Multivariate Analysis for the Behavioral Sciences, Second Edition (Chapman and Hall/CRC, 2019)

Solutions to Exercises of Chapter 6: Applying Logistic Regression

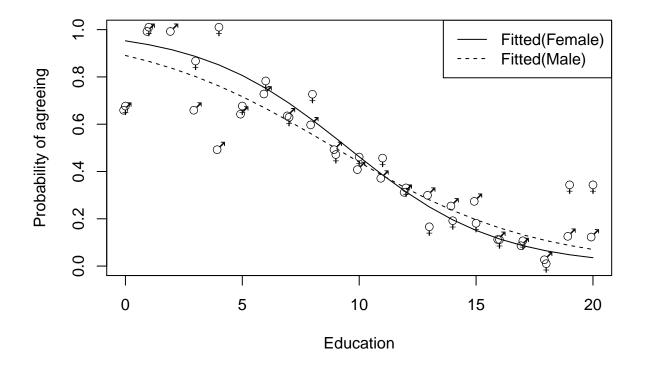
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Solutions

```
womensrole <- structure(list(</pre>
   education = c(OL, 1L, 2L, 3L, 4L, 5L, 6L, 7L, 8L, 9L, 10L, 11L, 12L, 13L, 14L, 15L,
                16L, 17L, 18L, 19L, 20L, 0L, 1L, 2L, 3L, 4L, 5L, 6L, 7L, 8L, 9L, 10L,
                11L, 12L, 13L, 14L, 15L, 16L, 17L, 18L, 19L, 20L),
 2L, 2L, 2L, 2L, 2L, 2L, 2L),
                .Label = c("Male", "Female"), class = "factor"),
 agree = c(4, 2, 4, 6, 5, 13, 25, 27, 75, 29, 32, 36, 115, 31, 28, 9, 15, 3, 1, 2, 3, 4,
          1, 0, 6, 10, 14, 17, 26, 91, 30, 55, 50, 190, 17, 18, 7, 13, 3, 0, 1, 2),
 disagree = c(2, 0, 0, 3, 5, 7, 9, 15, 49, 29, 45, 59, 245, 70, 79, 23, 110, 29, 28, 13, 20,
             2, 0, 0, 1, 0, 7, 5, 16, 36, 35, 67, 62, 403, 92, 81, 34, 115, 28, 21, 2, 4)),
.Names = c("education", "sex", "agree", "disagree"),
row.names = c("1", "2", "3", "4", "5", "6", "7", "8", "9", "10", "11", "12", "13", "14", "15",
"16", "17", "18", "19", "20", "21", "22", "23", "24", "25", "26", "27", "28", "29", "30", "31",
"32", "33", "34", "35", "36", "37", "38", "39", "40", "41", "42"), class = "data.frame")
head(womensrole)
    education sex agree disagree
## 1
           0 Male
           1 Male
           2 Male
## 3
           3 Male
## 5
           4 Male
                     5
                              5
                              7
           5 Male
attach(womensrole)
#main effects model
womensrole_glm <- glm(cbind(agree,disagree) ~ sex + education, family = "binomial")</pre>
summary(womensrole_glm)
##
## Call:
## glm(formula = cbind(agree, disagree) ~ sex + education, family = "binomial")
```

```
##
## Deviance Residuals:
##
       Min
                  1Q
                        Median
                                               Max
## -2.72544 -0.86302 -0.06525
                                           3.13315
                                0.84340
## Coefficients:
              Estimate Std. Error z value Pr(>|z|)
## (Intercept) 2.50937
                          0.18389 13.646
                                            <2e-16 ***
                          0.08415 -0.136
## sexFemale
             -0.01145
                                             0.892
## education -0.27062
                          0.01541 - 17.560
                                            <2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 451.722 on 40 degrees of freedom
## Residual deviance: 64.007 on 38 degrees of freedom
## AIC: 208.07
## Number of Fisher Scoring iterations: 4
#interaction model
womensrole_glm1 <- glm(cbind(agree, disagree) ~ sex * education, family = "binomial")
summary(womensrole_glm1)
##
## glm(formula = cbind(agree, disagree) ~ sex * education, family = "binomial")
## Deviance Residuals:
                        Median
       Min
                  1Q
                                      3Q
                                               Max
                       0.01532
## -2.39097 -0.88062
                                 0.72783
                                           2.45262
## Coefficients:
                      Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                       2.09820 0.23550 8.910 < 2e-16 ***
## sexFemale
                       0.90474
                                  0.36007
                                            2.513 0.01198 *
## education
                      -0.23403
                                  0.02019 -11.592 < 2e-16 ***
## sexFemale:education -0.08138
                                  0.03109 -2.617 0.00886 **
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 451.722 on 40 degrees of freedom
## Residual deviance: 57.103 on 37 degrees of freedom
## AIC: 203.16
## Number of Fisher Scoring iterations: 4
#interaction significant
fitted <- predict(womensrole_glm1, type = "response")</pre>
fittedF <- fitted[sex == "Female"]</pre>
fittedM <- fitted[sex != "Female"]</pre>
```

```
pobsv <- agree / (agree + disagree)
plot(education, pobsv, type = "n", xlab = "Education", ylab = "Probability of agreeing")
text(education, pobsv, ifelse(sex == "Female", "\\VE", "\\MA"), vfont = c("serif", "plain"), cex = 1.25
lines(education[sex == "Female"], fittedF)
lines(education[sex != "Female"], fittedM, lty = 2)
legend("topright", c("Fitted(Female)", "Fitted(Male)"), lty = 1:2)</pre>
```



detach(womensrole)

The interaction shows that, for fewer years of education, women have a higher probability of agreeing with the statement than men, but when the years of education exceed about 10, then this situation reverses.

```
accidents <- structure(list(</pre>
  weight = structure(c(1L, 1L, 1L, 1L, 2L, 2L, 2L, 2L),
                     .Label = c("Small", "Standard"), class = "factor"),
  eject = structure(c(1L, 1L, 2L, 2L, 1L, 1L, 2L, 2L),
                    .Label = c("No", "Yes"), class = "factor"),
  type = structure(c(1L, 2L, 1L, 2L, 1L, 2L, 1L, 2L),
                   .Label = c("Collision", "Rollover"), class = "factor"),
  severely = c(150, 112, 23, 80, 1022, 404, 161, 265),
 nseverely = c(350, 60, 26, 19, 1878, 148, 111, 22)),
.Names = c("weight", "eject", "type", "severely", "nseverely"),
row.names = c(NA, -8L), class = "data.frame")
head(accidents)
##
      weight eject
                        type severely nseverely
## 1
       Small
               No Collision
                                  150
                                             350
                                             60
## 2
       Small
               No Rollover
                                  112
## 3
       Small
              Yes Collision
                                   23
                                              26
                                   80
## 4
       Small Yes Rollover
                                             19
## 5 Standard No Collision
                                 1022
                                            1878
## 6 Standard
              No Rollover
                                            148
                                  404
attach(accidents)
accident_glm <- glm(cbind(severely,nseverely) ~ weight + eject + type, family = "binomial")
summary(accident_glm)
##
## Call:
## glm(formula = cbind(severely, nseverely) ~ weight + eject + type,
      family = "binomial")
##
## Deviance Residuals:
                          3
                                   4
                                            5
                                                     6
                                                                        8
        1
## 0.9445 -0.4631 -0.7447 -1.1072 -0.1301 -0.3219 -0.4458
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                 -0.94006
                             0.08284 -11.348 < 2e-16 ***
## weightStandard 0.33667
                                      3.909 9.26e-05 ***
                             0.08612
## ejectYes
                  1.03036
                             0.09891 10.417 < 2e-16 ***
                             0.08281 19.787 < 2e-16 ***
## typeRollover
                  1.63859
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
```

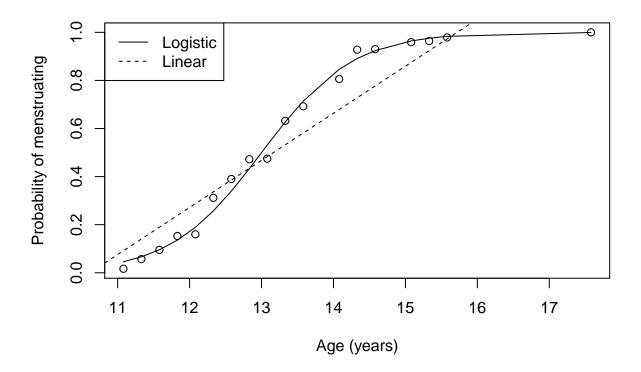
```
## Null deviance: 737.894 on 7 degrees of freedom
## Residual deviance: 7.309 on 4 degrees of freedom
## AIC: 61.976
##
## Number of Fisher Scoring iterations: 4
detach(accidents)
```

```
statistics <- structure(list(</pre>
  result = structure(c(1L, 1L, 2L, 1L, 2L, 2L, 2L, 2L, 2L, 2L,
                       2L, 2L, 2L, 2L, 1L, 2L, 1L, 1L, 2L),
                     .Label = c("Fail", "Pass"), class = "factor"),
  test = c(525, 533, 545, 582, 581, 576, 572, 609, 559, 543,
           576, 525, 574, 582, 574, 471, 595, 557, 557, 584),
  grade = structure(c(2L, 3L, 2L, 1L, 3L, 4L, 2L, 1L, 3L, 4L,
                      2L, 1L, 4L, 3L, 2L, 2L, 3L, 1L, 1L, 1L),
                    .Label = c("A", "B", "C", "D"), class = "factor")),
.Names = c("result", "test", "grade"), row.names = c(NA, -20L), class = "data.frame")
head(statistics)
   result test grade
## 1
     Fail 525
                     В
## 2
      Fail 533
                     C
## 3
      Pass 545
                     В
## 4
      Fail 582
                     Α
## 5
      Pass 581
                     C
## 6
      Pass 576
                     D
tail(statistics)
##
     result test grade
       Pass 574
## 15
## 16
       Fail 471
       Pass 595
## 17
## 18
       Fail 557
                      Α
## 19
       Fail 557
## 20
       Pass 584
                      Α
attach(statistics)
statistics_glm <- glm(result ~ test + grade, family = "binomial")</pre>
summary(statistics_glm)
##
## Call:
## glm(formula = result ~ test + grade, family = "binomial")
##
## Deviance Residuals:
      \mathtt{Min}
           1Q Median
                                  3Q
                                           Max
## -1.4921 -0.4241 0.3154
                             0.4158
                                        2.2950
##
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -32.71260 16.98723 -1.926
                                              0.0541 .
## test
                                               0.0535 .
                 0.05744
                             0.02974
                                       1.931
## gradeB
                  2.35718
                             1.77681
                                       1.327
                                               0.1846
## gradeC
                 1.79580
                            1.67943
                                       1.069
                                               0.2849
```

```
19.11562 3487.42366 0.005 0.9956
## gradeD
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 24.435 on 19 degrees of freedom
## Residual deviance: 14.382 on 15 degrees of freedom
## AIC: 24.382
##
## Number of Fisher Scoring iterations: 17
#find prediction of pass and fail from model and cross tab with actual result
pred <- predict(statistics_glm, type = "response")</pre>
pred[pred > 0.5] <- "P"</pre>
pred[pred <= 0.5] <- "F"</pre>
table(result, pred)
##
        pred
## result F P
##
   Fail 5 1
    Pass 1 13
##
detach(statistics)
```

```
menstruation <- structure(list(</pre>
  age = c(11.08, 11.33, 11.58, 11.83, 12.08, 12.33, 12.58, 12.83, 13.08,
          13.33, 13.58, 14.08, 14.33, 14.58, 15.08, 15.33, 15.58, 17.58),
  bmens = c(2, 5, 10, 17, 16, 29, 39, 51, 47, 67, 81, 79, 90, 93, 117, 107, 92, 1049)
  n = c(120, 88, 105, 111, 100, 93, 100, 108, 99, 106, 117,
        98, 97, 100, 122, 111, 94, 1049)),
.Names = c("age", "bmens", "n"), row.names = c(NA, -18L), class = "data.frame")
menstruation
##
        age bmens
                    n
## 1 11.08
               2 120
## 2 11.33
                   88
               5
## 3 11.58
               10 105
## 4 11.83
              17 111
## 5 12.08
              16 100
## 6 12.33
              29
                  93
## 7 12.58
              39 100
              51 108
## 8 12.83
## 9 13.08
              47
                  99
## 10 13.33
              67 106
## 11 13.58
              81 117
## 12 14.08
              79
                  98
## 13 14.33
              90
                  97
## 14 14.58
              93 100
## 15 15.08
              117 122
## 16 15.33
              107 111
## 17 15.58
              92
                   94
## 18 17.58 1049 1049
attach(menstruation)
menstruation_reg <- glm(cbind(bmens, n-bmens) ~ age, family = "binomial")</pre>
summary(menstruation_reg)
##
## Call:
## glm(formula = cbind(bmens, n - bmens) ~ age, family = "binomial")
##
## Deviance Residuals:
##
       Min
                1Q
                    Median
                                  3Q
                                          Max
## -1.7447 -0.6822 -0.1522 0.7488
                                        1.2276
##
## Coefficients:
##
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -20.56351
                            0.88838 -23.15
                                             <2e-16 ***
                                             <2e-16 ***
## age
                 1.58172
                            0.06823
                                    23.18
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 1990.93
                               on 17
                                      degrees of freedom
##
## Residual deviance:
                        13.72
                               on 16 degrees of freedom
## AIC: 88.204
##
## Number of Fisher Scoring iterations: 4
plot(age, bmens/n, xlab = "Age (years)", ylab = "Probability of menstruating")
abline(lm(bmens/n ~ age), lty = 2)
lines(age, predict(menstruation_reg, type = "response"))
legend("topleft", c("Logistic", "Linear"), lty = 1:2)
```



detach(menstruation)

This shows why the linear model is useless and the logistic model is not.