

Assignment - 11

18K41A0505
AREEFA ①

Manual Calculation for two iterations with first two samples (NAG optimizer)

Sample	X	Y
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Step 1 $\eta = 0.1$, $m = 0$, $c = -1$, $v_m = 0$, $v_c = 0$, $\gamma = 0.9$
epochs = 2

Step 2 $i \in \mathcal{I} = 1$

Step 3 sample = 1

Step 4 $y = mx + c = 0$

$$g_m = \frac{\partial E}{\partial m} = -(y_i - (m + \gamma v_m)x_i - (c + \gamma v_c))x_i$$

$$= -(3.4 - (1 + 0.9(0))0.2 - (-1 + (0.9)0))0.2$$
$$= 0.84$$

$$g_c = \frac{\partial E}{\partial c} = -(y_i - (m + \gamma v_m)x_i - (c + \gamma v_c))$$

$$= -(3.4 - (1 + 0.9(0))0.2 - (-1 + (0.9)0))$$

$$g_c = -4.2$$

step 5 ~~dm~~

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$$V_m = \gamma V_m - \eta g_m \\ = (0.9)0 - (-0.1) \times (-0.84) = \underline{-0.084}$$

$$V_c = \gamma V_c - \eta g_c \\ = (0.9)0 - (-0.1)(-4.2) = \underline{-0.42}$$

step 6: $m = m + V_m = 1 - 0.084 = \underline{0.916}$

$$c = c + V_c = -1 - 0.42 = \underline{-1.42}$$

step 7 sample + 1 $\Rightarrow 2$

step 8: if (sample > ns)
goto step 9 (next)

else
goto step 4

step 4: $g_m = \frac{\partial E}{\partial m} = - (3.8 - (0.916 + (0.9 \times -0.084))) 0.4 \\ - (-1.42 + (0.9)(-0.42)) 0.4$

$$g_m = \underline{-1.983}$$

$$g_c = \frac{\partial E}{\partial c} = \underline{-4.959}$$

step 5 $V_m = \gamma V_m - \eta g_m$

$$= (0.9 \times -0.084) - (-0.1 \times -1.983) = \underline{-0.2739}$$

$$V_c = (0.9 \times -0.42) - (-0.1 \times -4.959) = \underline{-0.873}$$

Step 6 $m = m + V_m$

$$= 0.916 - 0.2739 = 0.6421$$

$$C = C + V_c = -1.42 - 0.8739 = -2.293$$

Step 7 sample + 1 $\Rightarrow 3$

Step 8: if (sample > ns)

$$3 > 2$$

goto next

Step 9: iter + 1 $\Rightarrow 2$

Step 10: if (iter > epochs)

$$2 > 2 \times$$

goto step 3

Step 3 sample = 1

$$\text{Step 4: } \frac{\partial E}{\partial m} = - \left((3.4 - (0.642 + (0.9 \times 0.273)) \times 0.2 - (-2.29 + (0.9 \times -0.273)) \times 0.2 \right)$$

$$\underline{g_m = -1.171}$$

$$\underline{g_c = \frac{\partial E}{\partial c} = -5.859}$$

Step 5: $V_m = \gamma V_m - \eta g_m$

$$= [0.9 \times (-0.273)] - (-0.1 \times -1.81)$$

$$\underline{V_m = -0.3627}$$

$$V_c = \cancel{\alpha} V_c \gamma - \eta g_c$$

$$= (0.9)(-0.873) - (-0.1 \times -5.859)$$

$$V_c = -1.370$$

step 6 : $m = m + V_m = 0.64 + (-0.362) = \underline{0.279}$

$$c = c + V_c = -2.293 - 1.370 = \underline{-3.66}$$

step 7 : sample = sample + 1 = 2

step 8 : if (sample > ns)

$$2 > 2 \times$$

goto step 4

step 4 $g_m = \frac{\partial E}{\partial m} = - \frac{[3.8 - (0.27 + (0.9 \times -0.362))] \times 0.4}{-3.66 + (0.9 \times (-1.37))} (0.4)$

$$g_m = \underline{-2.985}$$

$$g_c = \frac{\partial E}{\partial c} = \underline{-7.465}$$

step 5 $V_m = [0.9 \times -0.362] - [-0.1 \times -2.985] = \underline{-0.624}$

$$V_c = V_c \gamma - \eta g_c$$

$$V_c = [0.9 \times (-1.37)] - [0.1(-7.46)] = \underline{-1.980}$$

step 6 $m + V_m = 0.277 + (-0.624) = \underline{-0.327}$

$$c + V_c = -3.66 - 1.98 = \underline{-4.644}$$

step 7: $\text{sample} = \text{sample} + 1 = 3$

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step 8: if ($\text{sample} > n_s$)
goto step 9

else goto step 4

step 9 $\text{iter} + 1 = 2 + 1 = 3$

step 10 if ($\text{iter} > \text{epochs}$)
goto step 4 (next step)

else
goto step 3

step 11 print m, c

$m = 0.327$

$c = -4.64$

for 2 iterations (2 samples)