Multivariate Analysis for the Behavioral Sciences, Second Edition (Chapman and Hall/CRC, 2019)

Solutions to Exercises of Chapter 5: Generalized Linear Models

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Exercises

Exercise 5.1

```
2 < 3cm 1
## 3
          3 < 3 \text{cm} 1
          6 < 3cm 1
          8 < 3cm 1
## 6
         9 < 3 cm 1
        10 < 3 cm 1
## 8
        11 < 3cm 1
## 9
        13 < 3cm 1
        14 < 3cm 1
## 10
## 11
        16 < 3cm 1
## 12
        21 < 3cm 1
## 13
        22 < 3 \text{cm} 1
## 14
        24 < 3 \text{cm} 1
        26 < 3cm 1
## 15
        27 < 3cm 1
## 16
## 17
         7 < 3 \text{cm} 2
         13 < 3cm 2
## 18
         15 < 3cm 2
## 19
## 20
         18 < 3cm 2
## 21
        23 < 3cm 2
## 22
        20 < 3cm 3
## 23
        24 < 3 \text{cm } 4
## 24
         1 > 3 cm 1
## 25
         5 > 3 cm 1
## 26
         17 > 3cm 1
## 27
        18 > 3 cm 1
## 28
        25 > 3 cm 1
        18 > 3 cm 2
## 29
```

```
## 30   25 > 3cm 2
## 31   4 > 3cm 3
## 32   19 > 3cm 4
# (solution still in process - check that it corresponds to the comments below!)
```

The estimated model is

$$\log \lambda = -2.339 + 0.229x$$

So for smaller tumors (x=0), the estimated (baseline) rate is $\exp(-2.339) = 0.096$ and for larger tumors (x=1), the estimated rate is $\exp(-2.339 + 0.229) = 0.12$. The rate for larger tumors is estimated as 0.12 / 0.096 = 1.25 times the rate for smaller tumors. In terms of waiting times between recurrences the means are 1 / 0.096 = 10.42 months for smaller tumors and 1 / 0.12 = 8.33 months for larger tumors. But the regression coefficient for the dummy variable coding tumor size is seen to be non-significant so the data give no evidence that rates or waiting times for large and small tumors are different. This becomes apparent if we construct a confidence interval for the rate for larger tumors from the confidence limits given in the output as $[\exp(-2.339 - 0.371), \exp(-2.339 + 0.829)]$, i.e., [0.067, 0.221]. This interval contains the rate for smaller tumors. There is no evidence that size of primary tumor is associated with number of recurrent tumors.

Exercise 5.2