

Lecture 2: Image Classification pipeline

Administrative: Piazza

For questions about midterm, poster session, projects,
use Piazza instead of staff list!

SCPD students: Use your @stanford.edu address to register for Piazza; contact
scpd-customerservice@stanford.edu for help.

Administrative: Assignment 1



knn,

SVM, SoftMax.

2 layer

neural Netw.

Out tonight, due 4/18 11:59pm

- K-Nearest Neighbor
- Linear classifiers: SVM, Softmax
- Two-layer neural network
- Image features

Python, Numpy.

Matlab

Administrative: Python + Numpy

CS231n Convolutional Neural Networks for Visual Recognition

Python Numpy Tutorial

This tutorial was contributed by [Justin Johnson](#).

We will use the Python programming language for all assignments in this course. Python is a great general-purpose programming language on its own, but with the help of a few popular libraries (numpy, scipy, matplotlib) it becomes a powerful environment for scientific computing.

We expect that many of you will have some experience with Python and numpy; for the rest of you, this section will serve as a quick crash course both on the Python programming language and on the use of Python for scientific computing.

<http://cs231n.github.io/python-numpy-tutorial/>

Administrative: Google Cloud

Google Cloud Tutorial

For the class project and assignments, we offer an option to use Google Compute Engine for developing and testing your implementations. This tutorial lists the necessary steps of working on the assignments using Google Cloud. For each assignment, we will provide you with an image containing the starter code and all dependencies that you need to complete the assignment. This tutorial goes through how to set up your own Google Compute Engine (GCE)

<http://cs231n.github.io/gce-tutorial/>

Image Classification: A core task in Computer Vision



This image by Nikita is
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(assume given set of discrete labels)
{dog, cat, truck, plane, ...}

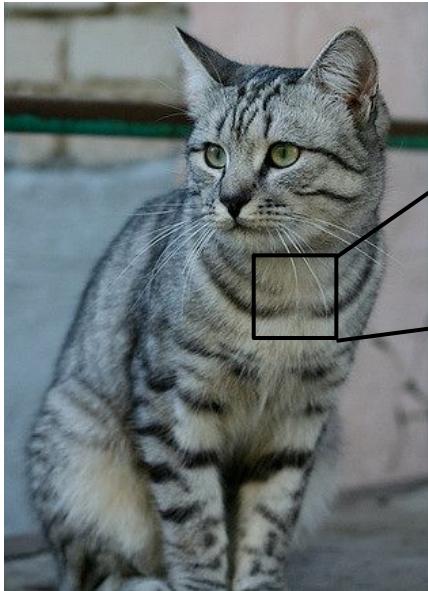


cat

(인간과 개/ القط/ 입장차이)

⇒ Semantic gap (의미鸿沟)

The Problem: Semantic Gap



This image by Nikita is
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[[105 112 108 111 104 99 106 99 96 103 112 119 104 97 93 87]
[91 98 102 106 104 79 98 103 99 105 123 136 110 105 94 85]
[76 85 90 105 128 105 87 96 95 99 115 112 106 103 99 85]
[99 81 81 93 120 131 127 100 95 98 102 99 96 93 101 94]
[106 91 61 64 69 91 88 85 101 107 109 98 75 84 96 95]
[114 108 85 55 55 69 64 54 64 87 112 129 98 74 84 91]
[133 137 147 103 65 81 80 65 52 54 74 84 102 93 85 82]
[128 137 144 140 109 95 86 70 62 65 63 63 60 73 86 101]
[125 133 148 137 119 121 117 94 65 79 80 65 54 64 72 98]
[127 125 131 147 133 127 126 131 111 96 89 75 61 64 72 84]
[115 114 109 123 150 148 131 118 113 109 100 92 74 65 72 78]
[89 93 90 97 108 147 131 118 113 114 113 109 106 95 77 80]
[63 77 86 81 77 79 102 123 117 115 117 125 125 130 115 87]
[62 65 82 89 78 71 80 101 124 126 119 101 107 114 131 119]
[63 65 75 88 89 71 62 81 128 138 135 105 81 98 110 118]
[87 65 71 87 106 95 69 45 76 130 126 107 92 94 105 112]
[118 97 82 86 117 123 116 66 41 51 95 93 89 95 102 107]
[164 146 112 88 82 120 124 104 76 48 45 66 88 101 102 109]
[157 170 157 128 93 86 114 132 112 97 69 55 70 82 99 94]
[130 128 134 161 139 100 109 118 121 134 114 87 65 53 69 86]
[128 112 96 117 150 144 128 115 104 107 102 93 87 81 72 79]
[123 107 96 86 83 112 153 149 122 109 104 75 80 107 112 99]
[122 121 102 88 82 86 94 117 145 148 153 102 58 78 92 107]
[122 164 148 103 71 56 78 83 93 103 119 139 102 61 69 84]

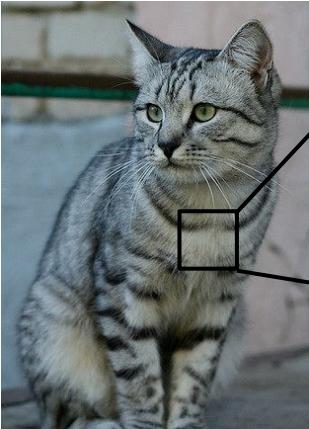
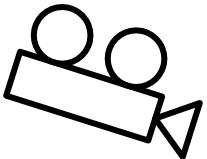
What the computer sees

An image is just a big grid of numbers between [0, 255]:

e.g. 800 x 600 x 3
(3 channels RGB)

컴퓨터에게
인식
수학적
구현
기계학
학습

Challenges: Viewpoint variation



```
[1185 112 188 111 184 99 186 99 96 183 112 119 184 97 93 87]  
[ 91 98 182 106 184 79 98 183 99 185 123 136 118 185 94 85]  
[ 76 85 98 185 128 185 87 96 95 99 115 112 106 183 99 85]  
[ 99 81 104 183 128 183 127 101 98 100 109 98 98 104 99 84]  
[104 91 86 84 69 91 68 85 101 101 109 98 75 84 96 95]  
[114 108 85 55 55 69 64 54 64 87 112 129 98 74 84 94 91]  
[133 137 147 183 65 81 80 65 52 54 74 84 102 93 85 82]  
[128 137 144 148 105 95 86 78 62 65 63 63 68 73 86 101]  
[102 125 131 147 133 127 116 131 111 98 89 75 61 64 72 89]  
[127 125 131 147 133 127 116 131 111 98 89 75 61 64 72 84]  
[115 115 189 123 150 148 131 118 113 109 108 92 74 65 72 78]  
[ 89 93 98 97 108 147 131 118 113 114 113 108 106 95 77 80]  
[ 63 77 86 81 77 79 182 123 137 115 111 125 125 130 115 87]  
[ 62 85 88 89 73 62 81 128 138 135 105 81 98 118 118]  
[ 63 65 75 88 89 73 62 81 128 138 135 105 81 98 118 118]  
[ 87 65 71 87 100 95 69 45 76 138 126 107 92 94 105 112]  
[118 97 82 86 117 123 116 66 41 51 95 93 89 89 95 102 107]  
[164 149 112 88 100 108 128 184 78 48 66 66 66 101 102 108]  
[157 129 104 118 93 86 104 128 128 109 98 89 75 70 81 84]  
[138 128 134 161 139 180 109 118 121 134 114 87 65 53 69 86]  
[128 112 96 117 150 144 120 115 104 107 102 93 87 81 72 79]  
[123 107 96 86 83 112 153 149 122 189 184 75 88 107 112 99]  
[122 121 102 88 82 86 94 117 145 148 153 105 58 78 92 107]  
[122 164 148 103 71 56 78 83 93 103 119 139 102 61 69 84]
```

쉽게
급변하기

All pixels change when
the camera moves!

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Challenges: Illumination

조명 문제로 있다.



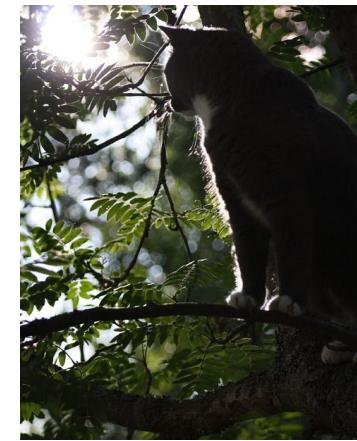
This image is CC0 1.0 public domain



This image is CC0 1.0 public domain



This image is CC0 1.0 public domain

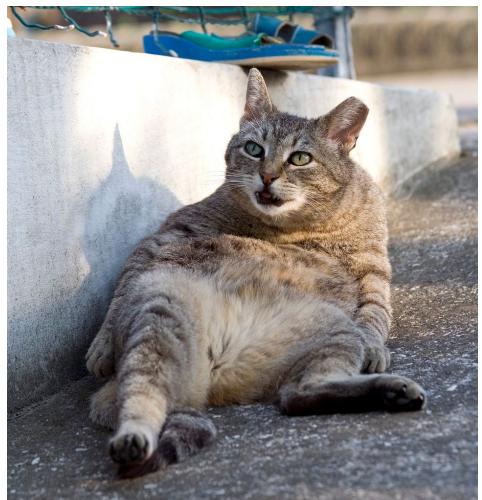


This image is CC0 1.0 public domain

Challenges: Deformation

變形。

고양이가
다양한
자세로
움직인다.



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This image by Tom Thai is
licensed under CC-BY 2.0

Challenges: Occlusion

가려짐 .



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[This image is CC0 1.0 public domain](#)



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Challenges: Background Clutter

배경 분석하기



[This image is CC0 1.0 public domain](#)



[This image is CC0 1.0 public domain](#)

Challenges: Intraclass variation

같은 클래스 내의 다양성.



This image is CC0 1.0 public domain

An image classifier

```
def classify_image(image):  
    # Some magic here?  
    return class_label
```

Unlike e.g. sorting a list of numbers,

no obvious way to hard-code the algorithm for
recognizing a cat, or other classes.

알고리즘 X

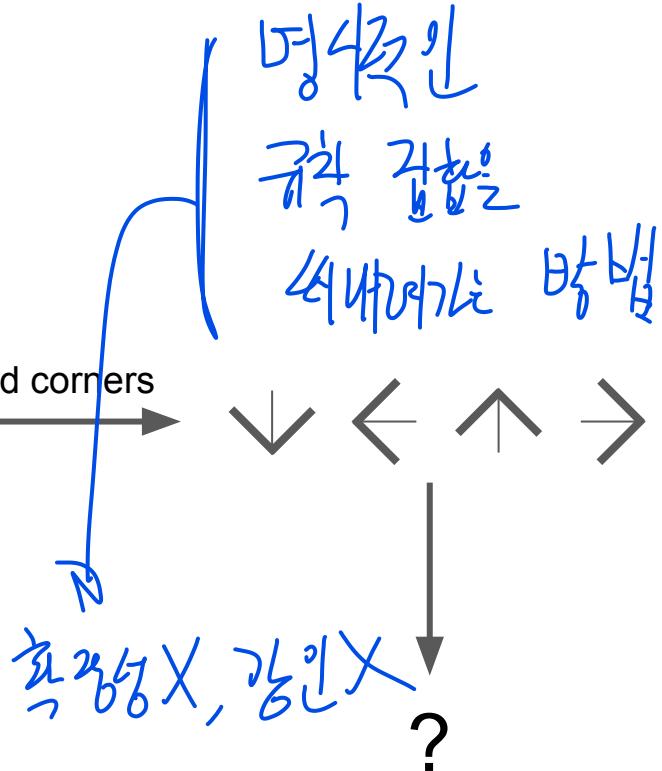
Attempts have been made



Find edges



Find corners



John Canny, "A Computational Approach to Edge Detection", IEEE TPAMI 1986

Data-Driven Approach

1. Collect a dataset of images and labels
2. Use Machine Learning to train a classifier
3. Evaluate the classifier on new images

Example training set

```
def train(images, labels):  
    # Machine learning!  
    return model
```

```
def predict(model, test_images):  
    # Use model to predict labels  
    return test_labels
```

airplane



automobile



bird



cat



deer



ML

key insight

First classifier: Nearest Neighbor

```
def train(images, labels):  
    # Machine learning!  
    return model
```



Memorize all
data and labels

R 만들기.

```
def predict(model, test_images):  
    # Use model to predict labels  
    return test_labels
```



Predict the label
of the most similar
training image

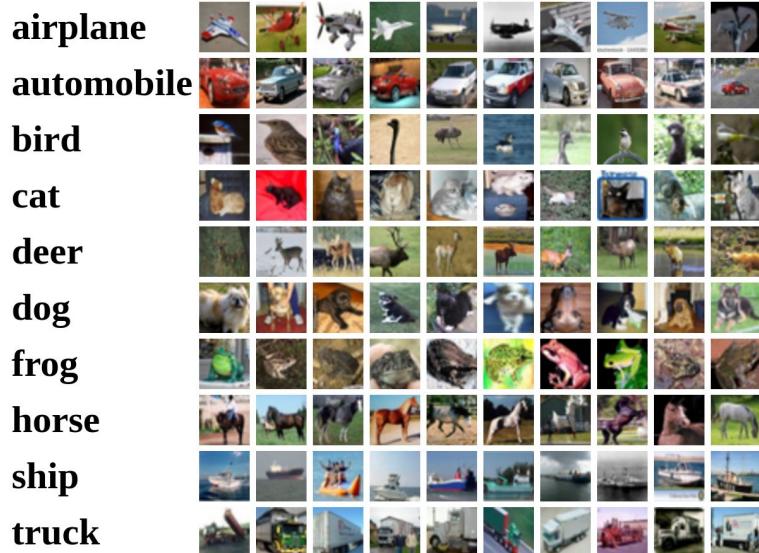
//

Example Dataset **CIFAR10**

10 classes

50,000 training images

10,000 testing images



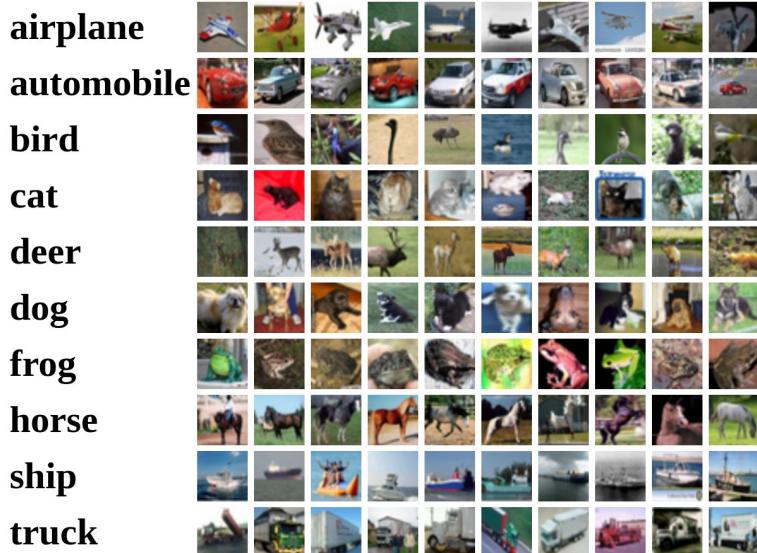
NN \rightarrow 가기 어렵겠지
200
20.

엄청 잘 각인은 X.

Alex Krizhevsky, "Learning Multiple Layers of Features from Tiny Images", Technical Report, 2009.

Example Dataset: CIFAR10

10 classes
50,000 training images
10,000 testing images



Alex Krizhevsky, "Learning Multiple Layers of Features from Tiny Images", Technical Report, 2009.

Distance Metric to compare images

Manhattan
distance

L1 distance:

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$

test image			
56	32	10	18
90	23	128	133
24	26	178	200
2	0	255	220

training image			
10	20	24	17
8	10	89	100
12	16	178	170
4	32	233	112

pixel-wise absolute value differences

46	12	14	1
82	13	39	33
12	10	0	30
2	32	22	108

add
→ 456

```

import numpy as np

class NearestNeighbor:
    def __init__(self):
        pass

    def train(self, X, y):
        """ X is N x D where each row is an example. Y is 1-dimension of size N """
        # the nearest neighbor classifier simply remembers all the training data
        self.Xtr = X
        self.ytr = y

    def predict(self, X):
        """ X is N x D where each row is an example we wish to predict label for """
        num_test = X.shape[0]
        # lets make sure that the output type matches the input type
        Ypred = np.zeros(num_test, dtype = self.ytr.dtype)

        # loop over all test rows
        for i in xrange(num_test):
            # find the nearest training image to the i'th test image
            # using the L1 distance (sum of absolute value differences)
            distances = np.sum(np.abs(self.Xtr - X[i,:]), axis = 1)
            min_index = np.argmin(distances) # get the index with smallest distance
            Ypred[i] = self.ytr[min_index] # predict the label of the nearest example

        return Ypred

```

Nearest Neighbor classifier

```

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```

Nearest Neighbor classifier

Memorize training data

```

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```

Nearest Neighbor classifier

For each test image:
 Find closest train image
 Predict label of nearest image

```

import numpy as np

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    def __init__(self):
        pass

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```

Nearest Neighbor classifier

Q: With N examples,
how fast are training
and prediction?

Train $O(1)$

Predict $O(N)$

Test Σ \rightarrow $O(N^2)$

```

import numpy as np

class NearestNeighbor:
    def __init__(self):
        pass

    def train(self, X, y):
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```

Nearest Neighbor classifier

Q: With N examples,
how fast are training
and prediction?

A: Train O(1),
predict O(N)

```

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```

Nearest Neighbor classifier

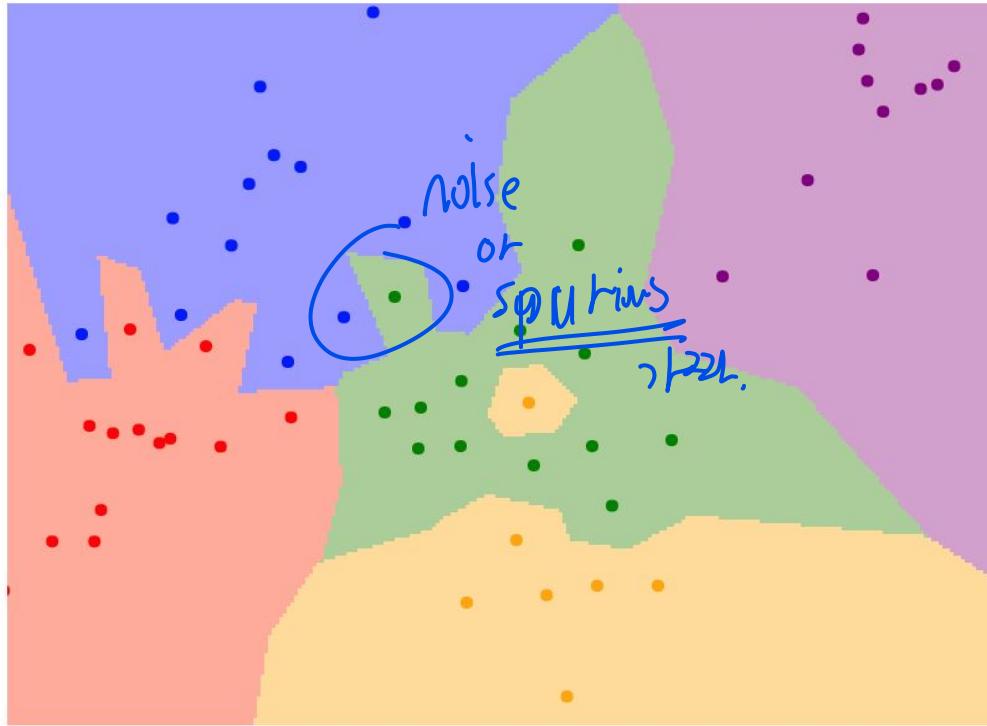
Q: With N examples, how fast are training and prediction?

A: Train O(1), predict O(N)

This is bad: we want classifiers that are **fast** at prediction; **slow** for training is ok

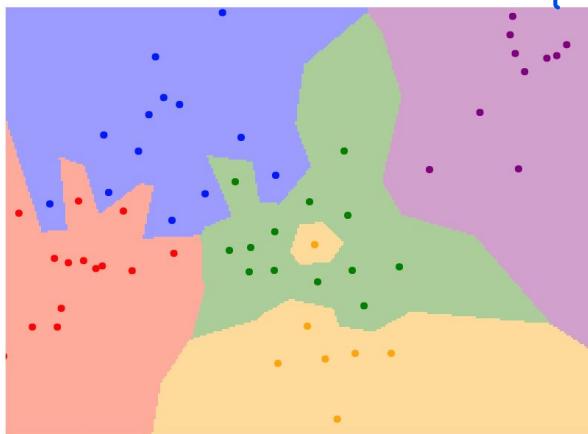
Slow
By all.

What does this look like?



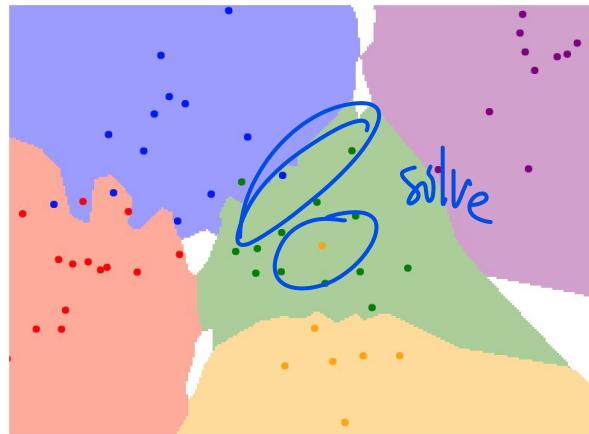
K-Nearest Neighbors

Instead of copying label from nearest neighbor,
take **majority vote** from K closest points



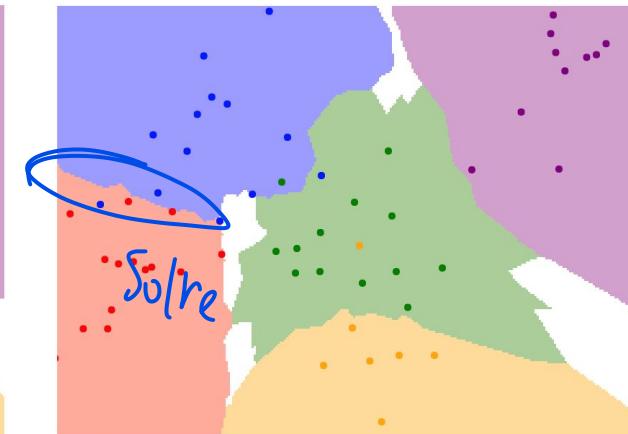
$K = 1$

한번 가까운 투표권 치.



$K = 3$

한번 가까운 투표권 치.



$K = 5$

한번 가까운 투표권 치.

What does this look like?



kNN

각 종류

)

What does this look like?



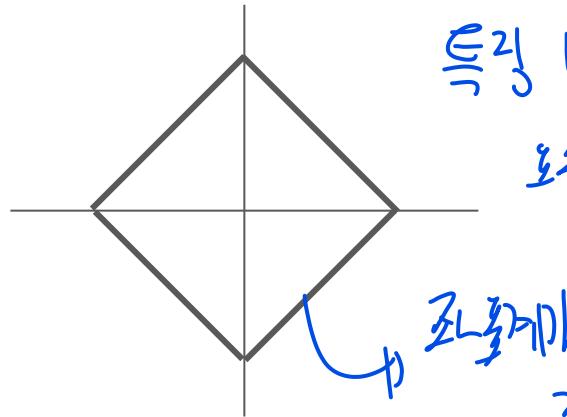
✓
P

$k \rightarrow 1 \text{ or } 2 \text{ or }$
그거나 그거나.

K-Nearest Neighbors: Distance Metric

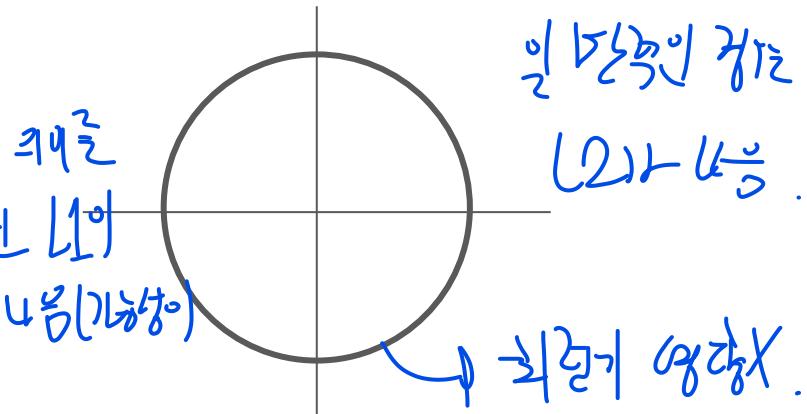
L1 (Manhattan) distance

$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$



L2 (Euclidean) distance

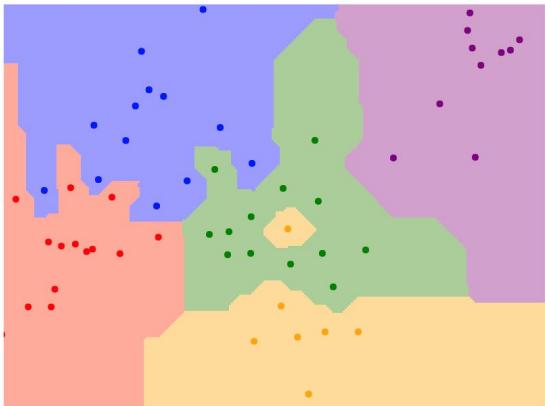
$$d_2(I_1, I_2) = \sqrt{\sum_p (I_1^p - I_2^p)^2}$$



K-Nearest Neighbors: Distance Metric

L1 (Manhattan) distance

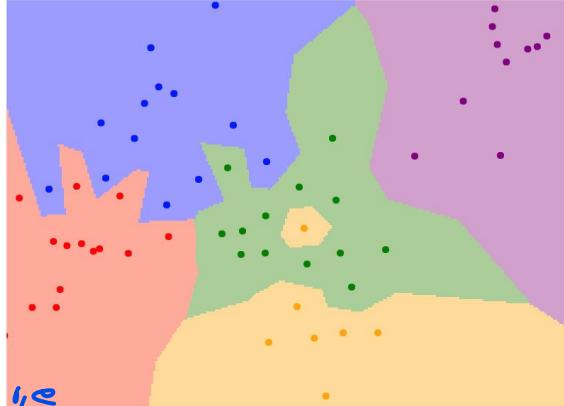
$$d_1(I_1, I_2) = \sum_p |I_1^p - I_2^p|$$



$K = 1$

L2 (Euclidean) distance

$$d_2(I_1, I_2) = \sqrt{\sum_p (I_1^p - I_2^p)^2}$$



$K = 1$

가장就近접근

쓰면 가장就近접근
거리 $\sqrt{2}$ 로 되고

무언가

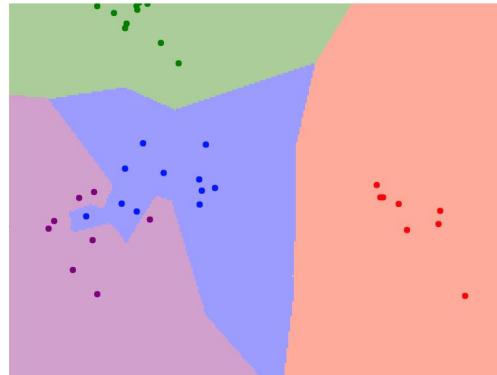
정답입니다.

K-Nearest Neighbors: Demo Time

K-Nearest Neighbors Demo

This interactive demo lets you explore the K-Nearest Neighbors algorithm for classification. Each point in the plane is colored with the class that would be assigned to it using the K-Nearest Neighbors algorithm. Points for which the K-Nearest Neighbor algorithm results in a tie are colored white.

You can move points around by clicking and dragging!



Metric

L1 L2

Num classes

2 3 4 5

Num Neighbors (K)

1 2 3 4 5 6 7

Num points

20 30 40 50 60

<http://vision.stanford.edu/teaching/cs231n-demos/knn/>

Hyperparameters

What is the best value of **k** to use?

What is the best **distance** to use?

These are **hyperparameters**: choices about the algorithm that we set rather than learn

Algorithm
선택.

Hyperparameters

What is the best value of k to use?

What is the best **distance** to use?

These are **hyperparameters**: choices about the algorithm that we set rather than learn

Very problem-dependent. 문제에 따라 달라.

Must try them all out and see what works best. 알고리즘 435가 제일 좋다.
하지만 문제에 따라 달라.

Setting Hyperparameters

Idea #1: Choose hyperparameters
that work ~~best~~ on the data

Your Dataset

최선의 선택

→ 이것이 우리 목표.

Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

BAD: $K = 1$ always works perfectly on training data



$k=1$ 는 늘 기준에서 훈련 데이터를

정확하게 예측하는 경우에 대해서는

$k=1$ 은 늘 정각을 예측하는 경우입니다.

그들이 예상합니다.

// 각각의 예상과 실제 예측이 정확합니다.

Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

BAD: $K = 1$ always works perfectly on training data

Your Dataset

Idea #2: Split data into train and test, choose hyperparameters that work best on test data

train

test

데이터를 2개로 나누면 좋다.

Setting Hyperparameters

Idea #1: Choose hyperparameters that work best on the data

BAD: $K = 1$ always works perfectly on training data



Idea #2: Split data into **train** and **test**, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data



여기서 문제
는 훈련 데이터로 훈련한 모델은
평가 데이터에 대한 예측을 잘 못해.

지도 학습의 단계
학습 | 평가 | 예측

Setting Hyperparameters

테스트셋이거나
“복습 훈련”

Idea #1: Choose hyperparameters that work best on the data

BAD: $K = 1$ always works perfectly on training data

Your Dataset

Idea #2: Split data into **train** and **test**, choose hyperparameters that work best on test data

BAD: No idea how algorithm will perform on new data

train

test

Idea #3: Split data into **train**, **val**, and **test**, choose hyperparameters on val and evaluate on test

엄격히 구분.

Better!

train test
validation test
_valightlance

train

validation

test

Setting Hyperparameters

기본적인 통계학적인 가정.— 데이터는 독립적이고,

이미 지속적으로 모인 나눠쓰면 문제, Shuffle은 필수적인데요.

유의한 점이며 분포에서 벗어난다.

Your Dataset

데이터를 수평으로 일관된 방법론을 가지고, 대량의 데이터를

Idea #4: **Cross-Validation**: Split data into **folds**,
try each fold as validation and average the results

날짜가 제작일

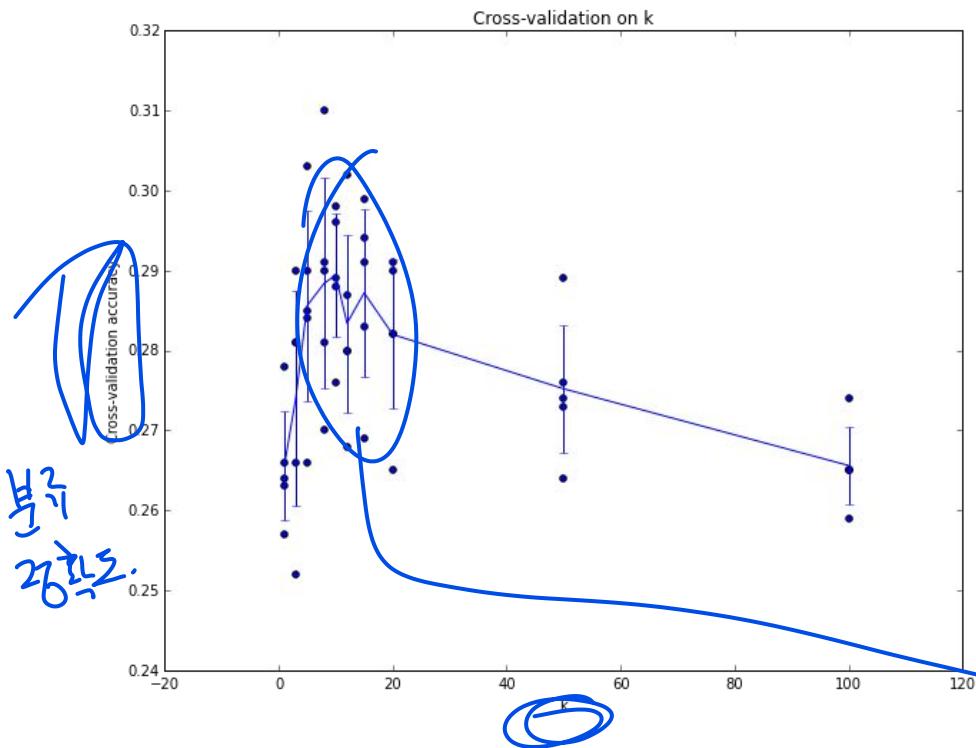
답변 잘안씀.

5-fold.

cycle 1	fold 1	fold 2	fold 3	fold 4	fold 5	test
①	fold 1	fold 2	fold 3	fold 4	fold 5	test
②	fold 1	fold 2	fold 3	fold 4	fold 5	test

Useful for **small datasets**, but not used too frequently in **deep learning**

Setting Hyperparameters

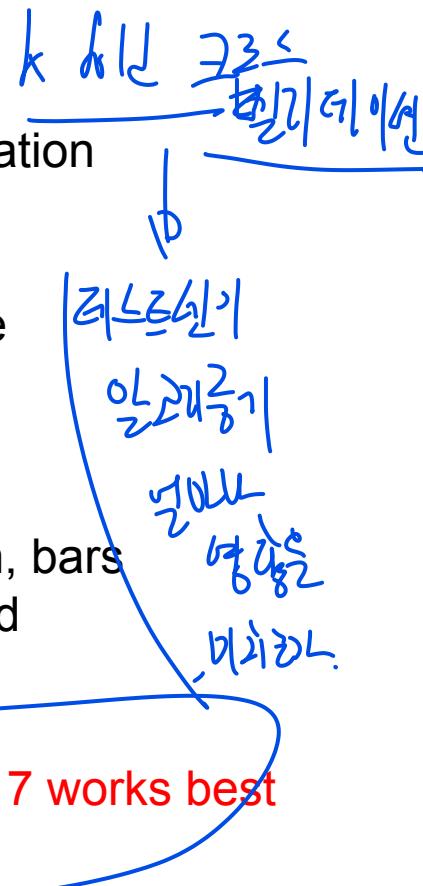


Example of
5-fold cross-validation
for the value of k .

Each point: single
outcome.

The line goes
through the mean, bars
indicated standard
deviation

(Seems that $k \approx 7$ works best
for this data)



k-Nearest Neighbor on images ~~never used~~

(업무 3주 차
기록)
7/29)

6/22

비교 9

증거 10

- Very slow at test time
- Distance metrics on pixels are not informative

Original



Boxed



Shifted



Tinted

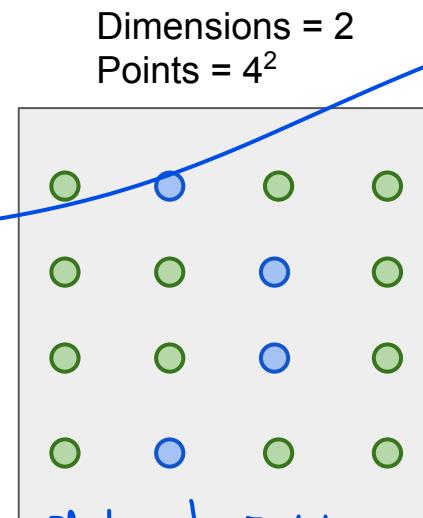
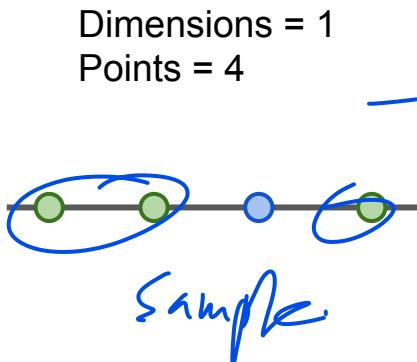


Original image is
CC0 public domain

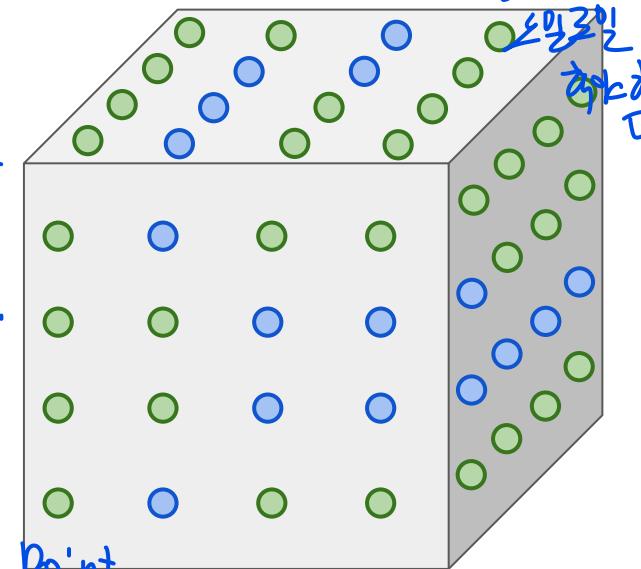
(all 3 images have same L2 distance to the one on the left)

k-Nearest Neighbor on images never used.

- Curse of dimensionality



같은 두 점이 차지하는 면적은 $\frac{1}{4}$ = point.



kNN은 성능의
만일 folds를 더 많으면
Dimensions = 3
Points = 4^3

K-Nearest Neighbors: Summary

In **Image classification** we start with a **training set** of images and labels, and must predict labels on the **test set**

The **K-Nearest Neighbors** classifier predicts labels based on nearest training examples

Distance metric and K are **hyperparameters**

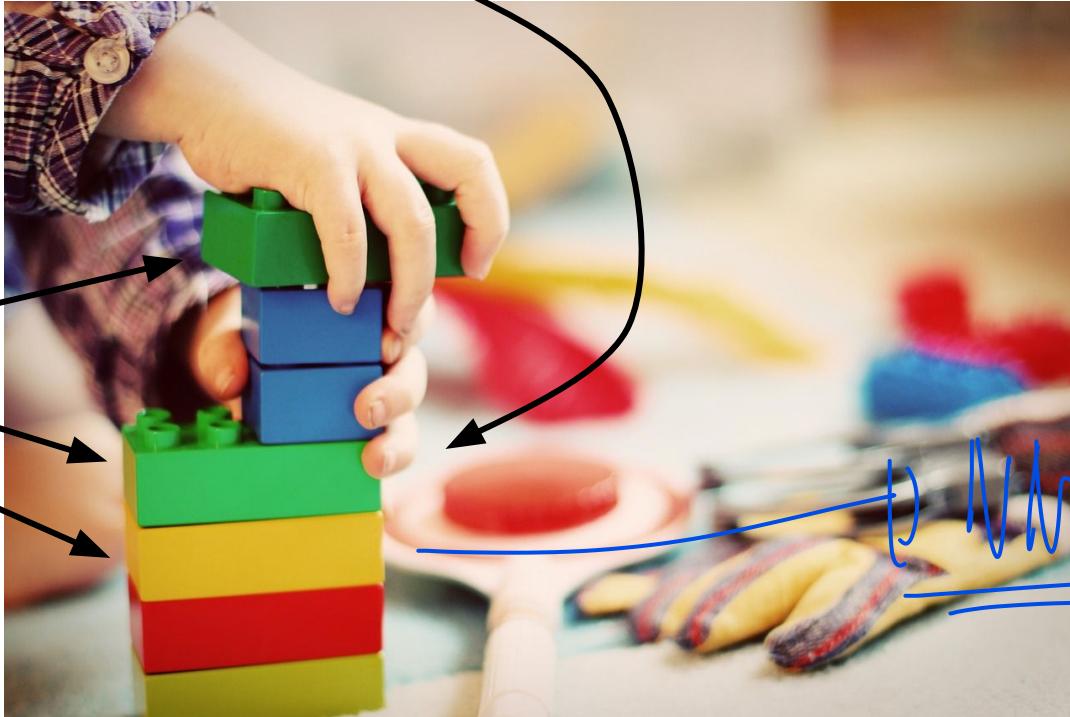
Choose hyperparameters using the **validation set**: only run on the test set once at the very end!

Linear Classification



Neural Network

Linear
classifiers



This image is CC0 1.0 public domain

NN & CNN
의 차이
NN vs 2D CNN
의 차이
LGL vs 3D CNN

Two young girls are playing with lego toy. *Boy is doing backflip on wakeboard*



Man in black shirt is playing guitar.

Construction worker in orange safety vest is working on road.

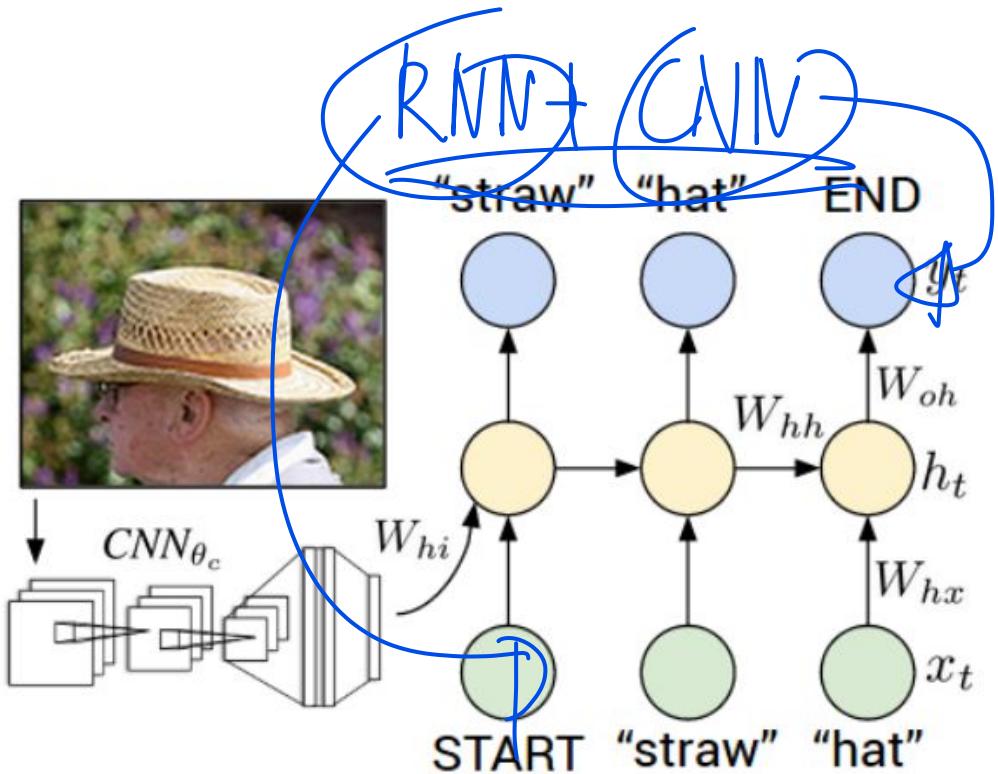
Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015
Figures copyright IEEE, 2015. Reproduced for educational purposes.

Two young girls are playing with lego toy. *Boy is doing backflip on wakeboard*



Man in black shirt is playing guitar.

Construction worker in orange safety vest is working on road.



Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015
Figures copyright IEEE, 2015. Reproduced for educational purposes.

Recall CIFAR10

airplane



automobile



bird



cat



deer



dog



frog



horse



ship



truck

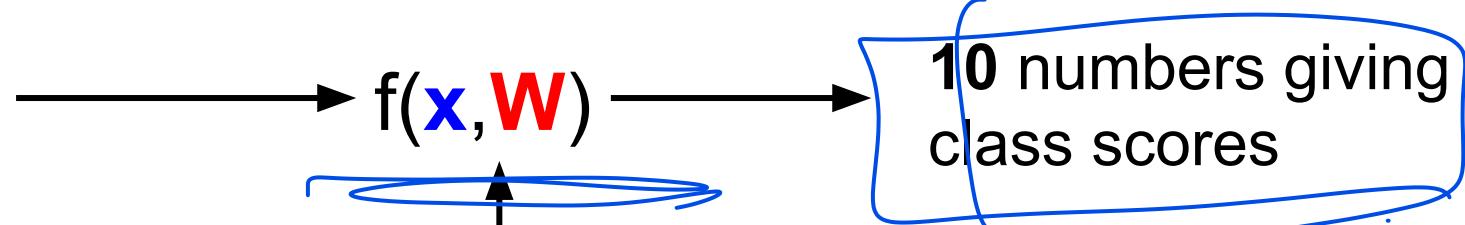


50,000 training images
each image is **32x32x3**

10,000 test images.

Parametric Approach

Image



Array of **32x32x3** numbers
(3072 numbers total)

W or ~~h1, h2, ...~~
parameters
or weights

Parametric Approach: Linear Classifier

Image



Array of **32x32x3** numbers
(3072 numbers total)

$$f(x, W) = \mathbf{W}x$$

$$f(\mathbf{x}, \mathbf{W})$$

W
parameters
or weights

10 numbers giving
class scores

Test time! E71014210141
2130.
With ch211.

Parametric Approach: Linear Classifier



Image

$$f(x, W) = Wx$$

$$f(x, W)$$

10 numbers giving
class scores

Array of **32x32x3** numbers
(3072 numbers total)

W
parameters
or weights

Parametric Approach: Linear Classifier

Image



Array of **32x32x3** numbers
(3072 numbers total)

$$f(x, W)$$

10x1

$$Wx \quad 10 \times 3072$$

3072x1

$$b \quad 10 \times 1$$

Bias

$$f(x, W)$$

10 numbers giving
class scores

W
parameters
or weights

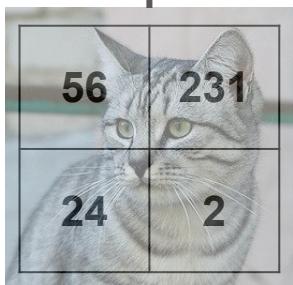
Bias : **バイアス**

(バイアス 독립변수) 무관한 특성에 영향.

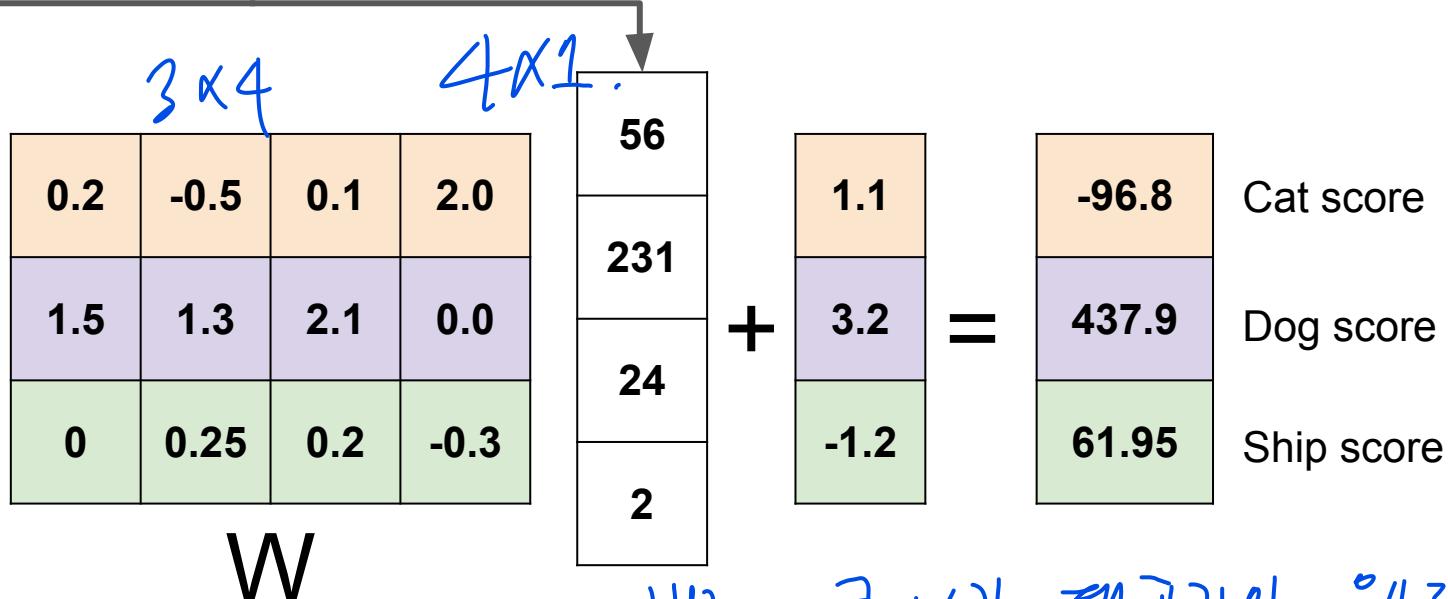
Scaling of data 영향을 줄여.

Example with an image with 4 pixels, and 3 classes (cat/dog/ship)

Stretch pixels into column

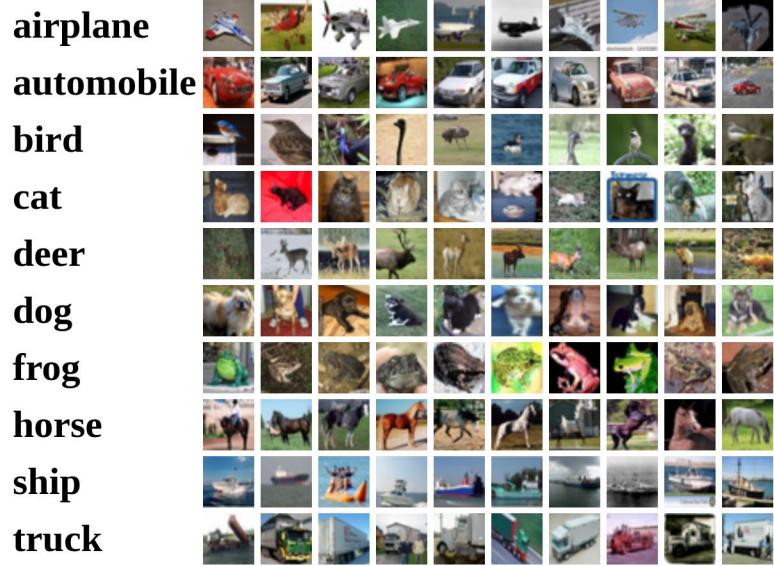


Input image



내가 한 글자는 행렬간의 곱셈을 죽여라.

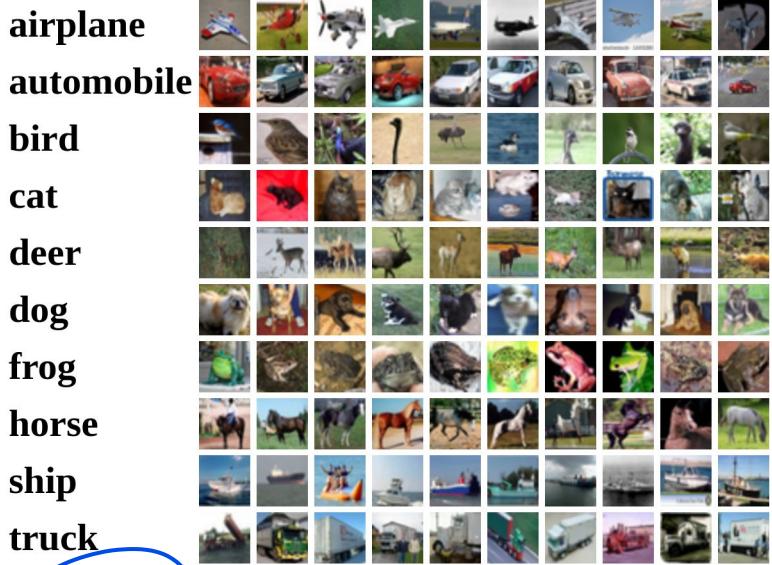
Interpreting a Linear Classifier



$$f(x, W) = Wx + b$$

What is this thing doing?

Interpreting a Linear Classifier



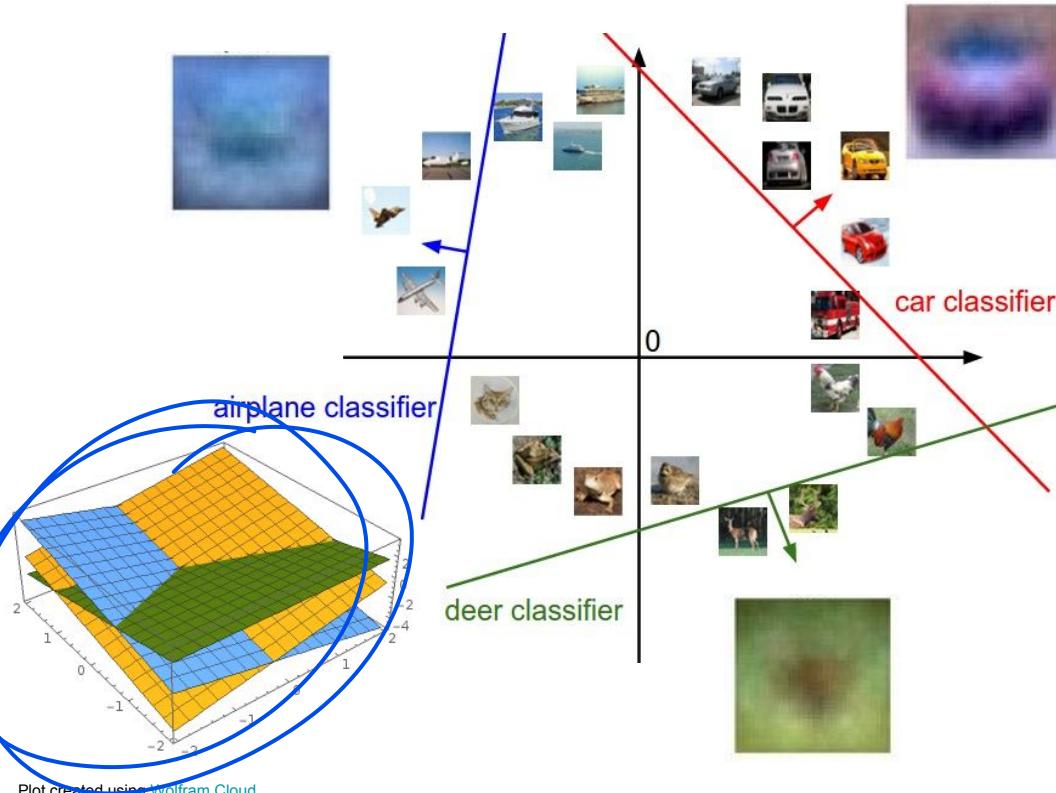
$$f(x, W) = Wx + b$$

Example trained weights
of a linear classifier
trained on CIFAR-10:

엥 끌래.



Interpreting a Linear Classifier



$$f(x, W) = Wx + b$$



Array of **32x32x3** numbers
(3072 numbers total)

[Cat image](#) by [Nikita](#) is licensed under [CC-BY 2.0](#)

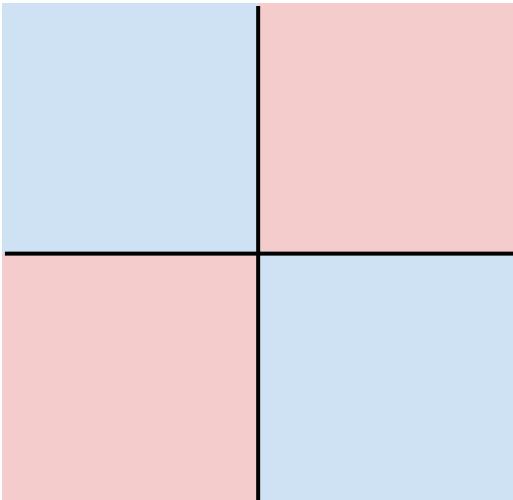
Hard cases for a linear classifier

Class 1:

number of pixels > 0 odd

Class 2:

number of pixels > 0 even

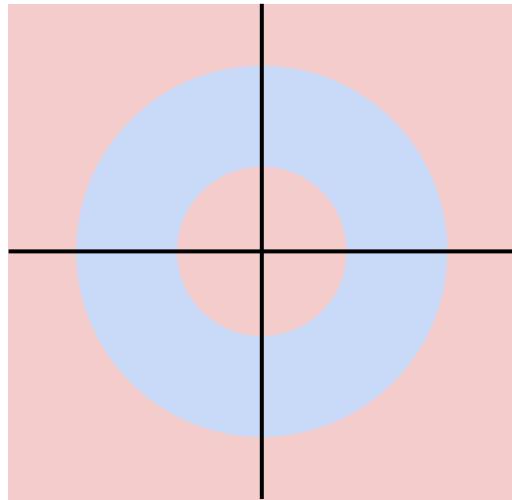


Class 1:

$1 \leq L_2 \text{ norm} \leq 2$

Class 2:

Everything else



여기서 문제는 1/2인
수를 찾는 것이다.

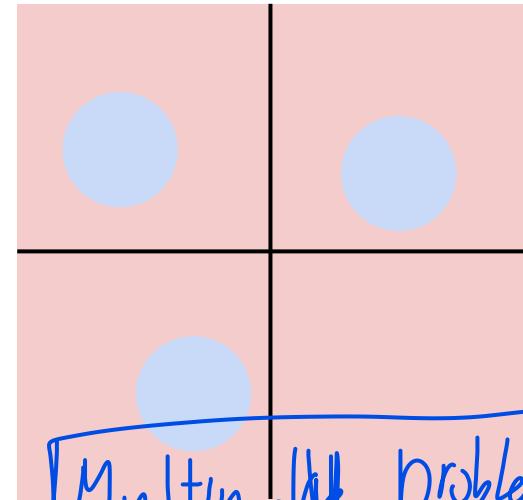
Class 1:

Three modes

별거 없을 듯
(Purity problem)

Class 2:

Everything else



So far: Defined a (linear) score function $f(x, W) = Wx + b$

Example class scores for 3 images for some W :

How can we tell whether this W is good or bad?



airplane	-3.45	-0.51	3.42
automobile	-8.87	6.04	4.64
bird	0.09	5.31	2.65
cat	2.9	-4.22	5.1
deer	4.48	-4.19	2.64
dog	8.02	3.58	5.55
frog	3.78	4.49	-4.34
horse	1.06	-4.37	-1.5
ship	-0.36	-2.09	-4.79
truck	-0.72	-2.93	6.14

[Cat image](#) by [Nikita](#) is licensed under [CC-BY 2.0](#)

[Car image](#) is [CC0 1.0](#) public domain

[Frog image](#) is in the public domain

$$f(x, W) = Wx + b$$

Coming up:

- Loss function
- Optimization
- ConvNets!

(quantifying what it means to have a “good” W)

(start with random W and find a W that minimizes the loss)

(tweak the functional form of f)