpp* file.
- Prepare a demo for each algorithm implemented.
- We do not accept assignments without code indentation and with code not organized in functions (for example where the entire code is in the main function).
- *The points from the requirements correspond to a correct and complete solution, quality of interpretation from the block comment and the correct answer to the questions from the teacher.*

1.3 Requirements

1.3.1 Generate k randomly sized sorted lists (having n elements in total, n and k given as parameters) and the merging of 2 lists (5p)

You will have to show your algorithm (*generation and merging*) works on a small-sized input (e.g. $k=4$, $n=20$).

1.3.2 Adapt *min-heap* operations to work on the new structure and the merging of k lists (3p)

You will have to show your algorithm (*merging*) works on a small-sized input (e.g. $k=4$, $n=20$).

1.3.3 Evaluation of the algorithm in average case (2p)

! Before you start to work on the algorithm's evaluation code, make sure you have a correct algorithm!

We will make the **average case** analysis of the algorithm. Remember that, in the average case, you have to repeat the measurements several times. Since both **k** and **n** may vary, we will make each analysis in turn:

- Choose, in turn, 3 constant values for k (**k1=5, k2=10, k3=100**); generate k **random** sorted lists for each value of k so that the number of elements in all the lists n varies between **100 and 10000**, with a maximum increment of 400 (we suggest 100); run the algorithm for all values of n (for each value of k); generate a chart that represents the **sum of assignments and comparisons** done by the merging algorithm for each value of k as a curve (total 3 curves).
- Set $n = 10.000$; the value of k must vary between 10 and 500 with an increment of 10; generate k **random** sorted lists for each value of k so that the number of elements in all the lists is 10000; test the merging algorithm for each value of k and generate a chart that represents the **sum of assignments and comparisons** as a curve.