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 A Turing machine is a mathematical model of computation that defines an abstract machine, which manipulates symbols on a strip of tape according to a table of rules. Despite the model's simplicity, given any computer algorithm, a Turing machine capable of simulating that algorithm's logic can be constructed.

Source: https://en.wikipedia.org/wiki/Turing_machine

 Church's thesis states that any real-world computation can be translated into an equivalent computation involving a Turing machine. In Church's original formulation (Church 1935, 1936), the thesis says that real-world calculation can be done using the lambda calculus, which is equivalent to using general recursive functions.

Source: https://mathworld.wolfram.com/Church-TuringThesis.html

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 - Variables = values (assignments)
 - If conditions
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- What is wrong? Side effects

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int x = 10;

f(x); (Corrected from video)

cout << x;
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NO, unless you check the internal code of function "f" since it could have changed the value of "x"

• Consider another example in Python:

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l = [1, 2, 3]
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TOO COMPLICATED TO DEBUG

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$$2 \rightarrow 4 \text{ (Corrected from video)}$$
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Can do more:

- Change value of x
- Delete file
- Update Database
- Same input can give different result based on time

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 - Control over the order of execution is of low importance.

- Functional languages such as Lisp, Scheme, FP, ML, Miranda, and Haskell are an attempt to realize Church's lambda calculus in practical form as a programming language
- The key idea: do everything by composing functions
 - no mutable state
 - no side effects