BDA - Project brms library test

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Contents

```
Load packages
```

##

age

Min. :18.00 female:662

```
library(aaltobda)
library(LaplacesDemon)
library(cmdstanr)
library(posterior)
library(loo)
library(tidyr)
library(dplyr)
options(pillar.neg=FALSE)
library(ggplot2)
library(gridExtra)
library(bayesplot)
library(ggdist)
theme_set(bayesplot::theme_default(base_family = "sans"))
library(rprojroot)
SEED <- 614273
Load data
data <- read.csv('Machine-Learning-with-R-datasets/insurance.csv')</pre>
head(data)
##
     age
            sex
                   bmi children smoker
                                          region
                                                    charges
## 1
     19 female 27.900
                       0
                                   yes southwest 16884.924
           male 33.770
                                   no southeast 1725.552
     18
                              1
## 3
     28
           male 33.000
                                    no southeast 4449.462
                              3
                                 no northwest 21984.471
## 4
     33
           male 22.705
                              0
                              0 no northwest 3866.855
## 5 32
           male 28.880
## 6 31 female 25.740
                                    no southeast 3756.622
Check for null values
colSums(is.na(data))
##
        age
                 sex
                          bmi children
                                         smoker
                                                  region charges
##
          0
                   0
                            0
                                     0
                                              0
Some typecasting
data$region <- as.factor(data$region)</pre>
data$sex <- as.factor(data$sex)</pre>
data$smoker <- as.factor(data$smoker)</pre>
data$children <- as.integer(data$children)</pre>
head(data)
##
     age
            sex
                   bmi children smoker
                                          region
                                                    charges
                                   yes southwest 16884.924
## 1 19 female 27.900
                             0
## 2 18
           male 33.770
                                  no southeast 1725.552
## 3
     28
           male 33.000
                             3
                                    no southeast 4449.462
## 4
     33
           male 22.705
                              0
                                    no northwest 21984.471
## 5
     32
           male 28.880
                              0 no northwest 3866.855
## 6 31 female 25.740
                                    no southeast 3756.622
Summary statistics of the data
summary(data)
```

children

Min. :0.000

smoker

no:1064

bmi

Min. :15.96

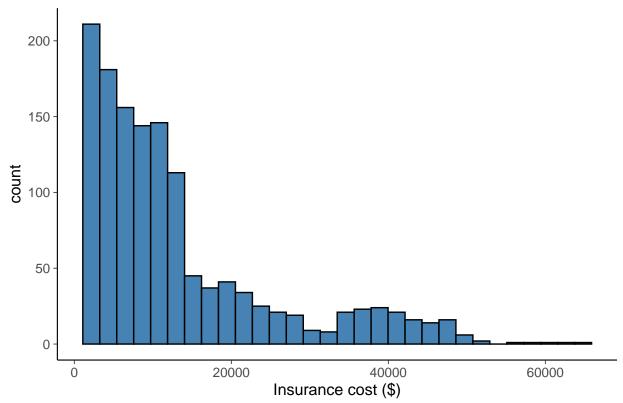
```
##
    1st Qu.:27.00
                    male :676
                                  1st Qu.:26.30
                                                   1st Qu.:0.000
                                                                    yes: 274
##
    Median :39.00
                                  Median :30.40
                                                   Median :1.000
##
    Mean
           :39.21
                                  Mean
                                          :30.66
                                                   Mean
                                                          :1.095
                                  3rd Qu.:34.69
    3rd Qu.:51.00
                                                   3rd Qu.:2.000
##
           :64.00
##
                                          :53.13
                                                   Max.
                                                           :5.000
##
          region
                        charges
##
    northeast:324
                            : 1122
                     1st Qu.: 4740
##
    northwest:325
    southeast:364
##
                     Median: 9382
    southwest:325
##
                     Mean
                            :13270
##
                     3rd Qu.:16640
##
                     Max.
                            :63770
```

Plot histogram of the insurance costs

```
ggplot() +
  geom_histogram(aes(data$charges), fill = 'steelblue', color = 'black') +
  labs(title = 'Medical costs billed by health insurance', x='Insurance cost ($)')
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.

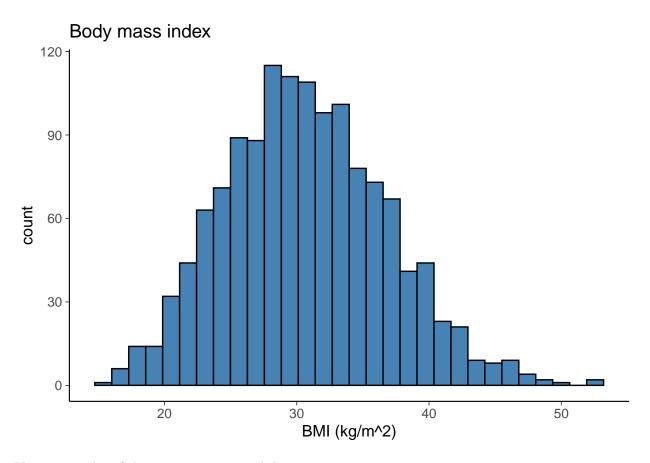
Medical costs billed by health insurance



Plot histogram of the BMI values

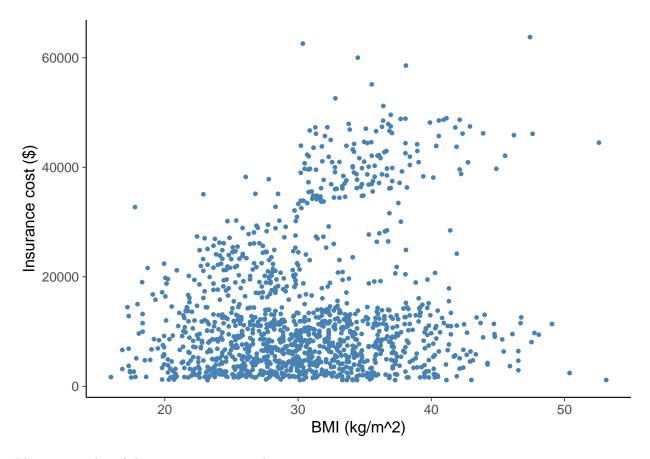
```
ggplot() +
  geom_histogram(aes(data$bmi), fill = 'steelblue', color = 'black') +
  labs(title = 'Body mass index', x='BMI (kg/m^2)')
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



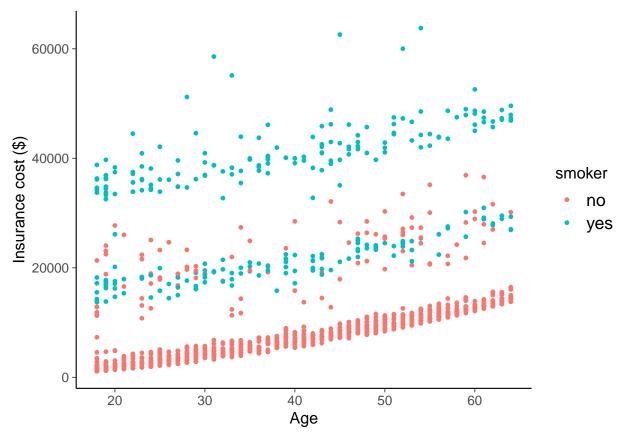
Plot scatter plot of the insurance costs with bmi as x-axis.

```
ggplot(data) +
geom_point(aes(x=bmi, y=charges), size = 1, color = 'steelblue') +
labs(y = 'Insurance cost ($)', x= 'BMI (kg/m^2)') +
guides(linetype = "none")
```



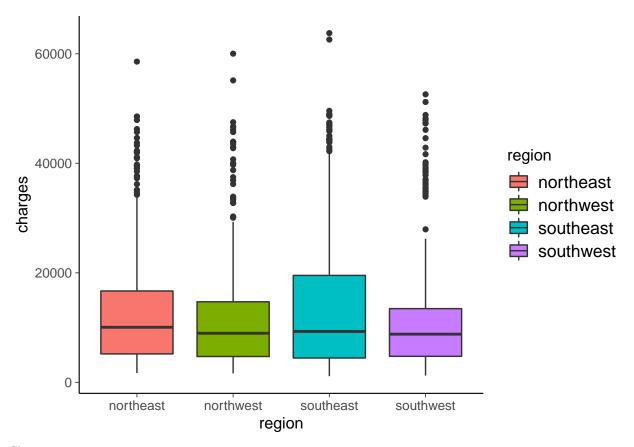
Plot scatter plot of the insurance costs with age as x-axis.

```
ggplot(data,aes(x=age,y=charges,col=smoker)) +
  geom_point(size = 1,) +
  labs(y = 'Insurance cost ($)', x= 'Age') +
  guides(linetype = "none")
```



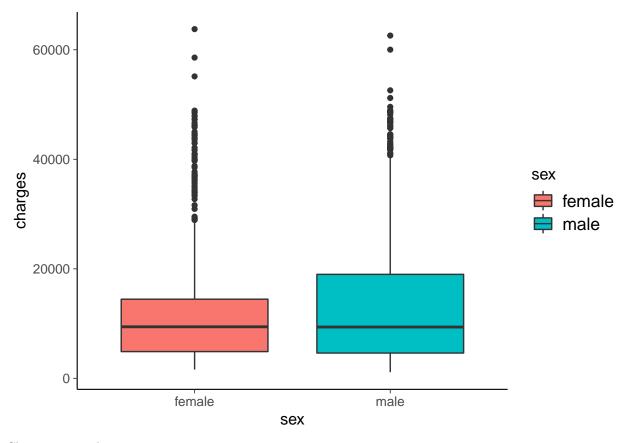
Charges vs region

ggplot(data, aes(x=region, y=charges, fill=region)) +
 geom_boxplot()



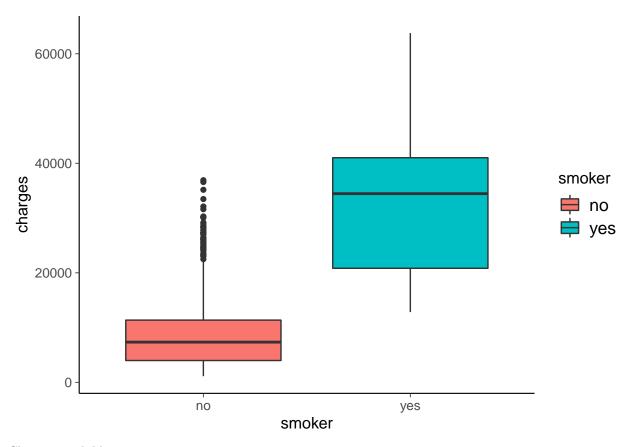
```
Charges vs sex \,
```

```
ggplot(data, aes(x=sex, y=charges, fill=sex)) +
  geom_boxplot()
```



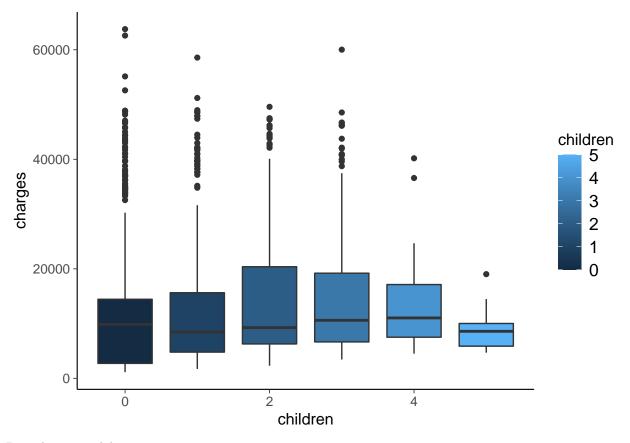
Charges vs smoker

```
ggplot(data, aes(x=smoker, y=charges, fill=smoker)) +
   geom_boxplot()
```



Charges vs children

```
ggplot(data, aes(x=children, y=charges, fill=children, group=children)) +
   geom_boxplot()
```



Basic linear model

basic_model = lm(charges~age+sex+bmi+children+smoker+region, data = data) #Create the linear regression
summary(basic_model) #Review the results

```
##
## Call:
## lm(formula = charges ~ age + sex + bmi + children + smoker +
      region, data = data)
##
##
## Residuals:
       Min
                 1Q
                      Median
                                   ЗQ
## -11304.9 -2848.1
                       -982.1
                               1393.9
                                       29992.8
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  -11938.5
                                987.8 -12.086 < 2e-16 ***
## age
                     256.9
                                 11.9 21.587 < 2e-16 ***
## sexmale
                    -131.3
                                332.9 -0.394 0.693348
## bmi
                     339.2
                                 28.6 11.860 < 2e-16 ***
                                137.8
## children
                     475.5
                                       3.451 0.000577 ***
## smokeryes
                   23848.5
                                413.1 57.723 < 2e-16 ***
                                476.3 -0.741 0.458769
## regionnorthwest
                    -353.0
                                478.7 -2.162 0.030782 *
## regionsoutheast -1035.0
## regionsouthwest
                    -960.0
                                477.9 -2.009 0.044765 *
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 6062 on 1329 degrees of freedom
## Multiple R-squared: 0.7509, Adjusted R-squared: 0.7494
## F-statistic: 500.8 on 8 and 1329 DF, p-value: < 2.2e-16
Bauesian mode with brms
library(brms)
## Loading required package: Rcpp
## Loading 'brms' package (version 2.17.0). Useful instructions
## can be found by typing help('brms'). A more detailed introduction
## to the package is available through vignette('brms_overview').
## Attaching package: 'brms'
## The following objects are masked from 'package:ggdist':
##
       dstudent_t, pstudent_t, qstudent_t, rstudent_t
##
## The following object is masked from 'package:posterior':
##
##
       rhat
## The following objects are masked from 'package:LaplacesDemon':
##
       ddirichlet, rdirichlet, WAIC
##
## The following object is masked from 'package:stats':
##
       ar
pr = prior(normal(0, 10), class = 'b')
bayesian_mixed = brm(
 charges ~ age + sex + bmi + children + (1|region) + (1|smoker),
 data = data,
 prior = pr,
  cores = 4
)
## Compiling Stan program...
## Trying to compile a simple C file
## Running /usr/lib/R/bin/R CMD SHLIB foo.c
## clang -flto=thin -I"/usr/share/R/include" -DNDEBUG -I"/usr/local/lib/R/site-library/Rcpp/include/"
## In file included from <built-in>:1:
## In file included from /usr/local/lib/R/site-library/StanHeaders/include/stan/math/prim/mat/fun/Eigen
## In file included from /usr/local/lib/R/site-library/RcppEigen/include/Eigen/Dense:1:
## In file included from /usr/local/lib/R/site-library/RcppEigen/include/Eigen/Core:88:
## /usr/local/lib/R/site-library/RcppEigen/include/Eigen/src/Core/util/Macros.h:628:1: error: unknown t
## namespace Eigen {
## ^
## /usr/local/lib/R/site-library/RcppEigen/include/Eigen/src/Core/util/Macros.h:628:16: error: expected
## namespace Eigen {
##
##
```

```
## In file included from <built-in>:1:
## In file included from /usr/local/lib/R/site-library/StanHeaders/include/stan/math/prim/mat/fun/Eigen
## In file included from /usr/local/lib/R/site-library/RcppEigen/include/Eigen/Dense:1:
## /usr/local/lib/R/site-library/RcppEigen/include/Eigen/Core:96:10: fatal error: 'complex' file not fo
## #include <complex>
            ^~~~~~~
##
## 3 errors generated.
## make: *** [/usr/lib/R/etc/Makeconf:168: foo.o] Error 1
## Start sampling
## Warning: There were 93 divergent transitions after warmup. See
## https://mc-stan.org/misc/warnings.html#divergent-transitions-after-warmup
## to find out why this is a problem and how to eliminate them.
## Warning: Examine the pairs() plot to diagnose sampling problems
Model summary
summary(bayesian_mixed, waic=TRUE)
## Warning: There were 93 divergent transitions after warmup. Increasing
## adapt_delta above 0.8 may help. See http://mc-stan.org/misc/
## warnings.html#divergent-transitions-after-warmup
##
   Family: gaussian
    Links: mu = identity; sigma = identity
## Formula: charges ~ age + sex + bmi + children + (1 | region) + (1 | smoker)
     Data: data (Number of observations: 1338)
##
     Draws: 4 chains, each with iter = 2000; warmup = 1000; thin = 1;
##
            total post-warmup draws = 4000
##
##
## Group-Level Effects:
## ~region (Number of levels: 4)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
                             576.38
                                       10.03 1926.71 1.00
## sd(Intercept)
                   450.43
                                                                1315
                                                                         1788
##
## ~smoker (Number of levels: 2)
                 Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept) 13676.06
                            5425.23 6341.03 27984.04 1.00
                                                                1671
                                                                         1634
##
## Population-Level Effects:
##
             Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept 9721.70
                        6897.98 -3713.91 23691.93 1.00
                                                            1714
                                                                     2009
                                                                     2972
## age
                99.42
                           8.43
                                   82.28
                                           115.54 1.00
                                                            4133
                 0.09
                           9.97
                                  -20.49
## sexmale
                                            19.62 1.00
                                                            3746
                                                                     2918
                35.09
                           9.49
                                   16.69
                                            53.45 1.00
                                                            3896
                                                                     2536
## bmi
## children
                 2.14
                           9.97
                                  -17.96
                                            22.29 1.00
                                                            3731
                                                                     2547
##
## Family Specific Parameters:
         Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma 6794.02
                     138.12 6522.47 7071.38 1.00
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
make_stancode(charges ~ age + sex + bmi + children + (1|region) + (1|smoker), data=data, family = "gaus
## // generated with brms 2.17.0
## functions {
## }
## data {
     int<lower=1> N; \ // total number of observations
##
     vector[N] Y; // response variable
##
##
     int<lower=1> K; // number of population-level effects
     matrix[N, K] X; // population-level design matrix
##
##
     // data for group-level effects of ID 1
##
     int<lower=1> N_1; // number of grouping levels
     int<lower=1> M_1; // number of coefficients per level
##
     int<lower=1> J_1[N]; // grouping indicator per observation
##
##
     // group-level predictor values
##
    vector[N] Z_1_1;
##
     // data for group-level effects of ID 2
     int<lower=1> N_2; // number of grouping levels
##
##
     int<lower=1> M_2; // number of coefficients per level
##
     int<lower=1> J_2[N]; // grouping indicator per observation
##
     // group-level predictor values
##
     vector[N] Z_2_1;
##
     int prior_only; // should the likelihood be ignored?
## }
## transformed data {
##
    int Kc = K - 1;
##
    matrix[N, Kc] Xc; // centered version of X without an intercept
    vector[Kc] means_X; // column means of X before centering
##
##
     for (i in 2:K) {
##
      means_X[i - 1] = mean(X[, i]);
##
       Xc[, i - 1] = X[, i] - means_X[i - 1];
##
     }
## }
## parameters {
     vector[Kc] b; // population-level effects
     real Intercept; // temporary intercept for centered predictors
##
     real<lower=0> sigma; // dispersion parameter
##
##
     vector<lower=0>[M_1] sd_1; // group-level standard deviations
     vector[N_1] z_1[M_1]; // standardized group-level effects
##
     vector<lower=0>[M_2] sd_2; // group-level standard deviations
##
     vector[N_2] z_2[M_2]; // standardized group-level effects
##
## }
## transformed parameters {
    vector[N_1] r_1_1; // actual group-level effects
##
    vector[N_2] r_2_1; // actual group-level effects
##
##
    real lprior = 0; // prior contributions to the log posterior
     r_1_1 = (sd_1[1] * (z_1[1]));
##
##
    r_2_1 = (sd_2[1] * (z_2[1]));
##
    lprior += student_t_lpdf(Intercept | 3, 9382, 7440.8);
##
     lprior += student_t_lpdf(sigma | 3, 0, 7440.8)
##
      - 1 * student_t_lccdf(0 | 3, 0, 7440.8);
##
     lprior += student_t_lpdf(sd_1 | 3, 0, 7440.8)
##
      - 1 * student_t_lccdf(0 | 3, 0, 7440.8);
    lprior += student_t_lpdf(sd_2 | 3, 0, 7440.8)
```

```
- 1 * student_t_lccdf(0 | 3, 0, 7440.8);
##
## }
## model {
     // likelihood including constants
##
     if (!prior_only) {
##
##
       // initialize linear predictor term
##
       vector[N] mu = Intercept + rep_vector(0.0, N);
##
       for (n in 1:N) {
##
         // add more terms to the linear predictor
##
         mu[n] += r_1_1[J_1[n]] * Z_1_1[n] + r_2_1[J_2[n]] * Z_2_1[n];
##
##
       target += normal_id_glm_lpdf(Y | Xc, mu, b, sigma);
##
##
     // priors including constants
##
     target += lprior;
     target += std_normal_lpdf(z_1[1]);
##
##
     target += std_normal_lpdf(z_2[1]);
## }
## generated quantities {
     // actual population-level intercept
##
     real b_Intercept = Intercept - dot_product(means_X, b);
## }
```

Conditional effects

conditional_effects(bayesian_mixed)

