Multivariate Analysis for the Behavioral Sciences, Second Edition (Chapman and Hall/CRC, 2019)

Exercises of Chapter 4: Multiple Linear Regression

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Exercises

Exercise 4.1

Use the usapol data (see below) and modify the R code given in the **Examples of Chapter 4** to create suitable graphics and to analyse the data as instructed. Use the procedure involving the AIC described in the text to search for a more parsimonious model for the data. For the final model chosen, use some regression diagnostics to investigate the assumptions made in fitting the model.

```
usapol <- structure(list(</pre>
S02 = c(10, 13, 12, 17, 56, 36, 29, 14, 10, 24, 110, 28, 17, 8, 30, 9, 47,
        35, 29, 14, 56, 14, 11, 46, 11, 23, 65, 26, 69, 61, 94, 10, 18, 9,
        10, 28, 31, 26, 29, 31, 16),
Temp = c(70.3, 61, 56.7, 51.9, 49.1, 54, 57.3, 68.4, 75.5, 61.5, 50.6, 52.3,
         49, 56.6, 55.6, 68.3, 55, 49.9, 43.5, 54.5, 55.9, 51.5, 56.8, 47.6,
         47.1, 54, 49.7, 51.5, 54.6, 50.4, 50, 61.6, 59.4, 66.2, 68.9, 51,
         59.3, 57.8, 51.1, 55.2, 45.7),
Manuf = c(213, 91, 453, 454, 412, 80, 434, 136, 207, 368, 3344, 361, 104, 125,
          291, 204, 625, 1064, 699, 381, 775, 181, 46, 44, 391, 462, 1007, 266,
          1692, 347, 343, 337, 275, 641, 721, 137, 96, 197, 379, 35, 569),
Pop = c(582, 132, 716, 515, 158, 80, 757, 529, 335, 497, 3369, 746, 201, 277,
        593, 361, 905, 1513, 744, 507, 622, 347, 244, 116, 463, 453, 751, 540,
        1950, 520, 179, 624, 448, 844, 1233, 176, 308, 299, 531, 71, 717),
Wind = c(6, 8.2, 8.7, 9, 9, 9, 9.3, 8.8, 9, 9.1, 10.4, 9.7, 11.2, 12.7, 8.3,
         8.4, 9.6, 10.1, 10.6, 10, 9.5, 10.9, 8.9, 8.8, 12.4, 7.1, 10.9, 8.6,
         9.6, 9.4, 10.6, 9.2, 7.9, 10.9, 10.8, 8.7, 10.6, 7.6, 9.4, 6.5, 11.8),
Precip = c(7.05, 48.52, 20.66, 12.95, 43.37, 40.25, 38.89, 54.47, 59.8, 48.34,
           34.44, 38.74, 30.85, 30.58, 43.11, 56.77, 41.31, 30.96, 25.94, 37,
           35.89, 30.18, 7.77, 33.36, 36.11, 39.04, 34.99, 37.01, 39.93, 36.22,
           42.75, 49.1, 46, 35.94, 48.19, 15.17, 44.68, 42.59, 38.79, 40.75, 29.07),
Days = c(36, 100, 67, 86, 127, 114, 111, 116, 128, 115, 122, 121, 103, 82, 123,
         113, 111, 129, 137, 99, 105, 98, 58, 135, 166, 132, 155, 134, 115, 147,
         125, 105, 119, 78, 103, 89, 116, 115, 164, 148, 123)),
```

```
.Names = c("SO2", "Temp", "Manuf", "Pop", "Wind", "Precip", "Days"),
row.names = c("Phoenix", "Little Rock", "San Francisco", "Denver", "Hartford",
             "Wilmington", "Washington", "Jacksonville", "Miami", "Atlanta",
             "Chicago", "Indianapolis", "Des Moines", "Wichita", "Louisville",
             "New Orleans", "Baltimore", "Detroit", "Minneapolis-St. Paul",
             "Kansas City", "St. Louis", "Omaha", "Alburquerque", "Albany",
             "Buffalo", "Cincinnati", "Cleveland", "Columbus", "Philadelphia",
             "Pittsburgh", "Providence", "Memphis", "Nashville", "Dallas",
             "Houston", "Salt Lake City", "Norfolk", "Richmond", "Seattle",
             "Charleston", "Milwaukee"), class = "data.frame")
head(usapol, n = 10)
##
                SO2 Temp Manuf Pop Wind Precip Days
## Phoenix
                10 70.3
                         213 582 6.0
                                        7.05
## Little Rock 13 61.0
                          91 132 8.2 48.52 100
## San Francisco 12 56.7 453 716 8.7 20.66
                                              67
## Denver 17 51.9 454 515 9.0 12.95
                                              86
## Hartford
              56 49.1 412 158 9.0 43.37 127
## Wilmington 36 54.0
                         80 80 9.0 40.25 114
## Washington
               29 57.3 434 757 9.3 38.89 111
## Jacksonville 14 68.4 136 529 8.8 54.47 116
## Miami
                10 75.5 207 335 9.0 59.80 128
## Atlanta
                24 61.5
                          368 497 9.1 48.34 115
tail(usapol, n = 10)
                SO2 Temp Manuf Pop Wind Precip Days
##
## Memphis
                10 61.6
                           337 624 9.2 49.10 105
## Nashville
                18 59.4
                           275 448 7.9 46.00 119
## Dallas
                 9 66.2 641 844 10.9 35.94
## Houston
                10 68.9 721 1233 10.8 48.19 103
## Salt Lake City 28 51.0 137 176 8.7 15.17
## Norfolk
                 31 59.3
                           96 308 10.6 44.68 116
## Richmond
                26 57.8 197 299 7.6 42.59 115
                29 51.1 379 531 9.4 38.79 164
## Seattle
              31 55.2 35 71 6.5 40.75 148
16 45.7 569 717 11.8 29.07 123
## Charleston
## Milwaukee
```

Use the quality data (see below) and modify the R code given in the **Examples of Chapter 4** to create suitable graphics and to analyse the data. Pay careful attention to how the categorical explanatory variables with more than two categories are coded.

```
quality <- structure(list(
1L, 2L, 2L, 1L), .Label = c("A5-6", "A8-9"), class = "factor"),
sex = structure(c(1L,2L, 1L, 2L, 1L, 2L, 2L, 2L, 1L, 2L, 1L, 1L, 2L, 1L, 2L, 1L, 2L, 2L, 2L,
                 2L, 1L, 1L, 1L, 1L), .Label = c("Male", "Female"), class = "factor"),
location = structure(c(3L, 2L, 1L, 2L, 3L, 3L, 4L, 2L, 3L, 2L, 3L, 1L, 3L, 2L, 4L,
                      2L, 3L, 4L, 2L, 4L, 4L, 4L),
                    .Label = c("Home", "School", "Room", "Kroom"), class = "factor"),
coherence = c(3.81, 1.63, 3.54, 4.21, 3.3, 2.32, 4.51, 3.18, 3.02, 2.77, 3.35, 2.66,
             4.7, 4.31, 2.16, 1.89, 1.94, 2.86, 3.11, 2.9, 2.41, 2.32, 2.78),
maturity = c(3.62, 1.61, 3.63, 4.11, 3.12, 2.13, 4.31, 3.08, 3, 2.71, 3.07, 2.72,
            4.98, 4.21, 2.91, 1.87, 1.99, 2.93, 3.01, 2.87, 2.38, 2.33, 2.79),
delay = c(45, 27, 102, 39, 41, 70, 72, 41, 71, 56, 88, 13, 29, 39, 10, 15, 46, 57,
         26, 14, 45, 19, 9),
prosecute = structure(c(1L, 2L, 1L, 1L, 1L, 2L, 1L, 1L, 1L, 2L, 2L, 1L, 1L, 2L, 1L, 2L,
                       2L, 1L, 2L, 1L, 1L, 2L, 2L),
                     .Label = c("No", "Yes"), class = "factor"),
qualityct = c(34.11, 36.59, 37.23, 39.65, 42.07, 44.91, 45.23, 47.53, 54.64, 57.87,
             57.07, 45.81, 49.38, 49.53, 67.08, 83.15, 80.67, 78.47, 77.59, 76.28,
             59.64, 68.44, 65.07)),
             .Names = c("age", "sex", "location", "coherence", "maturity", "delay",
                        "prosecute", "qualityct"),
row.names = c(NA, -23L), class = "data.frame")
str(quality)
                   23 obs. of 8 variables:
## 'data.frame':
             : Factor w/ 2 levels "A5-6", "A8-9": 1 1 1 1 1 1 1 2 2 ...
              : Factor w/ 2 levels "Male", "Female": 1 2 1 2 1 2 2 2 1 2 ...
   $ location : Factor w/ 4 levels "Home", "School", ...: 3 2 1 2 3 3 4 2 3 2 ...
## $ coherence: num 3.81 1.63 3.54 4.21 3.3 2.32 4.51 3.18 3.02 2.77 ...
  $ maturity : num 3.62 1.61 3.63 4.11 3.12 2.13 4.31 3.08 3 2.71 ...
            : num 45 27 102 39 41 70 72 41 71 56 ...
   $ prosecute: Factor w/ 2 levels "No", "Yes": 1 2 1 1 1 2 1 1 1 2 ...
## $ qualityct: num 34.1 36.6 37.2 39.6 42.1 ...
```

quality

##		age	sex	${\tt location}$	${\tt coherence}$	${\tt maturity}$	delay	prosecute	qualityct
##	1	A5-6	Male	Room	3.81	3.62	45	No	34.11
##	2	A5-6	${\tt Female}$	School	1.63	1.61	27	Yes	36.59
##	3	A5-6	Male	Home	3.54	3.63	102	No	37.23
##	4	A5-6	${\tt Female}$	School	4.21	4.11	39	No	39.65
##	5	A5-6	Male	Room	3.30	3.12	41	No	42.07
##	6	A5-6	${\tt Female}$	Room	2.32	2.13	70	Yes	44.91
##	7	A5-6	${\tt Female}$	Kroom	4.51	4.31	72	No	45.23
##	8	A5-6	${\tt Female}$	School	3.18	3.08	41	No	47.53
##	9	A8-9	Male	Room	3.02	3.00	71	No	54.64
##	10	A8-9	${\tt Female}$	School	2.77	2.71	56	Yes	57.87
##	11	A8-9	Male	Room	3.35	3.07	88	Yes	57.07
##	12	A5-6	Male	Home	2.66	2.72	13	No	45.81
##	13	A5-6	${\tt Female}$	Room	4.70	4.98	29	No	49.38
##	14	A5-6	Male	School	4.31	4.21	39	Yes	49.53
##	15	A8-9	${\tt Female}$	School	2.16	2.91	10	No	67.08
##	16	A8-9	Male	Kroom	1.89	1.87	15	Yes	83.15
##	17	A8-9	${\tt Female}$	School	1.94	1.99	46	Yes	80.67
##	18	A8-9	${\tt Female}$	Room	2.86	2.93	57	No	78.47
##	19	A5-6	${\tt Female}$	Kroom	3.11	3.01	26	Yes	77.59
##	20	A8-9	Male	School	2.90	2.87	14	No	76.28
##	21	A8-9	Male	Kroom	2.41	2.38	45	No	59.64
##	22	A8-9	Male	Kroom	2.32	2.33	19	Yes	68.44
##	23	A5-6	Male	Kroom	2.78	2.79	9	Yes	65.07

Use the quartet data (see below) and modify the R code given in the Examples of Chapter 4.

For more information, see the Wikipedia article:

https://en.wikipedia.org/wiki/Anscombe%27s_quartet

```
quartet <- structure(list(
    x1 = c(10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5),
    y1 = c(8.04, 6.95, 7.58, 8.81, 8.33, 9.96, 7.24, 4.26, 10.84, 4.82, 5.68),

    x2 = c(10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5),
    y2 = c(9.14, 8.14, 8.74, 8.77, 9.26, 8.1, 6.13, 3.1, 9.13, 7.26, 4.74),

    x3 = c(10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5),
    y3 = c(7.46, 6.77, 12.74, 7.11, 7.81, 8.84, 6.08, 5.39, 8.15, 6.42, 5.73),

    x4 = c(8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 8, 19),
    y4 = c(6.58, 5.76, 7.71, 8.84, 8.47, 7.04, 5.25, 5.56, 7.91, 6.89, 12.5)),

.Names = c("x1", "y1", "x2", "y2", "x3", "y3", "x4", "y4"),
    row.names = c(NA, -11L), class = "data.frame"
)</pre>
```

```
##
     x1
          y1 x2
                 y2 x3
                         y3 x4
                                  y4
     10 8.04 10 9.14 10 7.46 8
                                6.58
## 2
     8 6.95 8 8.14 8 6.77 8
                                5.76
        7.58 13 8.74 13 12.74
## 3 13
                             8
                                7.71
     9 8.81 9 8.77 9 7.11
                             8
                                8.84
## 5 11 8.33 11 9.26 11 7.81
                             8
                                8.47
## 6 14
        9.96 14 8.10 14
                        8.84
                             8
                                7.04
      6 7.24 6 6.13 6
                        6.08
## 7
                             8
                                5.25
## 8
     4 4.26 4 3.10 4 5.39 8 5.56
## 9 12 10.84 12 9.13 12 8.15 8 7.91
## 10 7 4.82 7 7.26 7 6.42 8 6.89
## 11 5 5.68 5 4.74 5 5.73 19 12.50
```

Use the fat data (see below) and modify the R code given in the Examples of Chapter 4.

```
##
      Sex Age Pcfat
## 1
        F
           23
                9.5
               27.9
## 2
           23
        M
## 3
        F
           27
               7.8
        F
## 4
           27
               17.8
## 5
        Μ
           39
               31.4
## 6
           41
               25.9
        М
## 7
        F
           45
               27.4
## 8
           49
        Μ
               25.2
## 9
        M
           50
               31.1
## 10
        M
           53
               34.7
## 11
        M
           53
              42.0
        F
               20.0
## 12
           54
## 13
        M 54
               29.1
               32.5
## 14
        M 56
## 15
        M 57
               30.3
               21.0
## 16
        F 57
              33.0
## 17
        M 58
## 18
        M
           58
               33.8
## 19
        M 60 41.1
## 20
        M 61 34.5
```

Use the blood data (see below) and modify the R code given in the Examples of Chapter 4.

```
blood <- structure(list(</pre>
 2L, 2L, 2L, 2L, 2L, 2L),
                    .Label = c("Present", "Absent"), class = "factor"),
 Smoking = structure(c(1L, 1L, 1L, 1L, 1L, 1L, 1L, 2L, 2L, 2L, 2L, 2L, 3L, 3L, 3L, 3L,
                      3L, 3L, 3L, 3L, 1L, 1L, 1L, 1L, 1L, 1L, 1L, 1L, 2L, 2L, 2L, 2L,
                      3L, 3L, 3L, 3L, 3L, 3L),
                    .Label = c("NonS", "ExS", "CS"), class = "factor"),
 Bloodp = c(125, 156, 103, 129, 110, 128, 135, 114, 107, 134, 140, 120, 115, 135, 120,
           123, 113, 165, 145, 120, 114, 110, 91, 136, 105, 125, 103, 110, 110, 128,
           105, 90, 140, 125, 123, 108, 113, 160)),
.Names = c("History", "Smoking", "Bloodp"), row.names = c(NA, -38L), class = "data.frame")
str(blood)
## 'data.frame':
                  38 obs. of 3 variables:
## $ History: Factor w/ 2 levels "Present", "Absent": 1 1 1 1 1 1 1 1 1 1 ...
## $ Smoking: Factor w/ 3 levels "NonS", "ExS", "CS": 1 1 1 1 1 1 2 2 2 ...
## $ Bloodp : num 125 156 103 129 110 128 135 114 107 134 ...
head(blood)
##
    History Smoking Bloodp
## 1 Present
              NonS
                      125
## 2 Present
              NonS
                      156
## 3 Present
              NonS
                      103
## 4 Present
              NonS
                      129
## 5 Present
              NonS
                      110
## 6 Present
              NonS
                      128
tail(blood)
##
     History Smoking Bloodp
## 33 Absent
                 CS
                      140
## 34 Absent
                 CS
                      125
## 35
     Absent
                 CS
                      123
                 CS
## 36
      Absent
                      108
## 37
      Absent
                 CS
                      113
## 38
     Absent
                 CS
                      160
```

Use the oestrogen data (see below) and modify the R code given in the Examples of Chapter 4.

```
oestrogen <- structure(list(</pre>
 2L, 2L, 2L, 2L, 2L, 2L, 2L, 2L, 2L),
           .Label = c("Placebo", "Active"), class = "factor"),
 BL1 = c(18, 25, 24, 19, 22, 27, 21, 26, 20, 24, 24, 27, 19, 25,
         19, 21, 21, 25, 25, 15, 27),
 BL2 = c(18, 27, 17, 15, 20, 28, 16, 26, 19, 20, 22, 27, 15, 28,
         18, 20, 21, 24, 25, 22, 26),
 Depression = c(15, 10, 12, 5, 5, 9, 11, 13, 6, 18, 10, 7, 8, 2,
               6, 11, 5, 11, 6, 6, 10)),
.Names = c("Treatment", "BL1", "BL2", "Depression"),
row.names = c(NA, -21L), class = "data.frame")
str(oestrogen)
## 'data.frame':
                  21 obs. of 4 variables:
## $ Treatment : Factor w/ 2 levels "Placebo", "Active": 1 1 1 1 1 1 1 1 1 1 ...
## $ BL1
              : num 18 25 24 19 22 27 21 26 20 24 ...
              : num 18 27 17 15 20 28 16 26 19 20 ...
## $ BL2
## $ Depression: num 15 10 12 5 5 9 11 13 6 18 ...
oestrogen
##
     Treatment BL1 BL2 Depression
## 1
       Placebo 18
                  18
```

```
## 2
       Placebo 25
                     27
                                10
## 3
       Placebo 24
                    17
                                12
## 4
       Placebo
                                 5
                19
                     15
## 5
       Placebo
                 22
                     20
                                 5
## 6
                                 9
       Placebo
                 27
                     28
## 7
       Placebo
                 21
                    16
                                11
## 8
       Placebo
                     26
                 26
                                13
## 9
       Placebo
                 20
                     19
                                 6
## 10
       Placebo 24
                    20
                                18
## 11
       Placebo 24
                     22
                                10
## 12
                                 7
         Active 27
                     27
## 13
                                 8
         Active 19
                    15
## 14
         Active 25
                     28
                                 2
## 15
         Active 19
                    18
                                 6
## 16
         Active 21
                     20
                                11
## 17
        Active 21
                    21
                                 5
## 18
        Active 25
                    24
                                11
## 19
         Active 25
                     25
                                 6
## 20
         Active
                15
                     22
                                 6
## 21
         Active 27 26
                                10
```