

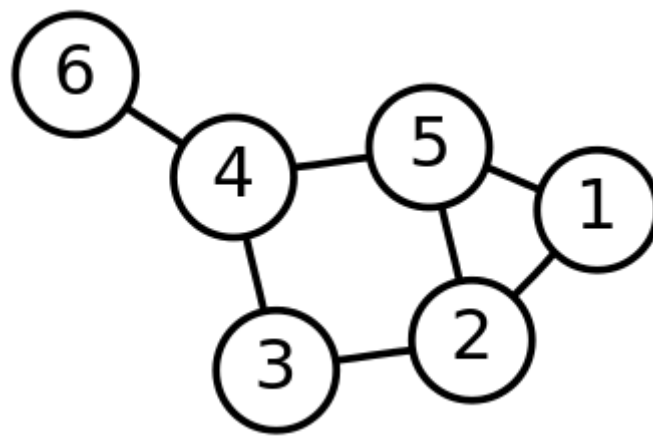
Graphs Search Algorithms (DFS & BFS)

1 Objectives

In this lesson, we will present how graph search algorithms can be implemented in Prolog. We will represent graphs using the edge-clause.

2 Theoretical Considerations

Example of undirected graph:



In Prolog:

```
edge(1,2).  
edge(1,5).  
edge(2,3).  
edge(2,5).  
edge(3,4).  
edge(4,5).  
edge(4,6).
```

```
is_edge(X,Y):- edge(X,Y);edge(Y,X).
```

2.1 Depth-First Search (DFS)

As in the previous session, we shall employ the *edge-clause* form for graph representation. Since depth-first search is the mechanism employed by the Prolog engine, all path predicates from the previous session employed a DFS search strategy. Below you have the predicates which implement a DFS search from a source node (by exploring the connected component of the source node).

We will use an auxiliary predicate to store already visited nodes.

```
:- dynamic visited_node/1.

% dfs(Source, Path)
dfs(X,_) :- df_search(X). % traversal of nodes
when finished, collection starts
dfs(_,L) :- !, collect_reverse([], L). % collecting results

% traversal predicate
df_search(X):-
    % store X as visited node
    asserta(visited_node(X)),
    % take a first edge from X to Y, rest are found through backtracking
    edge(X,Y),
    % check if this Y was already visited
    not(visited_node(Y)),
    % if it was not -this is why the negation is needed -
    % then we continue the traversal by moving the current node to Y
    df_search(Y).

% collecting predicate - collecting is done in reverse order
collect_reverse(L, P):-
    % we retract each stored visited node
    retract(visited_node(X)), !,
    % we add it to the list as the first element (reversed order)
    collect_reverse([X|L], P).
    % we unify the first and second arguments,
    % the result will be in the second argument
collect_reverse(L,L).
```

Follow the execution of:

```
?- dfs(1,R).
```

```
R = [1, 2, 3, 4, 5, 6].
```

2.2 Breadth-First Search (BFS)

The *BFS* strategy employs a queue to keep track of the expansion order of the nodes. In each step, a new node is read from the queue and is expanded – i.e. all its unvisited neighbors are added to the queue, in turn.

We will use a dynamic predicate to store the nodes to expand. The queue is „implemented” through the manner in which we insert (*assert*) and extract (*retract*) these visited nodes.

```
:- dynamic visited_node/1.  
:- dynamic queue/1. % the queue stores the nodes that need to be  
expanded  
  
% bfs(Source, Path)  
bfs(X, _):- % traversal of nodes  
    assertz(visited_node(X)), % add source as visited  
    assertz(queue(X)), % add source as first element in queue  
    bf_search.  
bfs(_,R):- !, collect_reverse([],R). % collecting results (same as previous)  
  
bf_search:-  
    retract(queue(X)), %retract node that needs to be expanded  
    expand(X), !, % call expand predicate  
    bf_search. % recursion  
  
expand(X):-  
    edge(X,Y), % find a node Y linked to given X  
    not(visited_node(Y)), % check if Y was already visited  
    % if Y was not visited before  
    asserta(visited_node(Y)), % add Y to visited nodes  
    assertz(queue(Y)), % add Y to queue to be expanded  
    % at some point  
    fail. % fail required to find another Y  
expand(_).
```

Follow the execution of:

?- bfs(1,R).

R = [1, 2, 5, 3, 4, 6].

2.3 Best-First Search

The *Best-first search* algorithm is an informed greedy search strategy, in that it employs a heuristic to estimate the cost of the path from the current node to the target node. In each step, the algorithm selects the node having the smallest estimated distance to the target node (via the heuristic function).

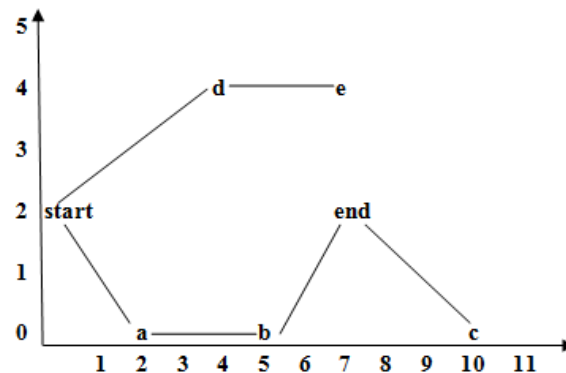


Figure 1: An example graph for the best-first search algorithm

The graph above can be represented using a variation of the neighbor list-clause form, as:

```
pos_vec(start,0,2,[a,d]).
pos_vec(a,2,0,[start,b]).
pos_vec(b,5,0,[a,c, end]).
pos_vec(c,10,0,[b, end]).
pos_vec(d,3,4,[start,e]).
pos_vec(e,7,4,[d]).
pos_vec(end,7,2,[b,c]).

is_target(end).
```

The end node is specified as being the target node, using a predicate clause. The predicate specifications are presented below:

```
best([], []):-!.
best([[Target|Rest]|_], [Target|Rest]):- is_target(Target),!.
best([[H|T]|Rest], Best):-
    pos_vec(H,_,_, Neighb),
    expand(Neighb, [H|T], Rest, Exp),
    quick_sort(Exp, SortExp, []),
    best(SortExp, Best).
```

**% Based on the current path (second argument), the expand/4 predicate
% searches for neighbours of the last expansion (first argument)**

```
expand([],_,Exp,Exp):- !.  
expand([H|T],Path,Rest,Exp):-  
    \+(member(H,Path)), !, expand(T,Path,[[H|Path]|Rest],Exp).  
expand([_|T],Path,Rest,Exp):- expand(T,Path,Rest,Exp).
```

% The quick_sort/3 predicate uses difference lists

```
quick_sort([H|T],S,E):-  
    partition(H,T,A,B),  
    quick_sort(A,S,[H|Y]),  
    quick_sort(B,Y,E).  
quick_sort([],S,S).
```

**% In this case, the partition/4 predicate uses an auxiliary predicate
% order/2 that defines how the partition should be made
% based on distances**

```
partition(H,[A|X],[A|Y],Z):- order(A,H), !, partition(H,X,Y,Z).  
partition(H,[A|X],Y,[A|Z]):- partition(H,X,Y,Z).  
partition(_,[],[],[]).
```

% predicate that calculates the distance between two nodes

```
dist(Node1,Node2,Dist):-  
    pos_vec(Node1, X1, Y1, _),  
    pos_vec(Node2, X2, Y2, _),  
    Dist is (X1-X2)*(X1-X2)+(Y1-Y2)*(Y1-Y2).
```

% the order/2 predicate based on distances used in partition/4

```
order([Node1|_],[Node2|_]):-  
    is_target(Target),  
    dist(Node1,Target,Dist1),  
    dist(Node2,Target,Dist2),  
    Dist1<Dist2.
```

Follow the execution of:

?- best([[start]], Best).

3 Exercises

1. Modify the DFS predicate such that it searches nodes only to a given depth (DLS – Depth-Limited Search). Set the depth limit via a predicate, `depth_max(2)`. for example.

```
edge_ex1(a,b).  
edge_ex1(a,c).  
edge_ex1(b,d).  
edge_ex1(d,e).  
edge_ex1(c,f).  
edge_ex1(e,g).  
edge_ex1(f,h).
```

?- d_search(a,DFS), dl_search(a, DLS).

DFS = [a, b, d, e, g, c, f, h],

DLS = [a, b, d, c, f].