

# Problem Set Assignment No. 2

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```
## Keep this line always
knitr::opts_chunk$set(echo = TRUE,
                      collapse = TRUE,
                      warning = FALSE, message = FALSE,
                      fig.align = 'center')
```

## 1. Setup your document

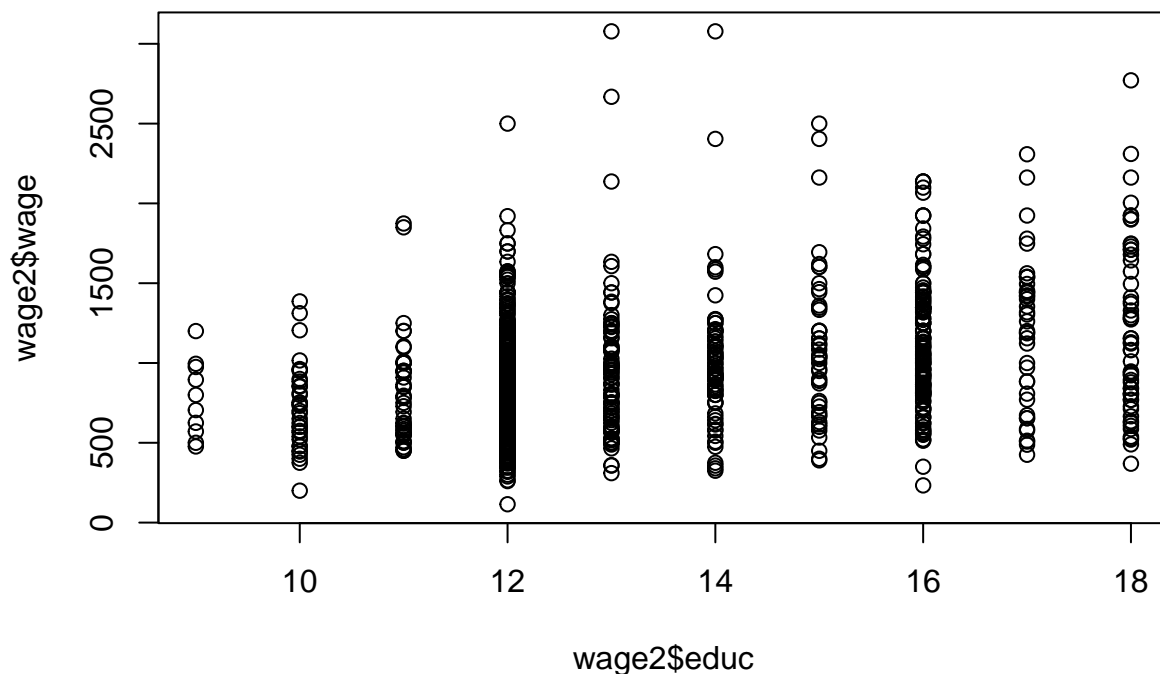
### A. Load Libraries

```
library(knitr)
library(wooldridge)
wage2=wooldridge::wage2
```

## 2. Single Variable Regression.

### A. Plot the relationship

```
plot(wage2$educ, wage2$wage)
```



Does there seem to be a relationship in the data between education and wage? If we were to “eyeball” a line, would it be upward sloping or downward sloping? What does economic theory tell us we should expect?

There seems to be a roughly positive linear relationship between education in wage. An eyeballed line would be upward sloping, which follows economic theory that years of education is an effective signal to employers of a worker’s ability, thus corresponding to a higher wage.

**B. Calculate wage-bar and educ-bar.**

```
wagebar=mean(wage2$wage)
educbar=mean(wage2$educ)
```

What is the mean of wage?

957.9455.

**C. Calculate the sample variance of educ**

```
a=wage2$educ-educbar
wage2$a<-a
n=nrow(wage2)-1
svar_educ=(1/n)*sum(a^2)
print(svar_educ)
## [1] 4.825288
```

What is the sample variance of educ?

4.825288

#### D. Repeat 2B and 2C, but for wage

```
b=wage2$wage-wagebar
wage2$b<-b
svar_wage=(1/n)*sum(b^2)
print(svar_wage)
## [1] 163507.7
```

What is the sample variance of wage?

163507.7

#### E. Calculate Cov(wage, educ) using the results from 2B and 2C

```
cov_wage_educ=sum(a*b)/n
```

Report the covariance. Is the covariance between educ and wage positive or negative?

290.5513: positive.

#### F. Calculate B1

```
beta1hat=cov_wage_educ/svar_educ
```

What is your B1? What is the interpretation of the coefficient in terms of the population regression function?

60.21428. This means that one additional year of education is associated with a \$60.21 increase in expected monthly earnings, all else held equal.

#### G. Calculate B0

```
beta0hat=wagebar-beta1hat*educbar
```

What is your B0? What is the interpretation of the coefficient in terms of the population regression function? When does  $\hat{y} = B0$ ?

146.9524.

Beta0 is the intercept. It is the y value when  $x=0$  on the regression function.  $\bar{y} = \beta_0$  if  $\bar{x}=0$ —the mean of x must be 0.

### 3. Goodness of Fit

#### A. Calculate the Sum of Squares Total (SST)

```
SST=sum((wage2$wage-wagebar)^2)
```

## B. Calculate the residuals $u$ from the regression in 2

```
residuals=wage2$wage-beta0hat-beta1hat*wage2$educ
wage2$residuals<-residuals
mean(residuals)
## [1] 4.412083e-14
```

*Is this a strange result, or did you expect this?*

The mean was almost 0, which makes sense because  $E(u)=0$  because the residuals are measures of deviations from the regression function, and the regression function is a line of best fit, so the deviations should average to 0.

## C. Calculate the SSR

```
SSR=sum(wage2$residuals^2)
```

*What is the SSR? Is this larger or smaller than the SST? Can it ever be larger than the SST?*

136375524, which is smaller than the SST, because it fundamentally has to be. It only measures a part of the deviation, while SST looks at total deviation. Another way to think about this is  $SST=SSR+SSE$  where none of these elements are  $<0$ . Thus, SSR is always less than or equal to SST.

## D. Calculate the $R^2$

```
Rsquare=1-(SSR/SST)
```

*Interpret that  $R^2$  in the context of our regression*

$R^2=0.1070001$ , which measures the fraction of variance in wage explained by the model. As  $R^2$  is close to 0, this indicates that the SSE is close to 0, so the model isn't explaining much of the variance in wage.

# 4. Simple regression

## A. Running our regression

```
myRegression<-lm(wage2$wage~wage2$educ,data = wage2)
summary(myRegression)
##
## Call:
## lm(formula = wage2$wage ~ wage2$educ, data = wage2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
```

```
## -877.38 -268.63 -38.38 207.05 2148.26
##
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 146.952      77.715   1.891  0.0589 .
## wage2$educ   60.214       5.695  10.573 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 382.3 on 933 degrees of freedom
## Multiple R-squared:  0.107, Adjusted R-squared:  0.106
## F-statistic: 111.8 on 1 and 933 DF, p-value: < 2.2e-16
```

*How do the coefficients from 4A compare to the estimates you did “by hand” in Q2?*

I was exactly correct on both.

*How does the R<sup>2</sup> compare to the R<sup>2</sup> you calculated in Q3?*

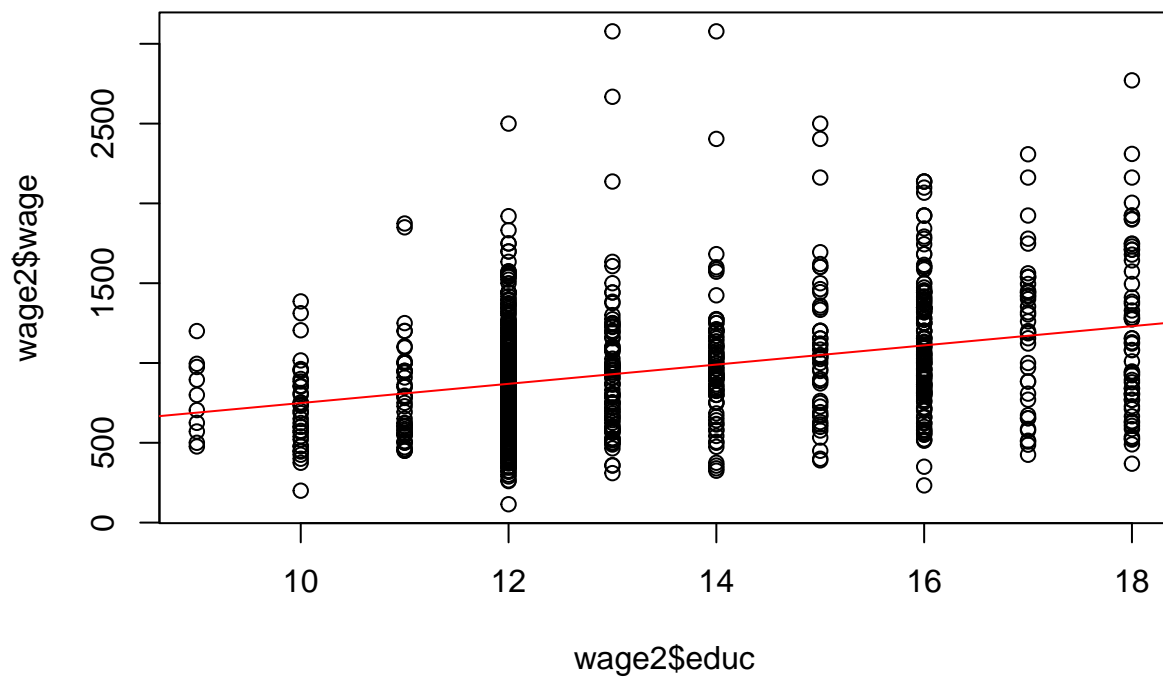
I was also correct on this.

*The output gives the degrees of freedom. How was this calculated?*

This was the sample size(935) minus the number of parameters needed to calculate during the analysis(2), resulting in DF=933.

## B. Plotting the Regression

```
plot(wage2$educ, wage2$wage)
abline(myRegression, col = 'red')
```



### C. Last Question

I spent 5 continuous hours on this problem set, but it took around half a day with breaks.