Cross Model Analysis

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Data Prep and Cleaning

```
# Load and clean data
original_tbl <- read.csv("./NBA-BoxScores-2023-2024.csv") |>
   START_POSITION = na_if(START_POSITION, "") |> factor(),
   COMMENT = na if(COMMENT, "") |> factor(),
   MIN = na_if(MIN, ""),
   MIN = str_replace(MIN, "([0-9]+)\\.[0-9]+:", "\\1:")
  )
# Filter to starters only
starting_dat <- original_tbl |>
  filter(!is.na(START_POSITION))
# Calculate team points per game
team_points <- original_tbl |>
  filter(!is.na(PTS)) |>
  group_by(GAME_ID, TEAM_ID) |>
  summarize(TeamPoints = sum(PTS), .groups = "drop")
# Join with itself to get opponent points
team_vs_opponent <- team_points |>
  inner_join(team_points, by = "GAME_ID", suffix = c("", ".opp")) |>
  filter(TEAM_ID != TEAM_ID.opp) |>
 rename(OPP_TEAM_ID = TEAM_ID.opp, OpponentPoints = TeamPoints.opp)
# Compute average opponent points allowed per team (DRTG)
team_drtg <- team_vs_opponent |>
  group_by(TEAM_ID) |>
  summarize(DRTG_proxy = mean(OpponentPoints), n_games = n(), .groups = "drop")
# Build opponent_map from distinct team-game pairs
game_team_pairs <- original_tbl |>
  select(GAME_ID, TEAM_ID) |>
  distinct()
# Create mapping of TEAM_ID and OPP_TEAM_ID for each game
opponent_map <- game_team_pairs |>
  inner_join(game_team_pairs, by = "GAME_ID") |>
 filter(TEAM_ID.x != TEAM_ID.y) |>
 rename(TEAM_ID = TEAM_ID.x, OPP_TEAM_ID = TEAM_ID.y)
```

```
# Join with defensive ratings (DRTG)
opponent_map <- opponent_map |>
  left_join(team_drtg |> rename(OPP_TEAM_ID = TEAM_ID, OPP_DRTG = DRTG_proxy), by = "OPP_TEAM_ID")
# Merge opponent info into starting dataset and center DRTG
mean_drtg <- mean(team_drtg$DRTG_proxy)</pre>
starting dat <- starting dat |>
  left_join(opponent_map, by = c("GAME_ID", "TEAM_ID")) |>
  mutate(centered_OPP_DRTG = OPP_DRTG - mean_drtg)
# For posterior predictive
# lebron 2544
# steph curry 201939
player_id = 2544
# GSW 1610612744
# LAL 1610612747
opp_team = 1610612744
player_dat = starting_dat[starting_dat$PLAYER_ID == player_id, ]
player_dat = player_dat[player_dat$OPP_TEAM_ID == opp_team, ]
n_{iter} = 100000
burnin = 10000
player_name = player_dat$PLAYER_NAME[1]
opp_team_name = starting_dat$TEAM_ABBREVIATION[starting_dat$TEAM_ID == opp_team][1]
if(length(player_dat$FGM) < 1) {</pre>
  print("ERROR, NO OBSERVATIONS")
```

Model functions

Model 1

```
log_q = function(theta, y, n) {
   if (theta < 0 || theta > 1) return(-Inf)
   sum(dbinom(y, size = n, prob = theta, log = TRUE)) + dbeta(theta, 5, 5, log = TRUE)
}

MH_beta_binom = function(current = 0.5, prop_sd = 0.05, n_vec, y_vec, n_iter = 1000) {
   samps = rep(NA, n_iter)
   for (i in 1:n_iter) {
      proposed = rnorm(1, current, prop_sd)
      logr = log_q(proposed, y = y_vec, n = n_vec) - log_q(current, y = y_vec, n = n_vec)
      if (log(runif(1)) < logr) current = proposed
      samps[i] = current
   }
   return(samps)
}</pre>
```

```
MH_beta_grid_search = function(current = 0.5, n_vec, y_vec, n_iter = 1000) {
  vals \leftarrow seq(0.005, 1, by = 0.005)
  effect_sizes <- data.frame(sd = vals, ess = NA)</pre>
  for (i in seq_along(vals)) {
    samps <- MH_beta_binom(current = current, prop_sd = vals[i],</pre>
                            n_{vec} = n_{vec}, y_{vec} = y_{vec}, n_{iter} = 5000)
    effect_sizes$ess[i] <- effectiveSize(samps)</pre>
  }
  best_sd <- effect_sizes$sd[which.max(effect_sizes$ess)]</pre>
  final_samps <- MH_beta_binom(current = current, prop_sd = best_sd,</pre>
                                 n_vec = n_vec, y_vec = y_vec, n_iter = n_iter)
  return(list(
    samples = final_samps,
    best_sd = best_sd,
    ess_table = effect_sizes
  ))
}
# Create Model
Y <- player_dat$FGM
N_vec <- player_dat$FGA
model_1 <- MH_beta_grid_search(current = 0.5,</pre>
                                   y_{vec} = Y,
                                   n_{vec} = N_{vec}
                                   n_iter = n_iter)
#Decided on using max for n
p_samples = model_1$samples
model_1_samps = rbinom(n_iter-burnin, max(N_vec), p_samples[burnin:n_iter])
```

Model 2

```
### MODEL 2 ###
log_n_con = function(p, lambda, n, y) {
  if (all(is.nan(log( ((1-p)*lambda)^sum(n) ) - sum(log((factorial(n-y)))) ))){
   return(rep(-Inf,length(y)))
 }else{
   log( ((1-p)*lambda)^sum(n) ) - sum(log((factorial(n-y))))
 }
}
mcmc_model_2 = function(data, player_id, opp_team_id, n_iter=5000,
                        init_lambda = c(), init_n = c(), gamma=0.01) {
  # Gather true data
  player_dat = data[data$PLAYER_ID == player_id, ]
  player_dat = player_dat[player_dat$OPP_TEAM_ID == opp_team_id, ]
  y = player_dat$FGM
 true_n = player_dat$FGA
  def_factor<- exp(gamma*(data$centered_OPP_DRTG[1]))</pre>
```

```
if(length(init_lambda) ==0) {
    init_lambda = mean(player_dat$FGA)
  if(length(init_n) ==0) {
    init_n = mean(player_dat$FGA)
  big_N<- length(y)</pre>
  lambda<- init_lambda</pre>
  n<- rep(init_n,big_N)</pre>
  # setting up lists/matrices for returning
  p_matrix<- matrix(NA, nrow=n_iter, ncol=big_N)</pre>
  lambda_list<- rep(lambda, n_iter)</pre>
  n_matrix<- matrix(NA, nrow=n_iter, ncol=big_N)</pre>
  y_new_list <- rep(NA, n_iter)</pre>
  n_new_list <- rep(NA, n_iter)</pre>
  for (i in 1:n_iter) {
    # sample p
    p_unscaled<- rbeta(big_N, 5 + sum(y), 5 + sum(n-y))</pre>
    p<- p_unscaled*def_factor</pre>
    # sample lambda
    lambda <- rgamma(1, shape=sum(n)-1/2, rate=big_N)
    \# sample n
    n_prop<- rnorm(big_N, n, 1) # the third 1 is a tuning parameter
    logr<- log_n_con(p, lambda, n_prop, y)-log_n_con(p, lambda, n, y)</pre>
    for (j in 1:length(logr)) {
      if (is.finite(logr[j]) && log(runif(1)) < logr[j]) {</pre>
        n[j] \leftarrow n_{prop}[j]
      }
    }
    # generate new values
    n_new = rpois(1, lambda)
    y_new <- rbinom(1, size = n_new, prob = mean(p))</pre>
    # save values
    p_matrix[i,] = p
    n_matrix[i,] = n
    lambda_list[i] = lambda
    n_new_list[i] = n_new
    y_new_list[i] = y_new
  return(data.frame(iteration=1:n_iter,
                     parameter=rep(c(paste("n[",1:big_N,"]", sep=""), "lambda", "n_new", "y_new", paste(
                     value=c(as.numeric(n_matrix),lambda_list,n_new_list,y_new_list, as.numeric(p_matrix
}
model_2 = suppressWarnings(mcmc_model_2(data = starting_dat,
```

model 3

```
### MODEL 3 ###
log_n_con = function(n, r, theta, y,p) {
        \frac{\operatorname{dummy} - \operatorname{sum}(\log((\operatorname{factorial}(n+r-1)))) - \operatorname{sum}(\log((\operatorname{factorial}(n-y)))) + \log((1-\operatorname{theta}) * ((1-p)^{\operatorname{sum}(n)})) }{\operatorname{theta}(n+r-1)} 
       if (all(is.nan(dummy))){
             return(rep(-Inf,length(n)))
      }else{
             return(dummy)
}
log_r_con = function(n, r, theta, y) {
        \frac{\text{dummy}}{\text{dummy}} + \frac{\log((\text{factorial}(n+r-1)))}{\text{dummy}} + \log((\text{factorial}(r-1)))) + \log((\text{theta}^s \text{sum}(r))) + \log(r^*((\text{length}(r-1)))) + \log((\text{theta}^s \text{sum}(r))) + \log(
       if (all(is.nan(dummy))){
             return(rep(-Inf,length(r)))
      }else{
             return(dummy)
       }
mcmc_model_3 = function(data, player_id, opp_team_id, gamma = 0.01,
                                                                                   n_iter=5000, init_r, init_theta, init_n, init_p,
                                                                                   prop_r_sd = 3.5, prop_n_sd = 3.5) {
       # Gather true data
       player_dat = data[data$PLAYER_ID == player_id, ]
       player_dat = player_dat[player_dat$OPP_TEAM_ID == opp_team_id, ]
       y = player_dat$FGM
       true_n = player_dat$FGA
       def_factor<- exp(gamma*(data$centered_OPP_DRTG[1]))</pre>
       # Start code
      big_N<- length(y)
       r<- init_r
      theta<- init_theta
      n<- rep(init_n,big_N)</pre>
      p<- init_p
       # setting up lists/matrices for returning
       r_list<- rep(NA, n_iter)
       theta_list<- rep(NA, n_iter)
       p_matrix<- matrix(NA, nrow=n_iter, ncol=big_N)</pre>
       n_matrix<- matrix(NA, nrow=n_iter, ncol=big_N)
       for (i in 1:n_iter) {
              # sample p
             p_unscaled<- rbeta(big_N, 5 + sum(y), 5 + sum(true_n-y))</pre>
```

```
p<- p_unscaled*def_factor</pre>
    # sample theta
    theta<- rbeta(1, sum(n)+1/2, r-1)
    \# sample r
    r_prop<- rnorm(1, r, prop_r_sd) # the third 1 is a tuning parameter
    logr<- log_r_con(n, r_prop, theta, y)-log_r_con(n, r, theta, y)</pre>
    if (is.finite(logr)) {
      if (log(runif(1))<logr) {</pre>
        r<- r_prop
    }
    # sample n
    n_prop<- rnorm(big_N, n, prop_n_sd) # the third 1 is a tuning parameter
    logr<- log_n_con(n_prop, r, theta, y,p)-log_n_con(n, r, theta, y,p)</pre>
    for (j in 1:length(logr)) {
      if (is.finite(logr[j])) {
        if (log(runif(1)) < logr[j]) {</pre>
          n[j]<- n_prop[j]</pre>
      }
    }
    # save values
    r_list[i] = r
    theta_list[i] = theta
    p_matrix[i,] = p
    n_{matrix[i,]} = n
  # return(data.frame(iteration=1:n_iter,
                       r = r_list,
  #
  #
                       theta = theta_list,
  #
                       p1 = p_matrix[,1],
                       p2 = p_{matrix[,2]}
                       p3 = p_{matrix[,3]}
  #
                       n1 = n_matrix[,1],
                       n2 = n_matrix[,2],
                       n3 = n_matrix[,3]))
  return(data.frame(iteration=1:n_iter,
                     parameter=rep(c("r","theta",paste("p[",1:big_N,"]", sep=""),paste("n[",1:big_N,"]",
                     value=c(r_list,theta_list,as.numeric(p_matrix),as.numeric(n_matrix))))
}
init_r<- max(player_dat$FGA) # maybe tune?</pre>
init_theta<- mean(player_dat$FG_PCT) # maybe tune ?</pre>
init_p<- mean(player_dat$FG_PCT) # maybe tune ?</pre>
init_n<- round(mean(player_dat$FGA)) #maybe tune ?</pre>
model_3 = suppressWarnings(mcmc_model_3(starting_dat, player_id = player_id, opp_team_id = opp_team, game
```

Creating our cool chart

```
df = data.frame(fixed = model_1_samps,
                poisson = model_2_samps,
                negbinom = model 3 samps,
                average = round(apply(data.frame(model_1_samps, model_2_samps, model_3_samps),1, mean))
                trueish = rbinom(n iter-burnin,round(mean(player dat$FGA)),mean(player dat$FG PCT)))
df_long <- df |>
 pivot_longer(
   cols = everything(),
   names_to = "group",
   values_to = "value"
title = paste("Model comparison for", player_name, " against ", opp_team_name)
  ggplot(aes(x = value, fill = group)) +
  geom_bar(position = "dodge") +
  labs(
   title = title,
   x = "Value",
   y = "Count",
   fill = "Group"
 theme_minimal()
```

