



## Code Generation & Optimization for Deep-Learning Computations via Multi-Dimensional Homomorphisms

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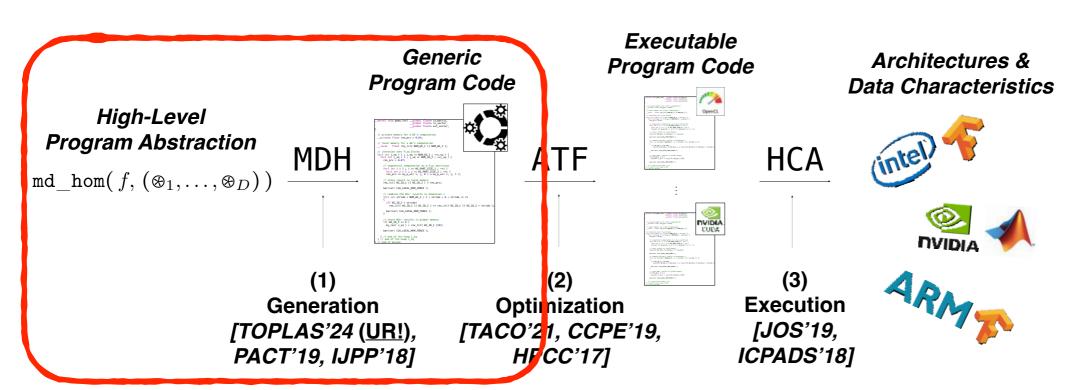
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#### Who are we?





We are the developers of the MDH+ATF+HCA approaches:







Richard Schulze

#### **Focus Today**

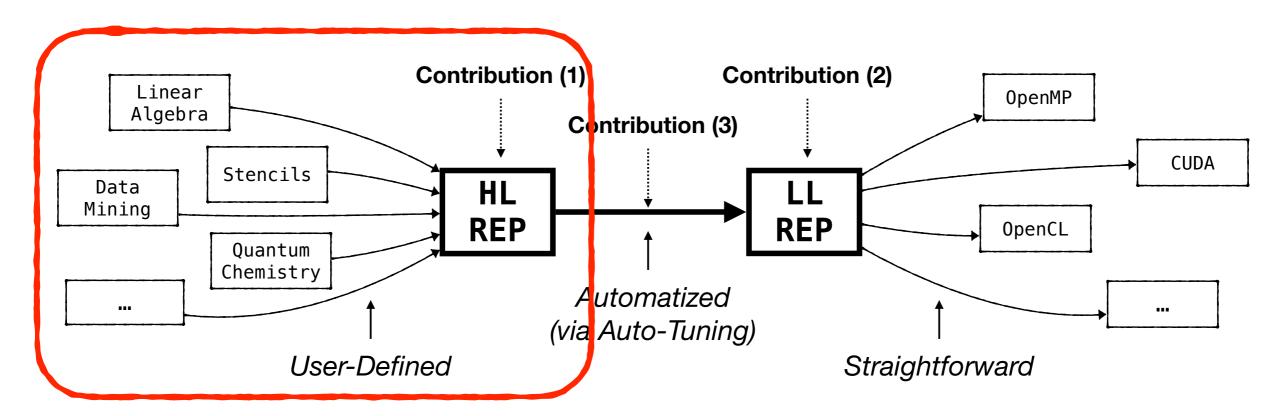
A holistic approach to code *generation* (MDH) & *optimization* (ATF) & *execution* (HCA):

- (1) MDH (Multi-Dimensional Homomorphisms): How to generate automatically optimizable (auto-tunable) code?
- (2) ATF (Auto-Tuning Framework): How to optimize (auto-tune) code?
- (3) HCA (Host Code Abstraction): How to execute code on (distr.) multi-dev. systems?



**Ari Rasch** 

## The MDH Approach



#### **Focus Today**

#### The MDH approach [1] (formally) introduces:

- (1) <u>High-Level Program Representation</u> for conveniently expressing data-parallel computations, agnostic from hardware and optimization details
- (2) <u>Low-Level Program Representation</u> that expresses device- and data-optimized de- and re-composition strategies of computations & straightforwardly transformable to executable program code
- (3) Lowering Process that fully automatically lowers a high-level MDH program to a device- and dataoptimized low-level MDH program (based on auto-tuning [2])
- [1] "(De/Re)-Composition of Data-Parallel Computations via Multi-Dimensional Homomorphisms" (under review at ACM TOPLAS)
- [2] "Efficient Auto-Tuning of Parallel Programs with Interdependent Tuning Parameters via Auto-Tuning Framework (ATF)", TACO'21

#### **Goals:**

#### 1. Uniform:

should be able to express any kind of data-parallel computation, but without relying on computation-specific building blocks, extensions, etc.

#### 2. Minimalistic:

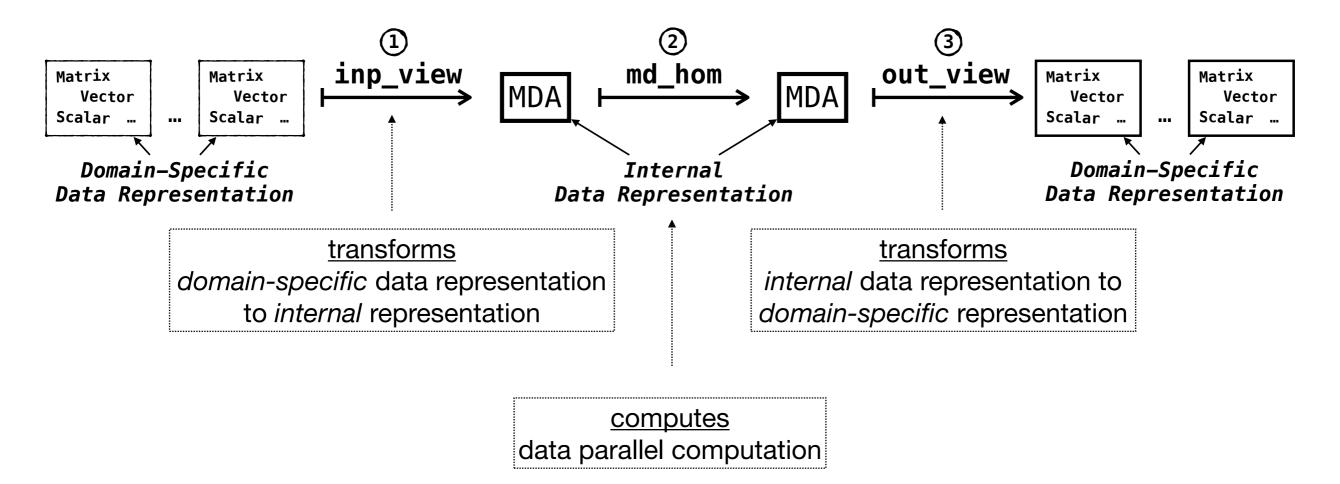
should rely on less building blocks to keep language small and simple

#### 3. Structured:

avoiding compositions and nestings of building blocks as much as possible, thereby further contributing to usability and simplicity of our language

While still capturing all information relevant for generating high performing program code, in a hardware- and data-agnostic manner

#### Overview:



Our high-level representation expresses any data-parallel computation

— agnostic from hardware and optimization details

using exactly three higher-order functions only

The MDH's high-level program representation illustrated:

MDH High-Level Representation for MatVec

#### What is happening here:

- inp\_view captures the accesses to input data
- md\_hom expresses the data-parallel computation
- out\_view captures the accesses to output data

md_hom	f	$  \circledast_1, \dots, \circledast_D  $
Fill	id	+,,+
ExpandDims<0>	id	+,,+
ExpandDims<1>	id	++,,++
ExpandDims<0,1>	id	++,,++
÷	:	:
Transpose< $\sigma$ >	id	++,,++
Exp	exp	+,,+
Mul	*	++,,++
BiasAdd <nhwc></nhwc>	+	++,++,++
BiasAdd <nchw></nchw>	+	++, ++, ++, ++
Range	$(s,d,i) \mapsto (s+d*i)$	+

CC-Based Operators
(computations specification)

md_hom	f	$\circledast_1, \dots, \circledast_D$
MatMul <f,f></f,f>	*	++,++,+
MatMul <f,t></f,t>	*	++,++,+
MatMul <t,f></t,f>	*	++,++,+
MatMul <t,t></t,t>	*	++,++,+
BatchMatMul <f,f></f,f>	*	++,,++,+
:	:	i :
BiasAddGrad <nhwc></nhwc>	id	+,+,+,++
BiasAddGrad <nchw></nchw>	id	+, ++, +, +
CheckNumerics	$(x)\mapsto (x==\mathtt{NaN})$	$\vee, \dots, \vee$
Sum<0> <f></f>	id	+,++,++,,++
Sum<0> <t></t>	id	+, ++, ++, , ++
Sum<1> <f></f>	id	$  \  \  ++,+,++,\dots,++$
Sum<0,1> <f></f>	id	+,+,+,,++
:	:	:
Prod<0> <f></f>	id	*, ++, ++, , ++
:	:	:
A11<0> <f></f>	id	&&, ++, ++, , ++
i l	:	i i

CT-Based Operators (computations specification)

	]	out_view	
Views	$I_1$	$I_2$	0
Fill	$(i_1,\ldots,i_D)\mapsto ()$	/	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$
ExpandDims<0>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto (0,i_1,i_2,\ldots,i_D)$
ExpandDims<0>	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$	/	$ (i_1,\ldots,i_D) \mapsto (i_1,0,i_2,\ldots,i_D) $
ExpandDims<0,1>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto (0,0,i_1,\ldots,i_D)$
÷	:	<u>:</u>	:
Transpose< $\sigma$ >	$(i_1,\ldots,i_D)\mapsto (\sigma(i_1),\ldots,\sigma(i_D))$	/	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$
Exp	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$
	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$
Mul	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$	$(i_1, \ldots, i_D) \mapsto (i_1, \ldots, i_{k-1}, i_{k+1}, \ldots, i_D)$	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$
	<u>:</u>	:	<u>:</u>
BiasAdd <nhwc></nhwc>	$(n,h,w,c)\mapsto (n,h,w,c)$	$(n,h,w,c)\mapsto(c)$	$(n,h,w,c)\mapsto (n,h,w,c)$
BiasAdd <nchw></nchw>	$(n,c,h,w) \mapsto (n,c,h,w)$	$(n,c,h,w) \mapsto (c)$	$(n,c,h,w) \mapsto (n,c,h,w)$
Range	$(i) \mapsto ()$	$(i) \mapsto ()$	$(i) \mapsto (i)$

CC-Based Operators (data-access specification)

	inp	out_view	
Views	$I_1$	$I_2$	O
MatMul <f,f></f,f>	$(i,j,k) \mapsto (i,k)$	$(i,j,k)\mapsto (k,j)$	$(i,j,k) \mapsto (i,j)$
MatMul <f,t></f,t>	$(i,j,k) \mapsto (i,k)$	$(i,j,k) \mapsto (j,k)$	$(i,j,k) \mapsto (i,j)$
<pre>MatMul<t,f></t,f></pre>	$(i,j,k) \mapsto (k,i)$	$(i,j,k) \mapsto (k,j)$	$(i,j,k) \mapsto (i,j)$
<pre>MatMul<t,t></t,t></pre>	$(i,j,k) \mapsto (k,i)$	$(i,j,k) \mapsto (j,k)$	$(i,j,k) \mapsto (i,j)$
BatchMatMul <f,f></f,f>	$(b_1,\ldots,i,j,k)\mapsto (b_1,\ldots,i,k)$	$(b_1,\ldots,i,j,k)\mapsto (b_1,\ldots,k,j)$	$(b_1,\ldots,i,j,k)\mapsto (b_1,\ldots,i,j)$
:	:	:	:
BiasAddGrad <nhwc></nhwc>	$(n,h,w,c)\mapsto (n,h,w,c)$	/	$(n,h,w,c)\mapsto (n,h,w)$
BiasAddGrad <nchw></nchw>	$(n,c,h,w) \mapsto (n,c,h,w)$	/	$(n,c,h,w) \mapsto (n,h,w)$
CheckNumerics	$(i_1,\ldots,i_D)\mapsto (i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto ()$
Sum<0> <f></f>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto(i_2,\ldots,i_D)$
Sum<0> <t></t>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$ (i_1,\ldots,i_D) \mapsto (0,i_2,\ldots,i_D) $
Sum<1> <f></f>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$ (i_1,\ldots,i_D) \mapsto (i_1,i_3,\ldots,i_D) $
Sum<0,1> <f></f>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto(i_3,\ldots,i_D)$
:	:	<u>:</u>	:
Prod<0> <f></f>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto(i_2,\ldots,i_D)$
<u>:</u>	<u>:</u>	<b>:</b>	: :
All<0> <f></f>	$(i_1,\ldots,i_D)\mapsto(i_1,\ldots,i_D)$	/	$(i_1,\ldots,i_D)\mapsto(i_2,\ldots,i_D)$
:	<u>:</u>	<b>:</b>	<u>:</u>

CT-Based Operators (data-access specification)

Our high-level representation is capable of expressing important DL operators

## **Experimental Results for DL Operators**

					NVIDIA	Ampere G	PU			
Deep		ResNe	et-50			VGG	-16		Mobi	leNet
Learning	Trai	ning	Infe	Inference		Training		rence	Training	Inference
	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MCC
TVM+Ansor	1.00	1.26	1.05	2.22	0.93	1.42	0.88	1.14	0.94	1.00
PPCG	3456.16	8.26	_	7.89	1661.14	7.06	5.77	5.08	2254.67	7.55
PPCG+ATF	3.28	2.58	13.76	5.44	4.26	3.92	9.46	3.73	3.31	10.71
cuDNN	0.92	-	1.85		1.22	-	1.94	-	1.81	2.14
cuBLAS	_	1.58	_	2.67	-	0.93	-	1.04	_	-
cuBLASEx	_	1.47	_	2.56	_	0.92	_	1.02	_	_
cuBLASLt	_	1.26	-	1.22	_	0.91	-	1.01	-	_

					Intel 9	Skylake C	PU			
Deep		ResN	et-50			VGG	-16		MobileNet	
Learning	Trai	ning	Inference		Training		Inference		Training	Inference
	MCC	MatMul	МСС	MatMul	MCC	MatMul	MCC	MatMul	MCC	MCC
TVM+Ansor	1.53	1.05	1.14	1.20	1.97	1.14	2.38	1.27	3.01	1.40
Pluto	355.81	49.57	364.43	13.93	130.80	93.21	186.25	36.30	152.14	75.37
Pluto+ATF	13.08	19.70	170.69	6.57	3.11	6.29	53.61	8.29	3.50	25.41
oneDNN	0.39	-	5.07	-	1.22	-	9.01	_	1.05	4.20
oneMKL	_	0.44	-	1.09	-	0.88	-	0.53	-	_
oneMKL(JIT)	_	6.43	-	8.33	-	27.09	-	9.78	_	_

					NVIDIA	Volta GF	PU			
Deep		ResNe	et-50			VGG	-16		MobileNet	
Learning	Trai	ning	Infe	Inference		Training		Inference		Inference
	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MCC
TVM+Ansor	0.75	1.21	0.72	1.79	1.00	1.11	1.06	1.00	1.00	1.00
PPCG	1976.38	5.88	_	5.64	994.16	3.41	8.21	2.51	1411.92	7.26
PPCG+ATF	3.43	3 <b>.</b> 54	3.42	4.93	3.85	3.15	8.13	2.05	3.49	3.56
cuDNN	1.21	-	1.29	-	2.80	-	3.50	-	2.32	3.14
cuBLAS	_	1.33	-	1.14	-	1.09	-	1.04	-	-
cuBLASEx	_	1.21	-	1.07	-	1.04	-	1.03	-	-
cuBLASLt	_	1.00	_	1.07	-	1.04	-	1.02	-	-

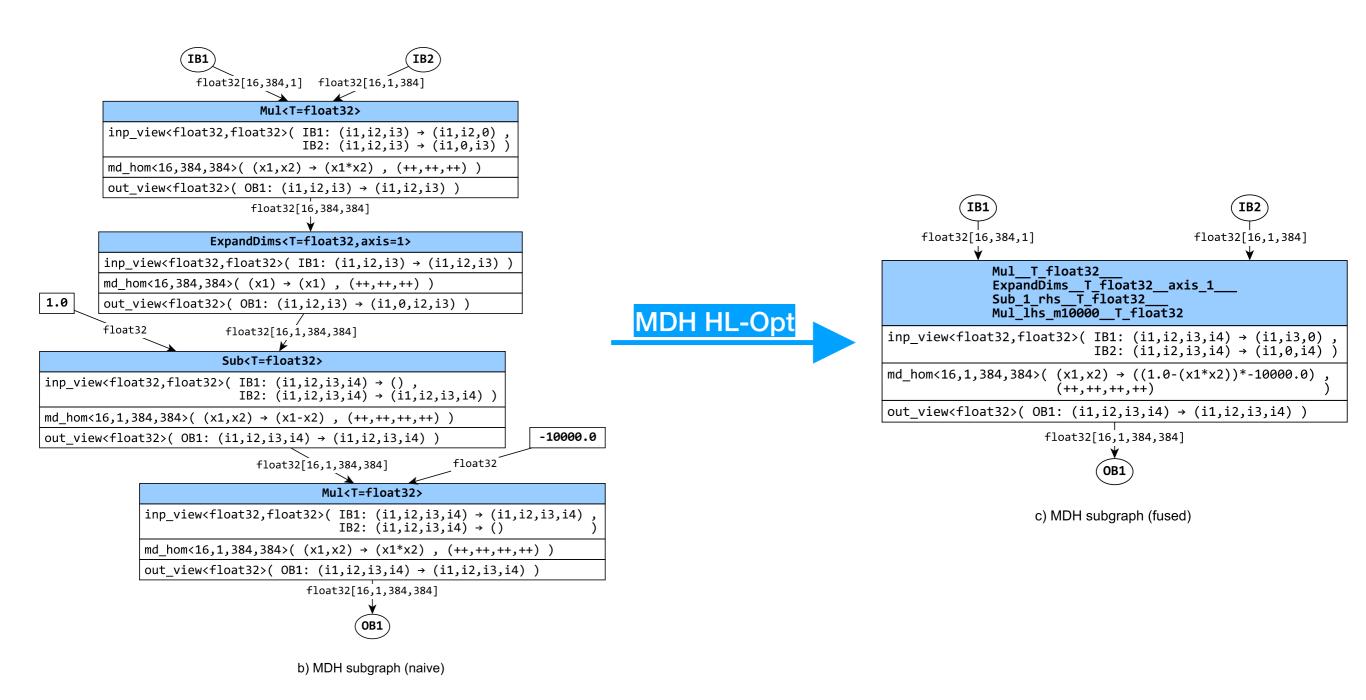
	Intel Broadwell CPU											
Deep		ResNe	et-50			VGG	-16		Mobi	leNet		
Learning	Trai	ning	Infe	rence	Training		Inference		Training	Inference		
	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MatMul	MCC	MCC		
TVM+Ansor	1.53	1.60	1.29	1.53	1.32	1.00	1.27	1.02	2.42	1.92		
Pluto	4349.20	40.41	137.21	15.96	1865.07	53.57	113.40	24.10	2255.00	53.85		
Pluto+ATF	6.43	8.93	61.60	6.91	5.07	4.38	42.63	4.45	6.43	29.18		
oneDNN	1.30	-	1.81	-	2.94	-	2.85	-	1.83	4.47		
oneMKL	_	1.45	_	1.36	-	1.35	_	0.50	-	-		
oneMKL(JIT)	_	19.78	_	9.77	-	50.58	_	10.70	_	-		

We achieve encouraging experimental results for DL Operators [1]

## **Excursion:** MDH High-Level Optimization



An optimization is considered *High Level* iff it operators on *MDH's High-Level Representation*:



We exploit the uniform MDH representation to analyze and fuse the DL graph

## **Experimental Results for DL Graphs**



	NVIDIA Ampere GPU									
	Number of	On a restore O a survivir or in Outh suremb	Runtime	Speedup over TF						
	Operators	Operators Occurring in Subgraph	Share	MDH	TC					
1.	13	(Sub,1),(Mul,5),(AddV2,4),(RealDiv,1),(Sqrt,1),(Square,1)	25.96%	65.93	45.72					
2.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	11.40%	30.99	30.50					
3.	41	(BiasAddGrad,1),(AddN,1),(Mul,17),(TanhGrad,2),(Pow,4),(AddV2,4),(Tanh,3),(BiasAdd,9),(Sub,1)	3.79%	1.41	0.05					
4.	3	(Mul,1),(Reshape,1),(AddV2,1)	3.60%	23.79	14.72					
5.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	2.87%	6.79	6.73					
3.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	2.70%	6.36	6.24					
7.	2	(BiasAddGrad,1),(Reshape,1),(Transpose,1)	2.64%	9.86	0.57					
3.	5	(BiasAddGrad,1),(Mul,2),(Reshape,1),(Cast,1),(GreaterEqual,1)	2.45%	4.55	1.60					
9.	13	(Sub,1),(Mul,5),(AddV2,4),(RealDiv,1),(Sqrt,1),(Square,1)	2.40%	39.57	36.93					
0.	9	(AddV2,2),(Mul,3),(Cast,1),(BiasAdd,1),(GreaterEqual,1),(Reshape,1)	1.47%	1.63	1.60					
$\Box$		Total Speed	up over TF:	2.29	0.79					

		Intel Skylake CPU		
	Number of	Out a market and Out a market	Runtime	Speedup over TF
	Operators	Operators Occurring in Subgraph	Share	MDH
1.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	17.33%	571.14
2.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	7.20%	248.81
3.	9	(AddV2,2),(Mul,3),(Cast,1),(BiasAdd,1),(GreaterEqual,1),(Reshape,1)	6.94%	110.51
4.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	6.06%	199.32
5.	8	(Mul,4),(Cast,1),(Softmax_Div,1),(GreaterEqual,1),(AddV2,1)	5.45%	12.76
6.	11	(Mul,6),(Sub,1),(Softmax_Div,1),(AddV2,1),(Cast,1),(GreaterEqual,1)	5.20%	10.81
7.	41	(BiasAddGrad,1),(AddN,1),(Mul,17),(TanhGrad,2),(Pow,4),(AddV2,4),(Tanh,3),(BiasAdd,9),(Sub,1)	3.71%	2.82
8.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	1.50%	24.77
9.	2	(Transpose,1),(Reshape,1)	0.59%	12.08
10.	15	(Sub,1),(Mul,6),(AddV2,5),(RealDiv,1),(Sqrt,1),(Square,1)	0.42%	875.92
		Total Speed	up over TF:	2.11

We achieve encouraging experimental results also for <u>DL Graphs</u> with MDH

### **Excursion: MDH in MLIR**

MLIR is a compiler framework that offers a solid, uniform infrastructure for compiler developers to conveniently design and implement *Domain-Specific Languages (DSLs)* (a.k.a. *dialect* in MLIR terminology)





Implemented by Jens & Lars Hunch (University of Muenster, Germany)

```
func.func @main()
 %M = memref.alloc() : memref<128x64xf32>
 %v = memref.alloc() : memref<64xf32>
  %w = mdh.compute "mdh_matvec"
    inp_view =
       affine_map<( i,k ) ->
       affine map<( i,k )
   md_hom =
      scalar func = @mul,
      combine_ops = [ "cc", ["pw",@add] ]
   },
    out_view =
       affine_map<( i,k ) -> ( i )> ]
    inp_types = [ f32, f32 ],
   mda size = [128,64],
   out\_types = [f32]
  }( %A,%B ):( memret<128x04x132>, memret<04xf32> )
               -> memref<128xf32>
  return
```





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# We look forward to discussions at the poster session









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