

## Visualization Techniques

### Multidimensional Visualization

## Data Models

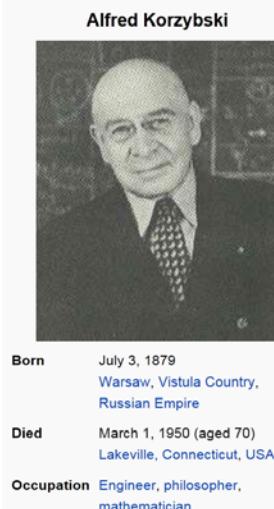
- Foundational topics for Multidimensional, graph and tree etc..
- Data types
- Data representations
- Data models
- Tables

# Data

- An abstraction of a real phenomenon
- Models objects we are interesting
- Data Visualization
  - Visualization is only as good as the data
  - Visualizations can be misleading
  - Good data is important!
- Map–territory relation

## Map–territory relation

- Map–territory relation
  - describes the relationship between an object and a representation of that object.
- “The map is not the territory”
  - an abstraction derived from something, or a reaction to it, is not the thing itself.

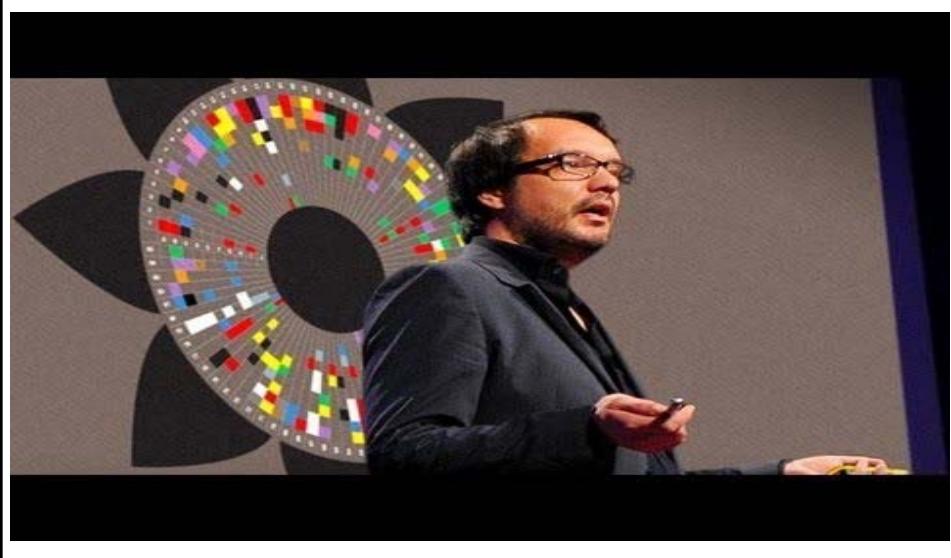


[http://en.wikipedia.org/wiki/Alfred\\_Korzybski](http://en.wikipedia.org/wiki/Alfred_Korzybski)

## Hans Rosling



The beauty of data visualization  
David McCandless (TED 2010)



## Digitized Data

- 5 - 10% structured data
- 90-95% unstructured
  - Images
  - Video
  - Sound
  - Log files
  - Text
  - Web pages

## Data Models

- Three types of entities for structured data generation
  - Objects
    - Actual items of interest
    - Different types possible
    - Example: people in a social network
  - Attributes
    - Characteristics of objects
    - Example: age, gender, email, IM, blog, etc..
  - Relations
    - Connections between objects
    - Examples: friends, chats, blog replies.

## Relational Data Model

- Records in a data table
- Structured from amenable to analysis and visualization
- Fixed-length tuples (attributes)
- Each column (attribute) has a domain (type)

## Data Dimensions

- Common dimensions: 1, 2, 3, (4?)
- 1D – univariate
  - Mass, distance, temperature, potential, energy
- 2D – bivariate
  - Positions on a map
- 3 dimensions – trivariate
  - Positions in space, velocity, acceleration, color in RGB
- More than 3 dimensions
  - Multivariate
  - Hypervariate

## US Census Data

- People: # of people in group
- Year: 1850 – 2000 (every decade)
- Age: 0 – 90+
- Sex: Male, Female
- Marital Status: Single, Married, Divorced, ...
- <http://factfinder.census.gov/>
- Data is there, what's next?

Total New Passenger Car Sales (in thousands)

	Total	Domestic	Imports	Japan	Germany	Other
1970	8,400	7,119	1,280	313	750	217
1975	8,624	7,053	1,572	808	493	271
1980	8,949	6,580	2,369	1,894	292	184
1985	10,979	8,205	2,775	2,171	408	196
1990	9,303	6,919	2,384	1,719	263	402
1991	8,189	6,162	2,028	1,505	193	330
1992	8,213	6,286	1,927	1,452	201	275
1993	8,518	6,742	1,776	1,328	186	262
1994	8,991	7,255	1,735	1,239	192	303
1995	8,635	7,129	1,506	982	207	317
1996	8,526	7,255	1,271	726	237	308
1997	8,272	6,917	1,355	726	297	332
1998	8,142	6,762	1,380	691	367	322
1999	8,698	6,979	1,719	758	467	494
2000	8,847	6,831	2,016	863	517	637
2001	8,423	6,325	2,098	837	523	738
2002	8,103	5,878	2,226	930	547	749
2003	7,610	5,527	2,083	830	544	709
2004	7,545	5,396	2,149	810	542	797
2005	7,720	5,533	2,187	923	534	729
2006	7,821	5,476	2,345	1,154	561	630
2007	7,618	5,253	2,365	1,183	567	615
2008	6,813	4,535	2,278	1,142	507	630

<http://www.bts.gov/>

Can you get  
some conclusions  
from the table?

Yes. Table is a  
great way for data  
visualization.

## Relational Data Model

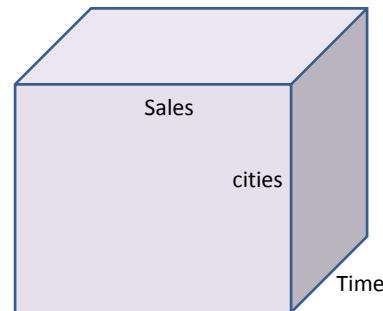
- Relational data model manipulation:  
Standard Query Language
  - Selection (SELECT)
  - Projection (WHERE)
  - Sorting (ORDER BY)
  - Aggregation (GROUP BY, SUM, MIN, ...)
  - Set operations (UNION, ...)
  - Join (INNER JOIN)

## OLAP

- OLAP -- Online analytical processing
  - Swiftly answer multi-dimensional analytical queries.
  - Borrow aspects of navigational databases and hierarchical databases that are faster than relational databases.
- Key concept: OLAP Cube

## OLAP Cube

- An OLAP cube is a data structure that allows fast analysis of data
- The cube metadata (structure) may be created from tables in a relational database.

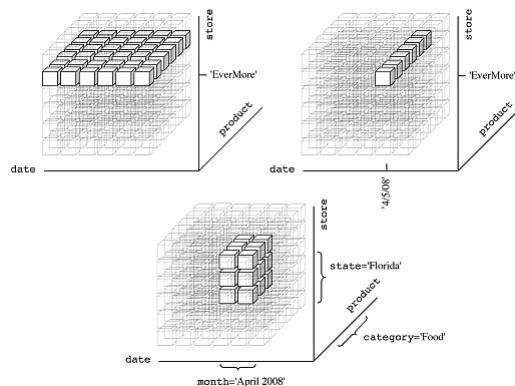


## OLAP Query Languages

- MDX -- Multidimensional Expressions
  - a query language for OLAP databases
  - Same role as SQL for relational databases.
  - a calculation language, with syntax similar to spreadsheet formulas.
- XMLA -- XML for Analysis (Microsoft 2001)
  - based on other industry standards such as XML, SOAP and HTTP
  - MDX statements can be enclosed in XMLA

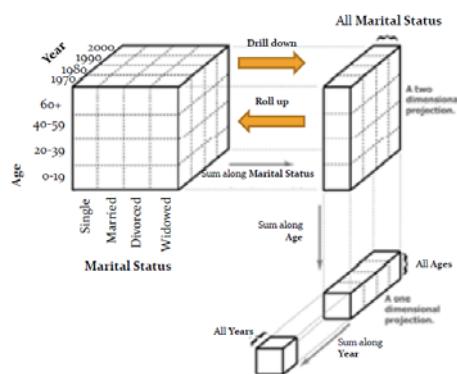
## OLAP Cube

- Sales data



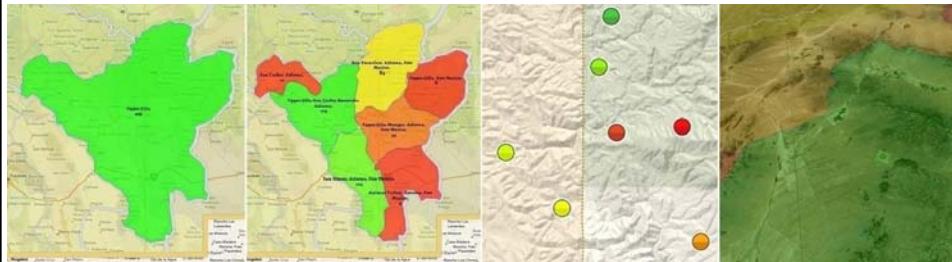
## OLAP Cube

- OLAP cube for US census data



## OLAP

- SOLAP – Spatial Online Analytical Processing
  - incorporates OLAP technology with mapping capabilities
- SOLAP with Virtual Earth (Polygons, Points on 2D and 3D maps)



## Tables vs Graphs

- Table -- Simple way to “visualize” data
- When to use tables?
  - look up individual values
  - Need precise data
- When to use graphs?
  - Need to know shapes and trends of values
  - Find relationships
- *“For small data sets, usually a simple table shows the data more effectively than a graph, let alone a chartjunk graph.” – E. R. Tufte, 2003*

## Multidimensional Visualization

- How to effectively present more than 3 dimensions of information in a visual display with 2 (to 3) dimensions?
- How to effectively visualize “inherently abstract” data?
- How to effectively visualize very large, often complex data sets?
- How to effectively display results – when you don’t know what those results will be?

From James Reffell

## Multidimensional Visualization

Goals of multidimensional visualization:

- Without loss of information
- With:
  - Minimal complexity
  - Any number of dimensions
  - Variables treated uniformly
  - Objects remain recognizable across transformations
  - Easy / intuitive conveyance of information
  - Mathematically / algorithmically rigorous

(Adapted from Inselberg)

# Multidimensional Visualization

## Purposes and applications

- Find clusters of similar data
- Find “hot spots” (exceptional items in otherwise homogeneous regions)
- Show relationships between multiple variables
- Similarity retrieval rather than boolean matching, show near misses

“Searching for patterns in the big picture and fluidly investigating interesting details without losing framing context” (Rao & Card)

# Multidimensional Visualization

## Visualization methods

- Geometric techniques
  - Scatter plot matrices, parallel coordinates, landscapes, Dust & Magnet ...
- Icon-based techniques
  - glyphs, shape-coding, color icons, ...
- Hierarchical techniques
  - Dimensional stacking, worlds-within-worlds, ...

# Multidimensional Visualization

## Visualization methods

- Pixel-oriented techniques
  - Recursive pattern, circle segments, spiral, axes techniques,...
- Table-based techniques
  - HeatMap, tableLens

# Multidimensional Visualization

- Complex problems → more dimensions
- Closer to real world situations → more dimensions
- Example: purchase a car
  - Price, model, company, new/used, finance, dealer
  - Use visualization to help decision making?

## Parallel Coordinates

### Case: Iris

- Iris is a genus of 260 species of flowering plants with showy flowers.
- Scientists measured sepal length, sepal width petal length, petal width of many Iris species.



	Classes	sepal-length	sepal-width	petal-length	petal-width
1	Iris-virginica	6.7	3	5.2	2.3
2	Iris-virginica	6	2.2	5	1.5
3	Iris-virginica	6.2	2.8	4.8	1.8
4	Iris-virginica	7.7	3.8	6.7	2.2
5	Iris-virginica	7.2	3	5.8	1.6
6	Iris-versicolor	5.5	2.4	3.8	1.1
7	Iris-versicolor	6	2.7	5.1	1.6
8	Iris-versicolor	5.5	2.5	4	1.3
9	Iris-versicolor	5.6	2.9	3.6	1.3
10	Iris-versicolor	5.7	2.9	4.2	1.3
11	Iris-setosa	5	3.2	1.2	0.2
12	Iris-setosa	4.9	3.1	1.5	0.1
13	Iris-setosa	5.3	3.7	1.5	0.2
14	Iris-setosa	4.8	3.1	1.6	0.2
...	...	...	...	...	...

Data source: ManyEyes

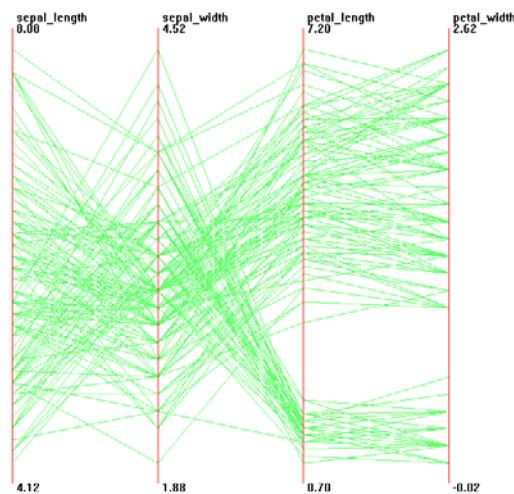
Question: How to visualize it?

## Parallel Coordinates

- Parallel coordinates were invented by Maurice d'Ocagne in 1885 and were independently rediscovered and popularized by Al Inselberg in 1959 and systematically developed as a coordinate system starting from 1977.

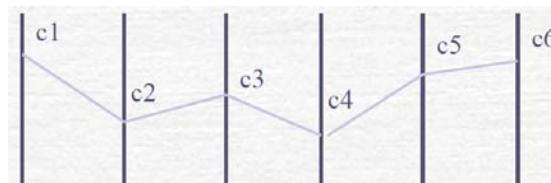
## Parallel Coordinates

	Classes	sepal-length	sepal-width	petal-length	petal-width
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11	Iris-setosa	5	3.2	1.2	0.2
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...	...	...	...	...	...

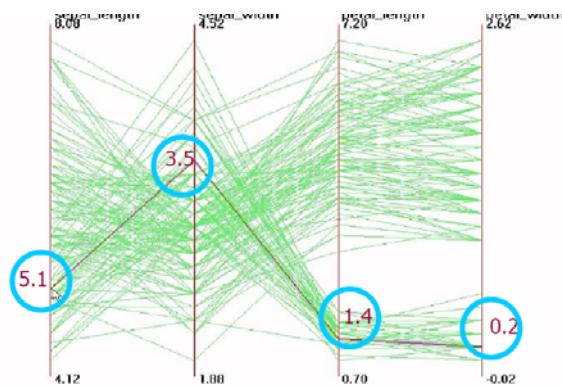


## Parallel Coordinates

- To represent N dimensional data
- Set N vertical axes in parallel
- Put data to intersects on corresponding axes
- Connect intersects
- Example: (c1, c2, c3, c4, c5, c6)



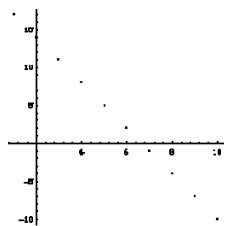
## Parallel Coordinates



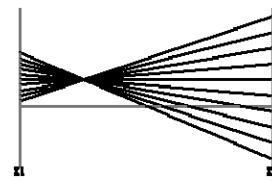
## Parallel Coordinates

(Inselberg)

Like a normal graph, but different views



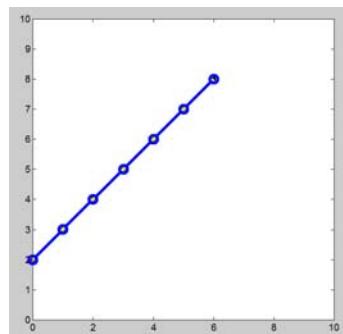
Dataset in a Cartesian graph



Same dataset in parallel coordinates

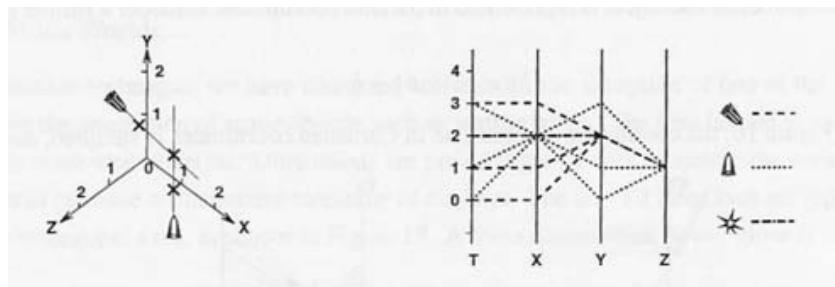
## Parallel Coordinates

Question: sketch the following graph in parallel coordinates?



## Parallel Coordinates

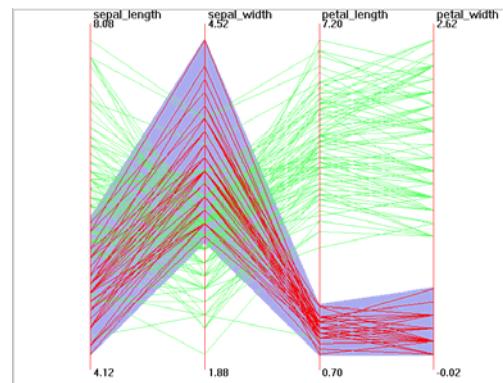
- Applications: View aircraft collisions



Pak Wong, 1997

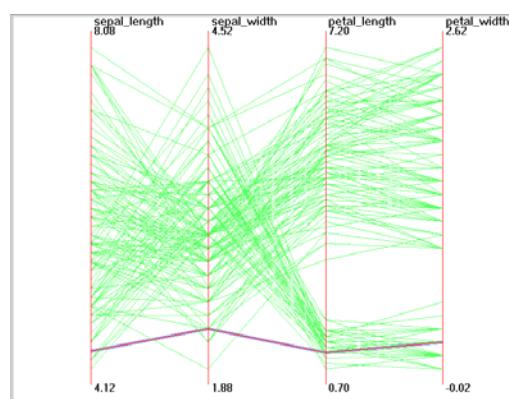
## Parallel Coordinates

- Cluster: A group of data items that are similar in all dimensions.



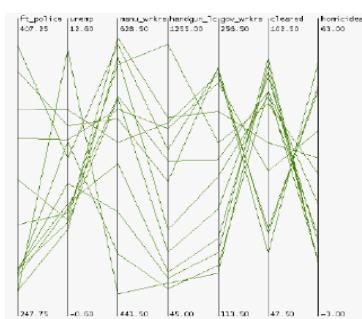
## Parallel Coordinates

- Outlier: A data item that is similar to few or no other data items.

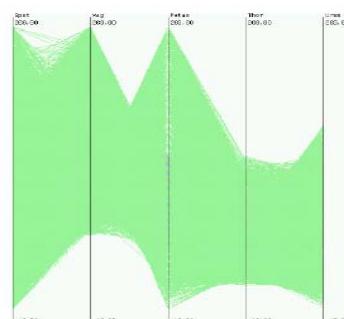


## Parallel Coordinates

Good visualization

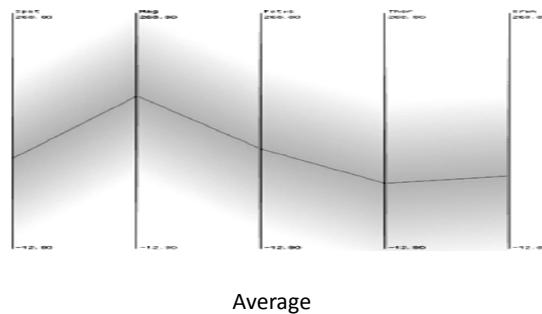


Bad visualization

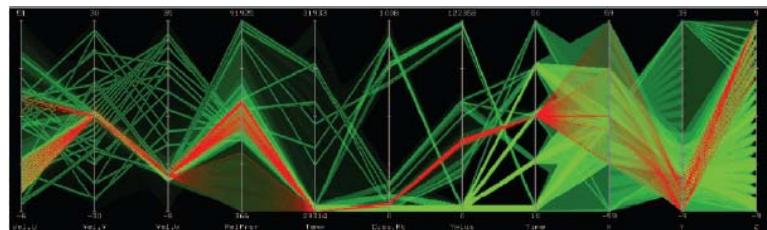


## Parallel Coordinates

- Simple statistical view



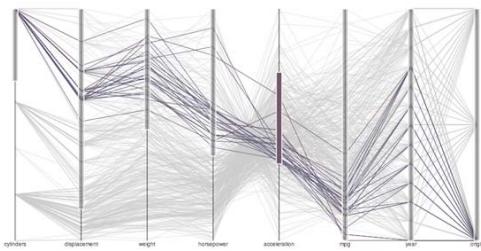
## Parallel Coordinates



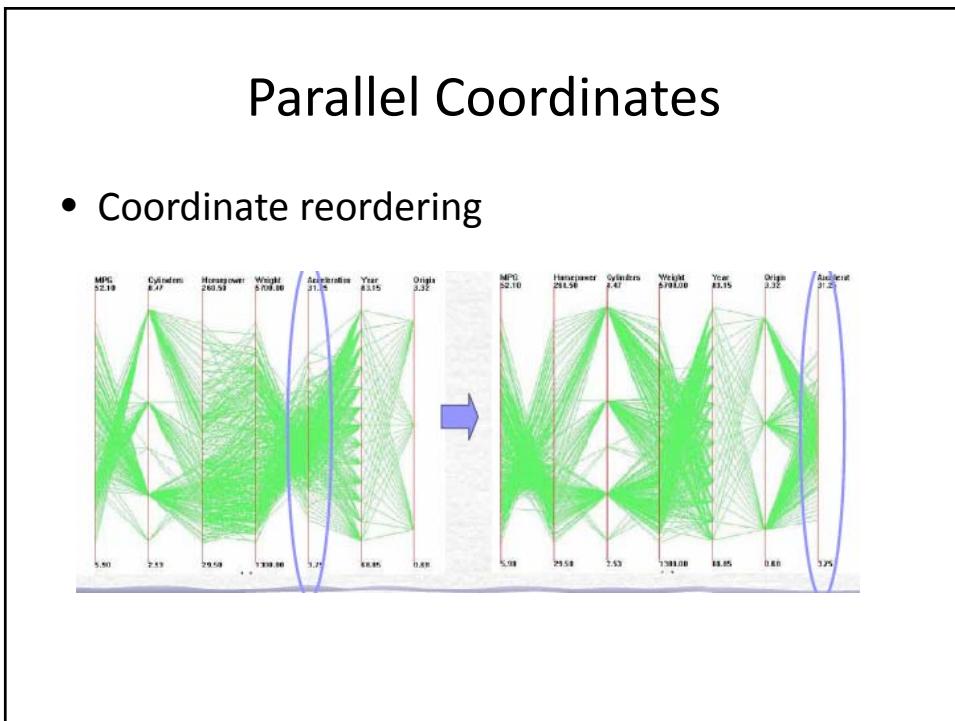
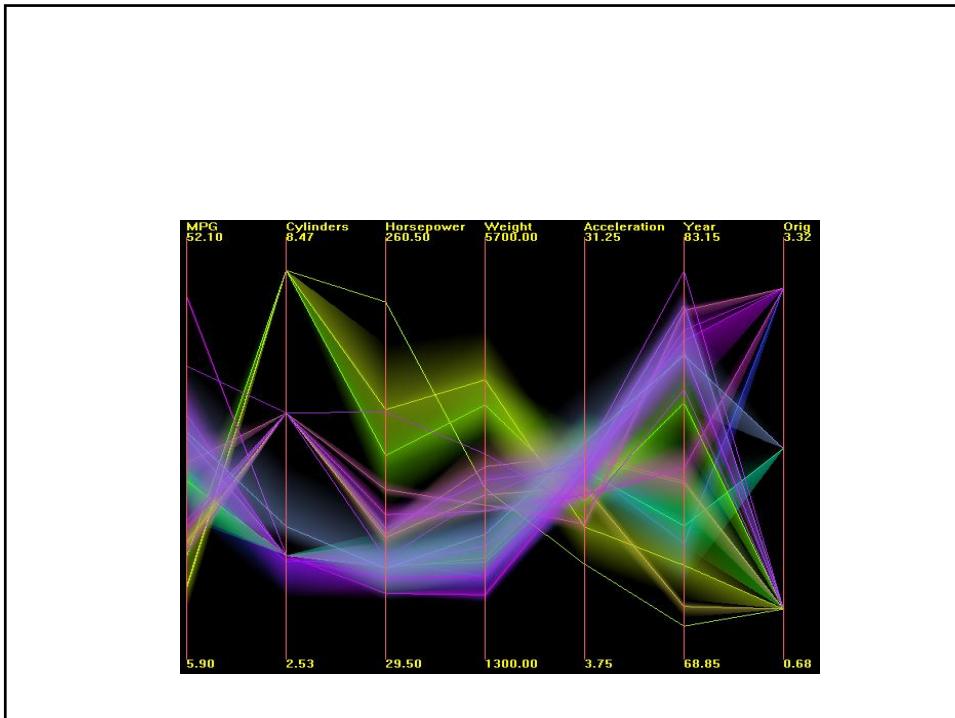
InfoVis 2006 "Outlier-preserving Focus+Context Visualization in Parallel Coordinates"  
by Matej Novotny, Helwig Hauser

## Parallel Coordinates

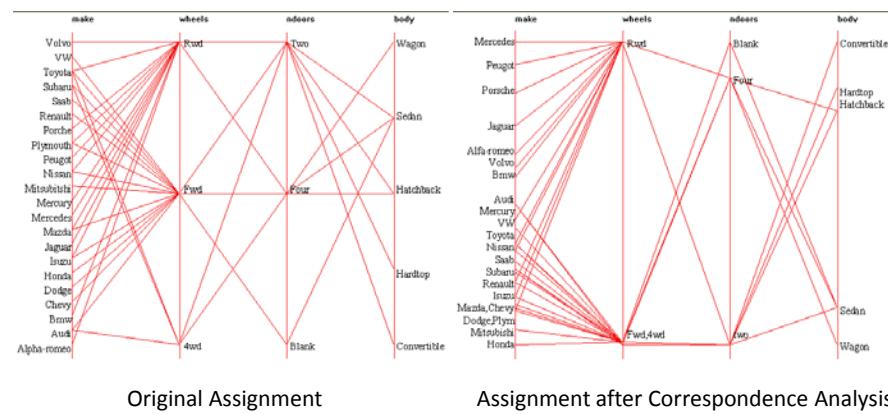
- Protovis Example: Select cars



<http://vis.stanford.edu/protovis/ex/cars.html>



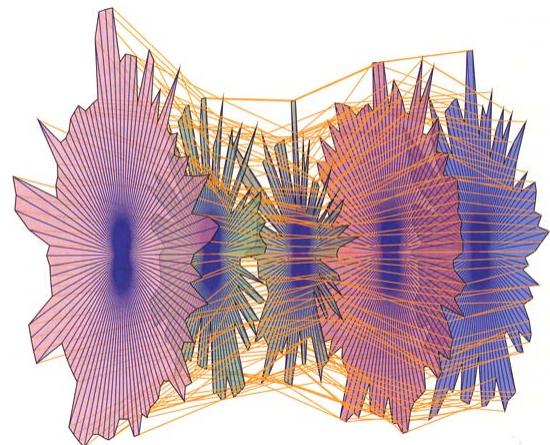
## Parallel Coordinates



M. Wade

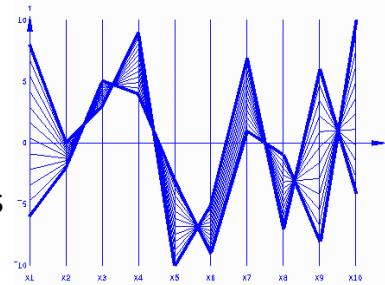
## Parallel Coordinates

- 3D?



## Parallel Coordinates

- Useful for recognizing patterns between the axes
  - Example: adding or removing parts of the data to see general patterns or more closely examine particular interactions.
- Articles offer suggestions on how to most effectively use this system.



## Parallel Coordinates

### Advantages, Strengths:

- Works for any dimensional
- Clearly displays data characteristics of the data
  - No explanation needed
- Easy to adjust or focus displays/ queries
- Can be used in decision support
  - Adjusting one parameter effects others

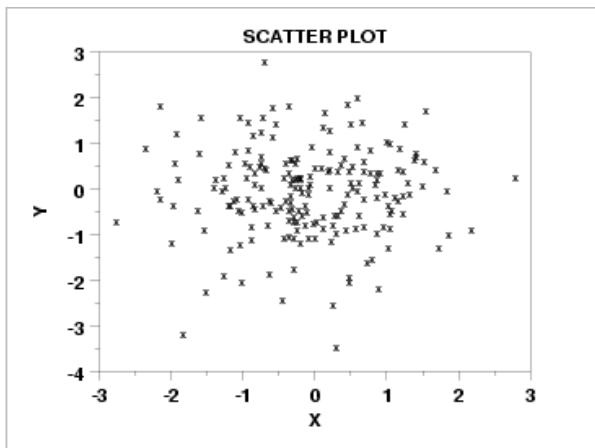
### Disadvantages, Weaknesses

- Formation of complex queries can be tricky
- Results can be hard to interpret

## Scatter Plot Matrix

## Scatter Plot

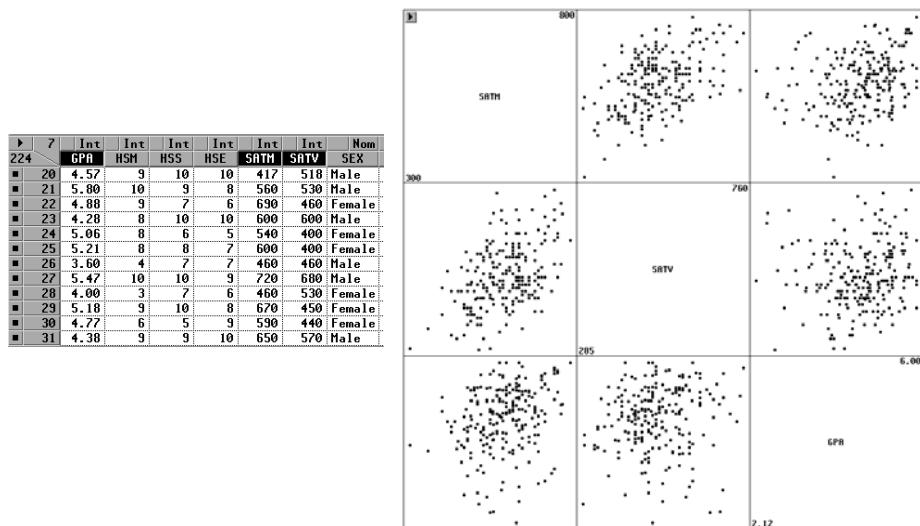
- Scatter Plot  
Plot (X,Y)



## Scatter Plot Matrix

▶	7	Int								Nom
		GPA	HSM	HSS	HSE	SATM	SATV	Int		
■	20	4.57	9	10	10	417	518	Male		
■	21	5.80	10	9	8	560	530	Male		
■	22	4.88	9	7	6	690	460	Female		
■	23	4.28	8	10	10	600	600	Male		
■	24	5.06	8	6	5	540	400	Female		
■	25	5.21	8	8	7	600	400	Female		
■	26	3.60	4	7	7	460	460	Male		
■	27	5.47	10	10	9	720	680	Male		
■	28	4.00	3	7	6	460	530	Female		
■	29	5.18	9	10	8	670	450	Female		
■	30	4.77	6	5	9	590	440	Female		
■	31	4.38	9	9	10	650	570	Male		

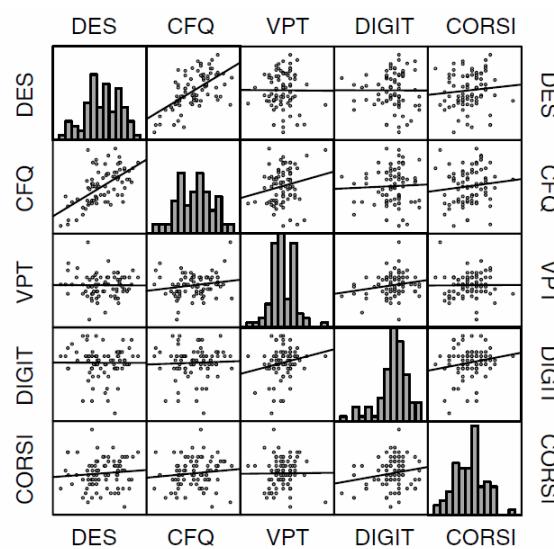
## Scatter Plot Matrix

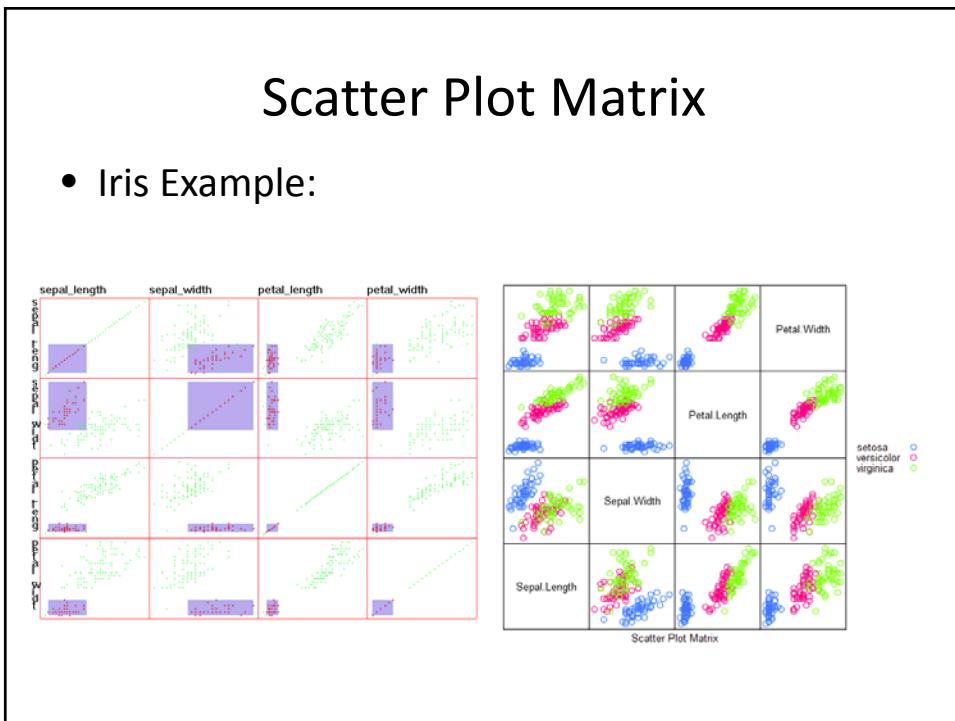
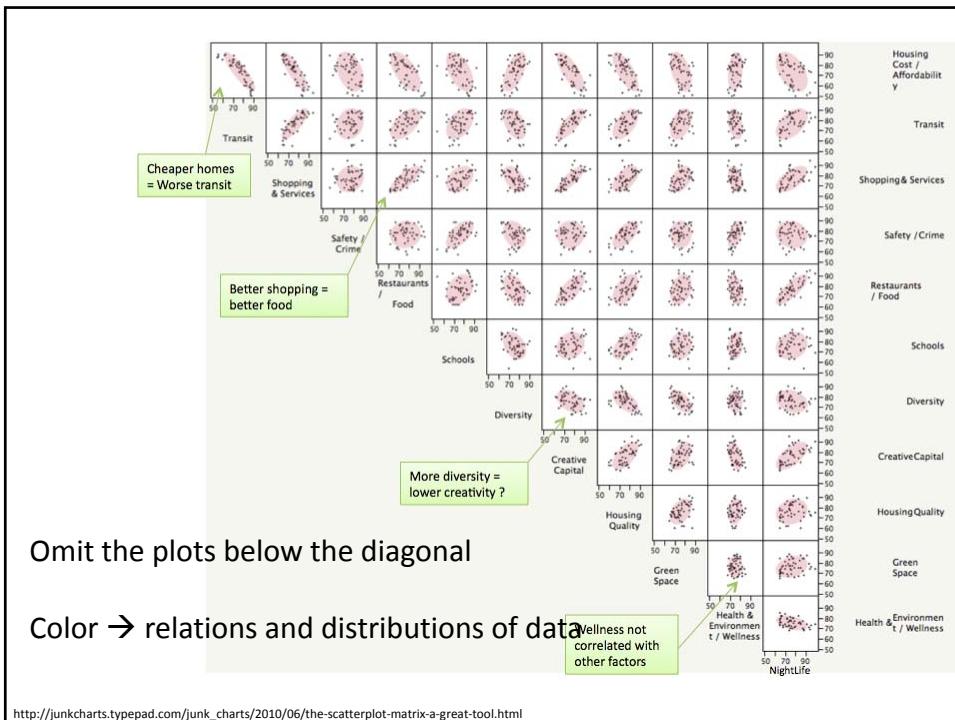


## Scatter Plot Matrix

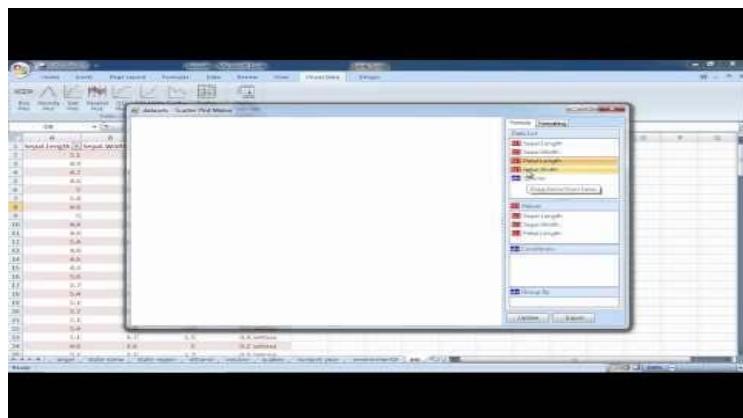
- Given a set of variables  $X_1, X_2, \dots, X_k$ , the scatter plot matrix contains all the pairwise scatter plots of the variables on a single page in a matrix format. That is, if there are  $k$  variables, the scatter plot matrix will have  $k$  rows and  $k$  columns and the  $i^{th}$  row and  $j^{th}$  column of this matrix is a plot of  $X_i$  versus  $X_j$ .
- Purpose:** Check pairwise relationships between variables

## Scatter Plot Matrix



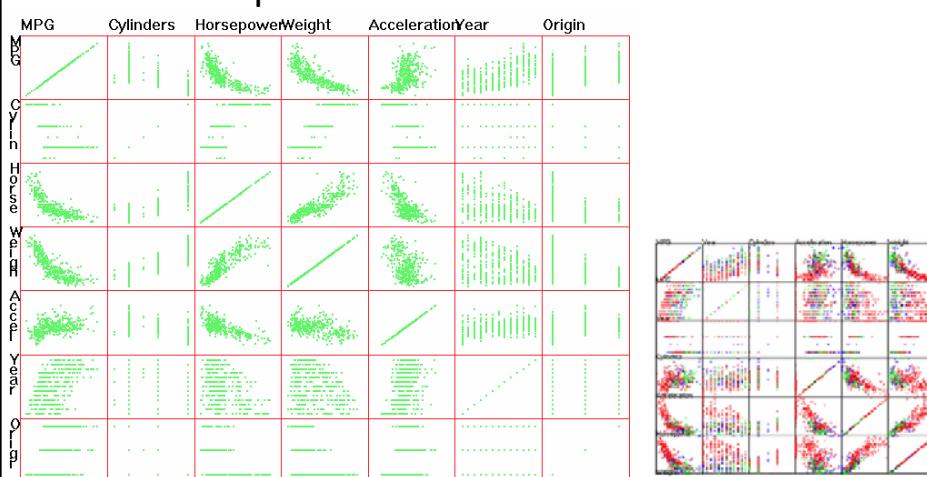


- Implementation in Excel



## Scatter Plot Matrix

- Car Example

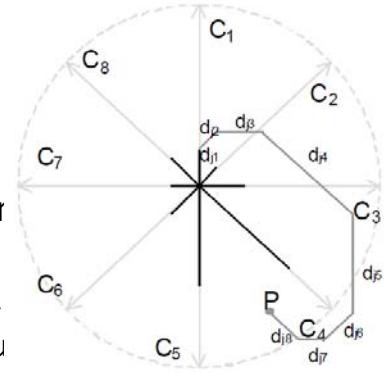


## Star Coordinates

### Star Coordinates

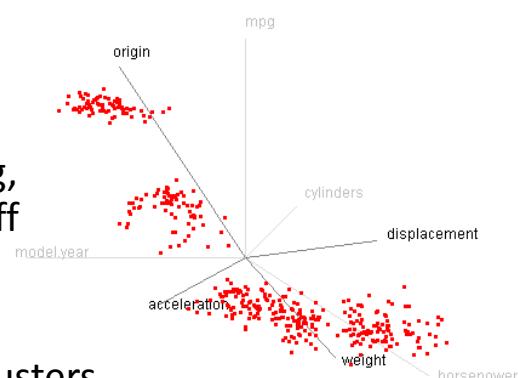
- The basic idea is to arrange the coordinate axes on a circle on a two-dimensional plane with equal (initially) angles between the axes with an origin at the center of the circle.

- 8 dimensional data ( $C_1-C_8$ )
- $P=(d_1,d_2,\dots,d_8)$
- $P$  location calculation:  
extension of typical 2d and 3d scatter-plots to higher dimensions with normalization
- Formula: Read Kandogan's paper "Star Coordinates: A Multi-dimensional Visualization Technique with Uniform Treatment of Dimensions"



Purpose: Gaining insight into hierarchically clustered datasets.

- Case: 400 cars
- Operations: scaling, rotating, turning off some coordinates
- Results: 4 major clusters



## Dimensional Stacking

- Discretizing and recursively embedding of dimensions
- Each resulting N-dimensional record occupying a unique position on the screen

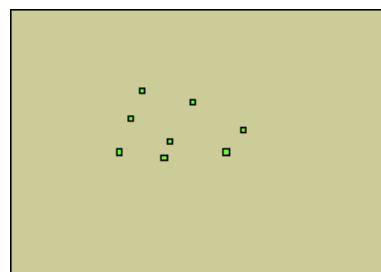
## Dimensional Stacking

- Iris case:

	Classes	sepal-length	sepal-width	petal-length	petal-width
1	Iris-virginica	6.7	3	5.2	2.3
2	Iris-virginica	6	2.2	5	1.5
3	Iris-virginica	6.2	2.8	4.8	1.8
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...	...	...	...	...	...

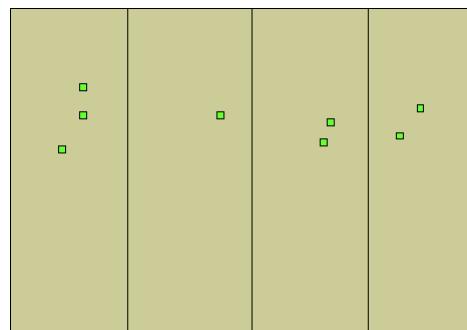
## Dimensional Stacking

- Imagine each data item (4 attributes) as a small block.
- Place all blocks on a table.



## Dimensional Stacking

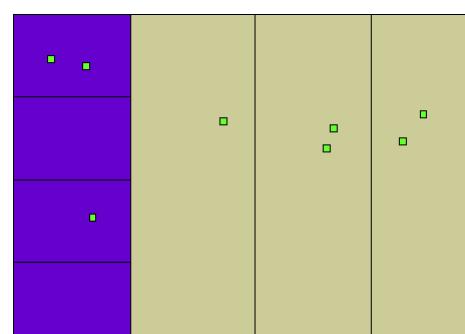
- Add grids on the table.
- Place the blocks in the grids according to their values of attribute1.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

## Dimensional Stacking

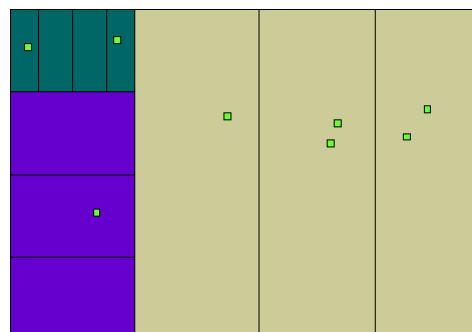
- Add grids in grids.
- Place the blocks in the grids according to their values of attribute2.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

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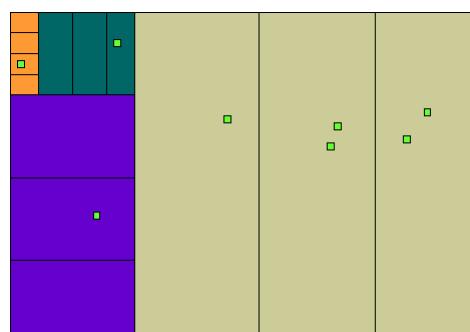
- Add grids in grids.
- Place the blocks in the grids according to their values of attribute3.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

## Dimensional Stacking

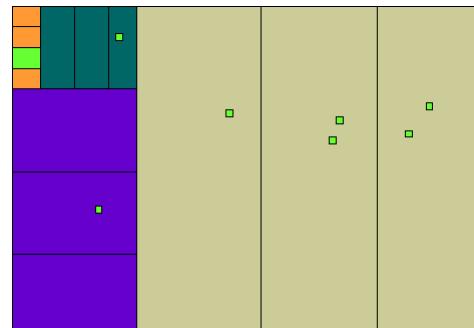
- Add grids in grids.
- Place the blocks in the grids according to their values of attribute4.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

## Dimensional Stacking

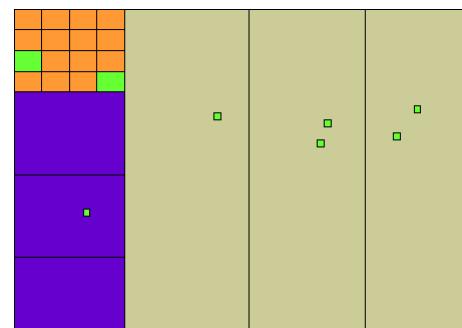
- Fix one block!
- Assign a color to it.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

## Dimensional Stacking

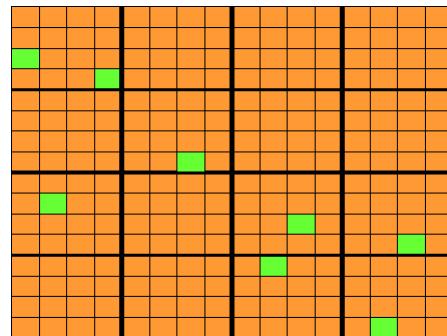
- Fix another block
- Assign a color to it.



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

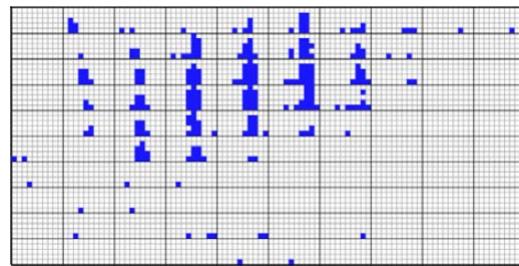
## Dimensional Stacking

- Move to next column until done



[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

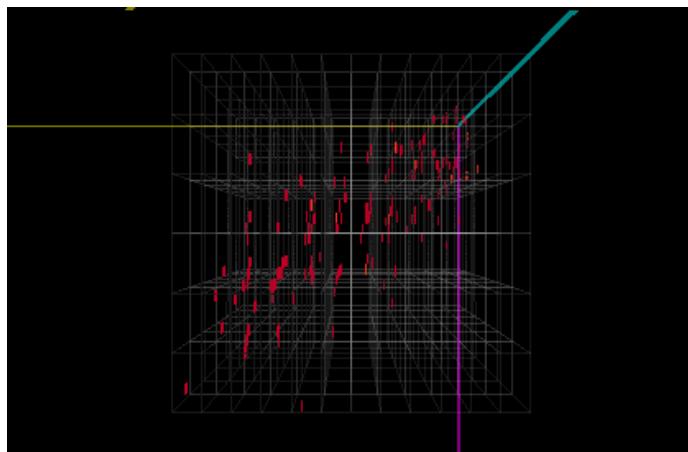
## Dimensional Stacking



visualization of oil mining data with longitude and latitude  
mapped to the outer x-, y- axes and ore grade and depth  
mapped to the inner x-, y- axes  
M. Ward, Worcester Polytechnic Institute

[http://coitweb.uncc.edu/~jyang13/6010/class1\\_intro\\_multi.pdf](http://coitweb.uncc.edu/~jyang13/6010/class1_intro_multi.pdf)

## Dimensional Stacking



Dimensional stacking in 3D

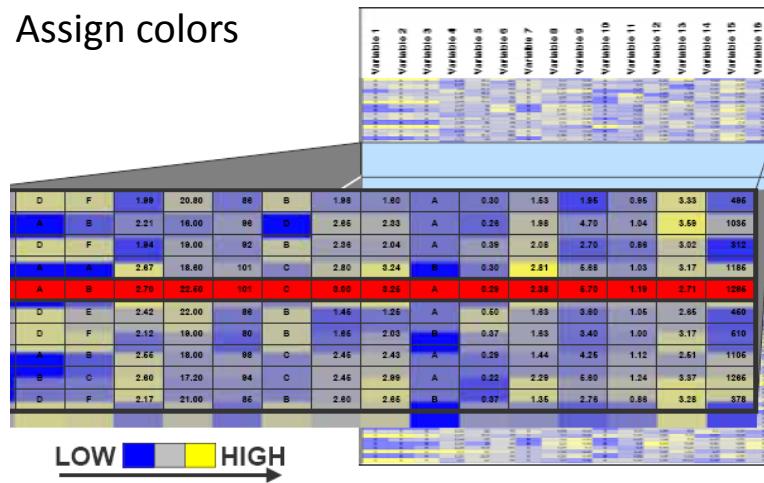
## Table Visualization Enhancement

## Table Visualization Enhancement

- Visualization that improves the existing table format
  - HeatMap
  - Table Lens

### Heat Map

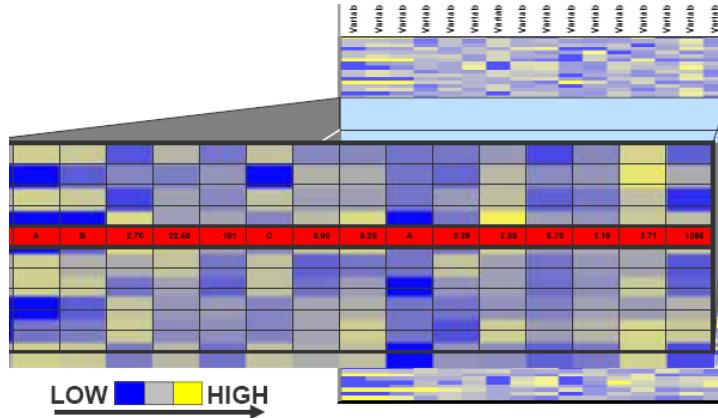
- Assign colors



Mat Ward

## Heat Map

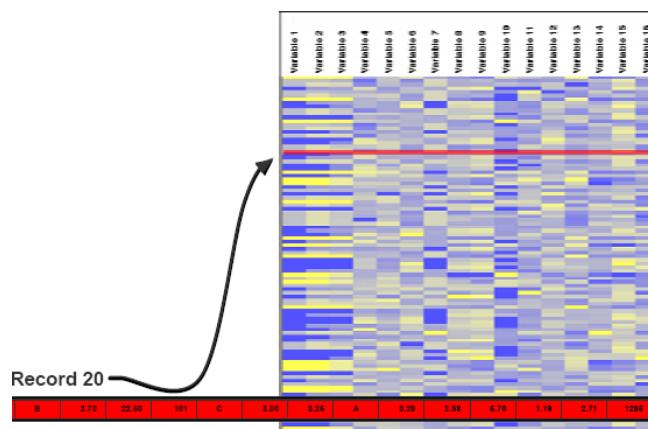
- Remove data



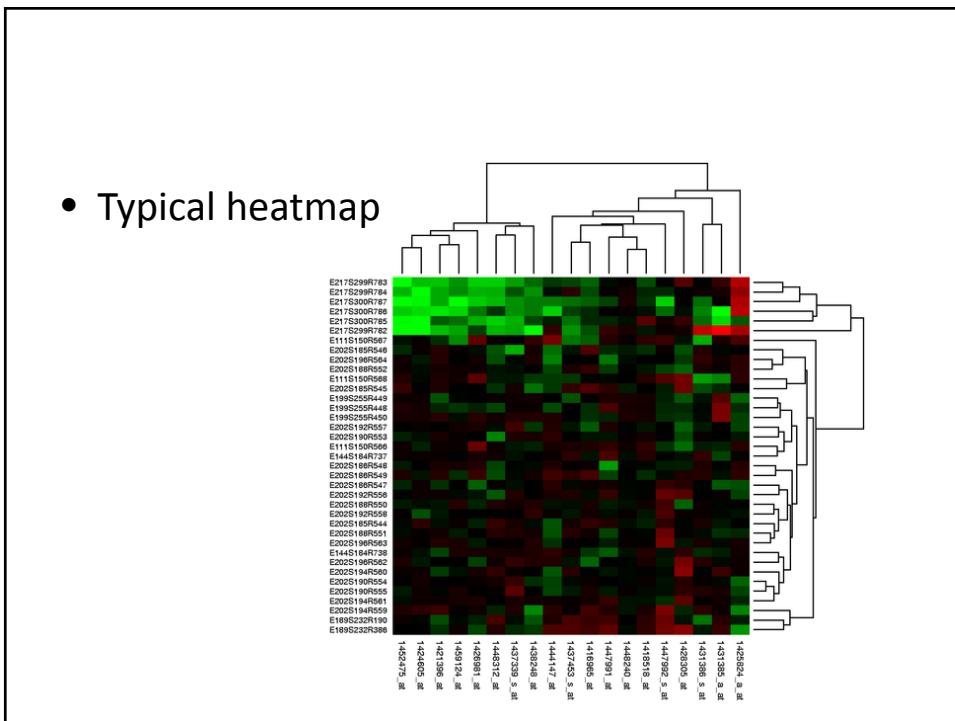
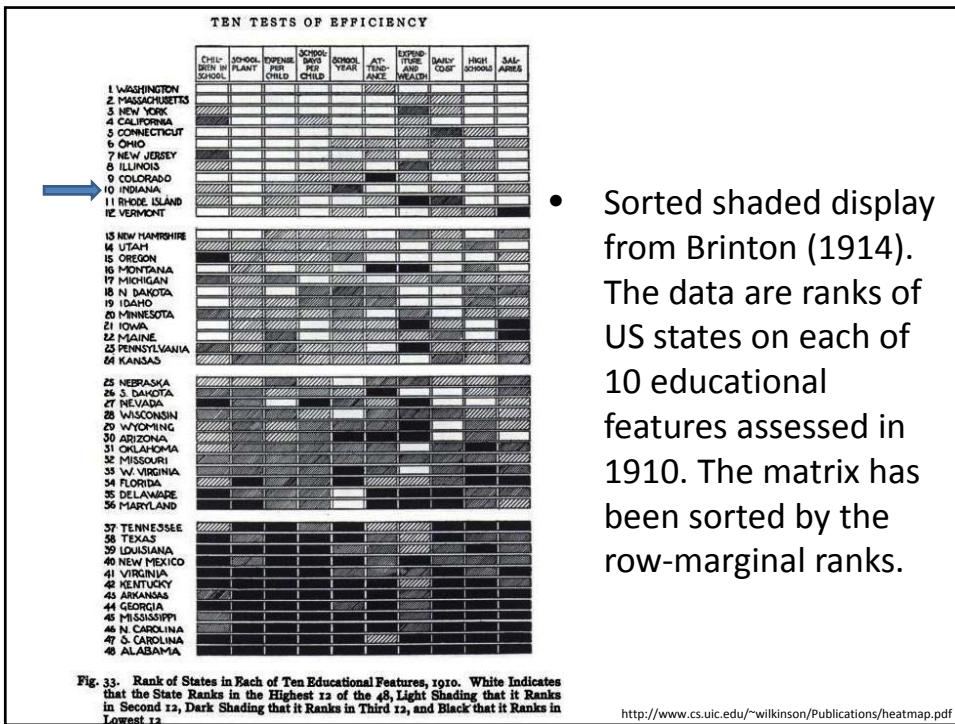
Mat Ward

## Heat Map

- Final heatmap



Mat Ward



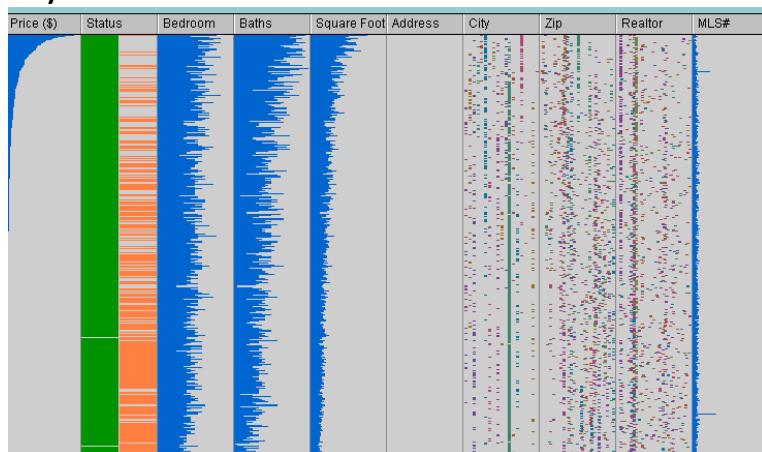
## Table Lens

- Rao R., Card S. K.: '*The Table Lens: Merging Graphical and Symbolic Representation in an Interactive Focus+Context Visualization for Tabular Information*', Proc. Human Factors in Computing Systems CHI '94 Conf., Boston, MA, 1994, pp. 318-322.

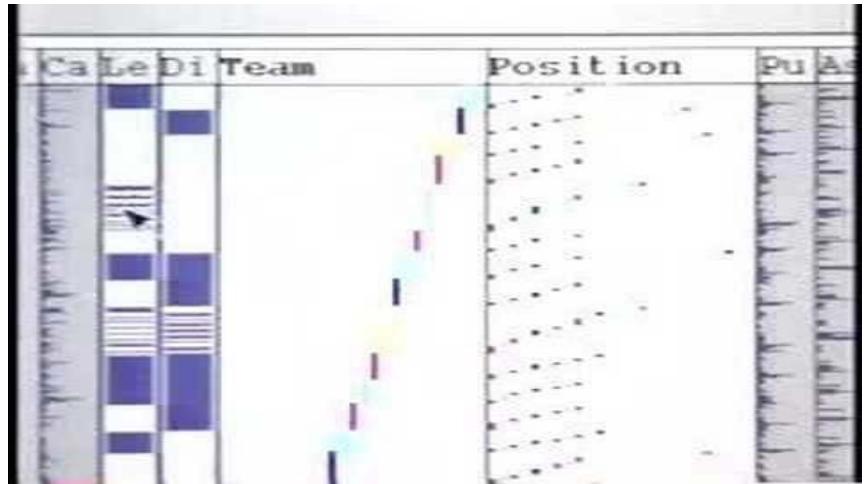
[Demo](#)

## Table Lens

- Buy a house



[http://www.sapdesignguild.org/community/blinks/ui\\_blinks\\_gw\\_01.asp](http://www.sapdesignguild.org/community/blinks/ui_blinks_gw_01.asp)



Exploring Large Tables with Table Lens -- 1994

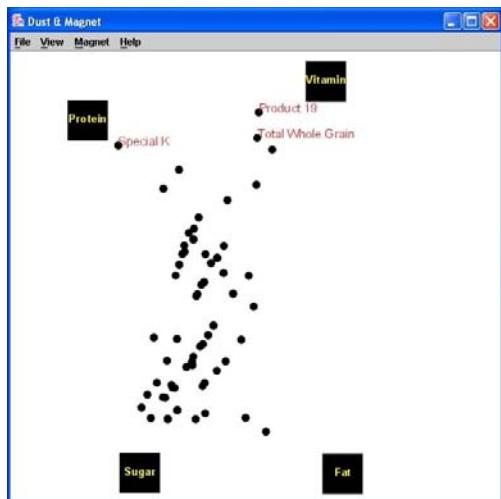
- Questions:
- 1) What is the difference between heat map and table lens?
- 2) When is a good time to use table lens?

## Dust and Magnet

## Dust and Magnet

- Uses a magnet metaphor
- Record  $\leftrightarrow$  Iron dust
- Variable/Attribute  $\leftrightarrow$  Magnet
- When a magnet is dragged, dust particles are attracted to the magnet based on the value of the attribute corresponding to the magnet.

## Dust and Magnet



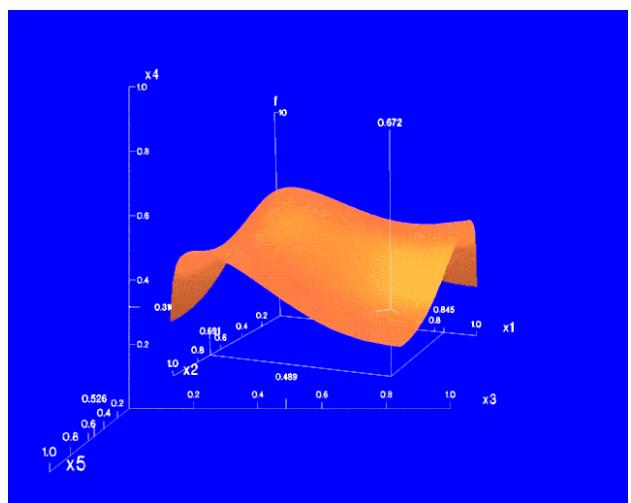
## Dust and Magnet

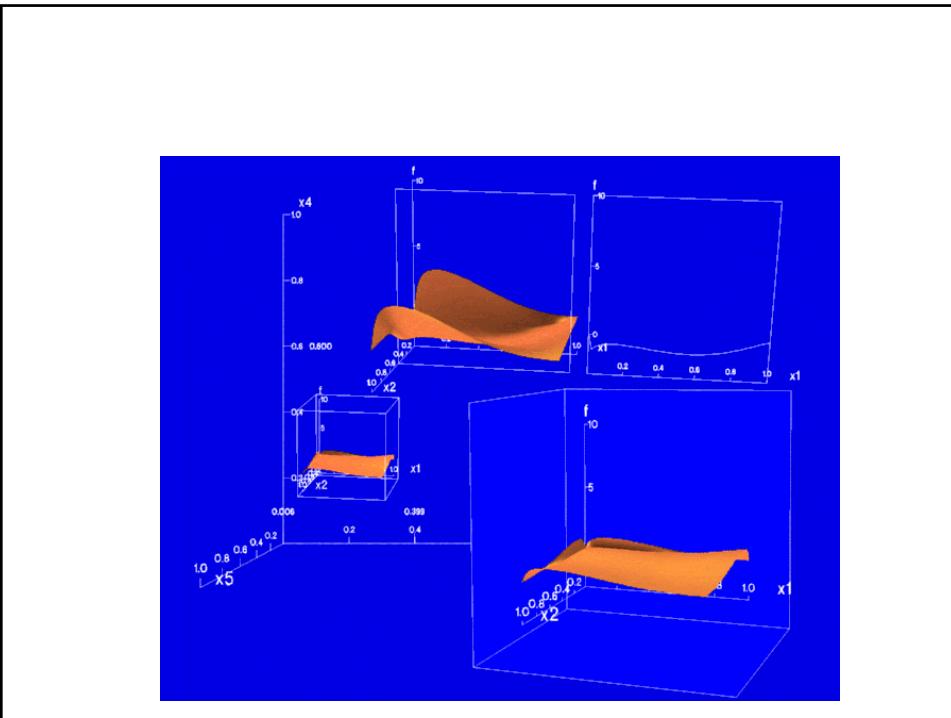
- Especially designed for use by people
  - who struggle with interpreting the complex data of everyday problems
  - who are not experts in information visualization and are not familiar with existing multivariate visualization techniques.

Worlds within Worlds

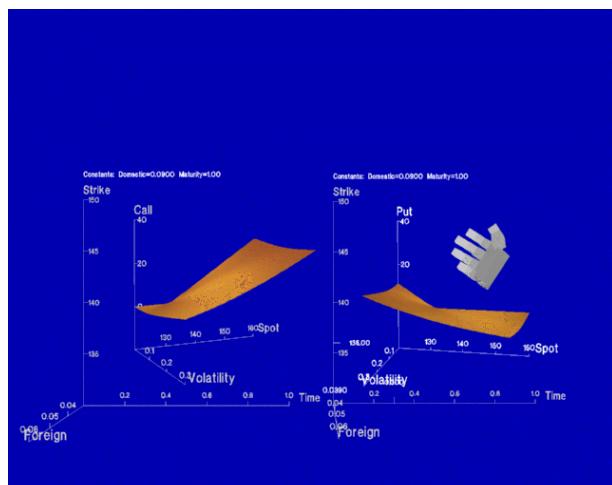
- Use nested, heterogeneous coordinate systems to map multiple variables onto each of the three spatial dimensions.
- Example:
- Function:  $f(x_1, x_2, x_3, x_4, x_5)$
- Set  $x_3, x_4, x_5$  as constant  $c_3, c_4, c_5$ .
- $f(x_1, x_2, c_3, c_4, c_5) \rightarrow$  surface plot

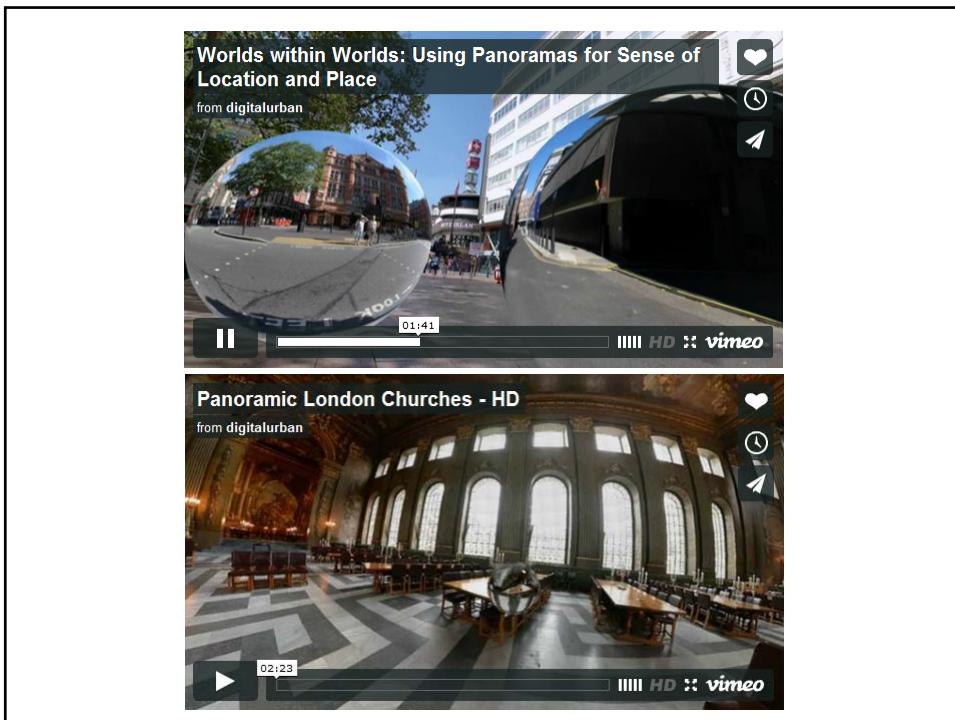
- The height field in the inner world encodes the function for constant values of  $x_3, x_4$ , and  $x_5$ , determined by the position of the inner world's origin relative to the outer world.





- Financial data visualization: Option

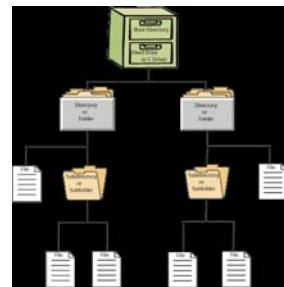




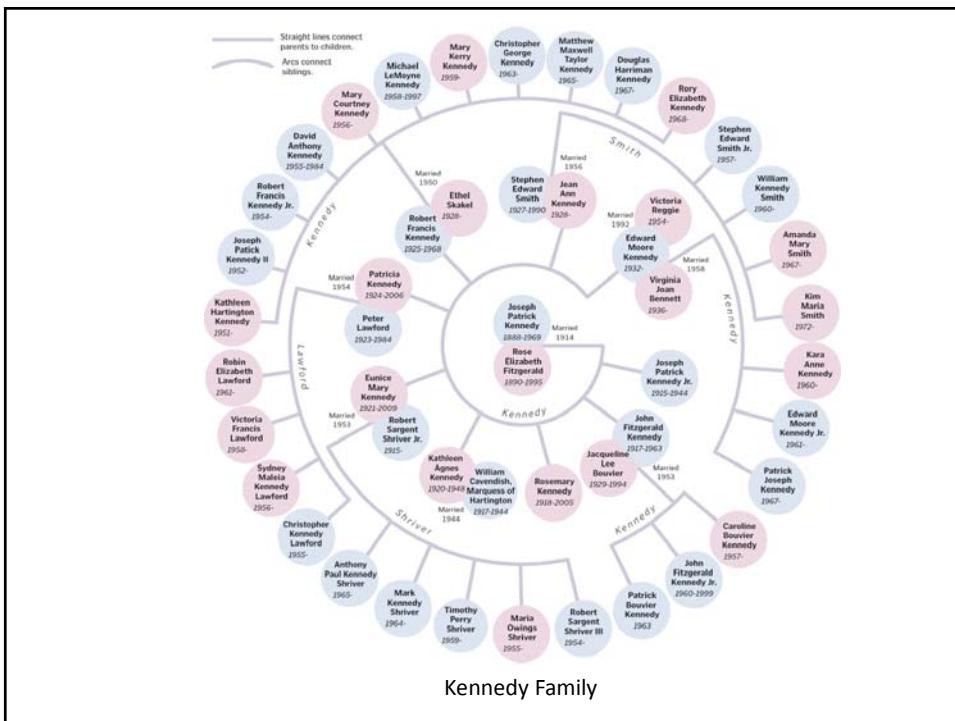
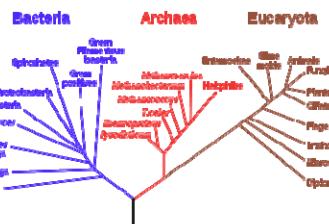
## Tree Visualization

## Examples:

- File systems
- Organization charts
- OO classes
- Phylogenetic trees
- Family trees
- More??



**Phylogenetic Tree of Life**



## Tree Visualization

### Good practice

- Allow adequate space within nodes to display information
- Allow users to understand relationship between a node and its context
- Allow users to find elements quickly
- Fit into a bounded region

## Tree Visualization

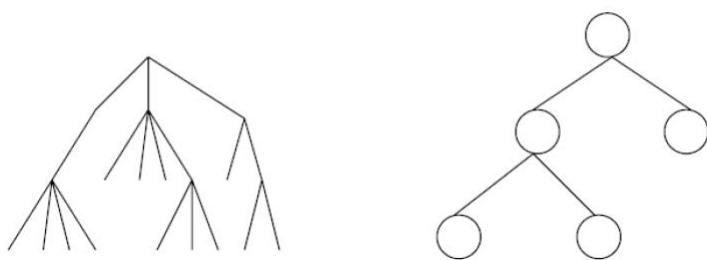
Two main techniques in hierarchical visualization

- Node-link representation (Most Common)
  - Edges – nodes
  - Root – branches – leaves
  - Parents – children
  - Algorithm: Recursive layout algorithm
- Spatial-Filling

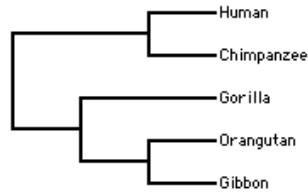
## Node-Link

## Tree Structure

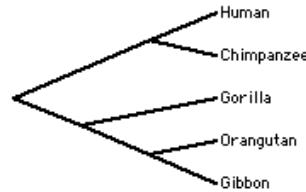
- Top down trees
  - Most common in node-link diagram
  - Root at the top, leaves at the bottom



- Tree Styles



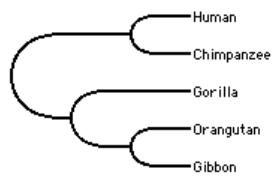
**Rectangular:** Well suited for displaying labeled/scaled trees.



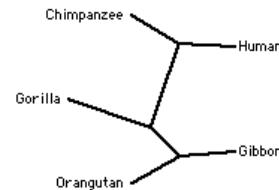
**Straight:** Works well only on rooted binary trees.

<http://www.hyphy.org/docs/GUIExamples/treepanel.html>

- Tree Styles



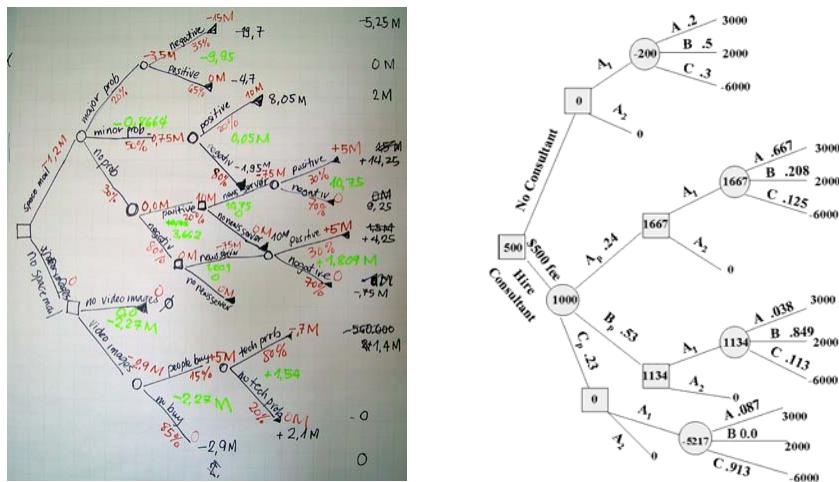
**Smooth Edges:** Very similar to the rectangular mode.



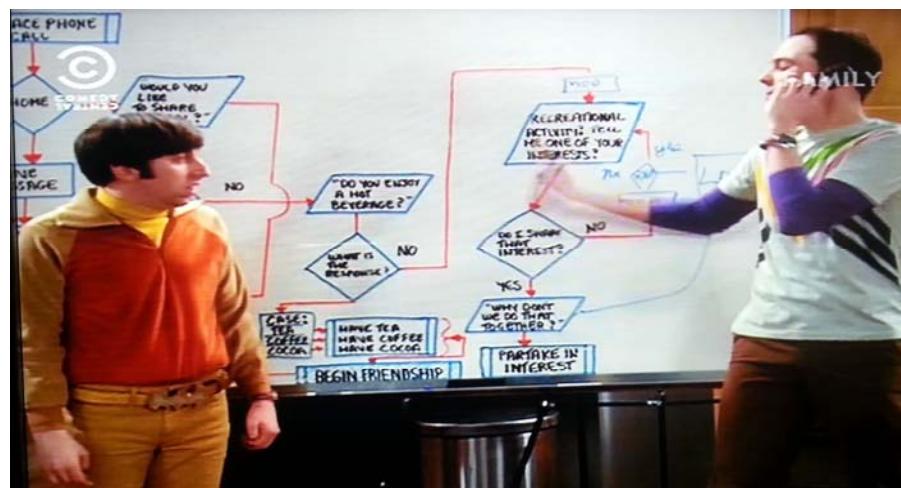
**Radial:** Works well for visualizing unrooted trees.

<http://www.hyphy.org/docs/GUIExamples/treepanel.html>

## Decision Tree

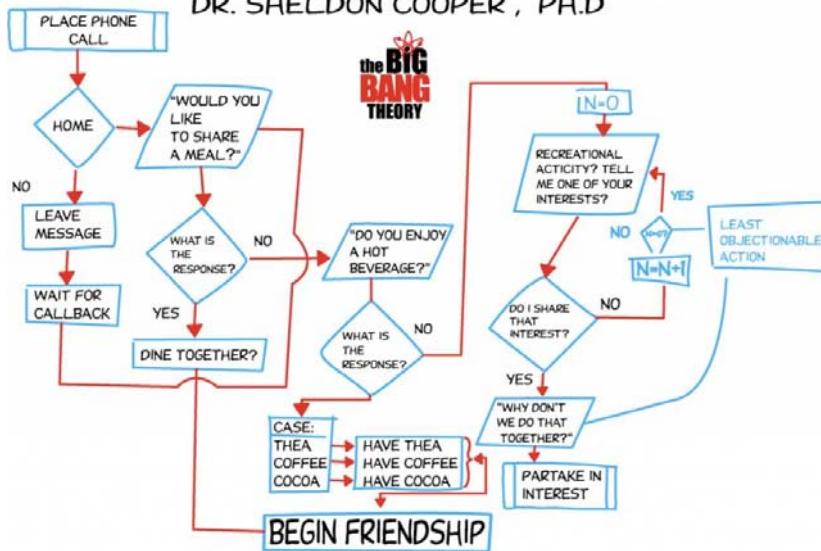


## Tree vs flowchart



# THE FRIENDSHIP ALGORITHM

DR. SHELDON COOPER , PH.D



Q: What is the difference between a Tree and a Flowchart?

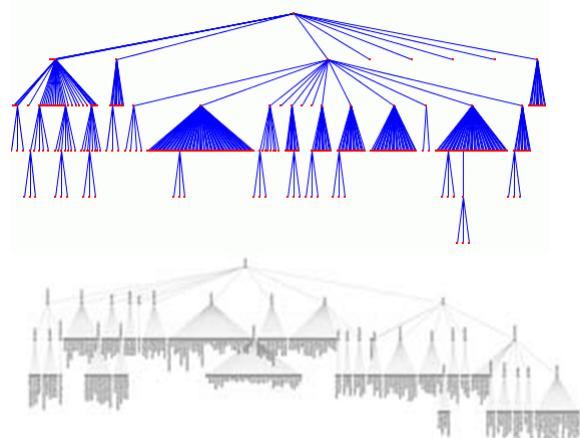
- Organization Chart



Edraw Soft

Question: What are potential problems in the standard node-link visualization?

- Too many nodes and/or leaves



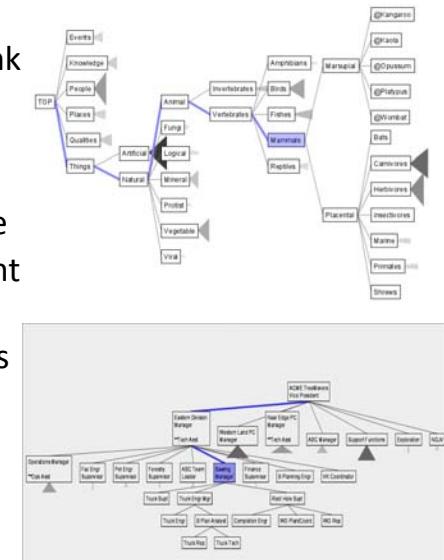
- Potential Problems
- Scalability
  - For top-down, width of fan-out uses up horizontal real estate very quickly
  - Number of nodes increases exponentially. E.g.  $2^N$  nodes at level N.
  - Space increases polynomially
- Tree might grow a lot along one particular branch
- Hard to draw it well in view without knowing how it will branch

Q: Any thoughts???

John Stasko at GIT

# Space Tree

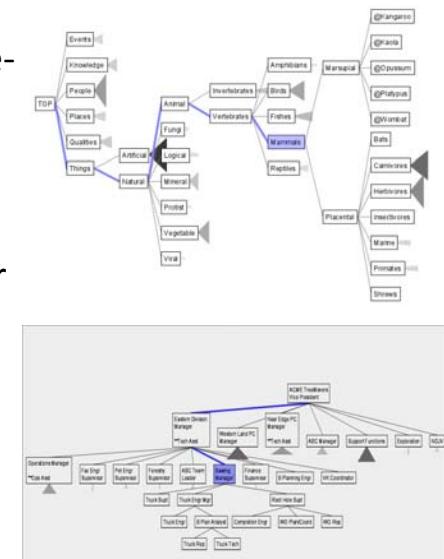
- Conventional layout node link diagrams
  - Dynamic rescaling of branches of the tree to best fit the available screen space
  - Optimized camera movement
  - Preview icons summarizing the topology of the branches that cannot be expanded
  - Integrated search and filter functions.



U of Maryland: <http://www.cs.umd.edu/hcil/spacetree/>

# Space Tree

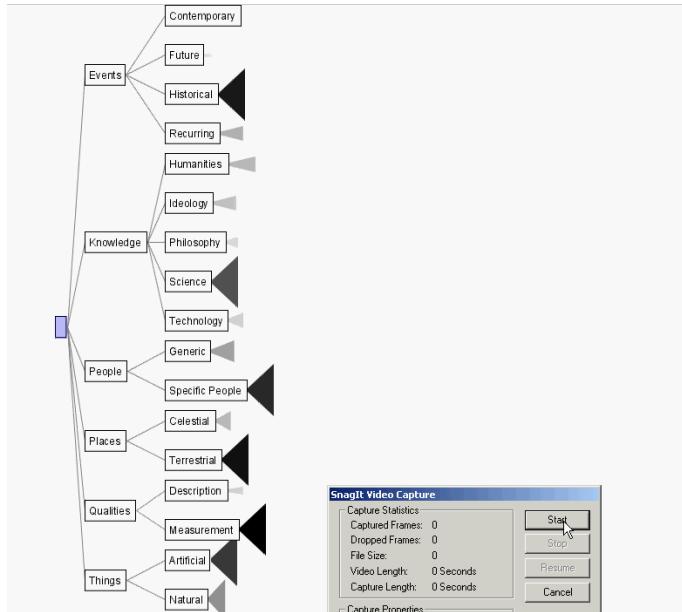
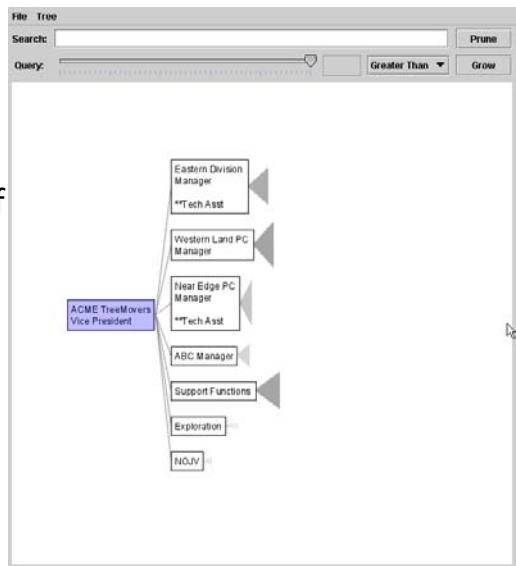
- Conventional layout node-link diagrams
  - Vertical or horizontal
    - Subtrees are triangles
    - Size indicates depth
  - Shading indicates number of nodes inside
  - Navigate by clicking on nodes
    - Strongly restrict zooming



U of Maryland: <http://www.cs.umd.edu/hcil/spacetree/>

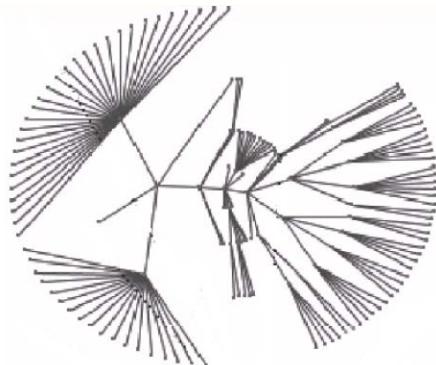
## Features of Space Tree

- Make labels readable
- Maximize number of levels opened
- Decompose tree animation
- Use landmarks
- Use overview and dynamic filtering



## Radio Tree View

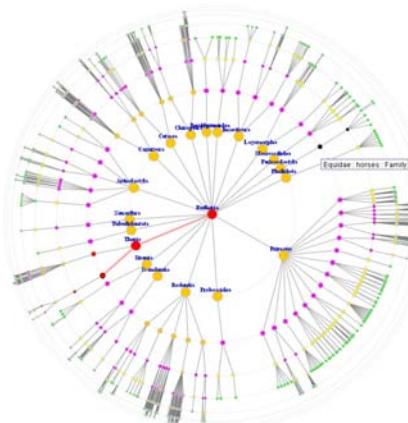
- Recursively position children of a subtree into circular wedges
- The central angle of these wedges are proportional to the number of leaves



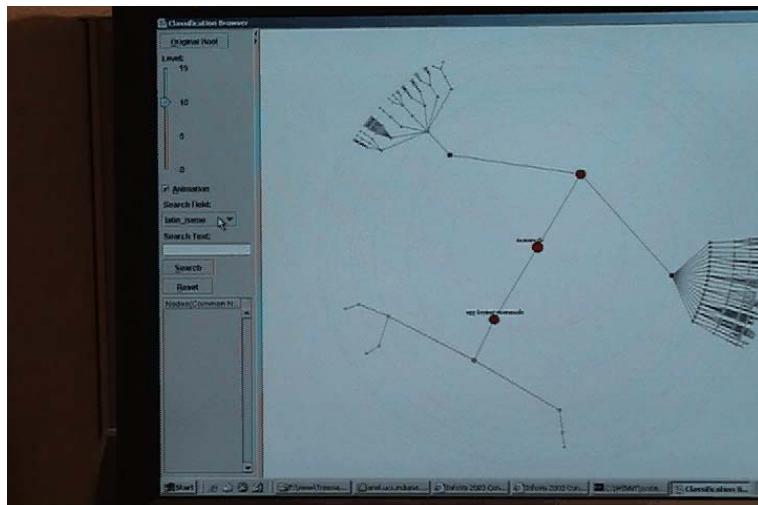
P. Eades, "Drawing Free Trees", *Bulleting of the Institute fro Combinatorics and its Applications*, 1992, pp. 10-36.

## Radio Tree View

- Indiana University Bloomington

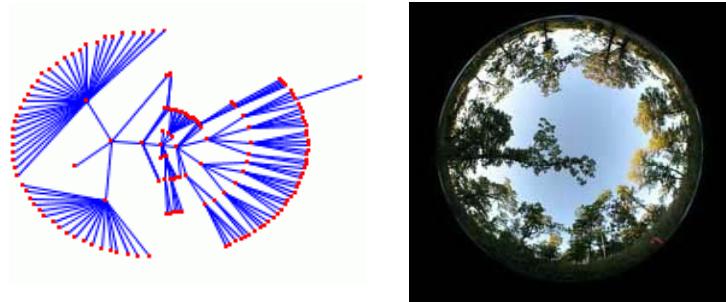


## Radio Tree View



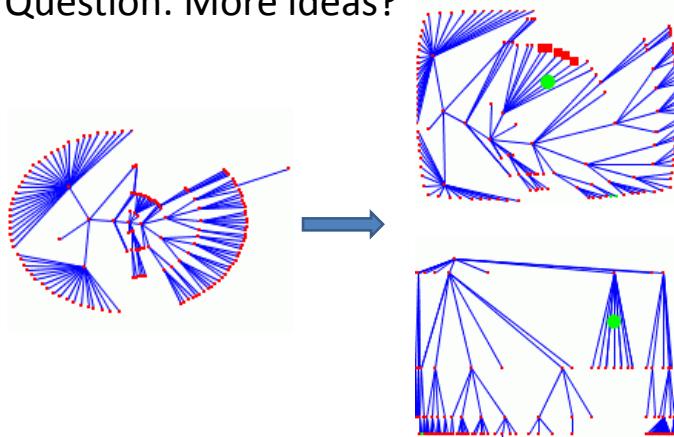
## Radio Tree View

- Radio tree view  $\leftrightarrow$  Fish eye distortion



## Radio Tree View

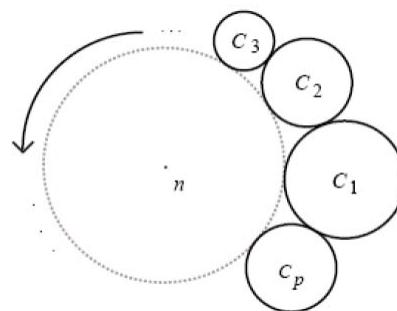
- Radio tree view  $\leftrightarrow$  Fish eye distortion
- Question: More ideas?



## Circular drawing of rooted trees

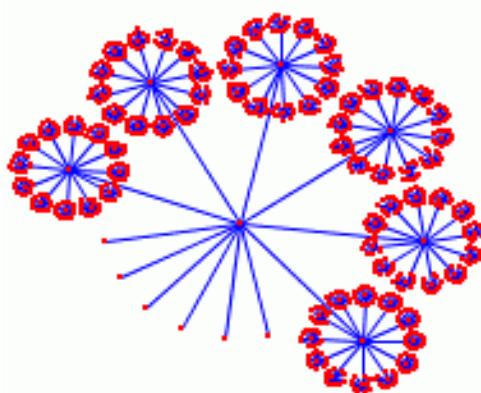
- Balloon View

Siblings of sub-trees are included in circles attached to the father node.



## Circular drawing of rooted trees

- Balloon View



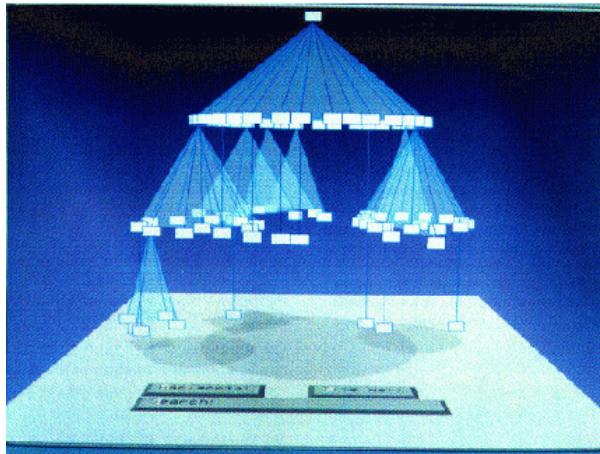
## 3D Visualization for Trees

- Add a third dimension into which layout can go
- Compromise of top-down and centered techniques mentioned earlier
- Children of a node are laid out in a cylinder “below” the parent
- Siblings live in one of the 2D planes

Robertson, Mackinlay, Card CHI '91

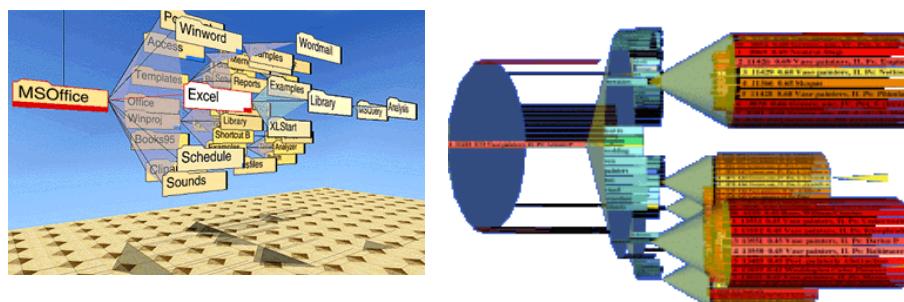
# Cone Tree

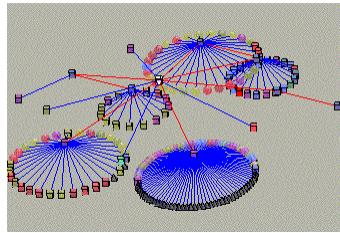
- Question: Advantages and disadvantages?



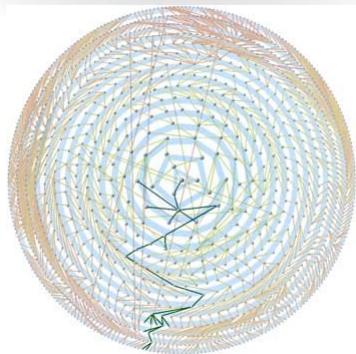
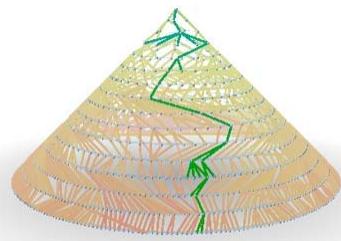
<http://davis.wpi.edu/~matt/courses/trees/>

# Cone Tree





A file system



A path through the social network

## Cone Trees

### Advantages

- More effective area to lay out tree
- Use of smooth animation to help person track updates
- Aesthetically pleasing ?

### Disadvantages

- As in all 3D, occlusion obscures some nodes
- Non-trivial to implement and requires some graphics horsepower

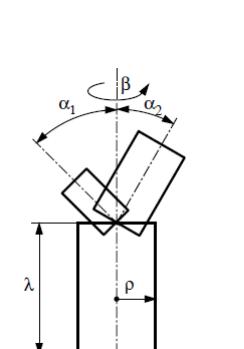
John Stasko

# Botanical Tree

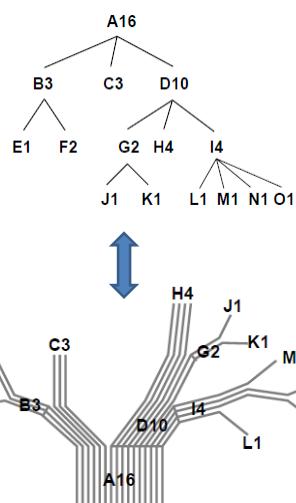
- Basic idea: People can easily see the branches, leaves, and their arrangement in a botanical tree
- Inspiration: Strand model of Holton
- Strands: internal vascular structure of a botanical tree
- Paper

Botanical Visualization of Huge Hierarchies  
Ernst Kleiberg, Huub van de Wetering†,  
Jarke J. van Wijk‡  
Department of Mathematics and Computer Science  
Eindhoven University of Technology

# Botanical Tree

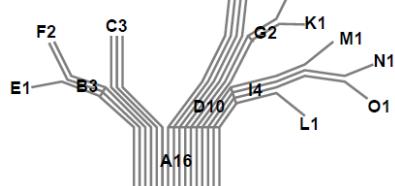


Stem and two subbranches

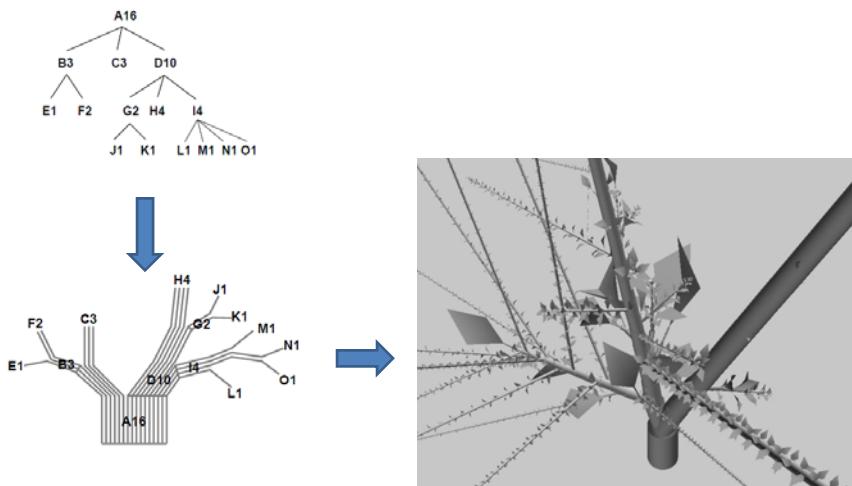


Node-link diagram

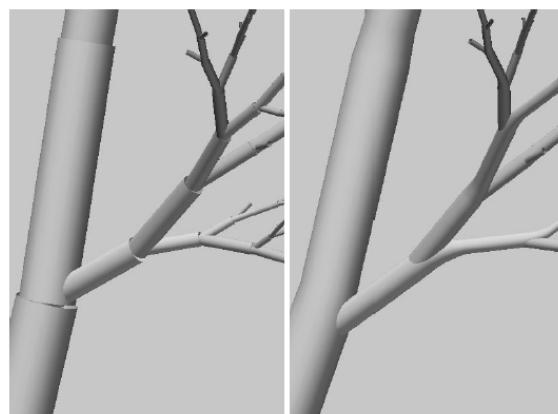
Corresponding strands model



## Botanical Tree

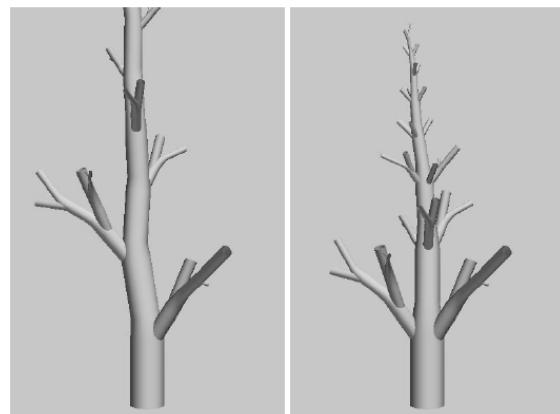


## Botanical Tree



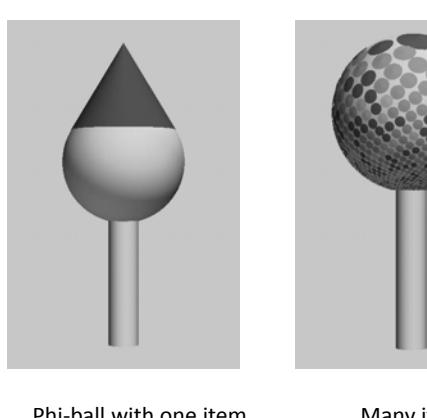
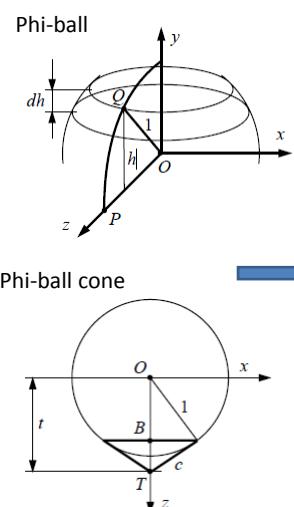
Cylinders or smoothed transition

## Botanical Tree



Binary tree or 'real' tree

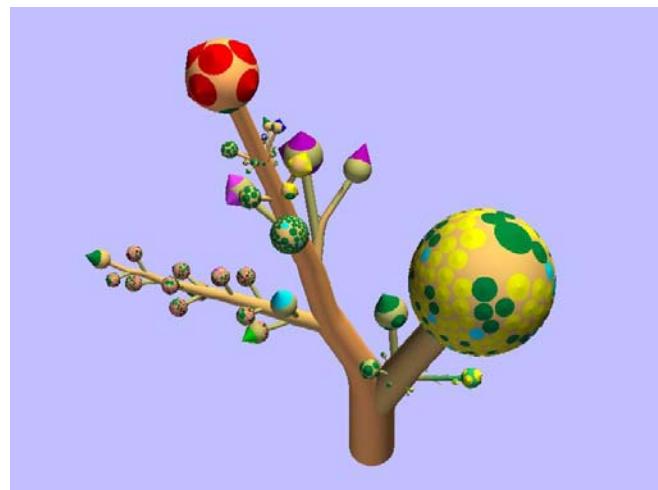
## Botanical Tree



Phi-ball with one item

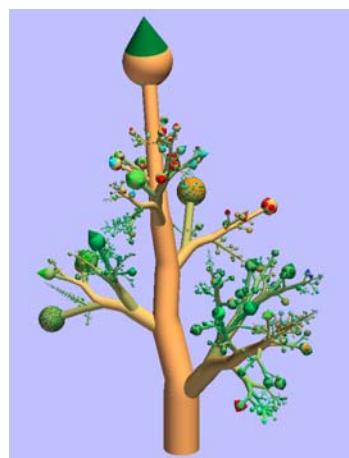
Many items

## Botanical Tree

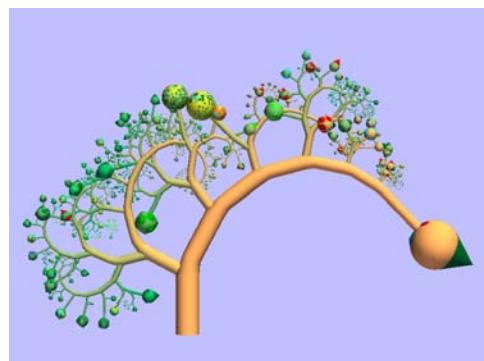
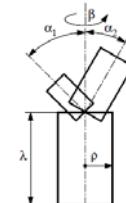


Final model with contraction, extrusion, and phiballs

## Botanical Tree

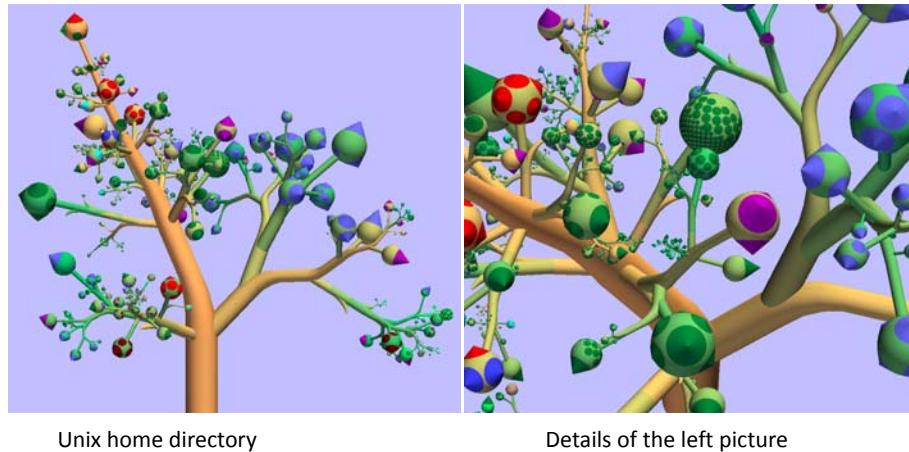


Complete hard disk  $\alpha=45^\circ$ ,  $\beta=180^\circ$



Complete hard disk  $\alpha=90^\circ$ ,  $\beta=0^\circ$

## Botanical Tree



Unix home directory

Details of the left picture

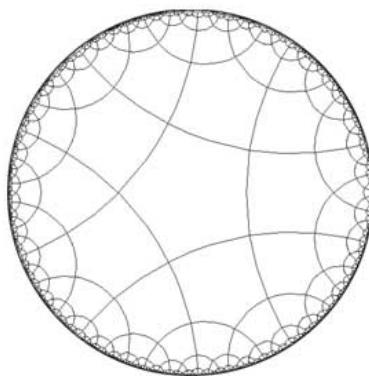
## Collapsible Cylindrical Tree

- Basic idea: use a set of nested cylinders according to the telescope metaphor
- Limitation: one path is visible in once
- Interactions: rotation, go down/up



## Tree in Hyperbolic Space

## Hyperbolic Space



A Hyperbolic Tessellation of the Circle



Escher's *Circle Limit IV*

<http://hollindale.co.uk/chris/images/hyperbolic.jpg>

## Hyperbolic

- Models of hyperbolic space
  - The hyperboloid model
  - The Klein model
  - The Poincaré models
- [Hyperbolic math](#)

## Hyperbolic Space for Tree Visualization

- Main Contributors
  - H3 -- Munzer 97,98
  - Webviz -- Munzer and Burchard 95
  - 2D Hyperbolic Trees -- Lamping and Rao 94,95
  - Fractal trees -- Koike and Yoshihara 93
  - Cone Trees -- Robertson 91
  - Xerox PARC patent

- Apply a hyperbolic transformation to the space
- Root is at center, subordinates around
- Apply idea recursively, distance decreases between parent and child as you move farther from center, children go in wedge rather than circle

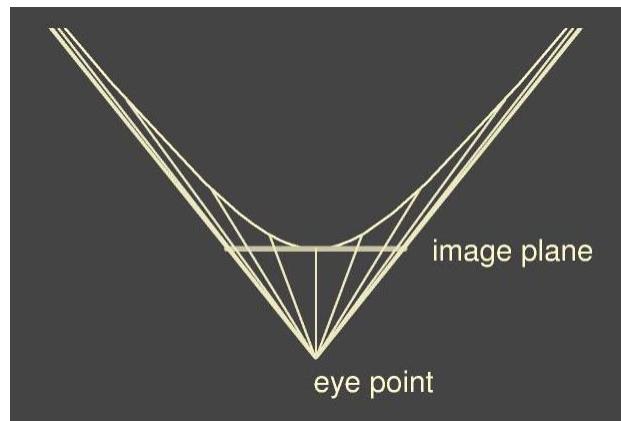
Stasko

Key idea:

- Find a space (hyperbolic space) that increases exponentially, lay the tree on it
- Transform from the hyperbolic space to 2D Euclidean space

## 1D Hyperbolic Space

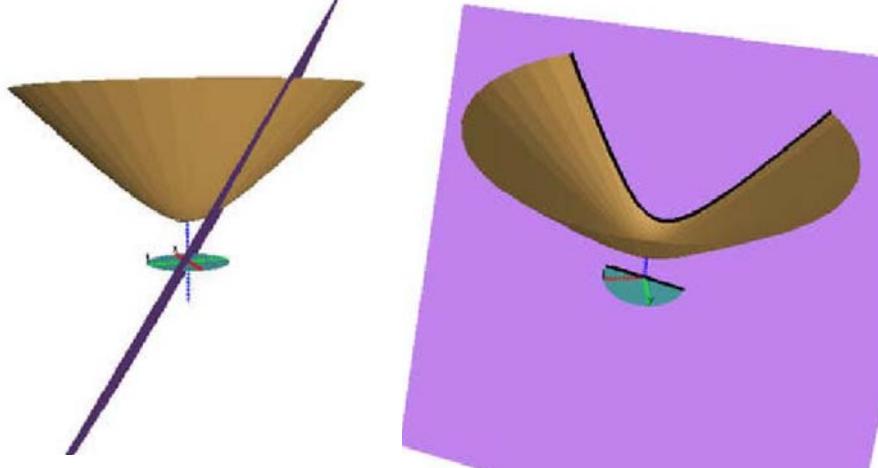
- Image plane → a line



<http://graphics.stanford.edu/~munzner/talks/calgary02/mgp00032.html>

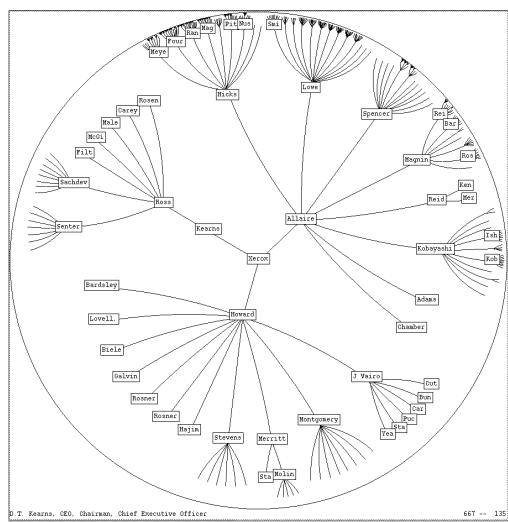
## 2D Hyperbolic Space

- Image plane → a circle or disk



Formula	Euclidean	Hyperbolic
right-angle triangle	$\tan \theta = \frac{\text{opp}}{\text{adj}}$	$\tan \theta = \frac{\tanh(\text{opp})}{\sinh(\text{adj})}$
right-angle triangle	$\sin \theta = \frac{\text{opp}}{\text{hyp}}$	$\sin \theta = \frac{\sinh(\text{opp})}{\sinh(\text{hyp})}$
circle area	$\pi r^2$	$2\pi(\cosh(r) - 1)$
hemisphere area	$2\pi r^2$	$2\pi \sinh^2(r)$
spherical cap area <sup>1</sup>	$2\pi r^2(1 - \cos \phi)$	$2\pi \sinh^2 r(1 - \cos \phi)$

Lamping and Rao, 1995



### Approach:

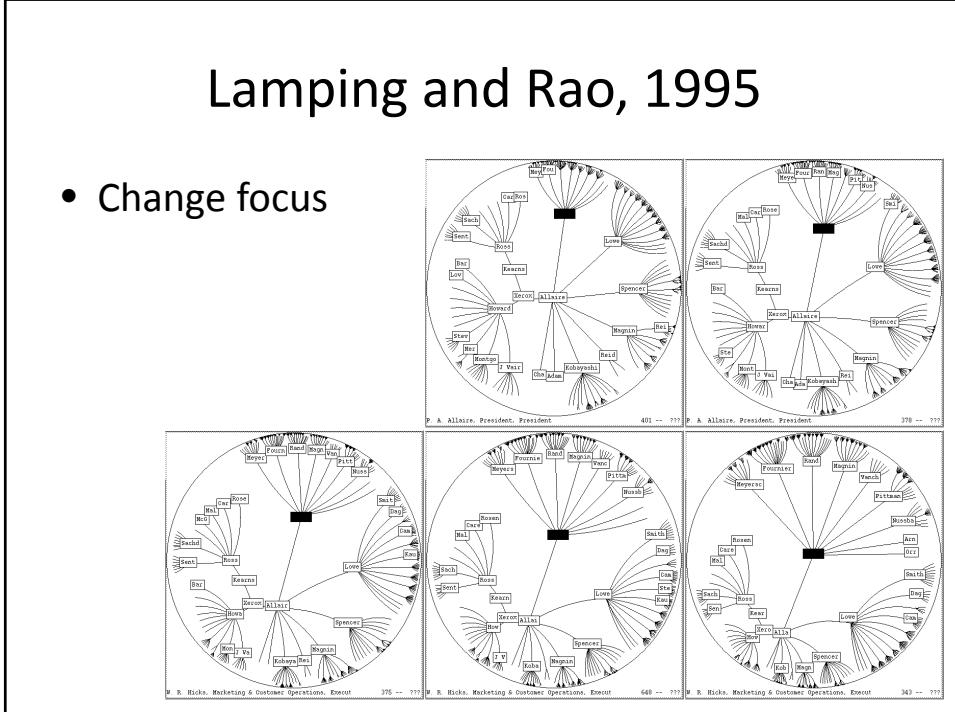
- Lay out the hierarchy on the hyperbolic plane and map this plane onto a display region.

## Comparison

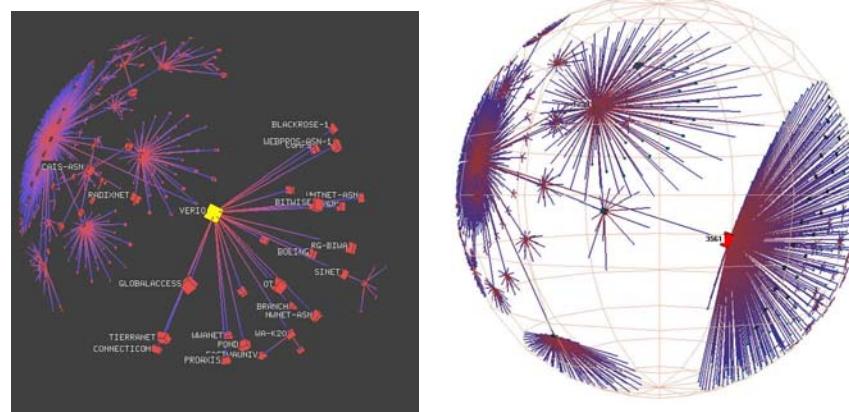
- A standard 2D browser:  
100 nodes (w/3 character  
text strings)
  - Hyperbolic browser: 1000  
nodes, about 50 nearest  
focus can show from 3 to  
dozens of characters

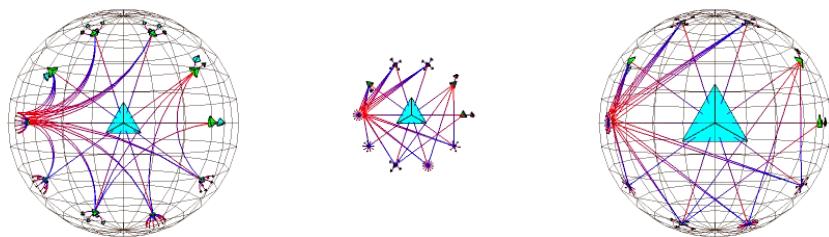
## Lamping and Rao, 1995

- Change focus



- Effects





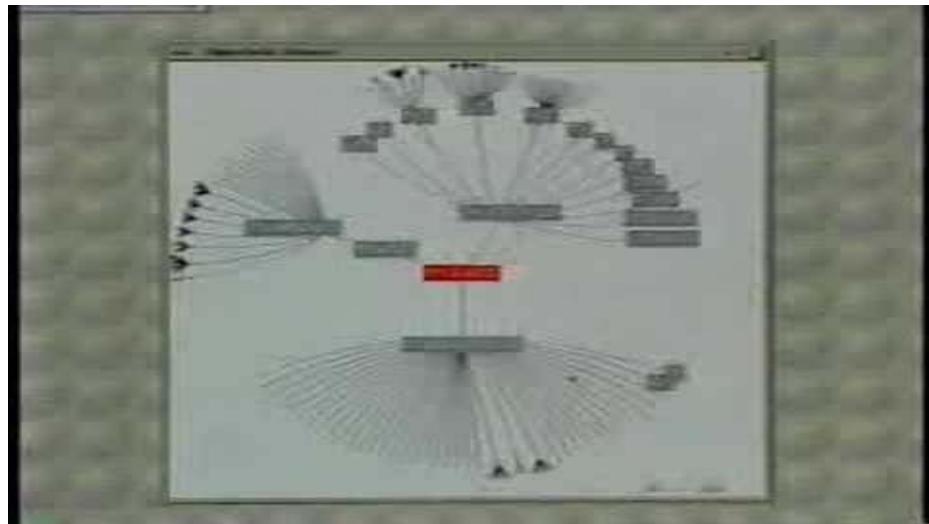
Conformal Model

"Insider" Model

Projective Model

- Natural magnification (fisheye) in center
- Layout depends only on 2-3 generations from current node
- Smooth animation for change in focus
- Don't draw objects when far enough from root (simplify rendering)

Original Authors

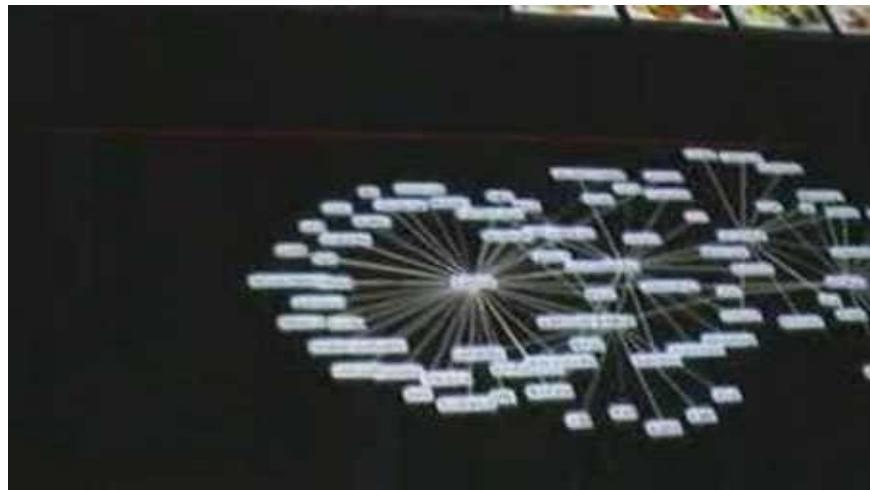


[InfoVis SpaceTree Demo](#)

[InfoVis HyperTree Demo](#)

Question:

- The difference between SpaceTree and HyperTree?
- When to use SpaceTree or HyperTree?



Potential Applications: Migrate to smart phone systems?

## gesture-based user interface -- Minority Report



## Hyperbolic Visualization

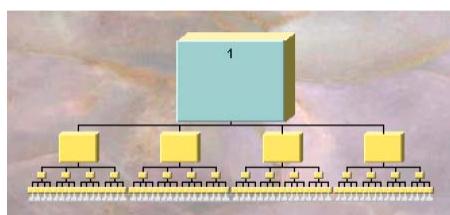
- Handle much larger graphs, i.e. >100,000 edges
- Support dynamic exploration & interactive browsing
- Maintain a guaranteed frame rate



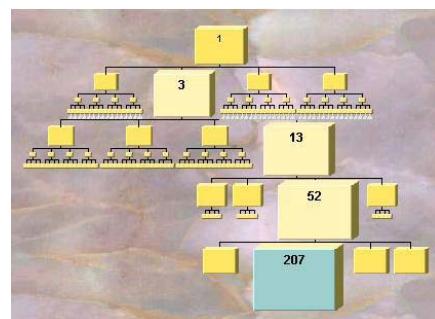
## 2D is Back

- After all the interest in 3D and hyperbolic techniques in the 1990s, recently, there has been renewed interest in the old 2D methods
- Recall SpaceTree

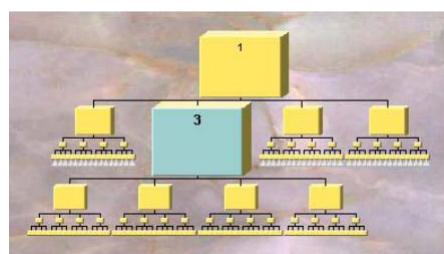
## Degree-of-Interest Trees



Display of a uniform tree of 4 levels

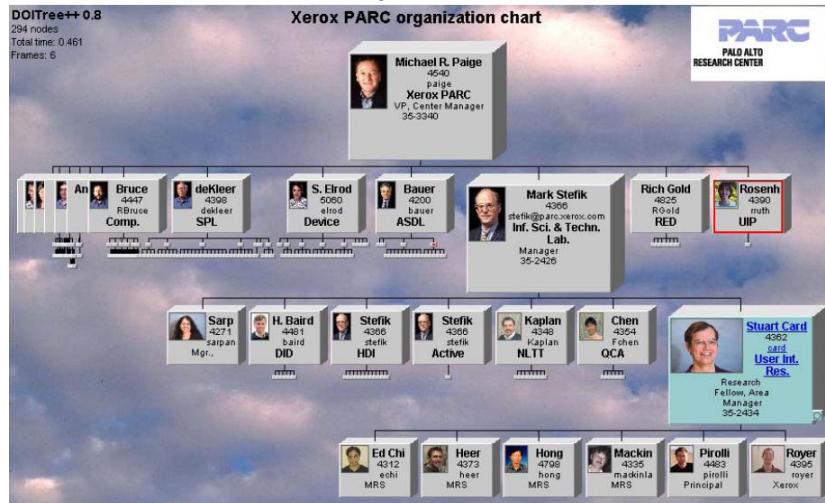


Same tree expanded down to a leaf node

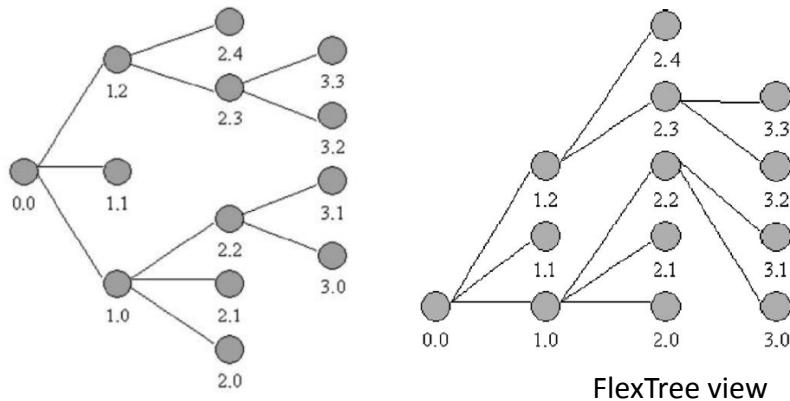


Same tree with focus on Node 3

## Degree-of-Interest Trees with Compression



## FlexTree

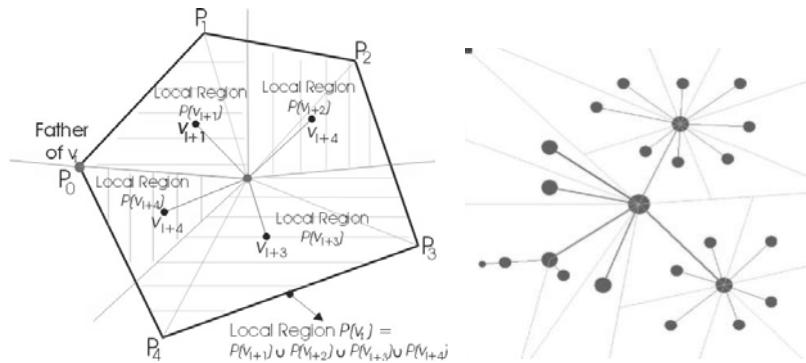


Question: What is the key concept in FlexTree?

Basic idea: Nodes as hard balls. Press them down.

## Space-Optimized Tree

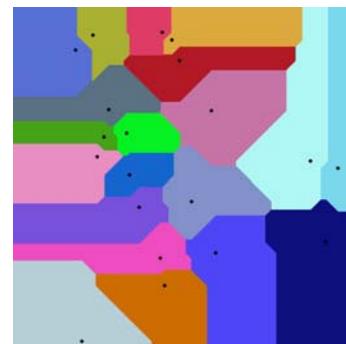
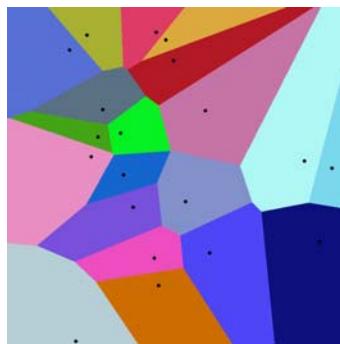
- Goal: Show relationships and optimize space



- Voronoi diagram of a set of points



- Voronoi diagrams of 20 points under two different metrics

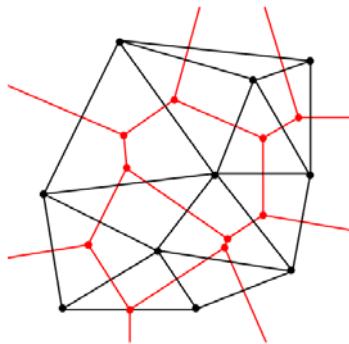
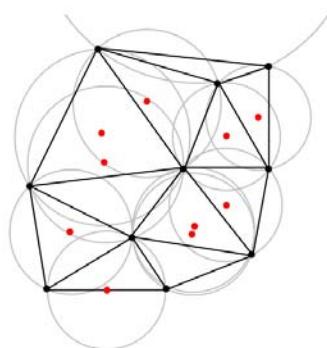


Euclidian distance =  $\sqrt{(a_1 - b_1)^2 + (a_2 - b_2)^2}$

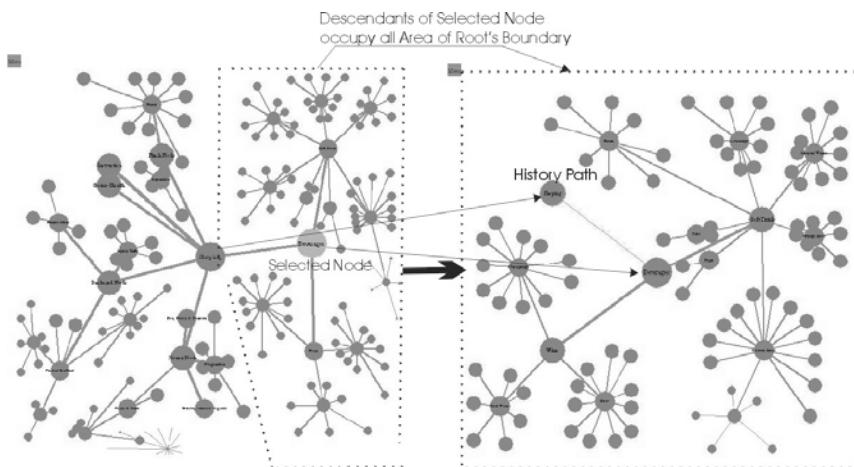
Manhattan distance =  $|a_1 - b_1| + |a_2 - b_2|$

[http://en.wikipedia.org/wiki/Voronoi\\_diagram](http://en.wikipedia.org/wiki/Voronoi_diagram)

- Delaunay triangulation and Voronoi Diagram



## Space-Optimized Tree



Nguyen and Huang, 2002

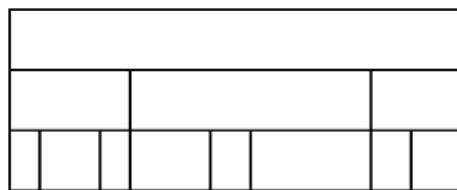
## Summary

- Original tree view
  - Space Tree
  - Radio tree
  - 3D Cone tree
  - Hyperbolic tree
  - Botanic tree
  - Collapsible Cylindrical Tree
  - Degree of interest tree
  - Flex tree
  - Space-optimized tree
- New view → solve problems.

## Space-Filling

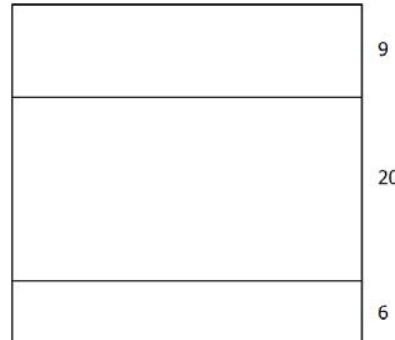
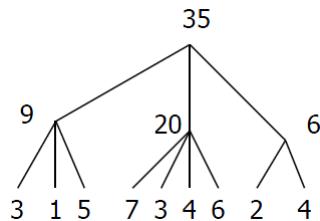
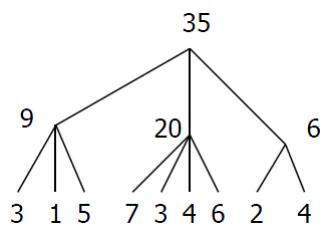
### Space-Filling

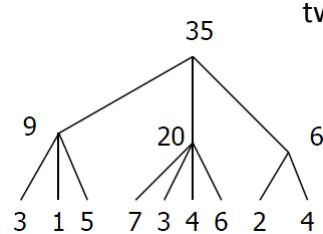
- Children are drawn inside their parents
- Alternate horizontal and vertical slicing at each successive level
- Use area to encode other variable of data items



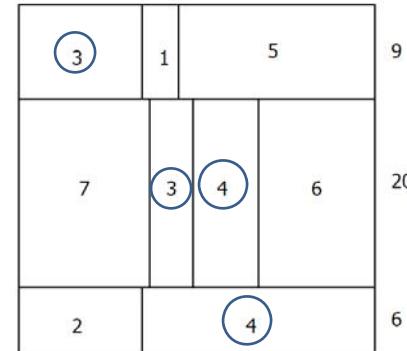
Space-filling representation developed by Shneiderman and Johnson, Vis91

- Map a tree to an area





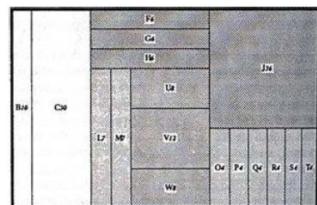
two 3s?



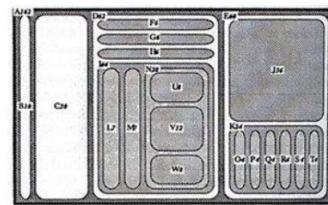
Question: two 4s have the same size (area)?

- Better use of space → Why??  
– Rectangular shape
- More attributes → Name some??  
– color and area
- Not as good at representing structure  
– Aspect ratios  
– Balanced tree, items with similar sizes

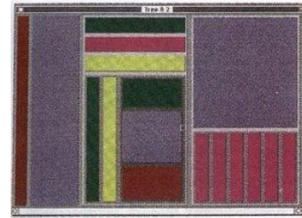
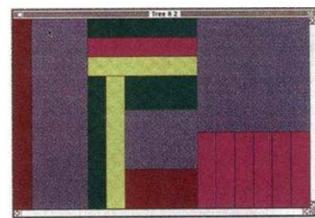
## Nested and Non-Nested



Non-nested Tree-Map



Nested Tree-Map



## TreeMaps: Tiling

- Tiling: a way to divide a rectangle into sub-rectangles of specified areas.
- Good practice
  - Create rectangles of **aspect ratio** close to one
  - Preserve some sense of **the ordering** in the input data
  - Change to reflect changes in the underlying data

<http://en.wikipedia.org/wiki/Treemapping>

## TreeMaps: Tiling

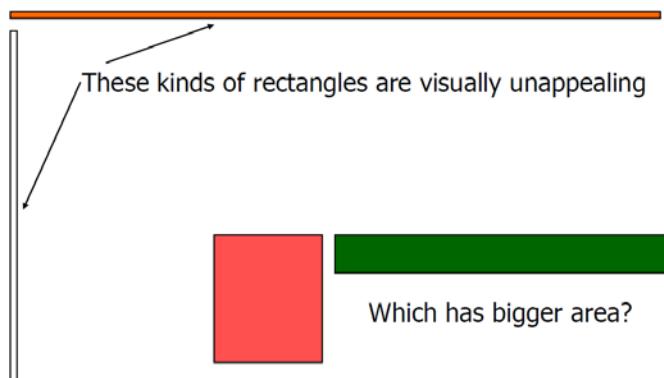
- Difficulties:

Inverse relationship between properties

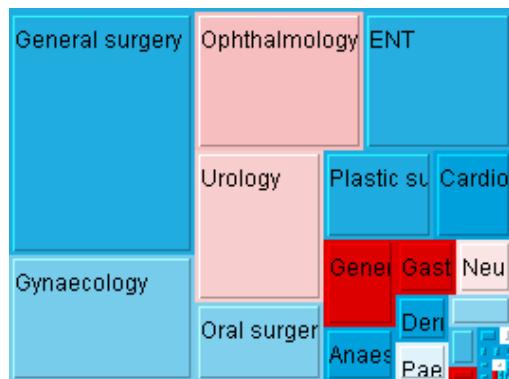
- Optimized aspect ratio → unpredictable order of placement
- Stable order → degraded aspect ratio

<http://en.wikipedia.org/wiki/Treemapping>

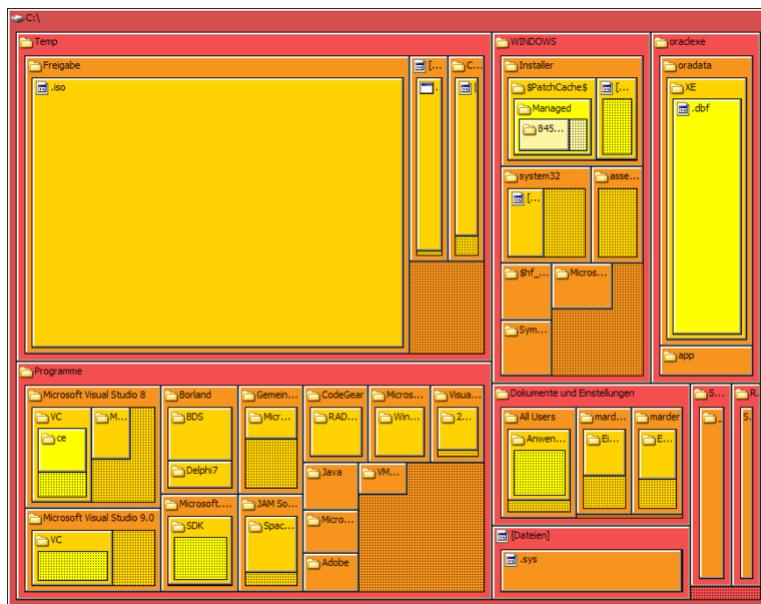
- Aspect ratios



- Tree visualization?



Changes in waiting times for patients

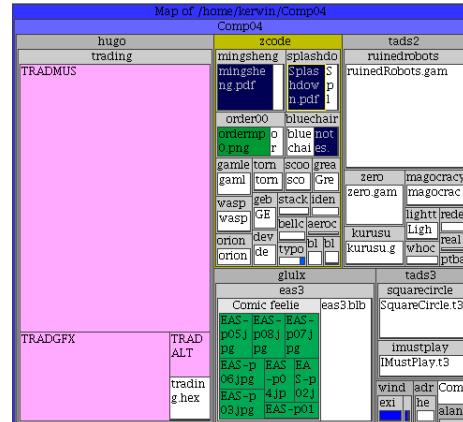


<http://en.wikipedia.org/wiki/Treemapping>

- Same dataset

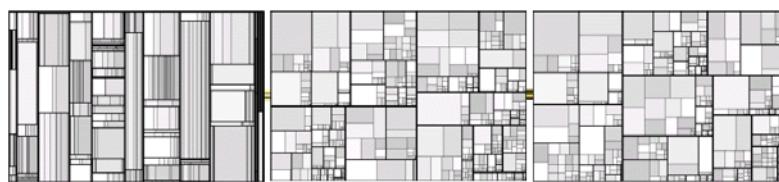


Original treemap



Squarefied treemap

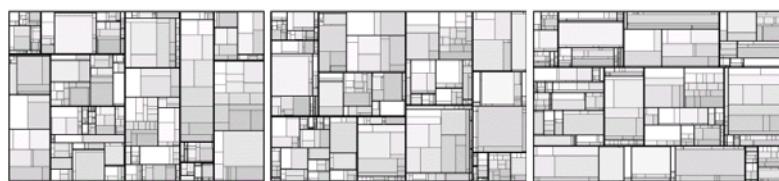
<http://www.cse.ohio-state.edu/~kerwin/treemap-survey.html>



Slice-and-dice

Cluster

Squarefied



Pivot-by-middle

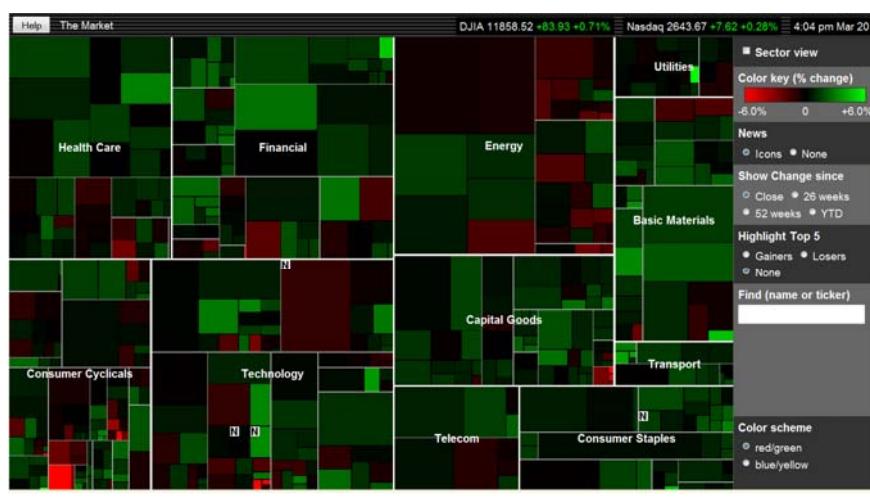
Pivot-by-size

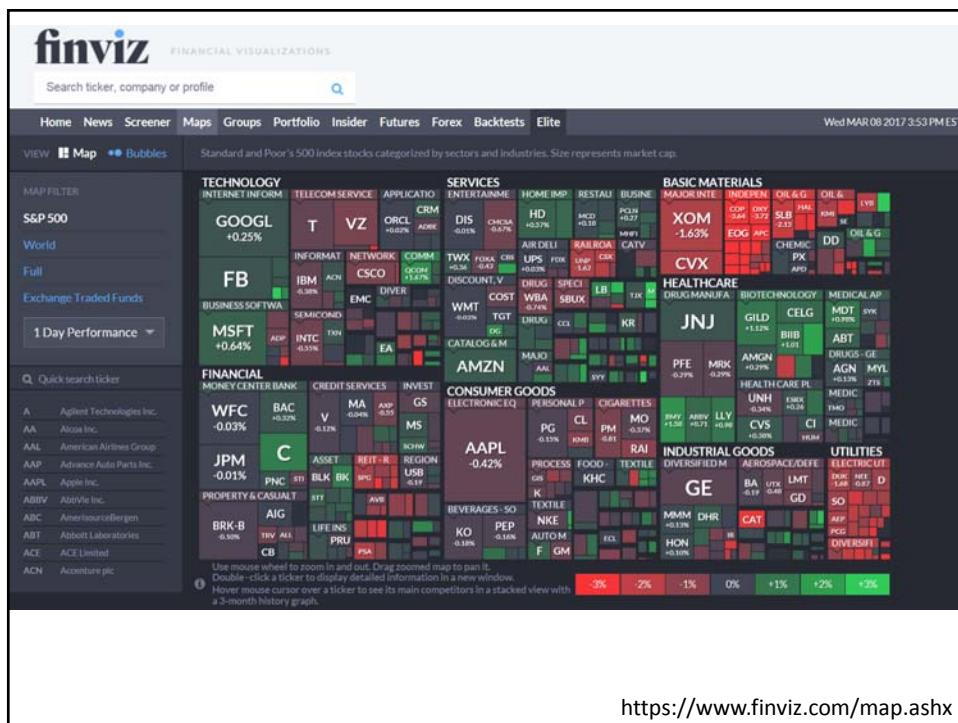
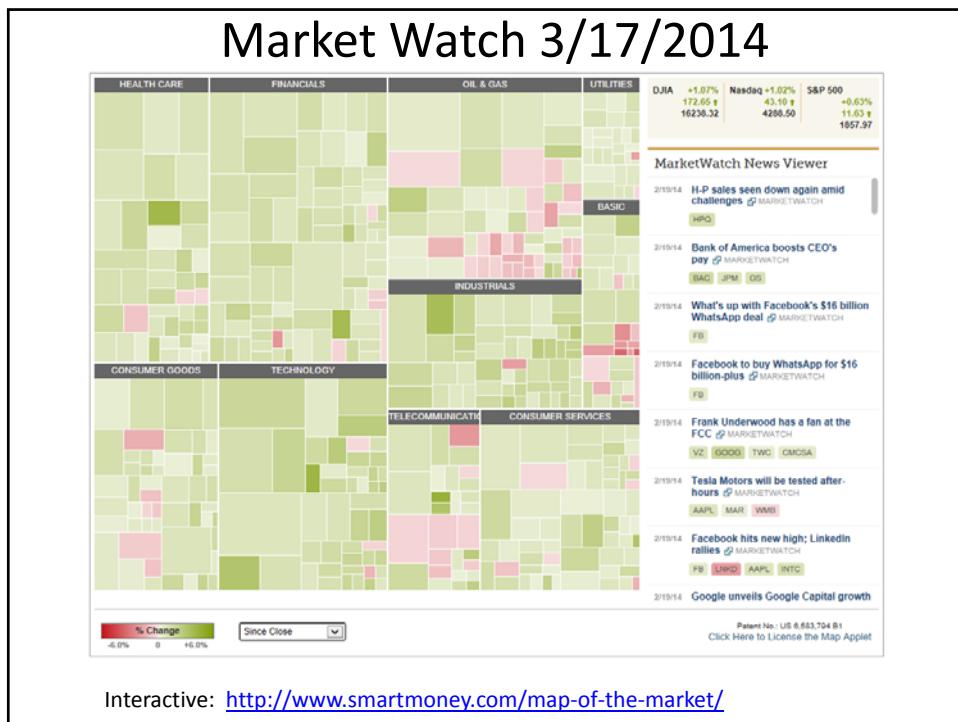
Strip

- Techniques by
  - aspect ratio
    - width to height
  - structural change
    - metric designed to measure movements of items
  - Readability
    - metric based on changes in direction of eye gaze as items scanned

[Demo: Dynamic treemap layout comparison](#)

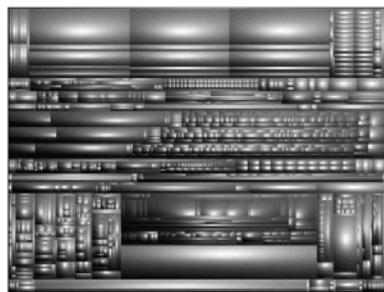
## Treemaps: SmartMoney (3/20/2011)



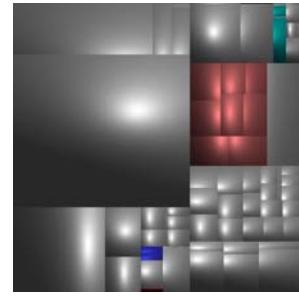


## Visual Improvements

- Cushion treemap



Add shading and texture to help convey structure of hierarchy

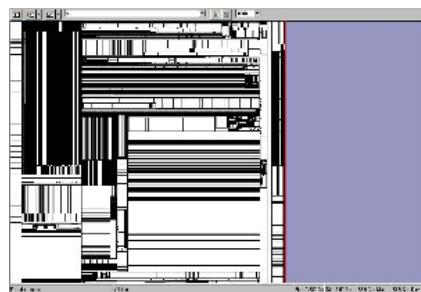


Add color

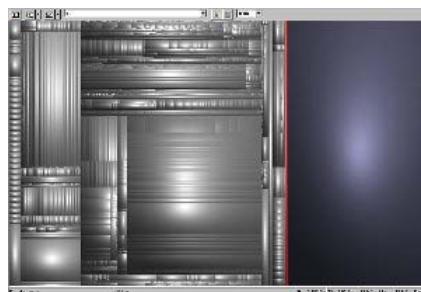
Van Wijk & van de Wetering, InfoVis 99

## TreeMap Example

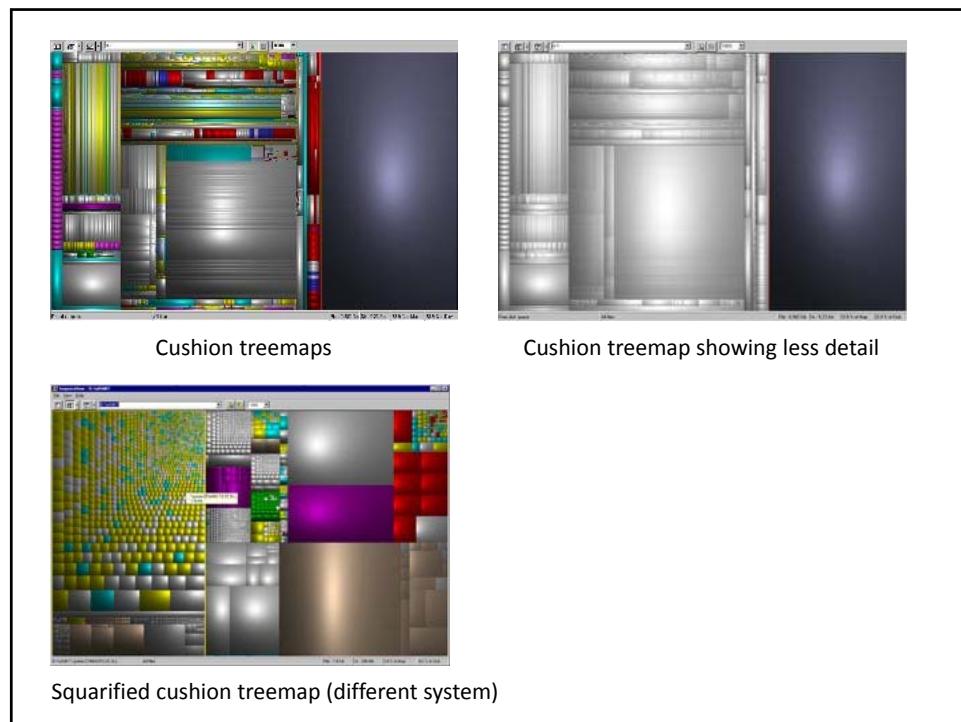
- **sequoiaView** -- disk browsing tool



The original treemap



Coloring files of different types

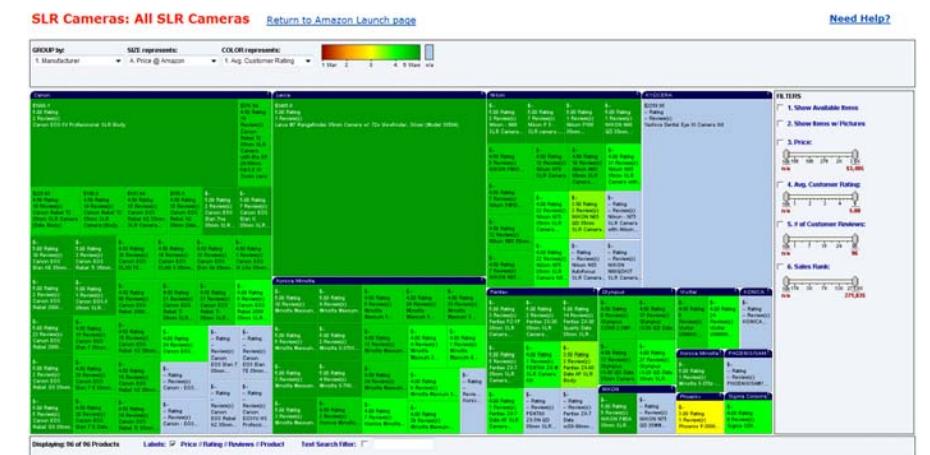


## Example: Photo management



PhotoMesa: <http://www.windsorinterfaces.com/photomesa.shtml>

# Example: Product Sale



Demo HiveGroup: <http://www.hivegroup.com/>

## Example: News

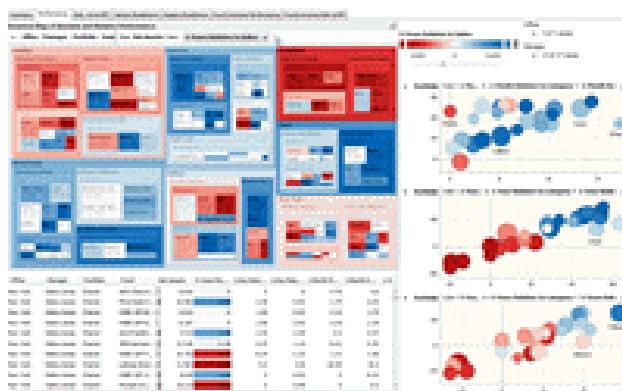
- News Map



Demo: NewsMap <http://newsmap.jp/> (Needs Flash)

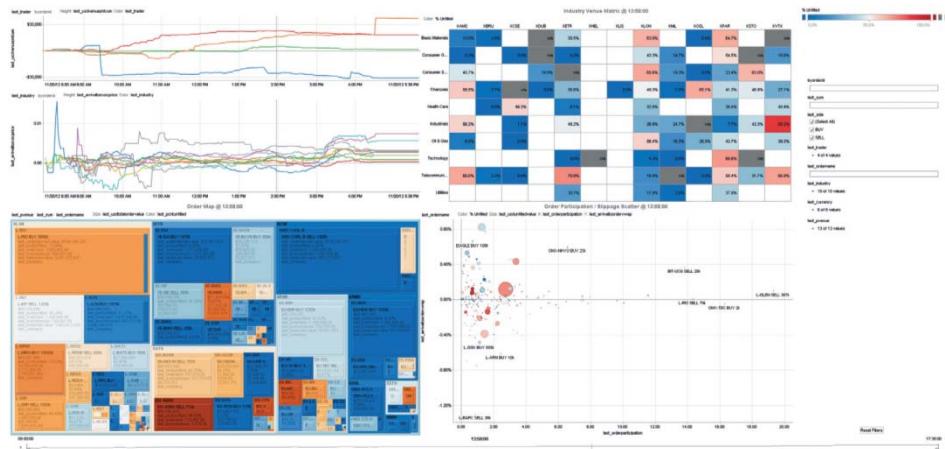
## Example: Investment

- Panopticon



<http://www.panopticon.com/>

- Panopticon



# 10 Lessons in Treemap Design

- Choose the right measures for size and color
- Space matters
  - size represents value in a treemap
  - distorts the values by arbitrarily using space, making it harder for the viewer to visually compare sizes.
- Labels should add value

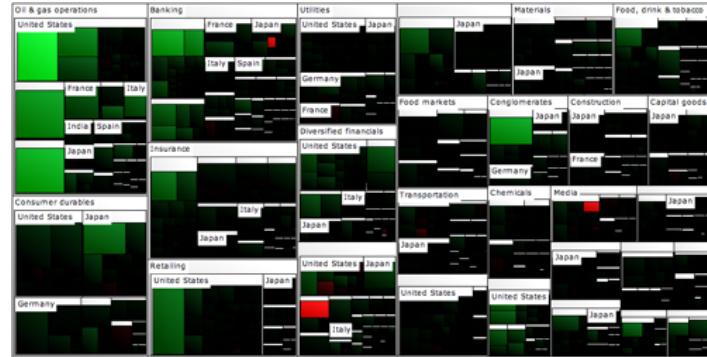
<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Bad example
  - MicroFocus TreeMap
  - majority of labels get reduced to just a few letters



<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Labels must stand-out against treemap colors



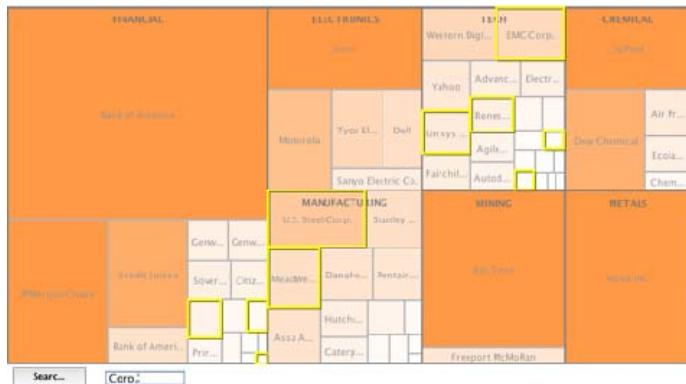
The ILOG Elixir treemap chooses to put the labels in a white text box. Unfortunately these text boxes look clunky, obscure some of the data, and don't always fit into the allotted space.

<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Explanatory legends
- Color ranges fit the data
  - Avoid to use complicated color schemes

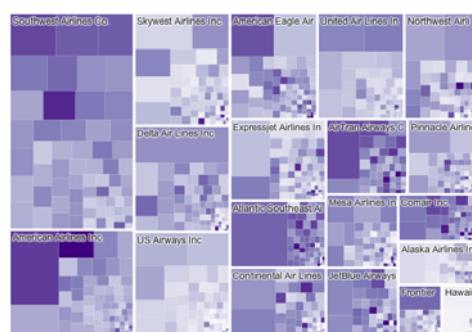
<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Show correlation by highlighting



<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Show changes with animation



Demo: <http://users.design.ucla.edu/~akoblin/work/faa/us.html>

<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

- Simple presentation of node detail



- Gradually reveal detail



Panopticon choose to show as much detail as possible, but in a faint grey text.

<http://www.juiceanalytics.com/writing/10-lessons-treemap-design/>

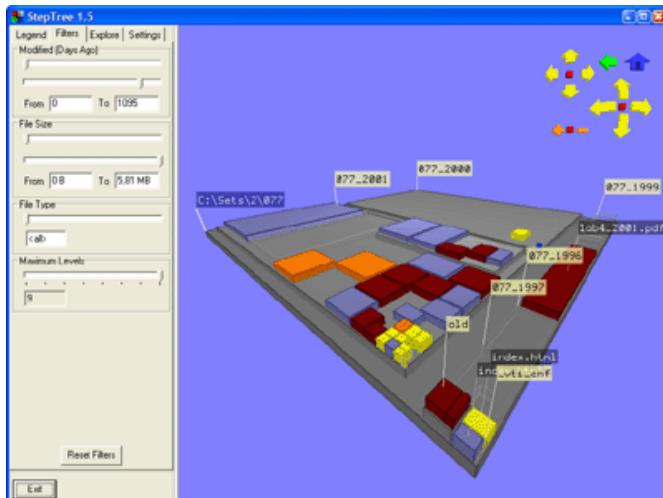
- What if nodes with zero value (mapped to area) are very important?
  - Example: Stock or mutual fund portfolios: Funds you don't currently hold have zero value in your portfolio, but you want to see them to potentially buy them

Stasko

- Context Treemap – Treemap with small distortion
  - Give zero-valued items (all together) some constant proportion of screen area
  - Provide dynamic query capabilities to enhance exploration leading to portfolio diversification

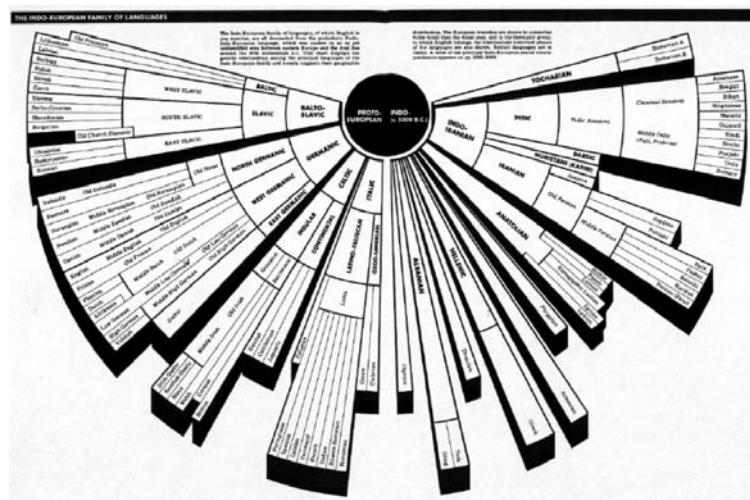
Stasko

## Treemap in 3D



<http://www.sm.luth.se/csee/csn/visualization/filesysvis.php>

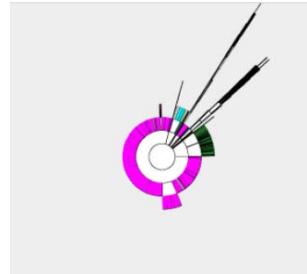
## Radio Space-Filling



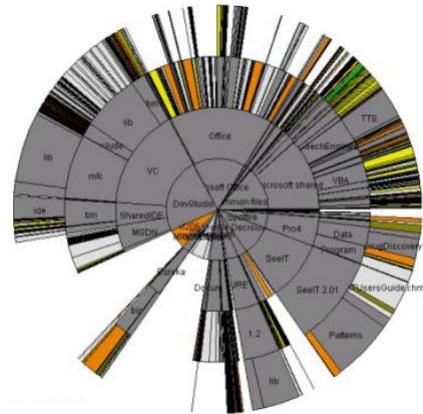
Appears in:  
*American Heritage Dictionary*, 3rd Ed. Houghton Mifflin, 1992

Stasko

- Potential Problems

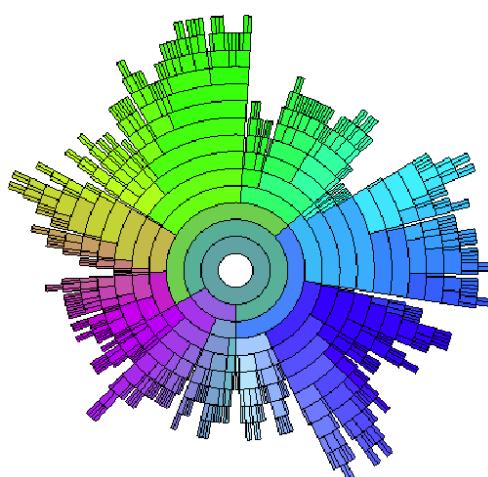


One branch with many nodes



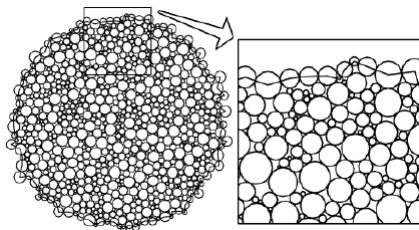
Tiny nodes at the periphery in a large tree

- InterRin

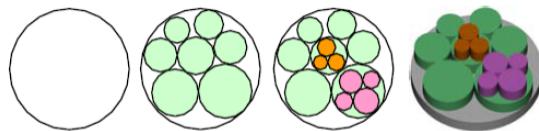


Yang, Ward & RudensteinerInfoVis „02

## Visualization of Large Hierarchical Data by Circle Packing

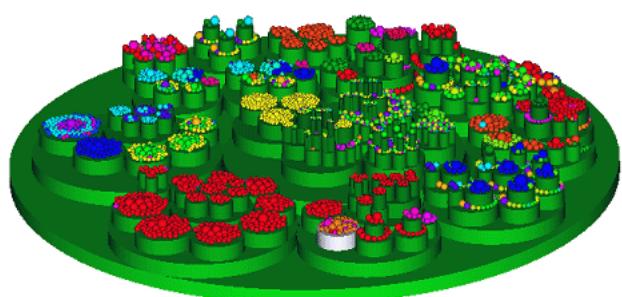
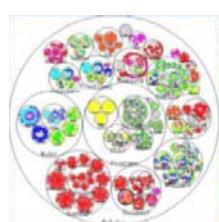


Pack circles



Pack circles in circles

Wang, Wang, Dai & Wang, CHI 06

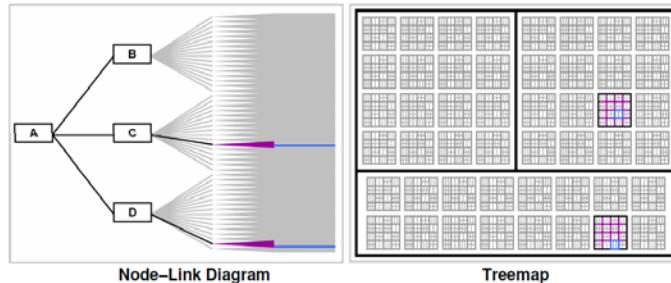


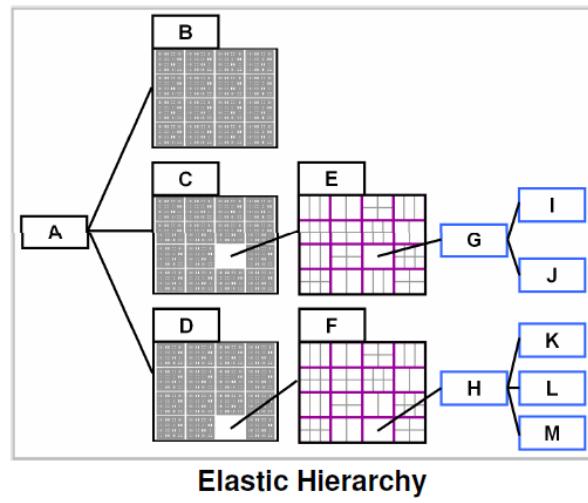
- Grokker: browsing Amazon for “Siberian Huskies”



## Hybrid

- Elastic Hierarchies: Combining Treemaps and Node-Link Diagrams





## Node-Link or Space Filling

- Depends on the properties of the data
- Node-link typically better at exposing information structure
- Space-filling good for focusing on one or two additional variables of cases

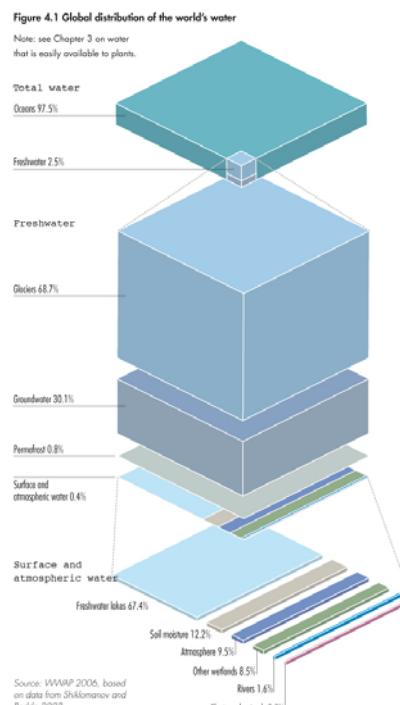
## Commercially available software

Software	Price	Windows	Mac OS X	Linux	Web service
<a href="#">DrasticData</a>	?	Yes	Yes	Yes	Yes
<a href="#">HiveOnDemand</a>	USD 425	No	No	No	Yes
<a href="#">Honeycomb</a>	?	Yes	Yes	Yes	Yes
<a href="#">Incito Mira</a>	GBP 1,199	Yes	Yes	Yes	Yes
<a href="#">Lab Escape Heat Map Explorer</a>	USD 1,295	Yes	No	No	Yes
<a href="#">Lab Escape Enterprise Tree Map SDK</a>	?	Yes	Yes	Yes	Yes
<a href="#">Macrofocus TreeMap</a>	USD 195	Yes	Yes	Yes	Yes
<a href="#">MagnaView</a>	?	Yes	No	Yes	Yes
<a href="#">Panopticon EX Enterprise Application and Developer SDK</a>	USD 900	Yes	Yes	Yes	Yes
<a href="#">UMD Treemap</a>	?	Yes	?	?	No

- Global distribution of the world's water

- Space-filling??

[http://www.wired.com/images\\_blogs/photos/uncategorized/2008/06/10/where\\_is\\_the\\_water.jpg](http://www.wired.com/images_blogs/photos/uncategorized/2008/06/10/where_is_the_water.jpg)



## Disk Space Management



Demo: SpaceSniffer and Scanner

Discussion: How to visualize the disk usage?

## Summary

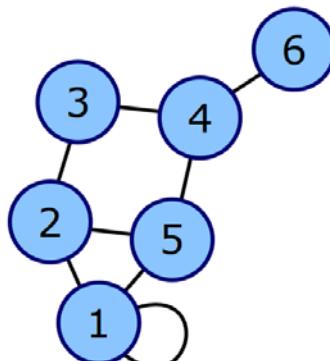
- Original space-filling
- (Tiling techniques)
- Cushion treemap
- 3D
- Radio space-filling
- Circle packing
- Hybrid. e.g. Elastic Hierarchies

## Graph Visualization

- Drawing
- Adjacency list
- Adjacency matrix

$$\begin{pmatrix} 2 & 1 & 0 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \end{pmatrix}$$

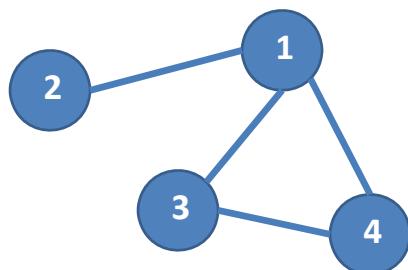
Coordinates are 1–6.



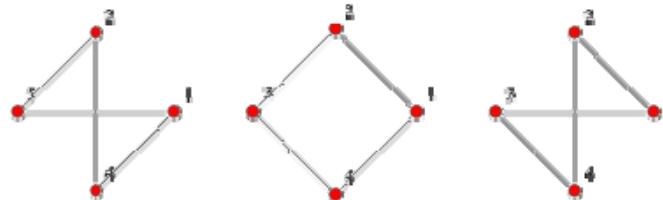
[https://en.wikipedia.org/wiki/Adjacency\\_matrix](https://en.wikipedia.org/wiki/Adjacency_matrix)

## Graph Representation

- Drawing
- Adjacency list
- Adjacency matrix

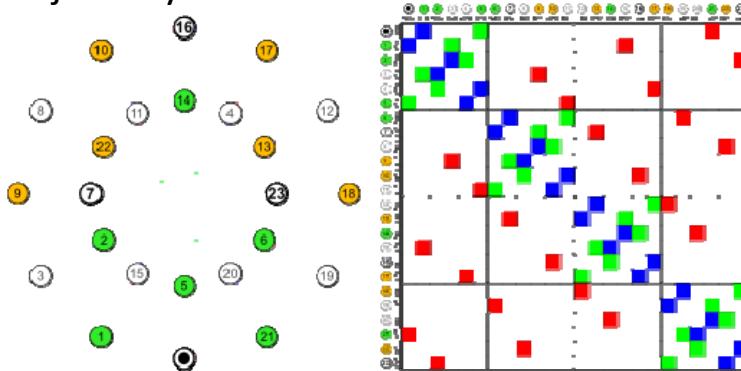


	1	2	3	4
1	0	1	1	1
2	0	0	1	0
3	1	0	0	1
4	1	0	1	0



## Graph Representation

- Drawing
- Adjacency list
- Adjacency matrix



Nauru graph

[http://en.wikipedia.org/wiki/Adjacency\\_matrix](http://en.wikipedia.org/wiki/Adjacency_matrix)

## Euler Characteristic

- The **Euler characteristic**  $\chi$  was classically defined for the surfaces of polyhedra, according to the formula

$$\chi = V - E + F$$

where  $V$ ,  $E$ , and  $F$  are respectively the numbers of vertices(corners), edges and faces in the given polyhedron.

- (Convex surface = 2)

- Graphs can have cycles
- Graph edges can be directed or undirected
- The degree of a **vertex** is the number of **edges** connected to it
- Nodes/vertices
  - *Degree of a vertex is the number of its edges*
  - In-degree and out-degree for directed graphs
- Edges/links
  - Common to associate *weights with edges*
  - Cost to travel on that edge (road networks, etc)

## Real World Examples

- In information visualization, any number of data sets can be modeled as a graph
  - WWW
  - Phone System
  - Social network

## Main Challenges

- Graph layout and positioning
  - No intrinsic position info
- Navigation/Interaction
  - Change focus
  - Navigate graph
- Scale
  - Large graph → Perceptual and technical limits

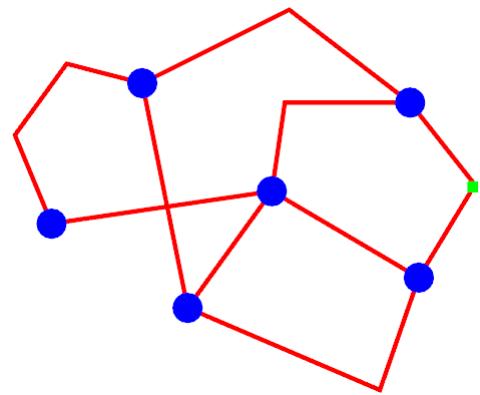
## Graph Positioning

### Constraints and Requirements

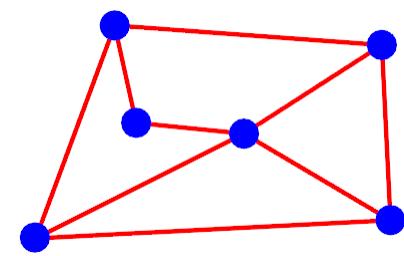
- Minimize edge crossings
- Minimize total edge length
- Minimize area of graph
- Minimize longest edge
- Make edge lengths uniform
- Minimize number of edge bends
- ... ...

Impossible to satisfy all constraints!

## Graph Drawing Conventions

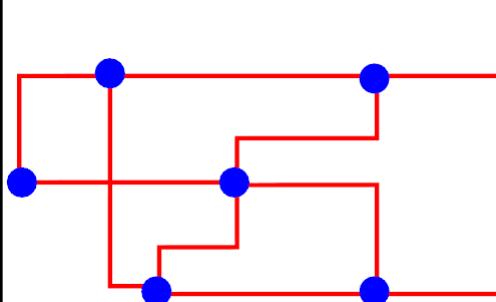


Poly-line drawing

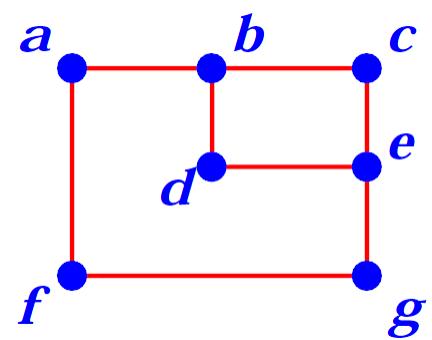


Straight-line drawing

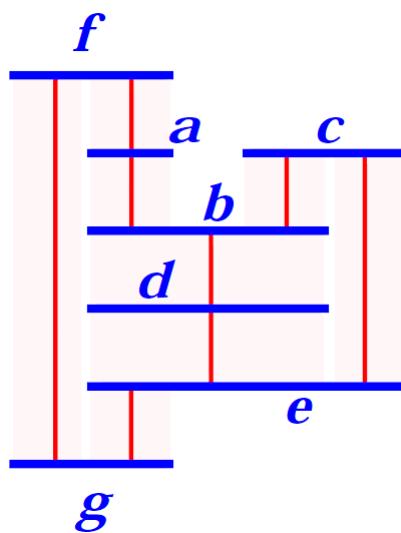
## Graph Drawing Conventions



Orthogonal drawing

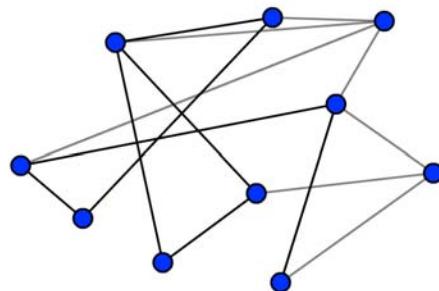


Orthogonal Straight-line drawing



strong visibility representation

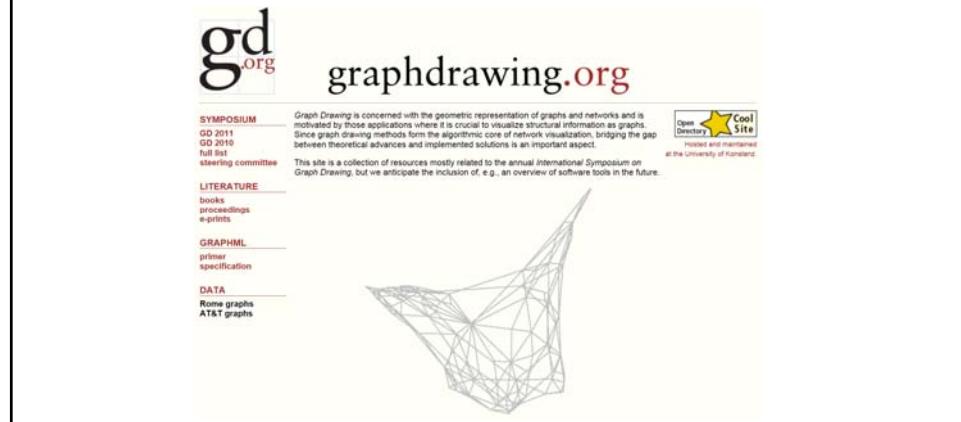
- Impossible to satisfy all constraints!



- Question: The most important constraint?

Most cases: Edge crossing

- Large research community on graph drawing
- <http://www.gd.org/>



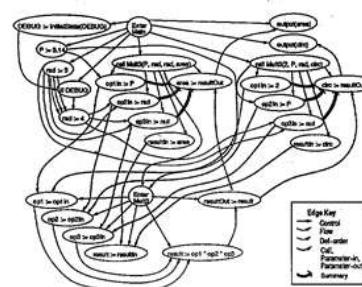
## Vertex and Edge

### Vertex

- Shape
- Color
- Size
- Location
- Label
- Spring

### Edge

- Color
- Size
- Label
- Form



Software Development  
<http://www.umcs.maine.edu/~ftp/wisr/wisr9/final-papers/Mili.gif>

## NetViz Nirvana

- Every node is visible
- Every node's degree is countable
- Every edge can be followed from source to destination
- Clusters and outliers are identifiable

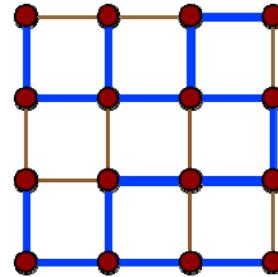
[Dunne and Shneiderman, 2009]

## Common Graph Layout Techniques

- Hierarchical
- Force-directed
- Circular
- Geographic-based
- Clustered
- Attribute-based
- Matrix

## Hierarchical Layout

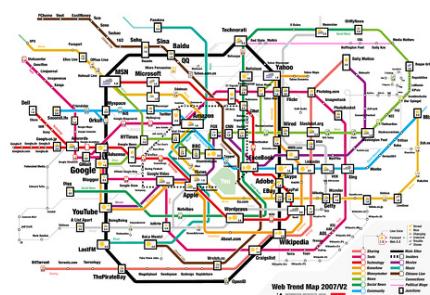
- Many graphs have a tree-like structure
- Simple layout idea
- Compute **spanning tree** of graph
- Lay out tree using tree layout algorithm
- Add edges for full graph
- High performance, not always optimal results



[http://en.wikipedia.org/wiki/Spanning\\_tree](http://en.wikipedia.org/wiki/Spanning_tree)

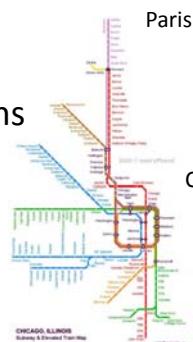


New York



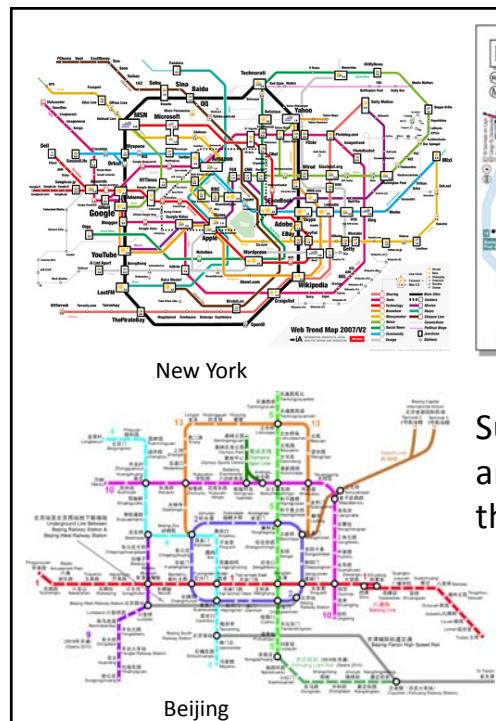
Subway Maps  
are more graphs  
than maps

Paris



Chicago

Beijing



# Motivations

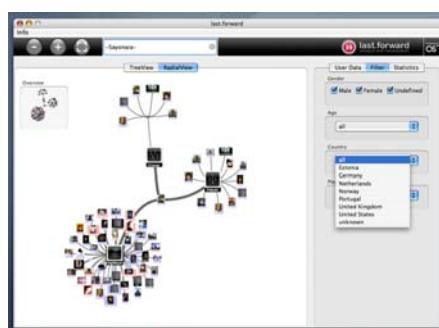
## Commercial Software

- A range of different relationship types are supported. Edges can be directed, undirected, and can show flow in both directions.
- Text and numerical attributes can be associated with nodes and edges. Tables display the attributes and allow sorting.
- Images can be associated with nodes.
- Advanced cluster computation reveals inherent groupings.
- Co-citations and co-occurrence analysis clarifies dense networks.

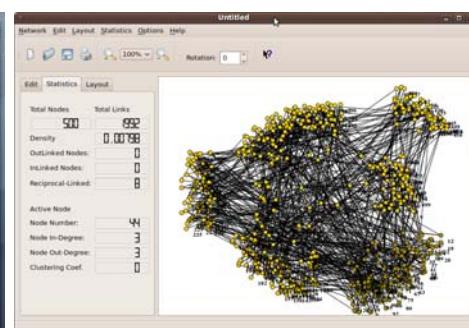


TouchGraph.com

# Social Network



Last.Forward



SocNetV

## Music Visualization

- Example:
  - The Shape of Song
  - [Live plasma](http://www.liveplasma.com/)

<http://www.liveplasma.com/>



Madonna, Like A Prayer

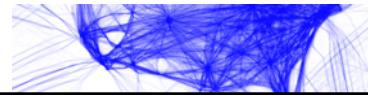


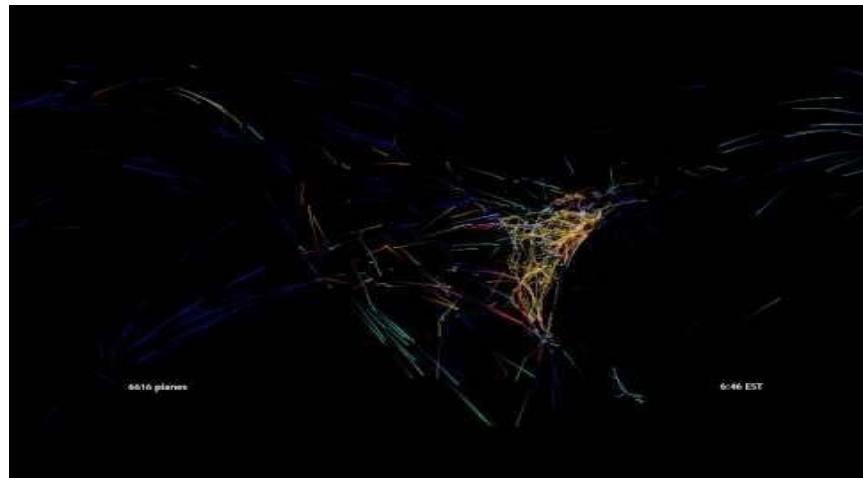
Bach, Three of the Goldberg Variations

## Fly Pattern (Aaron Koblin)



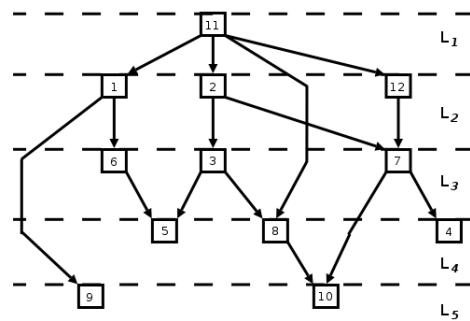
National Science Foundation 1st Pl. Science Visualization





## Hierarchical Layout

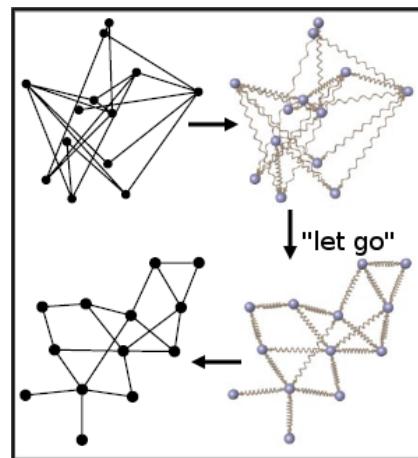
- Also called Sugiyama layout



<http://www.csse.monash.edu.au/hons/se-projects/2006/Kieran.Simpson/output/html/node7.html#sugiyamaexample>

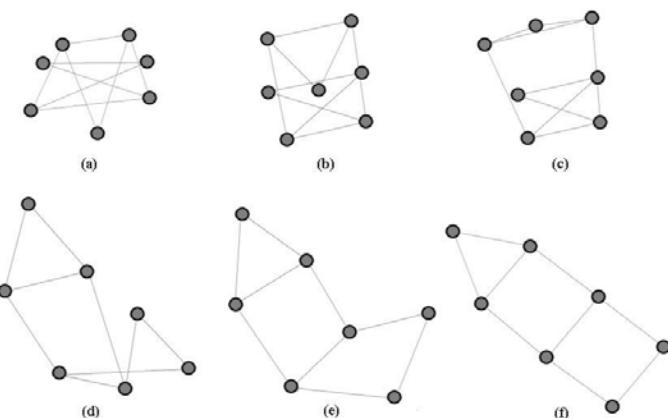
## Force-Directed Layout

- Spring model (common)
- Edges –Springs (gravity attraction)
- Vertices –Charged particles (repulsion)
- Equations for forces
- Iteratively recalculate to update positions of vertices

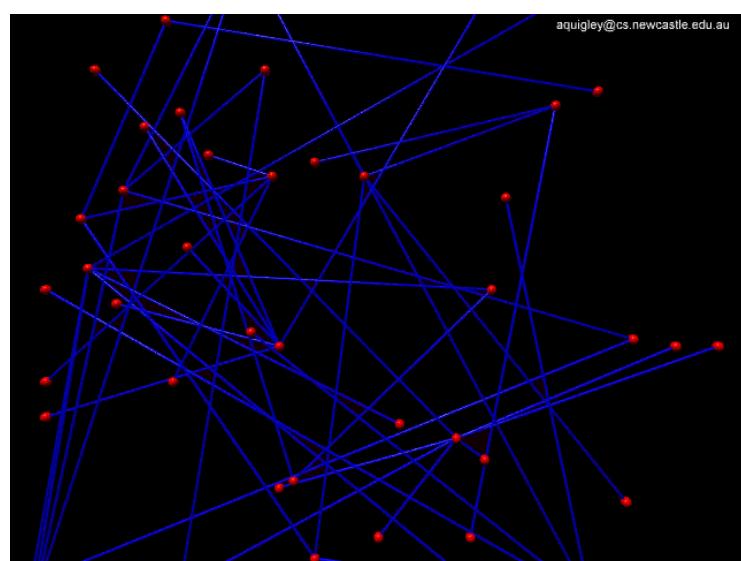


Spring model

<http://www.csse.monash.edu.au/hons/se-projects/2006/Kieran.Simpson/output/html/node8.html>

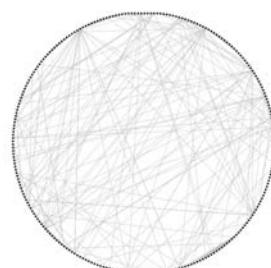
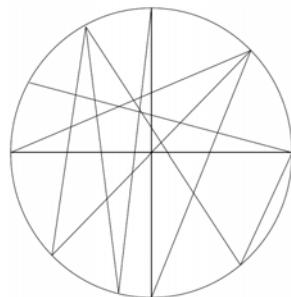


A graph drawing through a number of iterations of a force directed algorithm



## Circular Layout

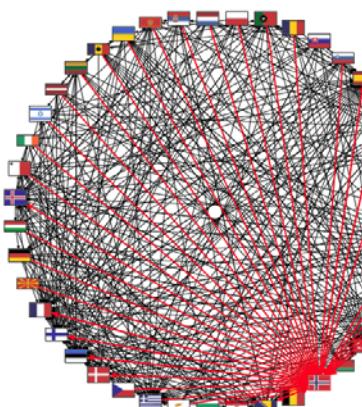
- Extremely simple



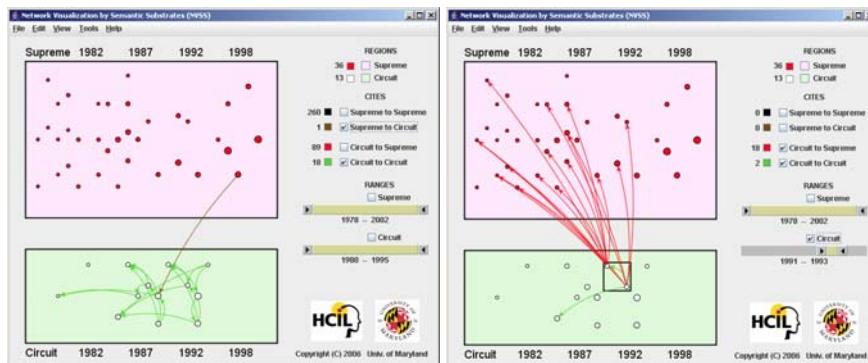
Many improvements.

## Eurovision Song Contest

- Annual competition held among active member countries of the European Broadcasting Union (EBU).
- Each member country submits a song to be performed on live television and then casts votes for the other countries' songs to determine the most popular song in the competition.
- Each country participates via one of their national EBU-member television stations, whose task it is to select a singer and a song to represent their country in the international competition.



# Network Visualization by Semantic Substrates



## Network Visualization by Semantic Substrates

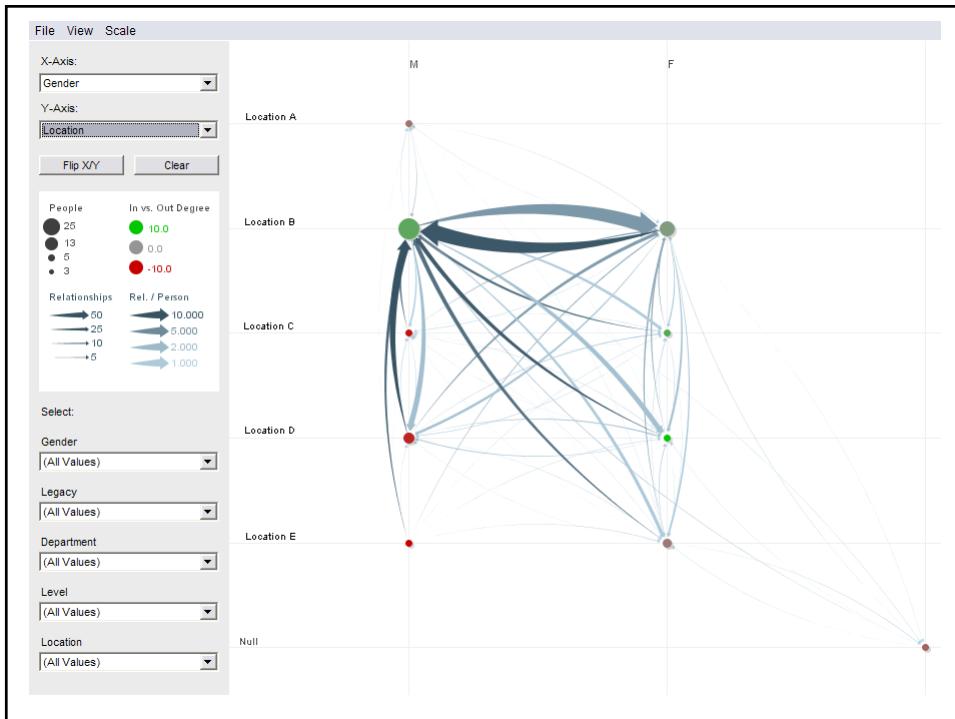
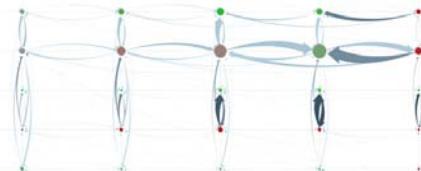
Ben Shneiderman and Aleks Aris  
University of Maryland, HCIL

Copyright 2006

<http://www.cs.umd.edu/hcil/nvss/#video>

## PivotGraph

- Cluster on common node attributes
  - Put all A's together, all B's together, ...
- Edges show how they are related
  - Draw edge from A to B depending on how many edges from some A to some B
- Position nodes into a grid based on attributes
- Node size represent number for each value



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[Dunne and Shneiderman, 2009]

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