Multivariate Analysis for the Behavioral Sciences, Second Edition (Chapman and Hall/CRC, 2019)

Examples of Chapter 16: Confirmatory Factor Analysis and Structural Equation Models

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Examples

Table 16.1: Observed Correlations for the Ability and Aspiration Example

```
0.73, 1.00, 0.00, 0.00, 0.00, 0.00,
                0.70,0.68,1.00,0.00,0.00,0.00,
                0.58,0.61,0.57,1.00,0.00,0.00,
                0.46,0.43,0.40,0.37,1.00,0.00,
                0.56, 0.52, 0.48, 0.41, 0.72, 1.00),
              ncol = 6, byrow = TRUE)
varNames <- c("SCA", "PPE", "PTE", "PFE", "EA", "CP")</pre>
dimnames(CORR) <- list(varNames, varNames)</pre>
CORR
       SCA PPE PTE PFE
                           EA CP
## SCA 1.00 0.00 0.00 0.00 0.00 0
## PPE 0.73 1.00 0.00 0.00 0.00 0
## PTE 0.70 0.68 1.00 0.00 0.00 0
## PFE 0.58 0.61 0.57 1.00 0.00 0
## EA 0.46 0.43 0.40 0.37 1.00 0
## CP 0.56 0.52 0.48 0.41 0.72 1
```

Figure 16.1

```
#install.packages("sem")
#install.packages("semPlot")
library(sem)
library(semPlot)
AAmodel <-specifyModel(text = "
             -> SCA, lambda[1], NA
-> PPE, lambda[2], NA
-> PTE, lambda[3], NA
-> PFE, lambda[4], NA
  Ability
  Ability
  Ability
  Ability
            -> PFE,
  Aspiration -> EA,
                             lambda[5], NA
  Aspiration -> CP,
                             lambda[6], NA
  Ability <-> Aspiration, rho,
  SCA
            <-> SCA, u[1],
                                        NA
  PPE
             <-> PPE,
                             u[2],
            <-> PTE,
                             u[3],
  PTE
                                       NA
  PFE
            <-> PFE,
                             u[4],
             <-> EA,
  EΑ
                             u[5],
                                       NA
  CP
             <-> CP,
                             u[6],
  Ability <-> Ability,
                             NA,
                                        1
  Aspiration <-> Aspiration, NA,
                                         1
## NOTE: it is generally simpler to use specifyEquations() or cfa()
        see ?specifyEquations
options(fit.indices = c("CFI", "NNFI", "RMSEA", "SRMR")) # (NNFI = TLI)
AAsem <- sem(AAmodel, CORR, N = 556)
semPaths(AAsem, # filetype = "pdf", filename = "AAmodel-KV",
         what = "path", whatLabels = "name", style = "lisrel", layout = "tree2",
         intercepts = FALSE, residuals = TRUE, thresholds = FALSE, reorder = FALSE,
         rotation = 1, nCharNodes = 0, nCharEdges = 0,
         sizeMan = 8, sizeLat = 20, sizeMan2 = 6, sizeLat2 = 10,
        manifests = varNames, latents = c("Ability", "Aspiration"),
        residScale = 12, as.expression = c("edges", "nodes"), centerLevels = FALSE,
         edge.label.cex = 1.2, esize = 2.5, label.scale = TRUE, curvePivot = TRUE,
         curvePivotShape = 0.67, edge.label.position = 0.67, width = 6, height = 2.5)
```

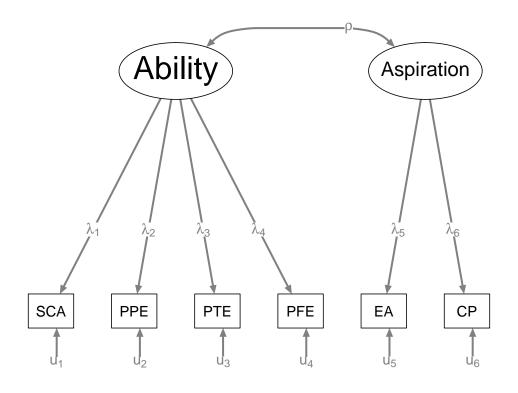


Table 16.2

summary(AAsem)

```
##
##
   Model Chisquare = 9.255732 Df = 8 \text{ Pr}(>\text{Chisq}) = 0.3211842
   RMSEA index = 0.01681733
                                90% CI: (NA, 0.05432054)
## Tucker-Lewis NNFI = 0.9987042
## Bentler CFI = 0.9993089
##
   SRMR = 0.01201145
##
  Normalized Residuals
##
                 1st Qu.
                                                  3rd Qu.
         Min.
                             Median
                                          Mean
## -0.4409685 -0.1870306 -0.0000018 -0.0130992 0.2107128 0.5333068
##
##
   R-square for Endogenous Variables
            PPE
                    PTE
##
      SCA
                           PFE
## 0.7451 0.7213 0.6482 0.4834 0.6008 0.8629
##
##
  Parameter Estimates
##
             Estimate Std Error z value
                                            Pr(>|z|)
## lambda[1] 0.8632049 0.03514508 24.561188 3.284552e-133
## lambda[2] 0.8493226 0.03545022 23.958178 7.593661e-127
## lambda[3] 0.8050861 0.03640470 22.114892 2.272503e-108
## lambda[4] 0.6952671 0.03863370 17.996387 2.079489e-72
## lambda[5] 0.7750850 0.04035675 19.205834 3.307658e-82
## lambda[6] 0.9289304 0.03940959 23.571177 7.615270e-123
## rho
            0.6663697 0.03095414 21.527645 8.578257e-103
## u[1]
            0.2548772 0.02336722 10.907470 1.061704e-27
## u[2]
            0.2786512 0.02412754 11.549097 7.460043e-31
## u[3]
            0.3518366 0.02691875 13.070321 4.865973e-39
## u[4]
            0.5166036 0.03472534 14.876847 4.659431e-50
            0.3992432 0.03819583 10.452535 1.426604e-25
## u[5]
## u[6]
            0.1370884 0.04350459 3.151126 1.626425e-03
##
## lambda[1] SCA <--- Ability
## lambda[2] PPE <--- Ability
## lambda[3] PTE <--- Ability
## lambda[4] PFE <--- Ability
## lambda[5] EA <--- Aspiration
## lambda[6] CP <--- Aspiration
## rho
            Aspiration <--> Ability
## u[1]
            SCA <--> SCA
## u[2]
            PPE <--> PPE
## u[3]
            PTE <--> PTE
## u[4]
            PFE <--> PFE
            EA <--> EA
## u[5]
## u[6]
             CP <--> CP
##
## Iterations = 29
```

Figure 16.2: Path diagram for the drug usage model

Revisiting the drug usage example introduced in **Chapter 13**:

```
DRUGcorr <- matrix(c(</pre>
  1.0, rep(0, 12),
  0.447, 1.0, rep(0, 11),
  0.422,0.619,1.0,rep(0,10),
  0.436, 0.604, 0.583, 1.0, rep(0,9),
  0.114,0.068,0.053,0.115,1.0,rep(0,8),
  0.203, 0.146, 0.139, 0.256, 0.349, 1.0, rep(0,7),
  0.091,0.103,0.110,0.122,0.209,0.221,1.0,rep(0,6),
  0.082, 0.063, 0.066, 0.097, 0.321, 0.355, 0.201, 1.0, rep(0,5),
  0.513,0.445,0.365,0.482,0.186,0.316,0.150,0.154,1.0,rep(0,4),
  0.304,0.318,0.240,0.368,0.303,0.377,0.163,0.219,0.534,1.0,rep(0,3),
  0.245,0.203,0.183,0.255,0.272,0.323,0.310,0.288,0.301,0.302,1.0,rep(0,2),
  0.101, 0.088, 0.074, 0.139, 0.279, 0.367, 0.232, 0.320, 0.204, 0.368, 0.340, 1.0, 0.0,
  0.245,0.199,0.184,0.293,0.278,0.545,0.232,0.314,0.394,0.467,0.392,0.511,1.0), ncol=13, byrow=T)
DRUGnames <- c("Cigs", "Beer", "Wine", "Liqr", "Cocn", "Tran", "Drug", "Hern",
               "Marj", "Hash", "Inhl", "Hall", "Amph")
dimnames(DRUGcorr) <- list(DRUGnames, DRUGnames)</pre>
DRUGcorr <- DRUGcorr + t(DRUGcorr)</pre>
diag(DRUGcorr) <- diag(DRUGcorr) - 1</pre>
DRUGcorr
##
         Cigs Beer Wine Liqr Cocn Tran Drug Hern Marj Hash Inhl
## Cigs 1.000 0.447 0.422 0.436 0.114 0.203 0.091 0.082 0.513 0.304 0.245
## Beer 0.447 1.000 0.619 0.604 0.068 0.146 0.103 0.063 0.445 0.318 0.203
## Wine 0.422 0.619 1.000 0.583 0.053 0.139 0.110 0.066 0.365 0.240 0.183
## Ligr 0.436 0.604 0.583 1.000 0.115 0.256 0.122 0.097 0.482 0.368 0.255
## Cocn 0.114 0.068 0.053 0.115 1.000 0.349 0.209 0.321 0.186 0.303 0.272
## Tran 0.203 0.146 0.139 0.256 0.349 1.000 0.221 0.355 0.316 0.377 0.323
## Drug 0.091 0.103 0.110 0.122 0.209 0.221 1.000 0.201 0.150 0.163 0.310
## Hern 0.082 0.063 0.066 0.097 0.321 0.355 0.201 1.000 0.154 0.219 0.288
## Marj 0.513 0.445 0.365 0.482 0.186 0.316 0.150 0.154 1.000 0.534 0.301
## Hash 0.304 0.318 0.240 0.368 0.303 0.377 0.163 0.219 0.534 1.000 0.302
## Inhl 0.245 0.203 0.183 0.255 0.272 0.323 0.310 0.288 0.301 0.302 1.000
## Hall 0.101 0.088 0.074 0.139 0.279 0.367 0.232 0.320 0.204 0.368 0.340
## Amph 0.245 0.199 0.184 0.293 0.278 0.545 0.232 0.314 0.394 0.467 0.392
         Hall Amph
## Cigs 0.101 0.245
## Beer 0.088 0.199
## Wine 0.074 0.184
## Ligr 0.139 0.293
## Cocn 0.279 0.278
## Tran 0.367 0.545
## Drug 0.232 0.232
## Hern 0.320 0.314
## Marj 0.204 0.394
## Hash 0.368 0.467
## Inhl 0.340 0.392
## Hall 1.000 0.511
## Amph 0.511 1.000
```

```
DRUGmodel <-specifyModel(text = "</pre>
Alcohol -> Cigs, lambda[1],NA
Cannabis -> Cigs, lambda[2],NA
Alcohol -> Beer, lambda[3],NA
Alcohol -> Wine, lambda[4],NA
Cannabis -> Wine, lambda[5],NA
Alcohol -> Ligr, lambda[6],NA
HardDrug -> Liqr, lambda[7],NA
HardDrug -> Cocn, lambda[8],NA
HardDrug -> Tran, lambda[9],NA
HardDrug -> Drug, lambda[10],NA
HardDrug -> Hern, lambda[11],NA
Cannabis -> Marj, lambda[12],NA
Cannabis -> Hash, lambda[13], NA
HardDrug -> Hash, lambda[14],NA
HardDrug -> Inhl, lambda[15],NA
HardDrug -> Hall, lambda[16],NA
HardDrug -> Amph, lambda[17],NA
     <-> Cigs, u[1],NA
Cigs
Beer
      <-> Beer, u[2],NA
Wine \langle - \rangle Wine, u[3],NA
      <-> Liqr, u[4],NA
Liqr
       <-> Cocn, u[5],NA
Cocn
Tran <-> Tran, u[6],NA
Drug <-> Drug, u[7],NA
      <-> Hern, u[8],NA
Hern
Marj
       <-> Marj, u[9],NA
Hash <-> Hash, u[10],NA
      <-> Inhl, u[11],NA
Inhl
       <-> Hall, u[12],NA
Hall
Amph
       <-> Amph, u[13],NA
Alcohol <-> Cannabis, rho[1],NA
Alcohol <-> HardDrug, rho[2],NA
Cannabis <-> HardDrug, rho[3],NA
Alcohol <-> Alcohol, NA,1
Cannabis <-> Cannabis, NA, 1
HardDrug <-> HardDrug,NA,1
")
## NOTE: it is generally simpler to use specifyEquations() or cfa()
        see ?specifyEquations
options(fit.indices = c("CFI", "NNFI", "RMSEA", "SRMR")) # (NNFI = TLI)
DRUGsem <- sem(DRUGmodel, DRUGcorr, N = 1634)</pre>
```

```
semPaths(DRUGsem, # filetype = "pdf", filename = "DRUGmodel-KV",
    what = "path", whatLabels = "hide",
    style = "lisrel", layout = "tree2",
    residuals = TRUE, rotation = 2, nCharNodes = 0,
    sizeMan = 8, sizeLat = 10, sizeMan2 = 4, sizeLat2 = 10,
    esize = 2, label.cex = 0.75, label.scale = FALSE, width = 6, height = 5)
```

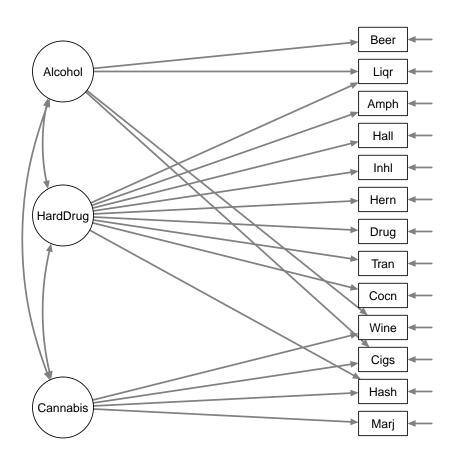


Table 16.3

summary(DRUGsem)

```
##
##
   Model Chisquare = 323.3541
                                  Df = 58 Pr(>Chisq) = 1.676805e-38
                                90% CI: (0.04738096, 0.05863211)
##
   RMSEA index = 0.05293048
   Tucker-Lewis NNFI = 0.9453964
   Bentler CFI = 0.9593974
##
##
   SRMR = 0.03899979
##
##
   Normalized Residuals
##
        Min.
               1st Qu.
                          Median
                                      Mean
                                             3rd Qu.
  -3.031458 -0.884693 -0.000004 -0.021815 0.998363
##
                                                      4.576743
##
##
   R-square for Endogenous Variables
##
            Beer
                   Wine
                         Liqr
                                 Cocn
                                        Tran
                                               Drug
                                                      Hern
                                                             Marj
## 0.3888 0.6264 0.6215 0.5922 0.2159 0.4562 0.1285 0.2265 0.8320 0.4531
##
     Inhl
            Hall
                   Amph
## 0.2948 0.3823 0.5828
##
##
   Parameter Estimates
##
              Estimate
                         Std Error z value
                                              Pr(>|z|)
              0.3580610 0.03449894 10.378898 3.093248e-25
## lambda[1]
## lambda[2]
               0.3317505 0.03527140 9.405651 5.170904e-21
## lambda[3]
              0.7914844 0.02260160 35.018962 1.157714e-268
## lambda[4]
               0.8759572 0.03759170 23.301881 4.242807e-120
## lambda[5] -0.1522411 0.03659116 -4.160598 3.174149e-05
## lambda[6]
               0.7222173 0.02354662 30.671802 1.353388e-206
## lambda[7]
              0.1226893 0.02265514 5.415519 6.111133e-08
              0.4646768 0.02572690 18.061903 6.359149e-73
## lambda[8]
## lambda[9]
              0.6754614 0.02397020 28.179212 1.051469e-174
## lambda[10] 0.3584240 0.02637142 13.591383 4.504847e-42
## lambda[11] 0.4759180 0.02564863 18.555299 7.389575e-77
## lambda[12]
              0.9121178 0.03045556 29.949139 4.514959e-197
              0.3955832 0.02960491 13.362081 1.007085e-40
## lambda[13]
## lambda[14]
              0.3817698 0.02923025 13.060776 5.516293e-39
## lambda[15] 0.5429839 0.02514237 21.596370 1.942958e-103
              0.6182726 0.02449908 25.236559 1.590899e-140
## lambda[16]
## lambda[17]
              0.7633843 0.02313045 33.003443 7.249129e-239
               0.6112369 0.02367015 25.823114 4.878528e-147
## u[1]
## u[2]
               0.3735526 0.01992742 18.745656 2.100659e-78
## u[3]
               0.3784784 0.02357593 16.053595 5.394692e-58
## u[4]
               0.4078314 0.01911408 21.336701 5.182466e-101
## u[5]
               0.7840758 0.02920268 26.849444 8.561618e-159
               0.5437528 0.02341101 23.226369 2.465982e-119
## u[6]
## u[7]
               0.8715324 0.03151476 27.654733 2.447978e-168
## u[8]
               0.7735019 0.02892760 26.739240 1.647200e-157
## u[9]
              0.1680413 0.04394465 3.823931 1.313404e-04
## u[10]
               0.5469320 0.02223445 24.598408 1.313719e-133
               0.7051680 0.02718073 25.943676 2.143063e-148
## u[11]
## u[12]
               0.6177393 0.02505445 24.655873 3.183322e-134
## u[13]
              0.4172447 0.02118572 19.694615 2.398122e-86
              0.6334751 0.02712849 23.350911 1.349094e-120
## rho[1]
```

```
## rho[2]
               0.3132784 0.02933063 10.680931 1.250110e-26
## rho[3]
               0.4993778 0.02711226 18.418889 9.268602e-76
##
## lambda[1] Cigs <--- Alcohol</pre>
## lambda[2] Cigs <--- Cannabis</pre>
## lambda[3] Beer <--- Alcohol</pre>
## lambda[4] Wine <--- Alcohol
## lambda[5] Wine <--- Cannabis</pre>
## lambda[6] Liqr <--- Alcohol</pre>
## lambda[7] Liqr <--- HardDrug</pre>
## lambda[8] Cocn <--- HardDrug</pre>
## lambda[9] Tran <--- HardDrug</pre>
## lambda[10] Drug <--- HardDrug</pre>
## lambda[11] Hern <--- HardDrug
## lambda[12] Marj <--- Cannabis</pre>
## lambda[13] Hash <--- Cannabis
## lambda[14] Hash <--- HardDrug
## lambda[15] Inhl <--- HardDrug
## lambda[16] Hall <--- HardDrug
## lambda[17] Amph <--- HardDrug
## u[1]
              Cigs <--> Cigs
## u[2]
              Beer <--> Beer
## u[3]
              Wine <--> Wine
## u[4]
              Ligr <--> Ligr
## u[5]
              Cocn <--> Cocn
## u[6]
              Tran <--> Tran
## u[7]
              Drug <--> Drug
## u[8]
              Hern <--> Hern
## u[9]
              Marj <--> Marj
              Hash <--> Hash
## u[10]
              Inhl <--> Inhl
## u[11]
## u[12]
              Hall <--> Hall
## u[13]
              Amph <--> Amph
## rho[1]
              Cannabis <--> Alcohol
## rho[2]
              HardDrug <--> Alcohol
## rho[3]
              HardDrug <--> Cannabis
##
## Iterations = 34
```

Figure 16.3: Corrgram for the Systems Intelligence data

Source of data: Törmänen, J., Hämäläinen, R. P. and Saarinen, E. (2016). Systems Intelligence inventory. *The Learning Organization*, 23, 218–231. (The data and parts of the R code by *Juha Törmänen* are used below with kind permission from the authors.)

See also:

6

- Saarinen, E. and Hämäläinen, R. P. (2004). Systems intelligence: Connecting engineering thinking with human sensitivity. In *Systems Intelligence—Discovering a Hidden Competence in Human Action and Organizational Life* (eds. R. P. Hämäläinen and E. Saarinen). Helsinki University of Technology, Research Reports A88. http://sal.aalto.fi/publications/pdffiles/systemsintelligence2004.pdf.
- Hämäläinen, R. P., Jones, R. and Saarinen, E. (2014). Being Better Better: Living with Systems Intelligence. Aalto University Publications Crossover 4/2014, http://systemsintelligence.aalto.fi/being_better_better/.

```
# Set seed to remove effect of random generator
set.seed(42)

# Load data (sidata.tsv contains renamed answer columns with names si1-si32)
si_cfa <- list()
si_cfa$data <- read.table("data/sidata.tsv", header = TRUE, sep = '\t')
si_cfa$dataset <- si_cfa$data$set

# SI model answers for the 32 items
si_cfa$answers <- si_cfa$data[, 10:41]
head(si_cfa$answers)</pre>
```

```
si1 si2 si3 si17 si13 si14 si15 si4 si25 si5 si26 si6 si27 si28 si7 si18
##
                        5
                               3
                                     4
                                                3
                                                      4
                                                           4
                                                                 5
                                                                      4
                                                                             4
                                                                                   3
                                                                                              4
## 1
        4
             5
                  4
                                           4
                                                                                        4
                        4
                               6
                                                           4
                                                                 4
                                                                             3
                                                                                        4
                                                                                              4
## 2
        4
             4
                  4
                                     5
                                           5
                                                5
                                                      3
                                                                      4
                                                                                   3
## 3
        4
             4
                  5
                        5
                               4
                                     5
                                           5
                                                4
                                                      4
                                                           4
                                                                 4
                                                                      6
                                                                             4
                                                                                   3
                                                                                        4
                                                                                              4
## 4
        4
             5
                  4
                        4
                               4
                                     4
                                           3
                                                5
                                                      3
                                                           5
                                                                 4
                                                                      5
                                                                             4
                                                                                   5
                                                                                        5
                                                                                              3
        5
             5
                  5
                        5
                               3
                                     5
                                           4
                                                5
                                                      5
                                                           5
                                                                 3
                                                                      5
                                                                                   4
                                                                                        5
                                                                                              4
## 5
                                                      5
             5
                  4
                        6
                               4
                                     4
                                                5
                                                                 5
                                                                      6
                                                                             4
                                                                                   5
                                                                                              5
##
   6
        3
                                           4
                                                           5
                                                                                        4
##
      si20
           si21 si9 si10 si11
                                   si22
                                          si8 si23 si19 si16 si29 si30 si12 si24
                                                                                          si31
## 1
         4
                5
                     3
                           3
                                 4
                                       3
                                            6
                                                         5
                                                               4
                                                                     4
                                                                           1
                                                                                        6
                                                                                              4
## 2
         5
                3
                     3
                           3
                                NA
                                       4
                                            3
                                                  4
                                                         5
                                                               5
                                                                     4
                                                                           2
                                                                                 3
                                                                                        3
                                                                                              4
                     3
                                            5
                                                                           3
                                                                                              3
## 3
         6
                5
                           5
                                 4
                                       5
                                                  3
                                                         4
                                                               4
                                                                     4
                                                                                 3
                                                                                        4
## 4
         4
                5
                     1
                           5
                                       5
                                            5
                                                  5
                                                         5
                                                               4
                                                                     4
                                                                           1
                                                                                 0
                                                                                        5
                                                                                              4
                                 1
         5
                     2
                           5
                                                         5
                                                                           2
                                                                                        5
                                                                                              5
## 5
                                 2
                                       3
                                            4
                                                               4
         6
                     3
                           6
                                       4
                                            4
                                                         5
                                                                           3
                                                                                        5
                                                                                              5
## 6
                                 3
                                                               5
                                                                     5
                                                                                 3
##
      si32
## 1
         4
## 2
         4
## 3
         3
## 4
         5
## 5
         4
```

```
#install.packages("corrplot")
library(corrplot)
```

corrplot 0.84 loaded

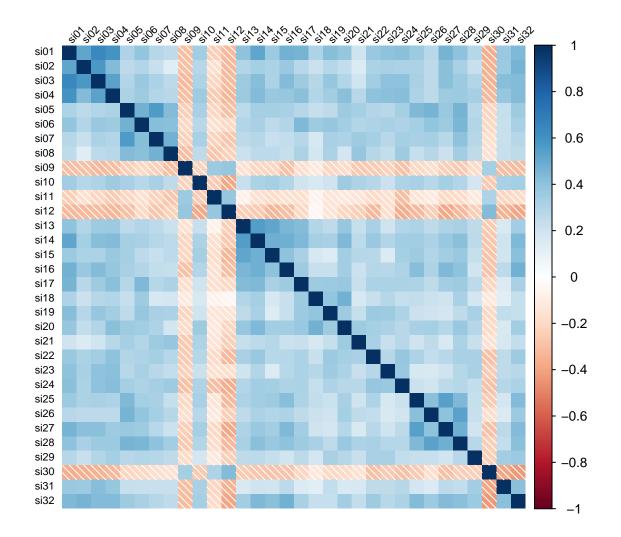
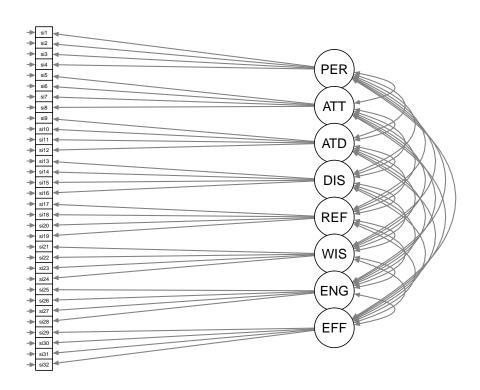


Figure 16.4

```
# DATA: Validation dataset rows with no missing data (N=815):
si_cfa$data.validation <- si_cfa$data[rowSums(is.na(si_cfa$answers)) == 0 &
                                                    si_cfa$dataset == 'validation', ]
# MODEL: Eight factors, free loadings:
# Free weight model: Each item is explained by one factor, factors have unit variance
# In total 8*4 loadings + 7*8/2 factor covariances + 8*4 item variances = 92 parameters
model.8free <- specifyEquations(text = "</pre>
si1 = a1(1)*PER
si2 = a2(1)*PER
si3 = a3(1)*PER
si4 = a4(1)*PER
si5 = a5(1)*ATT
si6 = a6(1)*ATT
si7 = a7(1)*ATT
si8 = a8(1)*ATT
# ATD factor starting values coded negatively here; othersize sem has trouble converging
si9 = a9(1)*ATD
si10 = a10(-1)*ATD
si11 = a11(1)*ATD
si12 = a12(1)*ATD
si13 = a13(1)*DIS
si14 = a14(1)*DIS
si15 = a15(1)*DIS
si16 = a16(1)*DIS
si17 = a17(1)*REF
si18 = a18(1)*REF
si19 = a19(1)*REF
si20 = a20(1)*REF
si21 = a21(1)*WIS
si22 = a22(1)*WIS
si23 = a23(1)*WIS
si24 = a24(1)*WIS
si25 = a25(1)*ENG
si26 = a26(1)*ENG
si27 = a27(1)*ENG
si28 = a28(1)*ENG
si29 = a29(1)*EFF
si30 = a30(-1)*EFF
si31 = a31(1)*EFF
si32 = a32(1)*EFF
```

```
V(PER) = 1
V(ATT) = 1
V(ATD) = 1
V(DIS) = 1
V(REF) = 1
V(WIS) = 1
V(ENG) = 1
V(EFF) = 1
", covs = "PER, ATT, ATD, DIS, REF, WIS, ENG, EFF")
## NOTE: adding 32 variances to the model
options(fit.indices = c("SRMR", "CFI", "RMSEA"))
res.8free <- sem(model = model.8free, data = si_cfa$data.validation, objective = objectiveGLS)
\# summary(res.8free) outputs CFI = 0.951, RMSEA = 0.048, SRMR = 0.068
semPaths(res.8free, # filetype = "pdf", filename = "SImodel-KV",
         what = "path", whatLabels = "hide", style = "lisrel",
         residuals = TRUE, curve = 3.2, rotation = 4, nCharNodes = 0,
         sizeLat = 7, sizeMan = 3, sizeMan2 = 2, esize = 1.3, mar = c(3, 8, 3, 15))
```



summary(res.8free)

```
##
##
   Model Chisquare = 1256.666
                                  Df = 436 Pr(>Chisq) = 1.484832e-80
   RMSEA index = 0.04808702
                               90% CI: (NA, NA)
##
   Bentler CFI = 0.9507248
##
   SRMR = 0.06815243
##
##
   Normalized Residuals
##
     Min. 1st Qu. Median
                              Mean 3rd Qu.
##
  -3.9692 -0.5851 0.3119 0.4389 1.4955 5.0806
##
##
   R-square for Endogenous Variables
##
      si1
             si2
                    si3
                           si4
                                  si5
                                         si6
                                                si7
                                                       si8
                                                               si9
                                                                     si10
## 0.6853 0.4683 0.6063 0.5770 0.5986 0.4679 0.5216 0.4154 0.3048 0.3812
     si11
            si12
                   si13
                          si14
                                 si15
                                        si16
                                               si17
                                                      si18
                                                              si19
                                                                     si20
## 0.2329 0.4948 0.5226 0.5683 0.4666 0.4705 0.4399 0.3281 0.3864 0.5134
     si21
            si22
                   si23
                          si24
                                 si25
                                        si26
                                               si27
                                                      si28
                                                             si29
                                                                     si30
## 0.3039 0.3875 0.3102 0.4414 0.4525 0.4340 0.5544 0.5727 0.3177 0.4029
     si31
            si32
## 0.3903 0.5908
##
##
   Parameter Estimates
##
                                               Pr(>|z|)
              Estimate
                         Std Error z value
## a1
               0.6685600 0.03242847
                                     20.616450 1.953814e-94 si1 <--- PER
## a2
               0.5176584 0.03255797
                                     15.899592 6.377848e-57 si2 <--- PER
## a3
               0.5503226 0.02912131
                                     18.897592 1.193777e-79 si3 <--- PER
## a4
               0.6639999 0.03216349
                                     20.644522 1.093385e-94 si4 <--- PER
## a5
               0.7199893 0.03731261
                                     19.296137
                                                5.787753e-83 si5 <--- ATT
## a6
               0.5830731 0.03756700 15.520887
                                                2.505649e-54 si6 <--- ATT
## a7
               0.6052763 0.03284806
                                    18.426547
                                                8.045792e-76 si7 <--- ATT
## a8
               0.4726956 0.03702206
                                     12.767945
                                                2.476041e-37 si8 <--- ATT
                                     11.530257
                                                9.286654e-31 si9 <--- ATD
## a9
               0.5539789 0.04804567
## a10
              -0.5988248 0.04408796 -13.582504 5.085730e-42 si10 <--- ATD
## a11
               0.5207716 0.05559112
                                      9.367892 7.399543e-21 si11 <--- ATD
               0.7809641 0.05014166
                                     15.575156
                                                1.073899e-54 si12 <--- ATD
## a12
## a13
               0.7076282 0.04249851
                                     16.650660
                                                2.992851e-62 si13 <--- DIS
## a14
               0.7079806 0.03510499
                                     20.167519 1.888795e-90 si14 <--- DIS
## a15
               0.6562514 0.04315793
                                    15.205813 3.235861e-52 si15 <--- DIS
## a16
               0.6307662 0.04019476
                                    15.692747
                                                1.695563e-55 si16 <--- DIS
## a17
               0.5489697 0.03795019
                                     14.465532 2.000525e-47 si17 <--- REF
## a18
               0.5322472 0.04663205
                                    11.413762 3.569486e-30 si18 <--- REF
## a19
               0.4752247 0.03977588
                                     11.947560 6.685971e-33 si19 <--- REF
## a20
               0.7397153 0.04971787
                                     14.878259
                                                4.562140e-50 si20 <--- REF
                                                1.328092e-27 si21 <--- WIS
## a21
               0.5196336 0.04772932 10.887095
## a22
               0.5626853 0.03632400
                                     15.490729
                                                4.007202e-54 si22 <--- WIS
## a23
                                     12.241511
               0.4487358 0.03665690
                                                1.865266e-34 si23 <--- WIS
## a24
               0.6262280 0.03834655
                                     16.330752
                                                5.964490e-60 si24 <--- WIS
## a25
                                     14.998207
                                                7.542925e-51 si25 <--- ENG
               0.6894555 0.04596920
## a26
               0.6236446 0.03980360
                                     15.668046
                                               2.501507e-55 si26 <--- ENG
                                               9.703919e-71 si27 <--- ENG
## a27
                                     17.782232
               0.7692516 0.04325956
## a28
               0.6896095 0.03461536
                                     19.922065
                                                2.619637e-88 si28 <--- ENG
## a29
               0.4938007 0.04166490 11.851720
                                               2.108191e-32 si29 <--- EFF
## a30
              -0.6660330 0.04612172 -14.440766 2.866367e-47 si30 <--- EFF
```

```
## a31
               0.4733875 0.03523098 13.436683 3.685926e-41 si31 <--- EFF
## a32
               0.7197076 0.03831885
                                     18.782075 1.058611e-78 si32 <--- EFF
## C[PER, ATT]
               0.6762624 0.03215036
                                     21.034367 3.179857e-98 ATT <--> PER
## C[PER,ATD] -0.7810532 0.03194689 -24.448492 5.221765e-132 ATD <--> PER
## C[PER,DIS]
               0.8358883 0.02263808
                                     36.923990 1.904974e-298 DIS <--> PER
                                    31.760091 2.303946e-221 REF <--> PER
## C[PER,REF]
               0.8386651 0.02640626
## C[PER.WIS]
               0.8864440 0.02456816
                                    36.081004 4.504133e-285 WIS <--> PER
## C[PER, ENG]
               0.7638040 0.02683644
                                     28.461447 3.516906e-178 ENG <--> PER
## C[PER,EFF]
               0.8161309 0.02419588
                                     33.730154 2.089629e-249 EFF <--> PER
## C[ATT,ATD] -0.7987056 0.03383097 -23.608712 3.136551e-123 ATD <--> ATT
## C[ATT,DIS]
               0.7021611 0.03129715
                                     22.435302 1.780974e-111 DIS <--> ATT
                                     21.945047 9.656894e-107 REF <--> ATT
## C[ATT, REF]
               0.7505247 0.03420019
## C[ATT,WIS]
               0.8241651 0.03052199
                                     27.002334 1.387521e-160 WIS <--> ATT
## C[ATT, ENG]
               0.8679997 0.02244717
                                     38.668562 0.000000e+00 ENG <--> ATT
                                     21.587405 2.358938e-103 EFF <--> ATT
## C[ATT,EFF]
               0.7144656 0.03309641
## C[ATD,DIS] -0.7679736 0.03658449 -20.991782 7.796705e-98 DIS <--> ATD
## C[ATD,REF] -0.7656555 0.04034199 -18.979119 2.538162e-80 REF <--> ATD
## C[ATD,WIS] -0.8709160 0.03342931 -26.052468 1.261453e-149 WIS <--> ATD
## C[ATD,ENG] -0.8200374 0.03157837 -25.968327 1.129124e-148 ENG <--> ATD
## C[ATD,EFF] -0.8454915 0.03057594 -27.652180 2.627332e-168 EFF <--> ATD
## C[DIS,REF]
              0.8317475 0.02898892 28.691912 4.813321e-181 REF <--> DIS
## C[DIS, WIS]
               0.7894968 0.03083435
                                     25.604454 1.360900e-144 WIS <--> DIS
## C[DIS,ENG]
               0.7614736 0.02868166
                                     26.549150 2.626927e-155 ENG <--> DIS
## C[DIS.EFF]
               0.7731367 0.03071951
                                     25.167615 9.066424e-140 EFF <--> DIS
## C[REF, WIS]
               0.8840439 0.02962020
                                     29.845978 9.899816e-196 WIS <--> REF
## C[REF, ENG]
               0.7464520 0.03291526
                                     22.677990 7.388787e-114 ENG <--> REF
                                     21.418043 9.072026e-102 EFF <--> REF
## C[REF,EFF]
               0.7541803 0.03521238
## C[WIS, ENG]
               0.7958373 0.03200873
                                     24.863133 1.864692e-136 ENG <--> WIS
                                     25.626374 7.755361e-145 EFF <--> WIS
## C[WIS,EFF]
               0.8044019 0.03138961
## C[ENG, EFF]
               0.7464017 0.03060912
                                     24.384941 2.470795e-131 EFF <--> ENG
## V[si1]
               0.2052307 0.01510102
                                     13.590525
                                               4.557998e-42 si1 <--> si1
## V[si2]
               0.3042285 0.01850548
                                     16.439912 9.906310e-61 si2 <--> si2
## V[si3]
               0.1966617 0.01289154
                                     15.255091
                                                1.522818e-52 si3 <--> si3
## V[si4]
               0.3232391 0.02100144
                                     15.391286
                                                1.872739e-53 si4 <--> si4
## V[si5]
               0.3475479 0.02503211
                                     13.884081
                                                7.910845e-44 si5 <--> si5
                                     15.628634
## V[si6]
               0.3865663 0.02473449
                                               4.646611e-55 si6 <--> si6
## V[si7]
               0.3359755 0.02189731
                                     15.343234
                                                3.931117e-53 si7 <--> si7
## V[si8]
               0.3145093 0.02064421
                                     15.234745
                                                2.079377e-52 si8 <--> si8
                                     16.708624
                                                1.134231e-62 si9 <--> si9
## V[si9]
               0.6999811 0.04189340
## V[si10]
               0.5820615 0.03774915
                                     15.419196
                                                1.216088e-53 si10 <--> si10
## V[si11]
               0.8933729 0.05247718
                                     17.024026
                                                5.449204e-65 si11 <--> si11
               0.6227930 0.04302111
                                     14.476450
                                                1.706870e-47 si12 <--> si12
## V[si12]
## V[si13]
               0.4573467 0.03065546
                                     14.918931
                                                2.482176e-50 si13 <--> si13
               0.3807060 0.02525753
                                     15.072966
                                                2.439107e-51 si14 <--> si14
## V[si14]
## V[si15]
               0.4924139 0.03225694
                                     15.265361
                                                1.301064e-52 si15 <--> si15
                                                2.808320e-54 si16 <--> si16
## V[si16]
               0.4477171 0.02885971
                                     15.513568
## V[si17]
               0.3836756 0.02518243
                                     15.235849
                                                2.044538e-52 si17 <--> si17
## V[si18]
               0.5800615 0.03521116
                                     16.473796
                                                5.660387e-61 si18 <--> si18
## V[si19]
               0.3585894 0.02326245
                                     15.414943
                                                1.298846e-53 si19 <--> si19
## V[si20]
               0.5187093 0.03803427
                                     13.637944
                                                2.381815e-42 si20 <--> si20
## V[si21]
               0.6185608 0.03814391
                                     16.216502
                                               3.855328e-59 si21 <--> si21
## V[si22]
               0.5003786 0.02999815
                                     16.680314
                                               1.822588e-62 si22 <--> si22
## V[si23]
               0.4477391 0.02610443
                                     17.151840 6.089339e-66 si23 <--> si23
## V[si24]
               0.4962187 0.03089210 16.062965 4.638357e-58 si24 <--> si24
```

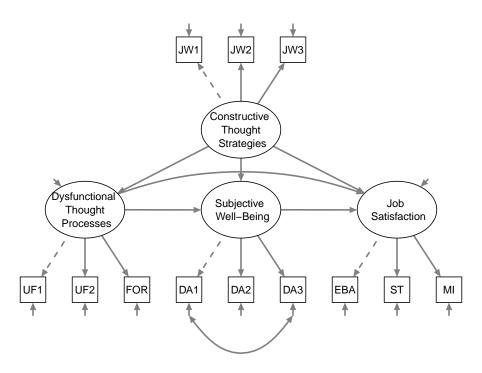
```
## V[si25]
              0.5751351 0.03580959 16.060923 4.793616e-58 si25 <--> si25
## V[si26]
              0.5072077 0.03030312 16.737804 6.950558e-63 si26 <--> si26
## V[si27]
              0.4756047 0.03209640 14.818008 1.120579e-49 si27 <--> si27
## V[si28]
              0.3548095 0.02422488 14.646492 1.418532e-48 si28 <--> si28
              0.5235896 0.03232428 16.198028 5.207018e-59 si29 <--> si29
## V[si29]
## V[si30]
          0.6575266 0.04082600 16.105584 2.330882e-58 si30 <--> si30
## V[si31]
              0.3500031 0.02195291 15.943356 3.168708e-57 si31 <--> si31
## V[si32]
            0.3587271 0.02777209 12.916819 3.617910e-38 si32 <--> si32
##
## Iterations = 84
```

Figure 16.5: Path diagram for the hypothesized structural equation model for job satisfaction data

Source of data: Kline, R. B. (2016). Principles and Practice of Structural Equation Modeling, 4th edition. Guilford Press, New York.

```
# Modified from https://www.quilford.com/add/kline/houghton-lavaan.r
# Fully latent model of thought strategies and job satisfaction
#install.packages("lavaan")
library(lavaan)
## This is lavaan 0.6-3
## lavaan is BETA software! Please report any bugs.
##
## Attaching package: 'lavaan'
## The following objects are masked from 'package:sem':
##
##
      cfa, sem
# Input the correlations in lower diagonal form
houghtonLower.cor <- '
1.000
.668 1.000
.635 .599 1.000
 .263 .261 .164 1.000
.290 .315 .247 .486 1.000
 .207 .245 .231 .251 .449 1.000
-.206 -.182 -.195 -.309 -.266 -.142 1.000
-.280 -.241 -.238 -.344 -.305 -.230 ..753 1.000
-.258 -.244 -.185 -.255 -.255 -.215 .554 .587 1.000
 .080 .096 .094 -.017 .151 .141 -.074 -.111 .016 1.000
 .061 .028 -.035 -.058 -.051 -.003 -.040 -.040 -.018 .284 1.000
 .113 .174 .059 .063 .138 .044 -.119 -.073 -.084
                                                    .563
                                                         .379 1.000 '
# Name the variables and convert to full correlation matrix
# KV: change names of manifest and factor variables (more according to the article diagram):
houghtonFull.cor <- getCov(houghtonLower.cor,
        names = c("JW1","JW2","JW3", "UF1","UF2","FOR", "DA1","DA2","DA3", "EBA","ST","MI"))
# add the standard deviations and convert to covariances
houghtonFull.cov <- cor2cov(houghtonFull.cor,
        sds = c(0.939, 1.017, 0.937, 0.562, 0.760, 0.524, 0.585, 0.609, 0.731, 0.711, 1.124, 1.001))
houghtonFull.cov
              JW1
                         JW2
                                     JW3
                                                 UF1
                                                             UF2
## JW1 0.88172100 0.63791528 0.55870031 0.138789834 0.20695560
## JW2
       0.63791528 1.03428900 0.57080447 0.149175594 0.24346980
## JW3
       0.55870031 0.57080447 0.87796900 0.086361416 0.17589364
## UF1
       ## UF2 0.20695560 0.24346980 0.17589364 0.207580320 0.57760000
```

```
## FOR 0.10185145 0.13056246 0.11341823 0.073916488 0.17880976
## DA1 -0.11315889 -0.10827999 -0.10688828 -0.101589930 -0.11826360
## DA2 -0.16011828 -0.14926407 -0.13581065 -0.117736752 -0.14116620
## DA3 -0.17709352 -0.18139619 -0.12671520 -0.104759610 -0.14166780
## EBA 0.05341032 0.06941635 0.06262346 -0.006792894 0.08159436
       ## ST
## MI
       0.10621311 0.17713496 0.05533828 0.035441406 0.10498488
##
               FOR
                          DA1
                                      DA2
                                                   DA3
## JW1
       0.101851452 -0.11315889 -0.16011828 -0.177093522 0.053410320
## JW2 0.130562460 -0.10827999 -0.14926407 -0.181396188 0.069416352
## JW3 0.113418228 -0.10688828 -0.13581065 -0.126715195 0.062623458
## UF1 0.073916488 -0.10158993 -0.11773675 -0.104759610 -0.006792894
## UF2 0.178809760 -0.11826360 -0.14116620 -0.141667800 0.081594360
## FOR 0.274576000 -0.04352868 -0.07339668 -0.082354460 0.052531524
## DA1 -0.043528680 0.34222500 0.26826754 0.236909790 -0.030779190
## DA2 -0.073396680 0.26826754 0.37088100 0.261320073 -0.048062889
## DA3 -0.082354460 0.23690979 0.26132007 0.534361000 0.008315856
## EBA 0.052531524 -0.03077919 -0.04806289 0.008315856
## ST -0.001766928 -0.02630160 -0.02738064 -0.014789592 0.226962576
       0.023079056 - 0.06968461 - 0.04450146 - 0.061465404 0.400693293
##
                ST
                           МТ
## JW1 0.064381596
                   0.10621311
## JW2 0.032007024
                   0.17713496
## JW3 -0.036861580 0.05533828
## UF1 -0.036637904 0.03544141
## UF2 -0.043566240 0.10498488
## FOR -0.001766928 0.02307906
## DA1 -0.026301600 -0.06968461
## DA2 -0.027380640 -0.04450146
## DA3 -0.014789592 -0.06146540
## EBA 0.226962576 0.40069329
## ST
       1.263376000 0.42642200
## MI
       0.426421996 1.00200100
# Specify SEM (with Lavaan notation):
JSmodel <- '
# measurement part
CTS = \sim EBA + ST + MI
DTP = ~DA1 + DA2 + DA3
SWB =~ UF1 + UF2 + FOR
JS = ~JW1 + JW2 + JW3
# error covariance
UF1 ~~ FOR
# structural part
DTP ~ CTS
SWB ~ CTS + DTP
JS ~ CTS + DTP + SWB
options(fit.indices = c("CFI", "NNFI", "RMSEA", "SRMR")) # (NNFI = TLI)
```



```
summary(JSsem, fit.measures = TRUE, standardized = TRUE, rsquare = TRUE)
## lavaan 0.6-3 ended normally after 48 iterations
##
##
     Optimization method
                                                    NLMINB
     Number of free parameters
##
                                                        31
##
##
     Number of observations
                                                       263
##
##
     Estimator
                                                        ML
##
    Model Fit Test Statistic
                                                    56.662
```

```
##
     Degrees of freedom
                                                          47
##
     P-value (Chi-square)
                                                      0.158
##
## Model test baseline model:
##
##
     Minimum Function Test Statistic
                                                   1087.490
##
     Degrees of freedom
                                                          66
     P-value
                                                      0.000
##
##
## User model versus baseline model:
##
     Comparative Fit Index (CFI)
                                                      0.991
##
     Tucker-Lewis Index (TLI)
                                                      0.987
##
##
## Loglikelihood and Information Criteria:
##
##
     Loglikelihood user model (HO)
                                                  -3121.267
     Loglikelihood unrestricted model (H1)
##
                                                  -3092.936
##
                                                         31
##
     Number of free parameters
##
     Akaike (AIC)
                                                   6304.534
##
     Bayesian (BIC)
                                                   6415.270
##
     Sample-size adjusted Bayesian (BIC)
                                                   6316.985
##
## Root Mean Square Error of Approximation:
##
##
     RMSEA
                                                      0.028
##
     90 Percent Confidence Interval
                                               0.000 0.052
     P-value RMSEA <= 0.05
                                                      0.936
##
##
## Standardized Root Mean Square Residual:
##
                                                      0.037
##
     {\tt SRMR}
##
## Parameter Estimates:
##
##
     Information
                                                   Expected
##
     Information saturated (h1) model
                                                 Structured
##
     Standard Errors
                                                   Standard
##
## Latent Variables:
##
                      Estimate Std.Err z-value P(>|z|)
                                                               Std.lv Std.all
##
     CTS =~
##
       EBA
                          1.000
                                                                0.460
                                                                         0.648
##
       ST
                          1.056
                                   0.178
                                             5.922
                                                      0.000
                                                                0.486
                                                                         0.433
                                   0.331
                                             5.717
                                                                0.870
                                                                         0.870
##
       ΜI
                          1.890
                                                      0.000
     DTP =~
##
##
                          1.000
                                                                0.485
                                                                         0.830
       DA1
                                                                0.549
##
       DA2
                          1.133
                                   0.080
                                            14.105
                                                      0.000
                                                                         0.904
##
       DA3
                          0.993
                                   0.089
                                            11.175
                                                      0.000
                                                                0.481
                                                                         0.660
##
     SWB =~
##
       UF1
                          1.000
                                                                0.376
                                                                         0.671
##
       UF2
                          1.490
                                   0.219
                                             6.799
                                                      0.000
                                                                0.561
                                                                         0.739
                          0.821
                                                                0.309
##
       FOR
                                   0.126
                                             6.535
                                                      0.000
                                                                         0.591
```

## JW1 1.000	##	JS =~						
## Regressions: ## Regressions: ## CTS	##		1.000				0.786	0.839
## Regressions: ## CTS	##	JW2	1.035	0.081	12.770	0.000	0.814	0.802
## Regressions: ## Estimate Std.Err z-value P(> z) Std.lv Std.lal ## DTP - ## CTS	##	JW3	0.891	0.073	12.145	0.000	0.700	0.749
## DTP - ## CTS	##							
## OTP -	##	Regressions:						
## CTS	##		Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
## CTS	##							
## CTS			-0.131	0.078	-1.681	0.093	-0.124	-0.124
## DTP								
## OTS								
## CTS			-0.365	0.064	-5.664	0.000	-0.470	-0.470
## DTP								
## SWB								
## Covariances: ## Covariances: ## #Covariances: ## #Covariances: ## LUF1 ~~ ## .FOR								
## Covariances: ##		SWB	0.797	0.202	3.946	0.000	0.382	0.382
## UF1		C						
## .UF1 ~~ ## .FOR		Covariances:	Eatimata	C+d Err	~~~~~ <u>~~~</u>	D(> -)	C+4 1	C+4 511
## .FOR		IIE1 ~~	Estimate	Stu.EII	Z-varue	F(> 2)	Sta.IV	Stu.all
## ## Variances: ##			-0 043	0.018	-2 390	0 017	-0 043	-0 243
## Variances: ## EBA		.1 010	0.040	0.010	2.000	0.017	0.040	0.240
## LEBA 0.292 0.043 6.862 0.000 0.292 0.580 ## ST 1.022 0.097 10.496 0.000 1.022 0.580 ## JD1 0.242 0.123 1.965 0.049 0.242 0.242 ## JD1 0.106 0.016 6.783 0.000 0.106 0.311 ## JD2 0.068 0.017 3.975 0.000 0.068 0.183 ## JUF1 0.173 0.025 6.877 0.000 0.106 0.564 ## JUF1 0.173 0.025 6.877 0.000 0.173 0.550 ## JUF2 0.261 0.044 5.970 0.000 0.178 0.651 ## JW1 0.260 0.042 6.231 0.000 0.178 0.661 ## JW2 0.368 0.050 7.394 0.000 0.368 0.357 ## JW3 0.384 0.044 8.692 0.000 0.384 0.439 ## CTS 0.212 0.049 4.285 0.000 1.000 1.000 ## JDTP 0.231 0.031 7.579 0.000 0.384 0.439 ## JSB 0.108 0.025 4.398 0.000 0.763 0.763 ## JSB 0.108 0.025 4.398 0.000 0.763 0.765 ## # SWB		Variances:						
## .EBA		, 42 2411000	Estimate	Std.Err	z-value	P(> z)	Std.lv	Std.all
## .ST		.EBA						
## .MI	##							
## .DA2	##							
## .DA2	##	.DA1	0.106	0.016	6.783	0.000	0.106	0.311
## .UF1	##	.DA2	0.068	0.017			0.068	0.183
## .UF2	##	.DA3	0.300	0.029	10.186	0.000	0.300	0.564
## .FOR	##	.UF1	0.173	0.025	6.877	0.000	0.173	0.550
## .JW1	##	.UF2	0.261	0.044	5.970	0.000	0.261	
## .JW2								
## .JW3								
## CTS								
## .DTP								
## .SWB								
## .JS 0.467 0.066 7.063 0.000 0.755 0.755 ## ## R-Square: ## EBA 0.420 ## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## R-Square: ## Estimate ## EBA 0.420 ## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## R-Square: ## EBA 0.420 ## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703		. JS	0.467	0.066	7.063	0.000	0.755	0.755
## EBA 0.420 ## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703		D-Causes.						
## EBA 0.420 ## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703		n-square.	Estimato					
## ST 0.188 ## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703		FRΔ						
## MI 0.758 ## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## DA1 0.689 ## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## DA2 0.817 ## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## DA3 0.436 ## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## UF1 0.450 ## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## UF2 0.547 ## FOR 0.349 ## JW1 0.703								
## FOR 0.349 ## JW1 0.703	##							
	##							
## JW2 0.643	##	JW1	0.703					
	##	JW2	0.643					

##	JW3	0.561
##	DTP	0.015
##	SWB	0.237
##	JS	0.245