

# FORMAL LANGUAGE AND AUTOMATA THEORY

## IT 305

TIME ALLOTTED: 3 HOURS

FULL MARKS: 70

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words as far as practicable*

**GROUP – A**  
**(Multiple Choice Type Questions)**

1. Answer any **ten** from the following, choosing the correct alternative of each question: **10×1=10**

SL	Question	Marks	Co	Blooms Taxonomy Level
(i)	The production of the form $A \rightarrow B$ , where A and B are non-terminals is called a) Null production b) Unit production c) Greibach Normal Form d) Chomsky Normal Form	1	CO1, CO3	Knowledge, Comprehension
(ii)	Which of the production rule can be accepted by Chomsky grammar? a) $A \rightarrow BC$ b) $A \rightarrow a$ c) $S \rightarrow e$ d) All of these	1	CO1, CO3	Knowledge, Comprehension
(iii)	A Language for which no DFA exist is a _____ a) Regular Language b) Non-Regular Language c) May be Regular d) none of these	1	CO1, CO3	Knowledge, Comprehension
(iv)	A context free grammar can be recognized by a) Push down automata b) 2 way linearly bounded automata c) Turing Machine d) Finite Automata	1	CO3	Application
(v)	Given: $L1 = \{x \in \Sigma^*   x \text{ contains even no's of 0's}\}$ $L2 = \{x \in \Sigma^*   x \text{ contains odd no's of 1's}\}$ No of final states in Language $L1 \cup L2$ ? a) 1 b) 2 c) 3 d) 4	1	CO3	Comprehension

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(vi)	Regular expression for all strings starts with ab and ends with bba is. a) $aba^*b^*bba$ b) $ab(ab)^*bba$ c) $ab(a+b)^*bba$ d) All of the mentioned	1	CO3	Comprehension
(vii)	$RR^*$ can be expressed in which of the forms: a) $R^+$ b) $R^-$ c) $R^+ \cup R^-$ d) $R$	1	CO3	Comprehension
(viii)	A turing machine operates over: a) finite memory tape b) infinite memory tape c) depends on the algorithm d) none of the mentioned	1	CO3	Application
(ix)	Push down automata accepts _____ languages. a) Type 3 b) Type 2 c) Type 1 d) Type 0	1	CO3	Application
(x)	Which among the following looks similar to the given expression? $((0+1).(0+1))^*$ a) $\{x \in \{0,1\}^* \mid x \text{ is all binary number with even length}\}$ b) $\{x \in \{0,1\} \mid x \text{ is all binary number with even length}\}$ c) $\{x \in \{0,1\}^* \mid x \text{ is all binary number with odd length}\}$ d) $\{x \in \{0,1\} \mid x \text{ is all binary number with odd length}\}$	1	CO1, CO3	Knowledge, Comprehension
(xi)	Simplify the following regular expression: $\epsilon + 1^*(011)^*(1^*(011)^*)^*$ a) $(1+011)^*$ b) $(1^*(011)^*)^*$ c) $(1+(011)^*)^*$ d) $(1011)^*$	1	CO3	Comprehension
(xii)	In Moore machine, output is produced over the change of: a) transitions b) states c) inputs d) none of these	1	CO1, CO2	Knowledge

**GROUP – B**  
**(Short Answer Type Questions)**  
**(Answer any three of the following) 3 x 5 = 15**

- | SL                | Question   | Marks            | Co  | Blooms Taxonomy Level                 |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
|-------------------|--|------------------|-----|---------------------------------------|-------------------|-------|-------|-------|-------|-------|-------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--|--|--|
| 2.                | Define Left factoring & Left recursion with proper example.  | 5                | CO3 | Knowledge, Comprehension              |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| 3.                | Construct a minimum state automaton equivalent to the finite automaton given in the table below.   | 5                | CO3 | Knowledge, Comprehension              |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
|                   | <table border="1" style="margin: auto; border-collapse: collapse;"> <thead> <tr> <th style="padding: 5px;">State / <math>\Sigma</math></th> <th style="padding: 5px;">0</th> <th style="padding: 5px;">1</th> </tr> </thead> <tbody> <tr> <td style="padding: 5px;"><math>\rightarrow q_0</math></td> <td style="padding: 5px;"><math>q_1</math></td> <td style="padding: 5px;"><math>q_5</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_1</math></td> <td style="padding: 5px;"><math>q_6</math></td> <td style="padding: 5px;"><math>q_2</math></td> </tr> <tr> <td style="padding: 5px;"><math>\odot q_2</math></td> <td style="padding: 5px;"><math>q_0</math></td> <td style="padding: 5px;"><math>q_2</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_3</math></td> <td style="padding: 5px;"><math>q_2</math></td> <td style="padding: 5px;"><math>q_6</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_4</math></td> <td style="padding: 5px;"><math>q_7</math></td> <td style="padding: 5px;"><math>q_5</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_5</math></td> <td style="padding: 5px;"><math>q_2</math></td> <td style="padding: 5px;"><math>q_6</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_6</math></td> <td style="padding: 5px;"><math>q_6</math></td> <td style="padding: 5px;"><math>q_4</math></td> </tr> <tr> <td style="padding: 5px;"><math>q_7</math></td> <td style="padding: 5px;"><math>q_6</math></td> <td style="padding: 5px;"><math>q_2</math></td> </tr> </tbody> </table> | State / $\Sigma$ | 0   | 1                                     | $\rightarrow q_0$ | $q_1$ | $q_5$ | $q_1$ | $q_6$ | $q_2$ | $\odot q_2$ | $q_0$ | $q_2$ | $q_3$ | $q_2$ | $q_6$ | $q_4$ | $q_7$ | $q_5$ | $q_5$ | $q_2$ | $q_6$ | $q_6$ | $q_6$ | $q_4$ | $q_7$ | $q_6$ | $q_2$ |  |  |  |
| State / $\Sigma$  | 0  | 1                |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $\rightarrow q_0$ | $q_1$  | $q_5$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_1$             | $q_6$  | $q_2$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $\odot q_2$       | $q_0$  | $q_2$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_3$             | $q_2$  | $q_6$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_4$             | $q_7$  | $q_5$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_5$             | $q_2$  | $q_6$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_6$             | $q_6$  | $q_4$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| $q_7$             | $q_6$  | $q_2$            |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| 4.                | Consider G whose productions are:<br>$S \rightarrow aAS \mid a, A \rightarrow SbA \mid SS \mid ba$<br>For the string aabbbaa, find leftmost derivation, rightmost derivation and derivation tree.  | 5                | CO3 | Knowledge, Comprehension, Application |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| 5.                | Minimize the states in the DFA depicted in the following diagram:  | 5                | CO3 | Knowledge, Comprehension              |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
|                   |  |                  |     |                                       |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |
| 6.                | Explain classification of languages and their relations  | 5                | CO3 | Knowledge, Comprehension              |                   |       |       |       |       |       |             |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |       |  |  |  |

**GROUP – C**  
**(Long Answer Type Questions)**  
**(Answer any three of the following) 3 x 15 = 45**

SL	Question	Marks	Co	Blooms Taxonomy Level																							
7.	(i) State & Prove Arden's Theorem.	5	CO2	Comprehension																							
	(ii) What is <i>ambiguous grammar</i> ? Comment on the ambiguity of the following grammar. Justify your answer with an example. $S \rightarrow SS, S \rightarrow a$ , where $S \in N, a \in T$ $L(G) = \{a^n \mid n \geq 1\}$	2 + 3	CO2, CO3, CO5	Knowledge, Application																							
	(iii) Convert the following Moore machine into Mealy machine:	5	CO1, CO3	Knowledge, Application																							
	<table border="1"><thead><tr><th rowspan="2">PRESENT STATE</th><th colspan="2">NEXT STATE</th><th rowspan="2">OUTPUT</th></tr><tr><th>a = 0</th><th>a = 1</th></tr></thead><tbody><tr><td><math>\rightarrow q_1</math></td><td><math>q_1</math></td><td><math>q_2</math></td><td>0</td></tr><tr><td><math>q_2</math></td><td><math>q_1</math></td><td><math>q_3</math></td><td>0</td></tr><tr><td><math>q_3</math></td><td><math>q_1</math></td><td><math>q_3</math></td><td>1</td></tr></tbody></table>	PRESENT STATE	NEXT STATE		OUTPUT	a = 0	a = 1	$\rightarrow q_1$	$q_1$	$q_2$	0	$q_2$	$q_1$	$q_3$	0	$q_3$	$q_1$	$q_3$	1								
PRESENT STATE	NEXT STATE		OUTPUT																								
	a = 0	a = 1																									
$\rightarrow q_1$	$q_1$	$q_2$	0																								
$q_2$	$q_1$	$q_3$	0																								
$q_3$	$q_1$	$q_3$	1																								
8.	(i) Explain Chomsky Normal Form or CNF of grammar with an example.	3	CO1, CO3	Knowledge, Application																							
	(ii) Convert the following grammar into CNF – $S \rightarrow aAD, A \rightarrow aB \mid bAB, B \rightarrow b, D \rightarrow d$	4	CO1, CO3	Knowledge, Application																							
	(iii) Find the equivalence class partition of the machine shown below:	8	CO1, CO3	Knowledge, Application																							
	<table border="1"><thead><tr><th rowspan="2">PRESENT STATE</th><th colspan="2">NEXT STATE, z</th></tr><tr><th>x=0</th><th>x=1</th></tr></thead><tbody><tr><td>A</td><td>E,0</td><td>D,1</td></tr><tr><td>B</td><td>F,0</td><td>D,0</td></tr><tr><td>C</td><td>E,0</td><td>B,1</td></tr><tr><td>D</td><td>F,0</td><td>B,0</td></tr><tr><td>E</td><td>C,0</td><td>F,1</td></tr><tr><td>F</td><td>B,0</td><td>C,0</td></tr></tbody></table>	PRESENT STATE	NEXT STATE, z		x=0	x=1	A	E,0	D,1	B	F,0	D,0	C	E,0	B,1	D	F,0	B,0	E	C,0	F,1	F	B,0	C,0			
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9.	(i) Construct a DFA equivalent to the NDFA given in the table below.	6	CO2, CO3	Knowledge, Comprehension																							
	<table border="1"><thead><tr><th>State / <math>\Sigma</math></th><th>a</th><th>b</th></tr></thead><tbody><tr><td><math>\rightarrow q_0</math></td><td><math>q_0, q_1</math></td><td><math>q_0</math></td></tr><tr><td><math>q_1</math></td><td><math>q_2</math></td><td><math>q_1</math></td></tr><tr><td><math>q_2</math></td><td><math>q_3</math></td><td><math>q_3</math></td></tr><tr><td><math>\odot q_3</math></td><td></td><td><math>q_2</math></td></tr></tbody></table>	State / $\Sigma$	a	b	$\rightarrow q_0$	$q_0, q_1$	$q_0$	$q_1$	$q_2$	$q_1$	$q_2$	$q_3$	$q_3$	$\odot q_3$		$q_2$											
State / $\Sigma$	a	b																									
$\rightarrow q_0$	$q_0, q_1$	$q_0$																									
$q_1$	$q_2$	$q_1$																									
$q_2$	$q_3$	$q_3$																									
$\odot q_3$		$q_2$																									
	(ii) Simplify the given grammar: $S \rightarrow aXb$	5	CO3	Application																							

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$X \rightarrow aXb \mid e$

	(iii)	What do you mean by unit production? Explain with an example.	4	CO1, CO2	Knowledge, Comprehension
10.	(i)	Prove that $(1+00^*1) + (1+00^*1)(0+10^*1)^*(0+10^*1) = 0^*1(0+10^*1)^*$	3	CO2, CO3	Knowledge, Comprehension
	(ii)	Explain Merger Graph with example	4	CO3	Knowledge, Comprehension, Application
	(iii)	Convert the following grammar into GNF - $S \rightarrow AB, A \rightarrow BS \mid b, B \rightarrow SA \mid a$	8	CO3	Application
11.	(i)	Define Push Down Automata.	2	CO2	Knowledge
	(ii)	Construct a push down automata for the language $L = \{ww^R \mid w \in \{a,b\}^*\}$	6	CO3, CO4	Application
	(iii)	What is derivation tree?	2	CO2, CO3	Knowledge
	(iv)	Convert the following grammar into CNF - $S \rightarrow aAD, A \rightarrow aB \mid bAB, B \rightarrow b, D \rightarrow d$	5	CO1, CO3	Knowledge, Comprehension
12.	(i)	Using Pumping Lemma check whether $L = \{a^n b^n \mid n \geq 1\}$ is regular or not.	5	CO3	Knowledge, Application
	(ii)	Construct a PDA accepting the set of all strings over $\{a,b\}$ with equal number of a's followed by equal number of b's.	5	CO3, CO4	Application
	(iii)	Find the highest type number of the following production rules - $S \rightarrow ASB \mid d, A \rightarrow aA, S \rightarrow aA \mid c, A \rightarrow ac, aAbcD \rightarrow abcDbcD$	5	CO1, CO3	Application